# Machine Learning Advances in Generative Models



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## Lecture Overview



#### Recap















- Density estimation
- Generative models
  - Learning a distribution over observations

#### Today's lecture

- Generative adversarial networks
- Wasserstein GANs, Conditional GANs
- Autoencoders and VAEs
- Improved latent space interpolation
- Skip connections (U-Net)



https://github.com/cwkx/ml-materials

Think about how you will make your **Pegasus** during this lecture.



## **GANs**

#### Generative Adversarial Networks

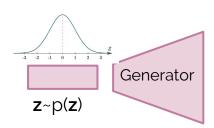
#### Generative Adversarial Nets - NIPS Proceedings

https://papers.nips.cc/paper/5423-generative-adversarial-nets ▼

by I Goodfellow - 2014 - Cited by 7299 - Related articles

We propose a new framework for estimating **generative** models via **adversarial nets**, in which we simultaneously train two models: a **generative** model G that ...

- Two-player zero-sum non-cooperative game (minmax) with the value function V(G,D) of two networks:
  - Discriminator (Critic)
    - Estimates probability of sample being real or generated (fake).
  - Generator
    - Learns to map noise from prior to samples from  $p_{\rm data}$









, 37% fake

$$\min_{G} \max_{D} L(D, G) = \mathbb{E}_{x \sim p_{\text{data}}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_{z}(z)}[\log(1 - D(G(z)))]$$
$$= \mathbb{E}_{x \sim p_{\text{data}}(x)}[\log D(x)] + \mathbb{E}_{x \sim p_{g}(z)}[\log(1 - D(x))].$$

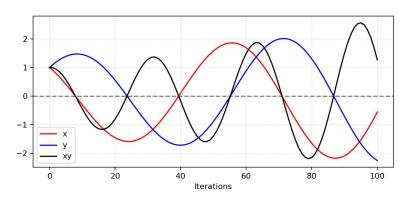
## Generative Adversarial Networks



"Stability does not come solely from G or D, but from their interaction through the adversarial process"

Notoriously difficult to train:

- Non-convergence
  - Hard to achieve Nash equilibrium
- Diminishing gradient
- Difficult to tune
- Mode collapse (next slide)



A simulation of our example for updating X to minimize XY and updating Y to minimize -XY. The learning rate  $\eta$ =0.1. With more iterations, the oscillation grows more and more unstable.

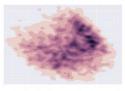
## Mode Collapse



#### Preferred behaviour:







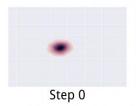


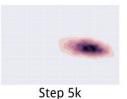


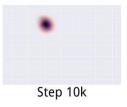


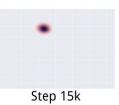


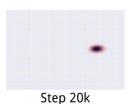
## Common mode collapse:

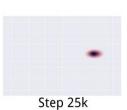














above from "Unrolled Generative Adversarial Networks"



left shows collapsed modes on CIFAR-10

## Wasserstein GANs

#### Wasserstein GAN

https://arxiv.org→stat ▼

by M Arjovsky - 2017 - Cited by 1272 - Related articles

26 Jan 2017 - Abstract: We introduce a new algorithm named WGAN, an alternative to traditional GAN training. In this new model, we show that we can ...

Cite as: arXiv:1701.07875

A real-valued function  $f:\mathbb{R} o\mathbb{R}$  is called **K**-Lipschitz continuous if there exists a real constant

$$K \geq 0$$
 such that, for all  $|x_1, x_2 \in \mathbb{R}$ ,  $|f(x_1) - f(x_2)| \leq K|x_1 - x_2|$ 

$$|f(x_1)-f(x_2)|\leq K|x_1-x|$$



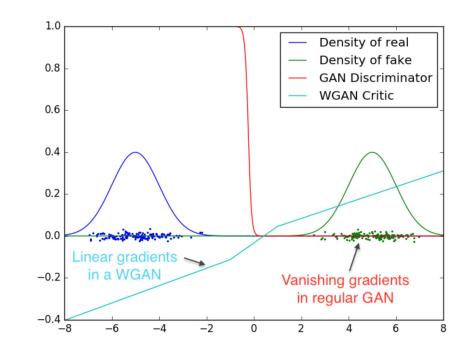
If K-Lipschitz

The original paper proposes clamping gradients to a Hypercube.

Tends to slide in corners.



https://github.com/cwkx/mlmaterials/blob/master/lectur es/notes/7-wasserstein.pv



## WGAN Gradient Penalty

Improved Training of Wasserstein GANs

https://arxiv.org → cs ▼

by I Gulrajani - 2017 - Cited by 998 - Related articles

31 Mar 2017 - Improved Training of Wasserstein GANs. Generative Adversarial Networks (GANs) are powerful generative models, but suffer from training instability. The recently proposed Wasserstein GAN (WGAN) makes progress toward stable training of GANs, but sometimes can still generate only low-quality samples or fail to converge.

Cite as: arXiv:1704.00028

Optimal critic contains straight lines with gradient norm 1 connecting coupled points from  $\mathbf{P}_r$  and  $\mathbf{P}_g$ 



Add another term 1-Lipschitz constraint:

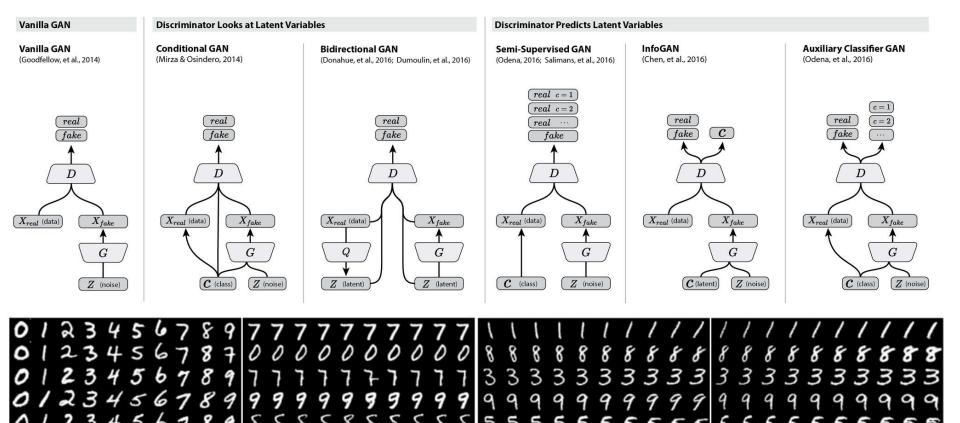
$$L = \underbrace{\mathbb{E}_{\hat{\boldsymbol{x}} \sim \mathbb{P}_g} \left[ D(\hat{\boldsymbol{x}}) \right] - \mathbb{E}_{\boldsymbol{x} \sim \mathbb{P}_r} \left[ D(\boldsymbol{x}) \right]}_{\text{Original critic loss}} + \underbrace{\lambda \, \mathbb{E}_{\hat{\boldsymbol{x}} \sim \mathbb{P}_{\hat{\boldsymbol{x}}}} \left[ (\|\nabla_{\hat{\boldsymbol{x}}} D(\hat{\boldsymbol{x}})\|_2 - 1)^2 \right]}_{\text{Our gradient penalty}}.$$

Backpropagating new loss requires computing gradient of gradients, which is quite slow.

torch.autograd.grad(outputs, inputs, grad\_outputs=None, retain\_graph=None, create\_graph=False,
only\_inputs=True, allow\_unused=False)

# GAN Conditioning & Disentanglement





## Autoencoder

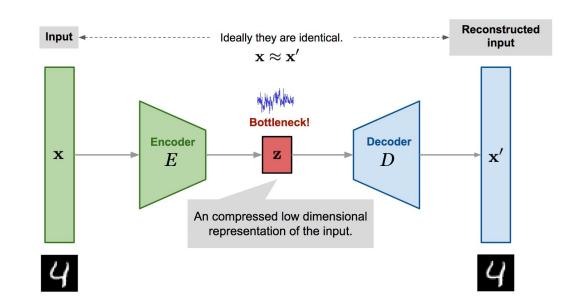


Learns an identify function unsupervised:  $\mathcal{L}_{auto} = \mathbb{E}_{\mathbf{x} \sim p_{data}} \left[ \|\mathbf{x} - D_{\theta}(E_{\theta}(\mathbf{x}))\|^2 \right]$ 

- Dimensionality reduction
- Compresses input
- Easy to train

#### **Problems**

- z~q(z) is difficult to draw samples from
- non-semantic reconstructions



# Can be Conditional & Constrained



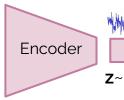
Can be used for translation tasks  $p(\mathbf{y}|\mathbf{x})$  (e.g. image-to-image)

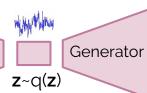
## Naive usage for:

- Deblurring
- Black and white to color
- Segmentation

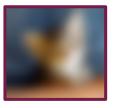
$$\mathcal{L}_{\text{translate}} = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}} \left[ \|\mathbf{y} - D(E(\mathbf{x}))\|^2 \right]$$











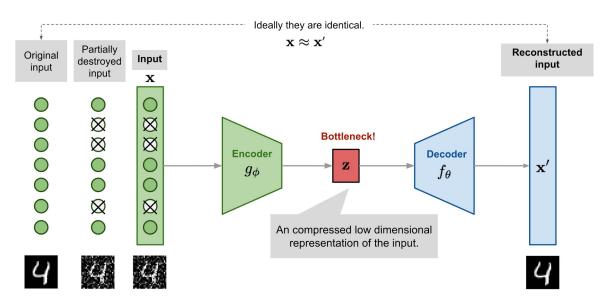


# Denoising Autoencoder



Repairs a partially corrupted input (just as humans are able to distinguish objects).

$$\mathcal{L}_{\text{denoise}} = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}, \hat{\mathbf{x}} \sim \mathcal{M}(\hat{\mathbf{x}}|\mathbf{x})} \left[ \|\mathbf{x} - D(E(\hat{\mathbf{x}}))\|^2 \right]$$



# Extended approaches:

- Inpainting
- Augmentation
- Layerwise corruption

## Variational Autoencoder

**Auto-Encoding Variational Bayes** 

https://arxiv.org > stat ▼

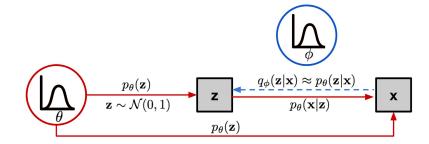
by DP Kingma - 2013 - Cited by 4052 - Related articles

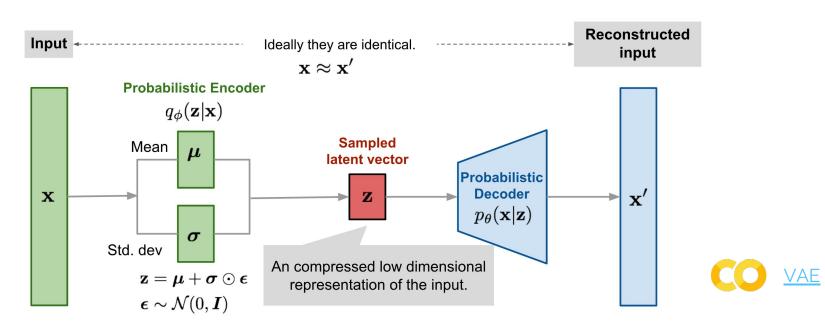
 $20~{\rm Dec}~2013$  - We introduce a stochastic <code>variational</code> inference and learning algorithm that scales to large datasets and, under some mild differentiability ...

Cite as: arXiv:1312.6114

Instead of mapping input into a *fixed* vector, what if we want to map into a distribution?

Prior  $p_{\theta}(\mathbf{z})$ , Likelihood  $p_{\theta}(\mathbf{x}|\mathbf{z})$ , Posterior  $q_{\theta}(\mathbf{z}|\mathbf{x})$ 

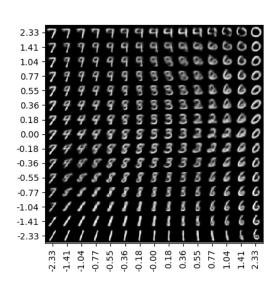


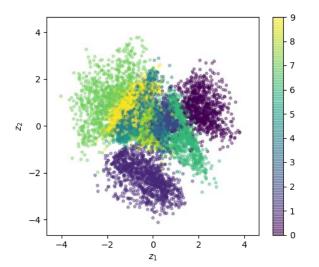


# Manifold learnt by a VAE



If we embed to 2D encoding, we can plot points for all inputs:





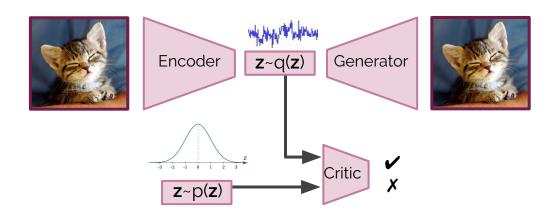
How can we improve this **manifold**?

- Labels = easy!
- Generate more samples
  - Adversarial strategies

## Adversarial Autoencoders



Uses an adversarial strategy to make aggregate posterior distribution look like a prior distribution:



...there's also a conditional version.

4	4	4	Ġ	6	6	6	0	0	0	0	0	0	0	0	0	0	0	0	0	0
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7	7	7	7	7	7	7	1	1	1	1	1	1	1	1	1	1	1	1	1	1

# Adversarially Improved Interpolation Durham



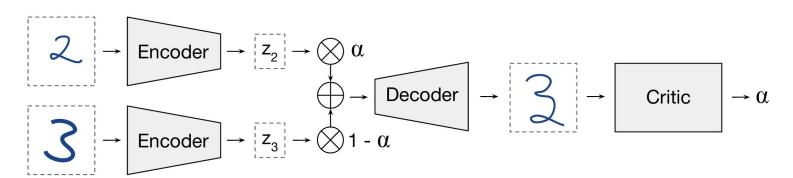
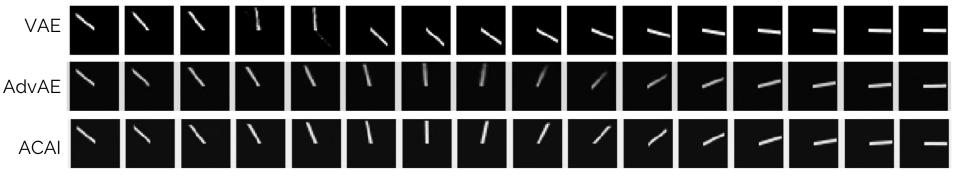
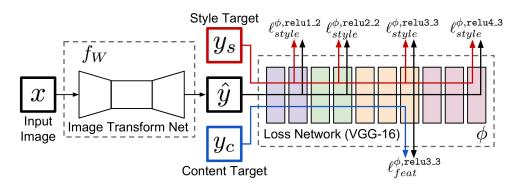


Figure 1: Adversarially Constrained Autoencoder Interpolation (ACAI). A critic network tries to predict the interpolation coefficient  $\alpha$  corresponding to an interpolated datapoint. The autoencoder is trained to fool the critic into outputting  $\alpha = 0$ .



# Style Transfer







- "A Neural Algorithm for Artistic Style"
- "Perceptual Losses for Real-Time Style Transfer and Super-Resolution"
- "Image-to-Image Translation with Conditional Adversarial Networks"











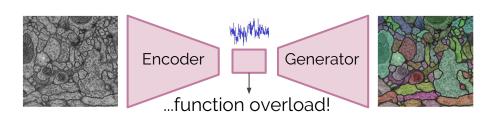






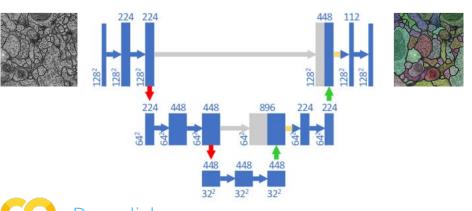
# Skip connections (U-Net)





Autoencoders are not well-suited for spatially-aligned image-to-image tasks (blurry outputs).

...so we add skip-connections concatenating encoder outputs to the decoder:



- Can't be used for reconstructive approaches, why?
- Great for segmentation



# Take away points



- Unsupervised learning is key to learning structure in the real universe
- We're learning the <u>boundaries of creativity</u>, and how to push at them (from a statistical perspective)
- GANs have led to lots of big advances in the field
  - Stick a GAN on the end (image translation)
  - Stick a GAN in the middle (adversarial autoencoder)
  - Stick a GAN on interpolation bit to improve them
- GAN training is still difficult and expensive for the really good stuff
- Still a long way to building good unsupervised density estimators

