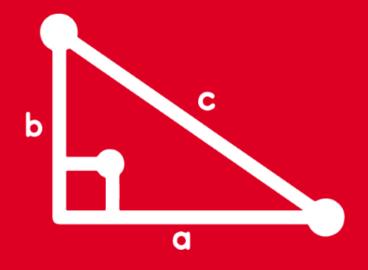
TRIGONOMETRY VOLUME II

4th SECONDARY



FEEDBACK



1. Si $5\cos\alpha - 2 = 0$, donde α es la medida de un ángulo agudo, efectúe: $Q = \sqrt{21}(\cot\alpha + \csc\alpha)$

RESOLUCIÓN



Recordar

$$\cos \alpha = \frac{CA}{H} \quad \cot \alpha = \frac{CA}{CO} \quad \csc \alpha = \frac{H}{CO}$$

Dato:

$$5\cos\alpha - 2 = 0 \qquad \cos\alpha = \frac{2}{5} = \frac{CA}{H}$$

$$\sqrt{21} = \text{CO}$$

$$\frac{5 = \text{H}}{\alpha}$$

$$2 = \text{CA}$$

Por teorema de Pitágoras

$$5^2 = 2^2 + (CO)^2$$
 $CO = \sqrt{21}$

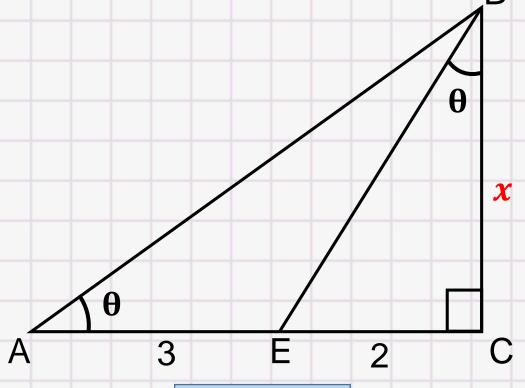
Efectuamos:

$$Q = \sqrt{21}(\cot\alpha + \csc\alpha)$$

$$Q = \sqrt{21}(\frac{2}{\sqrt{21}} + \frac{5}{\sqrt{21}})$$

$$Q = \sqrt{21}(\frac{7}{\sqrt{21}}) \qquad \therefore \mathbf{Q} = \mathbf{7}$$

2. Del gráfico, calcule cotθ.





Recordar

$$cot\alpha = \frac{CA}{CO}$$

RESOLUCIÓN

Sea BC = x

En el BCE:

$$\cot\theta = \frac{x}{2} \dots (1)$$

En el BCA:

$$\cot \theta = \frac{5}{x} \dots (2)$$

Igualamos las ecuaciones (1) y (2):

$$\frac{x}{2} = \frac{5}{x} \implies x = \sqrt{10}$$

$$\therefore \cot \theta = \frac{\sqrt{10}}{2}$$

3. Si $\tan \alpha = \sqrt{7}$, donde $0^{\circ} < \alpha < 90^{\circ}$, efectúe $E = \tan^{2} \alpha + 2\sqrt{8}\cos \alpha$.

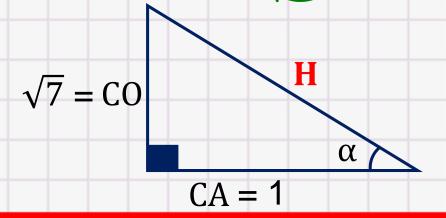
RESOLUCIÓN



Recordar

$$cos\alpha = \frac{CA}{H} \quad tan\alpha = \frac{CO}{CA}$$

Dato:
$$\tan \alpha = \frac{\sqrt{7}}{1} = \frac{\text{CO}}{\text{CA}}$$



Por teorema de Pitágoras:

$$H^2 = (\sqrt{7})^2 + (1)^2$$

$$H^2 = 7 + 1$$

$$H = \sqrt{8}$$

Efectuamos:

$$E = \tan^2 \alpha + 2\sqrt{8}\cos \alpha$$

$$E = (\sqrt{7})^2 + (2\sqrt{8})(\frac{1}{\sqrt{8}})$$

$$E = 7 + 2$$

$$\therefore E = 9$$

4. Calcule el valor de x, si

$$2x \cdot \sec^2 45^\circ \cdot \sec^2 30^\circ + \sec 60^\circ = 3x \cdot \csc^2 60^\circ \cdot \tan 37$$

RESOLUCIÓN

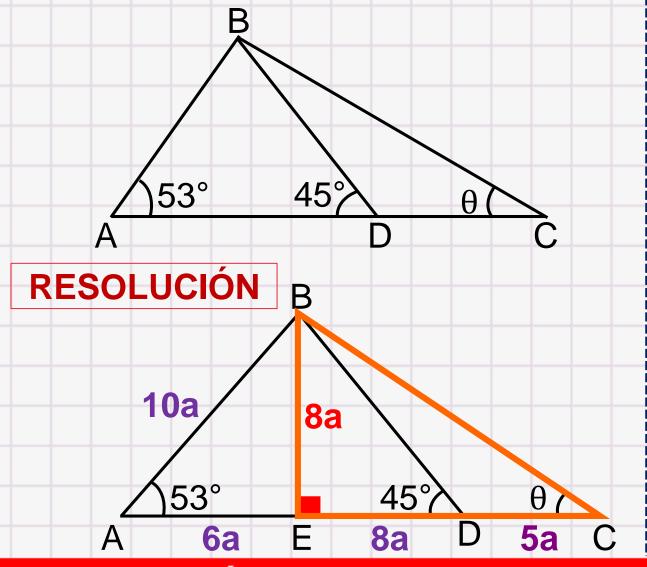
$$2x \cdot \left(\sqrt{2}\right)^2 \cdot \left(\frac{1}{2}\right)^2 + 2 = 3x \cdot \left(\frac{2}{\sqrt{3}}\right)^2 \cdot \left(\frac{3}{4}\right)$$

$$2x \cdot (2) \cdot \left(\frac{1}{4}\right) + 2 = 3x \left(\frac{4}{3}\right) \cdot \left(\frac{3}{4}\right)$$

$$x + 2 = 3x$$

$$\therefore x = 1$$

5. Del gráfico, calcule $\cot \theta$, si AB = 2DC.



Trazamos la altura BE

• En el ABE (37°-53°):

$$AB = 10a$$
; $BE = 8a$; $AE = 6a$

• En el BED (45°- 45°):

$$ED = 8a$$

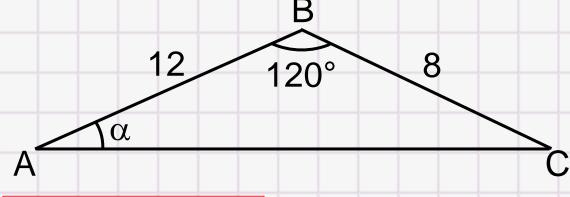
Dato:
$$AB = 2DC \longrightarrow DC = 5a$$

Finalmente:

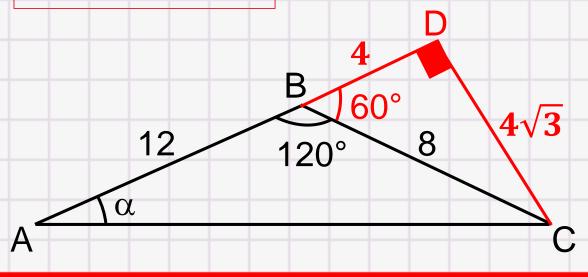
• En el BEC:
$$\cot \theta = \frac{13\pi}{8\pi}$$

$$\therefore \cot \theta = \frac{13}{8}$$

6. Del gráfico, calcule $tan\alpha$.



RESOLUCIÓN



Trazamos las líneas auxiliares \overline{BD} y \overline{DC} formando un ángulo de 90°.

Completamos el \triangleright BDC (60° – 30°):

Del ADC:
$$\tan \alpha = \frac{4\sqrt{3}}{16}$$

$$\therefore \tan \alpha = \frac{\sqrt{3}}{4}$$

7. Si tan9x = cot6x, efectúe $Q = tan^2 10x + csc5x$.

RESOLUCIÓN

Por RT de ángulos complementarios en:

$$9x + 6x = 90^{\circ}$$

$$15x = 90^{\circ}$$

$$x = 6^{\circ}$$

Efectuamos

$$Q = \tan^2 10(6^\circ) + \csc 5(6^\circ)$$

$$Q = \tan^2 60^\circ + \csc 30^\circ$$

$$Q = (\sqrt{3})^2 + 2$$

$$\therefore \mathbf{Q} = \mathbf{5}$$

8. Efectúe Q = sen(x + y) si

$$sen(x + 15^{\circ}) \cdot csc(35^{\circ} - x) = 1$$
 y $tan(3y - 20^{\circ}) = cot(30^{\circ} + y)$

RESOLUCIÓN

Dato:

$$sen(x + 15^{\circ}) \cdot csc(35^{\circ} - x) = 1 tan(3y - 20^{\circ}) = cot(30^{\circ} + y)$$

Por RT recíprocas:

$$x + 15^{\circ} = 35^{\circ} - x$$
$$2x = 20^{\circ}$$

$$x = 10^{\circ}$$

Dato:

$$\tan(3y - 20^\circ) = \cot(30^\circ + y)$$

Por RT de ángulos complementarios:

$$3y - 20 + 30^{\circ} + y = 90^{\circ}$$

$$4y = 80^{\circ}$$

$$y=20^{\circ}$$

Efectuamos:

$$Q = \operatorname{sen}(x + y)$$

$$Q = sen 30$$
°

$$\therefore \mathbf{Q} = \frac{1}{2}$$

9. Si
$$sen5\theta \cdot csc(2\theta + 45^\circ) = \frac{sen20^\circ \cdot sec70^\circ}{tan55^\circ \cdot tan35^\circ}$$
. Efectúe: M = $sec4\theta + tan3\theta$.

RESOLUCIÓN

Dato:

$$sen5\theta \cdot csc(2\theta + 45^{\circ}) = \frac{sen20^{\circ} \cdot sec70^{\circ}}{tan55^{\circ} \cdot tan35^{\circ}}$$

Por RT de ángulos complementarios en el 2° miembro:

$$sen5\theta \cdot csc(2\theta + 45^{\circ}) = sen20^{\circ} \cdot csc20^{\circ}$$

$$tan55^{\circ} \cdot cot55^{\circ}$$

$$sen5\theta \cdot csc(2\theta + 45^{\circ}) = \mathbf{1}$$

Por RT recíprocas:

$$5\theta = 2\theta + 45^{\circ}$$

 $3\theta = 45^{\circ}$ $\theta = 15^{\circ}$

Calculamos:

$$M = \sec 4(15^{\circ}) + \tan 3(15^{\circ})$$

 $M = \sec 60^{\circ} + \tan 45^{\circ}$
 $M = (2) + (1)$ $\therefore M = 3$

10. Se define como pandeo a la flexión RESOLUCIÓN producida por una carga axial pudiendo ser esta variable o crítica, sabiendo que una pieza metálica es sometida a 3 cargas axiales a, b y c definidas en Newton (N). Dar como respuesta el promedio de las cargas.



 $a = 8 sen 30^{\circ} - 3 tan 45^{\circ}$ $b = 4sec^2 45^\circ - sec60^\circ$ $c = 4\csc 53^{\circ} + 3\cot 45^{\circ}$

•
$$a = 8 \sin 30^{\circ} - 3 \tan 45^{\circ}$$

 $a = 8 \left(\frac{1}{2}\right) - 3(1)$ $a = 1 \text{ N}$

•
$$\mathbf{b} = 4\mathbf{sec}^2 \mathbf{45}^\circ - \mathbf{sec} \mathbf{60}^\circ$$

$$b = 4 (\sqrt{2})^2 - (2)$$
 $b = 6 N$

•
$$c = 4csc53^{\circ} + 3cot45^{\circ}$$

$$c = 4 \left(\frac{5}{4}\right) + 3(1) \qquad c = 8 \text{ N}$$

$$P = \frac{a+b+c}{3} = \frac{1+6+8}{3}$$
 : $P = 5N$

