Exercices

1.1 Weak forms

1.1.1 Basic exercices (MRAC/INPAM/ATVE/IMDEA)



Exercice 1.1. What is the weak form associated to problem

$$u''(x) + u(x) = 0 \text{ on }]0;1[, \quad u(0) = 0, \quad u'(1) = 1.$$
 (1.1)



Exercice 1.2. What is the weak form associated to problem

$$u''(x) + u'(x) + u(x) = f(x) \text{ on } [0; 1[, u(0) = 0, u(L) = 1.$$
 (1.2)

Exercice 1.3. Let consider the 1D acoustic cavity harmonic problem at circular frequency ω :

$$\Omega =]0; L[, p''(x) + k^2 p = 0, k = \frac{\omega}{c}, c = \sqrt{\frac{K}{\rho}}.$$
 (1.3)

k is the wave number, c is the sound velocity, K is the compressibilty and ρ is the density.

• What is the weak form associated to this problem with boundary conditions

$$p'(0) = 0, \quad p'(L) = -\rho\omega^2.$$
 (1.4)

• What is the physical significance of the boundary condition in x = L



Exercice 1.4. • What is the weak form associated to problem

$$p''(x) + k^2 p(x) = 0 \text{ on }]0; L[, p'(0) = 0, p'(1) = \rho \omega^2.$$
 (1.5)

ullet What is the physical significance of the boundary condition in x=1



Exercice 1.5. What is the elementary matrix associated to the following weak form:

$$\int_0^h u(x)v(x) \, \mathrm{d}x \tag{1.6}$$

with the following discretisation

$$u(x) = \left[\mathbf{\Phi}_1(x) \middle| \mathbf{\Phi}_2(x)\right] \left\{ \mathbf{u}_1 \\ \mathbf{u}_2 \right\}$$
 (1.7)

with

$$\mathbf{\Phi}_1(x) = \frac{x}{h}, \quad \mathbf{\Phi}_2(x) = \frac{x}{h} \tag{1.8}$$

1.1.2 Advanced exercices (MRAC/INPAM)