

4 uždavinys: Išspęsti lygtį

$$T(n) = T\left(\frac{n}{2}\right) + \log_2 n$$

Sudarome, medį:

$$\log_2(n) \rightarrow \log_2 \frac{n}{2} \rightarrow \log_2 \frac{n}{2^2} \rightarrow \log_2 \frac{n}{2^3} \rightarrow \dots \rightarrow \log_2 \frac{n}{2^{\lfloor \log_2 n \rfloor}} \approx \Theta(1)$$

Aukštis $h = \log_2 n$

$$T(n) = \sum_{i=1}^h \log_2 \frac{n}{2^i} = \sum_{i=1}^h (\log_2 n + i) = h \log_2 n + \sum_{i=1}^h i = h \log_2 n + \frac{h(h+1)}{2} = \Theta(\log_2^2 n)$$

5 uždavinys: Išspęsti lygtį

$$T(n) = T\left(\frac{n}{2}\right) + \log_2^2 n$$

Sudarome, medį:

$$\log_2^2(n) \rightarrow \log_2^2 \frac{n}{2} \rightarrow \log_2^2 \frac{n}{2^2} \rightarrow \log_2^2 \frac{n}{2^3} \rightarrow \dots \rightarrow \log_2^2 \frac{n}{2^{\lfloor \log_2 n \rfloor}} \approx \Theta(1)$$

Aukštis $h = \log_2 n$

$$\begin{aligned} T(n) &= \sum_{i=1}^h \log_2^2 \frac{n}{2^i} = \sum_{i=1}^h (\log_2 n + i)^2 = h \log_2^2 n + 2 \log_2 n \sum_{i=1}^h i + \sum_{i=1}^h i^2 \\ &= h \log_2^2 n + 2 \log_2 n \frac{h(h+1)}{2} + \frac{h(h+1)(2h+1)}{6} = \Theta(\log_2^3 n) \end{aligned}$$