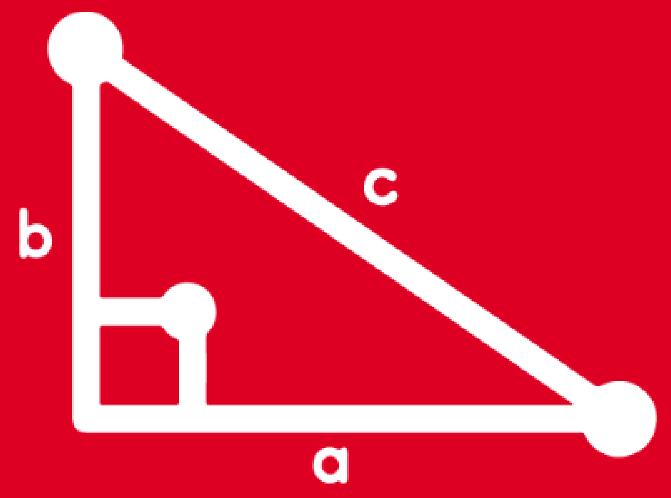
TRIGONOMETRY

TOMO VII

5th
SECONDARY



FEEDBACK

SACO OLIVEROS

HELICO-PRACTICE 1

Reduzca: $$E = \frac{\operatorname{sen}65° + \operatorname{sen}55°}{\cos 65° + \cos 55°}$$

Resolución:

Recordar:

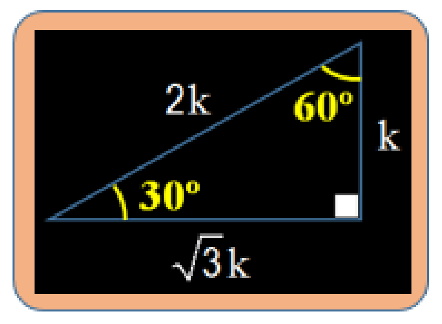
$$\operatorname{sen}A + \operatorname{sen}B = 2\operatorname{sen}\left(\frac{A+B}{2}\right).\cos\left(\frac{A-B}{2}\right)$$

$$\cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right).\cos\left(\frac{A-B}{2}\right)$$

$$E = \frac{\overbrace{\operatorname{sen}65° + \operatorname{sen}55°}^{\cancel{2}\operatorname{sen}60°\cancel{\cos 5°}}}{\underbrace{\cos 65° + \cos 55°}_{\cancel{2}\cos 60°\cancel{\cos 5°}}}$$

$$E = \frac{\operatorname{sen}60°}{\cos 60°}$$

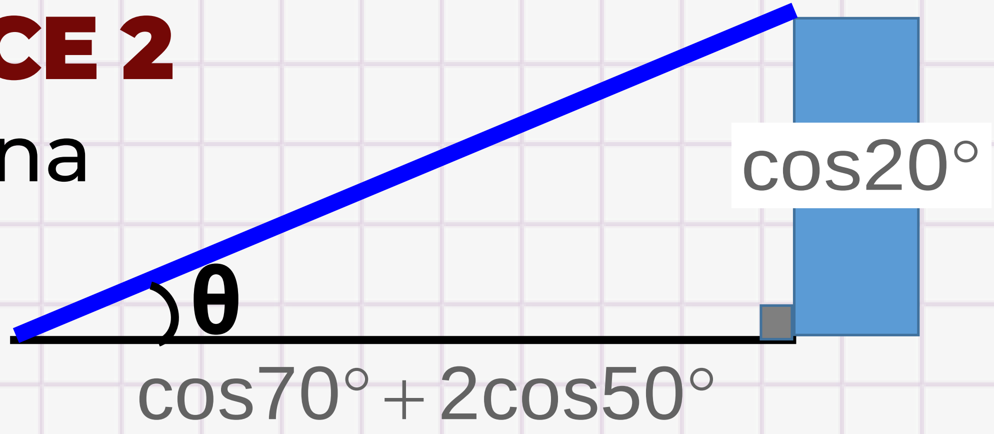
$$E = \tan 60°$$



$$\therefore E = \sqrt{3}$$

HELICO-PRACTICE 2

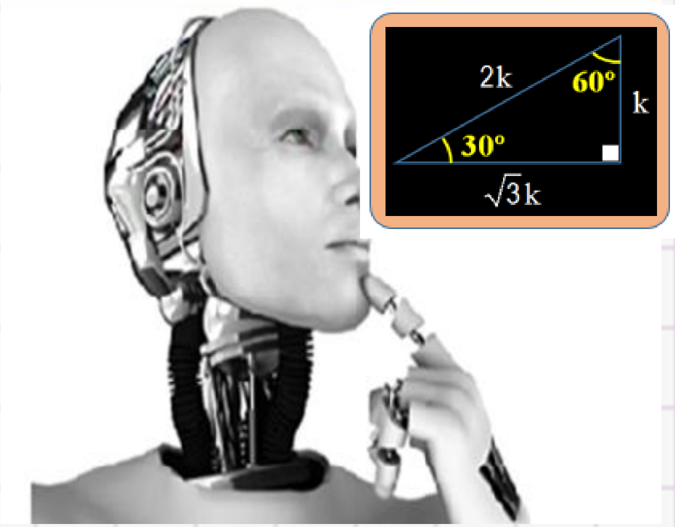
Una barra metálica descansa sobre una pared lisa, tal como se muestra en la figura. Calcule el valor de θ.



Resolución:

Recordar:

$$\cos A + \cos B = 2\cos\left(\frac{A+B}{2}\right).\cos\left(\frac{A-B}{2}\right)$$



$$\cot\theta = \frac{\cos 70° + 2\cos 50°}{\cos 20°} = \frac{\overbrace{\cos 70° + \cos 50°}^{2\cos 60° \cos 10°} + \cos 50°}{\cos 20°}$$

$$\cot\theta = \frac{\cancel{2}\left(\frac{1}{\cancel{2}}\right)\cos 10° + \cos 50°}{\cos 20°} = \frac{\overbrace{\cos 50° + \cos 10°}^{2\cos 30° \cancel{\cos 20°}}}{\cancel{\cos 20°}}$$

$$\cot\theta = 2\left(\frac{\sqrt{3}}{2}\right) \Rightarrow \cot\theta = \sqrt{3}$$

$$\boxed{\therefore \theta = 30°}$$

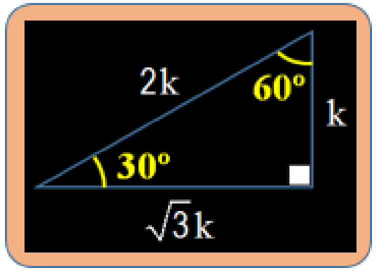
HELICO-PRACTICE 3

Halle el valor de m, si: $\dfrac{cos20°.cos10°}{sen30°} = m + sen80°$

Resolución:

Recordar

$$2cosxcosy = cos(x+y) + cos(x-y)$$



$$\frac{2cos20°cos10°}{2sen30°} = m + sen80°$$

$$\frac{cos30° + cos10°}{\cancel{2}\left(\frac{1}{\cancel{2}}\right)} = m + sen80°$$

$$\frac{\sqrt{3}}{2} + \cancel{sen80°} = m + \cancel{sen80°}$$

$$\therefore m = \frac{\sqrt{3}}{2}$$

HELICO-PRACTICE 4

Determine el rango de la función: $f(x) = 4\text{senx} + 5$

Resolución:

Se sabe que: $-1 \leq senx \leq 1$

Ahora le damos la forma de la función f:

$$-1 \leq senx \leq 1 \quad \ldots\ldots\ldots (x4)$$

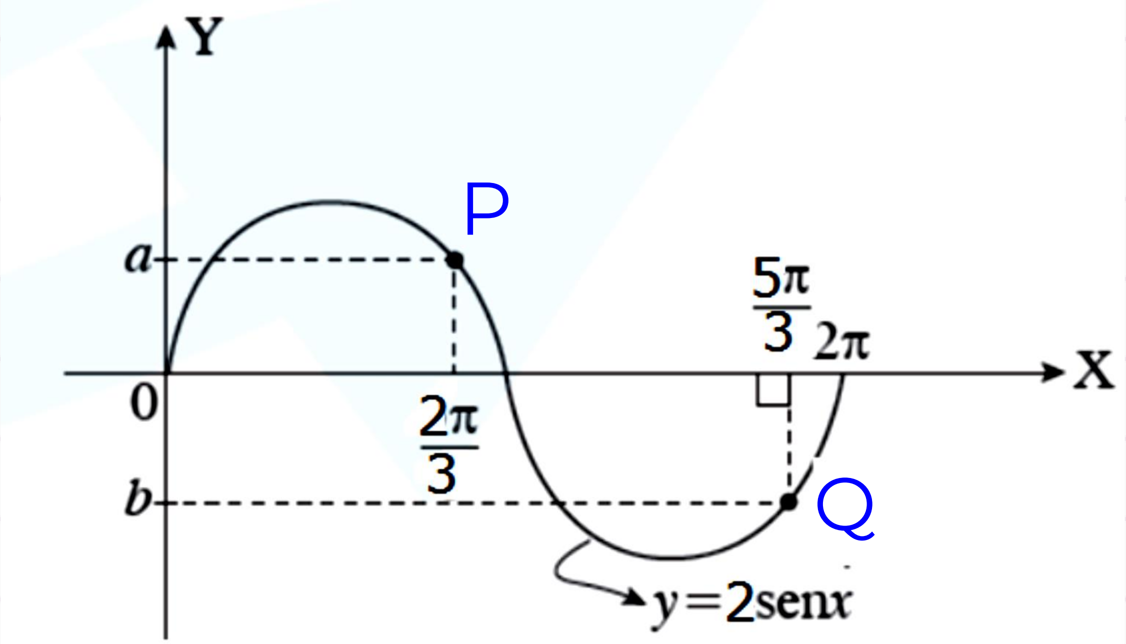
$$-4 \leq 4\,senx \leq 4 \quad \ldots\ldots\ldots (+5)$$

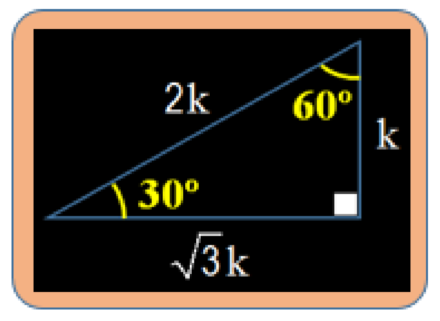
$$1 \leq \underbrace{4\,senx + 5}_{f(x)} \leq 9$$

$$\therefore Ranf = [1; 9]$$

HELICO-PRACTICE 5

Del gráfico, calcule a.b





Resolución:

Sea:

$f(x) = y = 2\text{sen}x$

$P\left(\frac{2\pi}{3}; a\right) \in f$

$a = 2\text{sen}\left(\frac{2\pi}{3}\right)$

$a = 2\left(\frac{\sqrt{3}}{2}\right) \Rightarrow a = \sqrt{3}$

$Q\left(\frac{5\pi}{3}; b\right) \in f$

$b = 2\text{sen}\left(\frac{5\pi}{3}\right)$

$b = 2\left(-\frac{\sqrt{3}}{2}\right) \Rightarrow b = -\sqrt{3}$

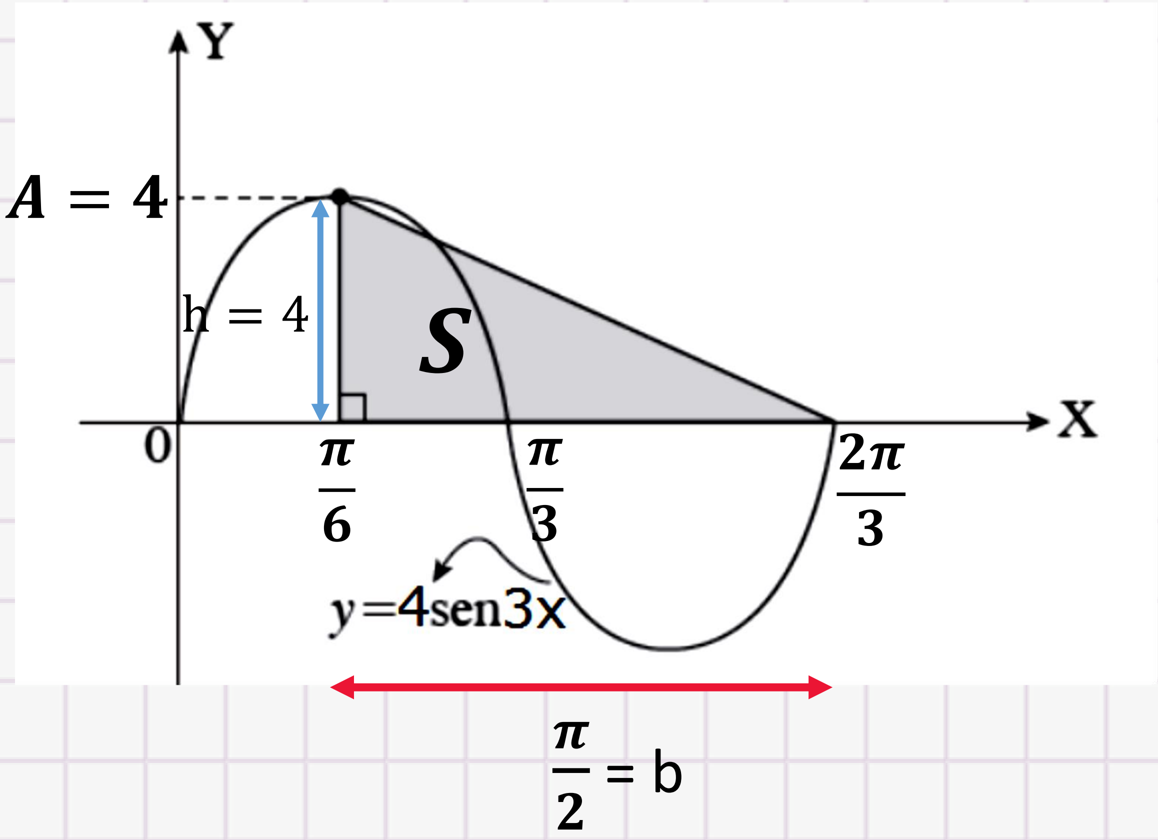
Piden:

$a.b = (\sqrt{3}).(-\sqrt{3})$

$\boxed{\therefore ab = -3}$

HELICO-PRACTICE 6

Del gráfico, determine el área de la región sombreada.



Resolución:

Sea la función: $f(x) = y = 4sen3x$

Periodo de la función:

$$T = \frac{2\pi}{B} \rightarrow T = \frac{2\pi}{3}$$

Amplitud: $A = 4$

Calculando el área:

$$S = \frac{b.h}{2} \Rightarrow S = \frac{\left(\frac{\pi}{2}\right).(4)}{2}$$

$$\therefore S = \pi\, u^2$$

HELICO-PRACTICE 7

Determine el rango de la función: $f(x) = 3\cos x - 2$

Resolución:

Se sabe que: $-1 \leq Cosx \leq 1$

Ahora le damos la forma de la función f:

$-1 \leq Cosx \leq 1 \ldots\ldots (x3)$

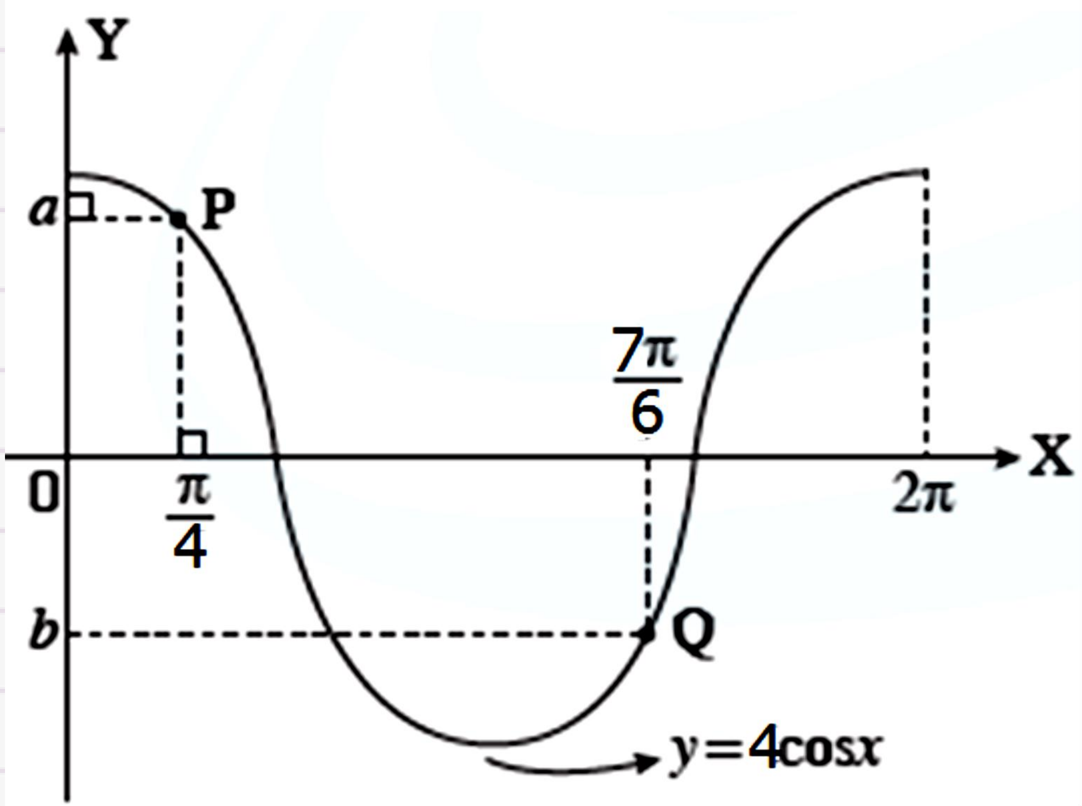
$-3 \leq 3Cosx \leq 3 \ldots\ldots (-2)$

$-5 \leq \underbrace{3Cosx - 2}_{f(x)} \leq 1$

$\therefore Ranf = [-5; 1]$

HELICO-PRACTICE 8

Del gráfico, calcule a·b



Resolución:

Sea : f (x) = y = 4cosx

$Q\left(\frac{7\pi}{6};b\right)\in f$

$\Rightarrow b=4\cos\left(\frac{7\pi}{6}\right)$

$\Rightarrow b=-4\cos\left(\frac{\pi}{6}\right)$

$\Rightarrow b=-4\left(\frac{\sqrt{3}}{2}\right)$

$\Rightarrow b=-2\sqrt{3}$

$P\left(\frac{\pi}{4};a\right)\in f$

$\Rightarrow a=4\cos\left(\frac{\pi}{4}\right)$

$\Rightarrow a=4\left(\frac{\sqrt{2}}{2}\right)$

$\Rightarrow a=2\sqrt{2}$

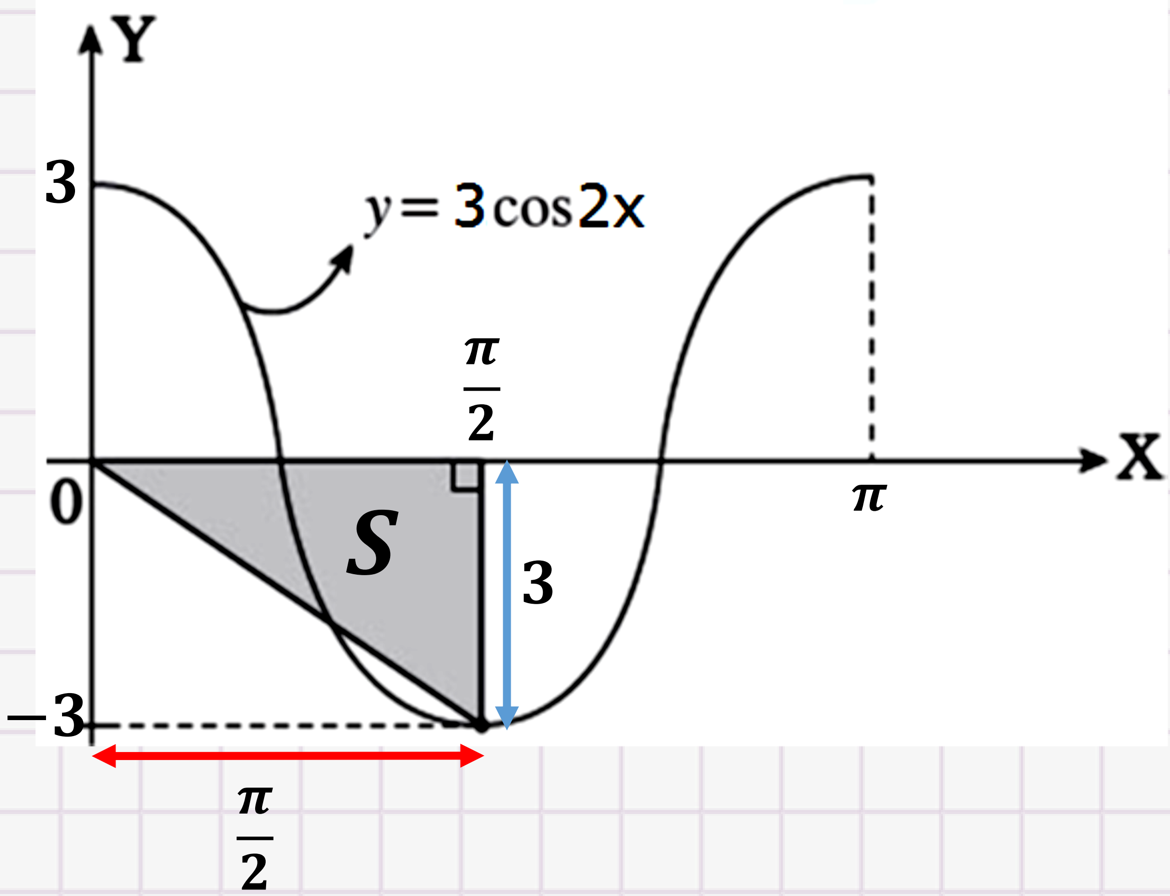
Nos piden:

$a.b=(2\sqrt{2})(-2\sqrt{3})$

$\boxed{\therefore\ ab=-4\sqrt{6}}$

HELICO-PRACTICE 9

Del gráfico, determine el área de la región sombreada.



Resolución:

$Sea\ la\ función:\ \ f(x) = y = 3\cos 2x$

$Periodo\ de\ la\ función:$

$$T = \frac{2\pi}{B} \longrightarrow T = \frac{2\pi}{2} = \pi$$

$Amplitud:\ A = 3$

$$Calculando\ el\ área:\ S = \frac{\left(\frac{\pi}{2}\right).(3)}{2}$$

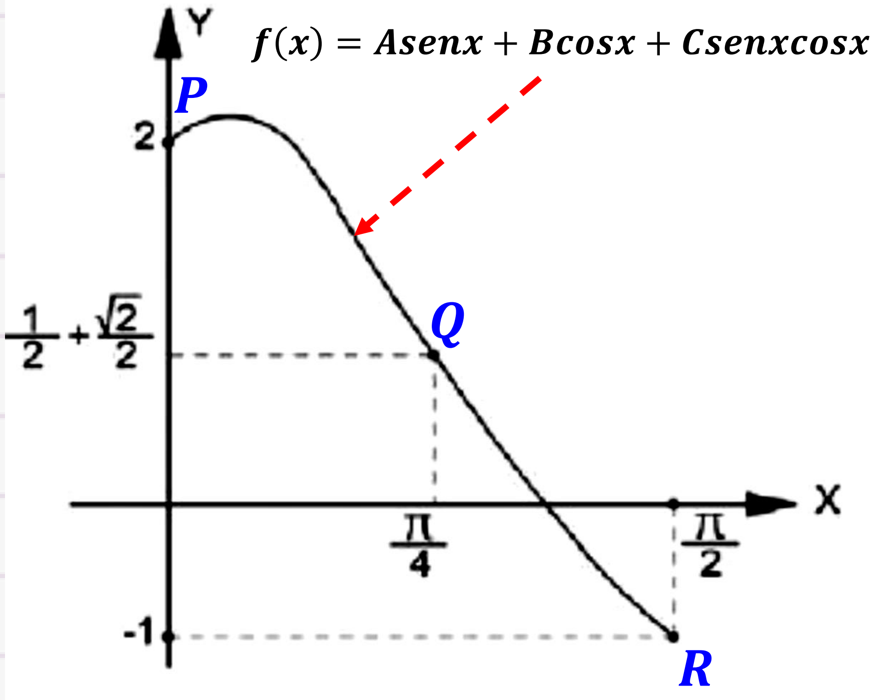
$$\therefore S = \frac{3\pi}{4}u^2$$

HELICO-PRACTICE 10

Sean A, B, C constantes y $f:\mathbb{R}\to\mathbb{R}$ dada por

$f(x)=A\,\text{sen}(x)+B\cos(x)+C\,\text{sen}(x)\cos(x)$

cuya gráfica parcial se muestra a continuación:



Calcule $A+B+C$

Resolución:

El punto P $\in \boldsymbol{f(x)}$

$$f(0) = Asen(0) + Bcos(0) + Csen(0)\cos(0)$$

$$2 = A(0) + B(1) + C(0)(1) \longrightarrow \boxed{\boldsymbol{2 = B}}$$

El punto R $\in \boldsymbol{f(x)}$

$$f\left(\frac{\pi}{2}\right) = Asen\left(\frac{\pi}{2}\right) + Bcos\left(\frac{\pi}{2}\right) + Csen\left(\frac{\pi}{2}\right)cos\left(\frac{\pi}{2}\right)$$

$$-1 = A(1) + 2(0) + C(1)(0) \longrightarrow \boxed{\boldsymbol{-1 = A}}$$

El punto Q $\in \boldsymbol{f(x)}$

$$f\left(\frac{\pi}{4}\right) = Asen\left(\frac{\pi}{4}\right) + Bcos\left(\frac{\pi}{4}\right) + Csen\left(\frac{\pi}{4}\right)cos\left(\frac{\pi}{4}\right)$$

$$\frac{1}{2}+\frac{\sqrt{2}}{2} = -1\left(\frac{\sqrt{2}}{2}\right) + 2\left(\frac{\sqrt{2}}{2}\right) + C\left(\frac{\sqrt{2}}{2}\right)\left(\frac{\sqrt{2}}{2}\right)$$

$$\frac{1}{2}+\cancel{\frac{\sqrt{2}}{2}} = \cancel{\frac{\sqrt{2}}{2}} + C\left(\frac{1}{2}\right) \longrightarrow \boxed{\boldsymbol{1 = C}}$$

$$\boxed{\therefore A+B+C=2}$$

SACO
OLIVEROS