

1.) Pogreške u postupcima analize

1.1)

24, 25

$$24 = 11000 = 2^4 \cdot 1.1$$

$$25 = 11001 = 2^4 \cdot 1.1001$$

$$\sqrt[4]{4} \rightarrow p=4$$

$$k=4, \quad a=2^{4-1}-1=7$$

$$15.5 = 1111.1$$

$$\rightarrow 2^3 \cdot 1.1111 = e-a=3, e=10$$

$$0.75 = 0.11$$

$$\rightarrow 2^{-1} \cdot 1.1 \quad e-a=-1, e=6$$

$$15.5 = 0.10101111$$

$$0.75 = 0.01101000$$

$$\begin{array}{r} 2^3 \cdot 1.1111 \\ + 2^3 \cdot 0.00011 \\ \hline 10.0000 = 10 \end{array}$$

1.2)

9, -0.1875

$$9 = 1001$$

$$= 2^3 \cdot 1.001$$

$$\rightarrow p=3$$

$$-0.1875 = -0.0011$$

$$= -2^{-3} \cdot 1.1$$

$$k=3 \text{ bit} \rightarrow e='110'=6, a=3, \text{exp} \in \{3, 2, 1, 0, -1, -2\}$$

$$-0.1875 \text{ kao denormirani: } -2^{-2} \cdot 0.11, \quad k=3 \checkmark$$

$$9 = 0.110001$$

$$-0.1875 = 1.000110$$

$$\begin{array}{r} 2^3 \cdot 1.001 \\ - 2^3 \cdot 0.000110 \\ \hline 2^3 \cdot 1.001 = 9 \end{array}$$

Bez greške frakcija mora

biti 7 (zbog 0.0000011)

$$\text{min} = 0.000000 \rightarrow 0$$

$$\text{max} = 0.110111 \rightarrow 2^3 \cdot 1.111 \rightarrow 15$$

ne može 111 jer bi (po tablici) to bio NaN

1.3)

$$k=4, p=4, \overset{e}{1}00001100$$

$$e = 0000 \rightarrow \text{denormirani!} \rightarrow -2^{1-2} \cdot 0.11$$

$$= -2^{-6} \cdot 0.75 = -0.01171875 //$$

1.4) $[-100, 100]$ $2^e = 0.5$ -99.45

$$100 = 1100100 = 2^6 \cdot 1.1001$$

$$k=4 \rightarrow e = 1110, a=7, \text{exp} \in \{7, 6, \dots, -6\} \checkmark$$

$$99 = 1100011 = 2^6 \cdot 1.100011, p=6 //$$

$$98 = 1100010 = 2^6 \cdot 1.10001$$

$$4.5 = 100.1 = 2^2 \cdot 1.001$$

$$\begin{array}{r} 2^6 \cdot 1.100011 \\ - 2^6 \cdot 0.0001001 \end{array}$$

\rightarrow može veći - manji i dodati predznak

$$2^6 \cdot 1.011111 = -95 //$$

1.5)

$$p=5, k=3, 2=3$$

a) $\min = 01000100001 \rightarrow 2^{-2} \cdot 2^{-5} = 2^{-7}$

$$\max = 011011111 \rightarrow 2^3 \cdot 1.1111 = 1111.11 = 15.75 //$$

b)

$$0 = 01000100000$$

$$\infty = 0111100000$$

c)

$$2^{2-p-1} = 2^{3-5-1} = 2^{-3} = 0.125 //$$

1.6)

$$k=4$$

$$p=5$$

$$249.5$$

$$-25.25$$

$$a=4$$

$$e-a = \text{exp}$$

$$249.5 = 11111001.1 = 2^7 \cdot 1.11110011$$

$$-25.25 = 11001.01 = 2^4 \cdot 1.100101$$

$$249.5 = 0.111011110 \quad (248) \checkmark$$

ili

$$11111 \quad (252)$$

$$-25.25 = 1.101110010 \quad (25)$$

ili

$$10011 \quad (25.5) \checkmark$$

Mislim da bi trebalo biti središnje ordje

$$\begin{array}{r} 2^7 \cdot 1.11110 \\ - 2^7 \cdot 0.0011010101 \\ \hline \end{array}$$

$$= 2^7 \cdot 1.11000 = 224 \quad \text{Greška je } 0.25 //$$

1.7)

$$k=3$$

$$p=5$$

$$0.10111100$$

$$e=5, a=3, \text{exp}=5-3=2$$

$$2^2 \cdot 1.111 = 111.1 = 7.5 //$$

1.8)

$$k=3$$

$$p=4$$

$$(4.75 + 0.25) + 10$$

$$4.75 + (0.25 + 10)$$

Ne vrijedi asocijativnost!

$$4.75 = 100.11 = 2^2 \cdot 1.0011$$

$$0.25 = 0.01 = 2^0 \cdot 0.01$$

$$10 = 1010 = 2^3 \cdot 1.01$$

I

$$4.75 + 0.25$$

$$\begin{array}{r} 2^2 \cdot 1.0011 \\ + 2^2 \cdot 0.0001 \\ \hline \end{array}$$

$$= 2^2 \cdot 1.0100 = 5 //$$

$$10 + 5$$

$$\begin{array}{r} 2^3 \cdot 1.0100 \\ + 2^3 \cdot 0.1010 \\ \hline 2^3 \cdot 1.1110 = 15 // \end{array}$$

II

$$10 + 0.25$$

$$\begin{array}{r} 2^3 \cdot 1.0100 \\ + 2^3 \cdot 0.0001 \\ \hline \end{array}$$

$$= 2^3 \cdot 1.0101 = 10 //$$

$$10 + 4.75$$

$$\begin{array}{r} 2^3 \cdot 1.0101 \\ + 2^3 \cdot 0.1011 \\ \hline 2^3 \cdot 1.1111 = 14.5 // \end{array}$$

manja je greška ako se prvo zbrajaju "bliži" brojevi

1.9) $[-10, 10]$ $a_p = 0,1$ $-9,9, 0,45$

$$10 = 1010 = 2^3 \cdot 1,010$$

$k=3// \rightarrow e = \{110\}, z=3, \text{exp} \in \{3, 2, 1, 0, -1, -2\} \checkmark$

$9,5 = 1001,1$ tačno

$9,7 = 1001,11 \dots$ $0,05$ greška

$9,6 = 1001,101 \dots$ $0,025$ greška

$9,9 = 1001,111 \dots$ $0,025$ greška $= 2^3 \cdot 1,001111$

$p=6//$

$0,45 = 0,011 = 2^{-4} \cdot 1,1$
greška $= 0,095$

$-9,9 = 11110,001111$

$0,45 = 0,00110000$

$2^3 \cdot 1,001111$

$- 2^3 \cdot 0,000011$

$2^3 \cdot 1,001100 = 1001,1 = -9,5$

\rightarrow greška $0,05 \checkmark$

Nadam se da je ovo tačno!

1.10)

$5,625$

$0,1001101101$

$5,625 = 101,101 = 2^2 \cdot 1,01101$

$p=5//$

$\text{exp} = 2$

$p = 01101$ pa je $e = 1001 = 9 \Rightarrow k=4$

Provjera:

$k=4 \rightarrow z=7$

$e-z = \text{exp}$
 $9-7=2 \checkmark$

1.11)

$$k=3$$

$$p=4$$

$$5.75, -11$$

$$z=3$$

$$5.75 = 101.11 = 2^2 \cdot 1.0111$$

$$-11 = -1011 = -2^3 \cdot 1.0110$$

$$5.75 = 0.1010111$$

$$-11 = 1.1100110$$

$$11 - 5.75$$

$$2^3 \cdot 1.0110$$

$$- 2^3 \cdot 0.10111$$

$$2^3 \cdot 0.1011 = 101.1 = 5.5 //$$

1.12)

$$31.25, 504$$

$$9.5, -25.25$$

$$\begin{array}{l} 31.25 = 11111.01 = 2^4 \cdot 1.111101 \\ 504 = 111111000 = 2^8 \cdot 1.11111 \end{array} \quad \left. \vphantom{\begin{array}{l} 31.25 \\ 504 \end{array}} \right\} p=6 //$$

$$k=5 \rightarrow z=15, e = \overset{30}{11110}, \text{exp } [15, 14] \checkmark$$

$$-25.25 = -11001.01 = -2^4 \cdot 1.100101$$

$$9.5 = 1001.1 = 2^3 \cdot 1.0011$$

$$-25.5 = 1.10011100101$$

$$9.5 = 0.10010001100$$

$$25.25 - 9.5$$

$$2^4 \cdot 1.100101$$

$$- 2^4 \cdot 0.100110$$

$$2^4 \cdot 0.111111 = 1111.11 = 15.75 //$$

Opet, može veći - manji i dodat predznak