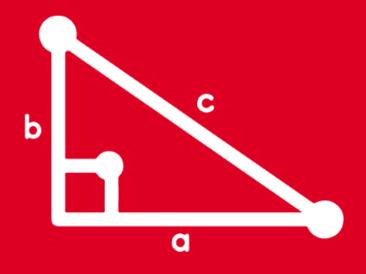
# TRIGONOMETRY Chapter 09



REDUCCIÓN AL PRIMER CUADRANTE II

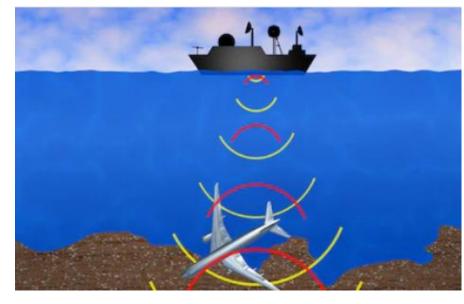




### **HELICO MOTIVACIÓN**

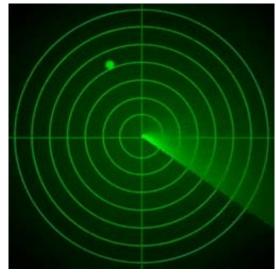
El SISTEMA DE SONAR es una técnica que principalmente usa la propagación del sonido bajo el agua para navegar, comunicarse o detectar objetos sumergidos.

El sonar funciona de forma similar al radar, con la diferencia de que en lugar de emitir ondas electromagnéticas emplea impulsos sonoros.



En la naturaleza, algunos animales como delfines y murciélagos usan el sonido para la detección de objetos





## REDUCCIÓN AL PRIMER CUADRANTE

## 3er CASO: Para ángulos positivos mayores a una vuelta.

De forma práctica utilizaremos:

$$\forall k \in \mathbb{Z}^+$$
:

$$RT[-360^{\circ}-k \pm \alpha] = RT(\pm \alpha)$$

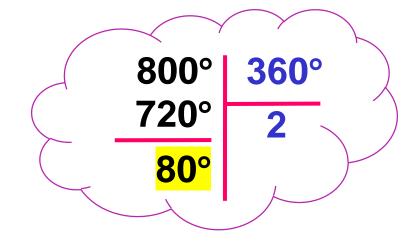
Para arcos múltiplos enteros de  $\pi$ :

$$RT[\frac{2k\pi}{par} \pm \alpha] = RT(\pm \alpha)$$

RT[
$$(2k + 1)\pi \pm \alpha$$
] = RT( $\pi \pm \alpha$ )  
impar

### **Ejemplo:**

$$sen800^{\circ} = sen(-360^{\circ}-2 + 80^{\circ})$$



### **OBSERVACIONES**

Para reducir arcos de la forma  $\left(\frac{a\pi}{b}\right)$ , donde a>2b

### **Efectuamos:**

### Luego:

$$\mathsf{RT}\!\left(\frac{\mathsf{a}\pi}{\mathsf{b}}\right) = \mathsf{RT}\!\left(\frac{\mathsf{r}\pi}{\mathsf{b}}\right)$$

Ejemplo: 
$$\cos\left(\frac{25\pi}{3}\right) = \cos\left(\frac{1\pi}{3}\right) = \frac{1}{2}$$

$$\forall k \in \mathbb{Z}$$
:

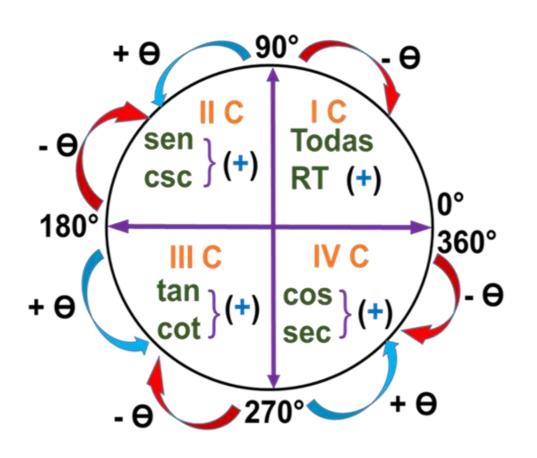
$$RT\left[\left(\frac{4k+1}{2}\pm\alpha\right]=RT\left(\frac{\pi}{2}\pm\alpha\right)$$

$$RT\left[\left(\frac{4k+3}{2}\right)\frac{\pi}{2}\pm\alpha\right]=RT\left(\frac{3\pi}{2}\pm\alpha\right)$$

$$\operatorname{sen}\left(\frac{17\pi}{2} + \alpha\right) = \operatorname{sen}\left(\frac{\pi}{2} + \alpha\right)$$

$$\cot\left(\frac{71\pi}{2} - \alpha\right) = \cot\left(\frac{3\pi}{2} - \alpha\right)$$

### **RECORDAR**



$$RT\begin{bmatrix} 180^{\circ} \pm \Theta \\ 360^{\circ} - \Theta \end{bmatrix} = \pm RT(\Theta)$$

$$RT\begin{bmatrix} 90^{\circ} + \Theta \\ 270^{\circ} \pm \Theta \end{bmatrix} = \pm CO-RT(\Theta)$$

$$\cos(-x) = \cos(x)$$

$$sec(-x) = sec(x)$$

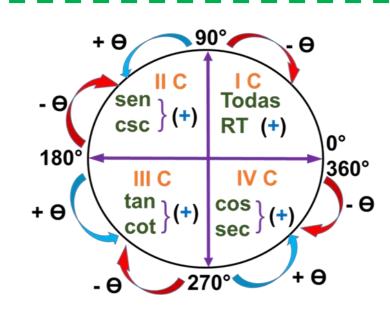
$$\begin{array}{c} \textbf{Co-RT} \\ \textbf{sen} & \leftrightarrow & \textbf{cos} \\ \textbf{tan} & \leftrightarrow & \textbf{cot} \\ \textbf{sec} & \leftrightarrow & \textbf{csc} \end{array}$$

Efectúe 
$$P = \frac{\text{sen}1500^{\circ} \cdot \text{cos}1110^{\circ}}{\text{tan}3645^{\circ}}$$

### **RESOLUCIÓN**

$$P = \frac{sen1500^{\circ} \cdot cos1110^{\circ}}{tan3645^{\circ}} = \frac{sen60^{\circ} \cdot cos30^{\circ}}{tan45^{\circ}} = \frac{\left(\frac{\sqrt{3}}{2}\right)\left(\frac{\sqrt{3}}{2}\right)}{1}$$

$$\therefore P = \frac{3}{4}$$



## Simplifique la expresión

$$\mathsf{E} = \frac{\mathrm{sen}(8\pi + x) \cdot \mathrm{cos}(7\pi + x)}{\mathrm{cos}(\frac{15\pi}{2} + x)}$$

### **RESOLUCIÓN**

$$E = \frac{\text{sen}(8\pi + x) \cdot \cos(7\pi + x)}{\cos(\frac{15\pi}{2} + x)}$$

$$E = \frac{senx. cos(\pi + x)}{cos(\frac{3\pi}{2} + x)}$$

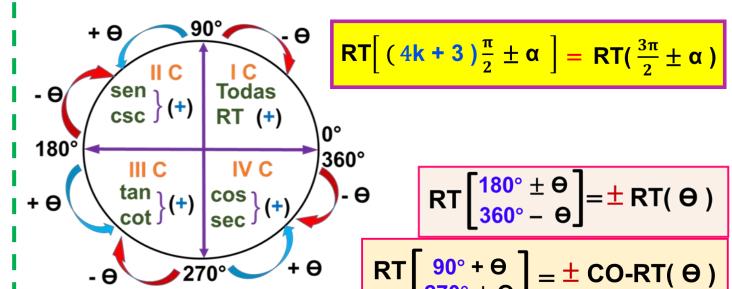
$$\mathbf{E} = \frac{-\mathbf{senx} (-\mathbf{cosx})}{-\mathbf{senx}}$$

$$E = -\cos x$$

$$RT[\frac{2k\pi}{2} \pm \alpha] = RT(\pm \alpha)$$

$$par$$

$$RT[(2k + 1)\pi \pm \alpha] = RT(\pi \pm \alpha)$$



impar

A Manuel se le entregó S/. x como incentivo por sus buenas calificaciones. Resolviendo la siguiente ecuación podrás averiguar con cuánto se le premió.  $sec420^{\circ} + x tan2565^{\circ} = 20 sen2213^{\circ}$ 

### **RESOLUCIÓN**

$$sec420^{\circ} + x tan2565^{\circ} = 20 sen2213^{\circ}$$

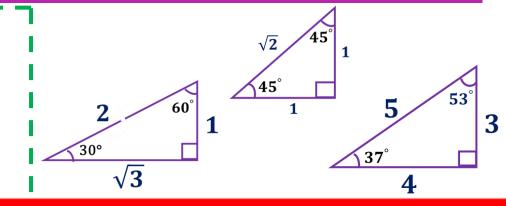
$$sec60^{\circ} + x tan45^{\circ} = 20 sen53^{\circ}$$

$$2 + x(1) = 20(\frac{4}{5})$$

$$2 + x = 16$$
  $x = 14$ 

A Manuel se le premió con S/.14

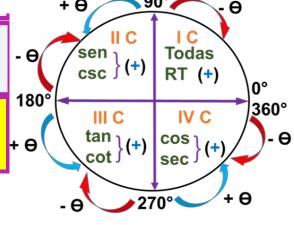
$$RT[\frac{360^{\circ} \cdot k}{2} \pm \alpha] = RT(\pm \alpha)$$



### Halle el valor de "n" si se cumple

que : sen( 
$$21\pi - \alpha$$
 ) =  $\frac{n-1}{3}$  ; cos( $\frac{41\pi}{2} + \alpha$ ) =  $\frac{n}{2} - 3$ 

# $RT[(2k + 1)\pi \pm \alpha] = RT(\pi \pm \alpha)$ impar $RT[(4k + 1)\frac{\pi}{2} \pm \alpha] = RT(\frac{\pi}{2} \pm \alpha)$



## **RESOLUCIÓN**

$$\frac{1}{3} = \operatorname{sen}(21\pi - \alpha) = \operatorname{sen}(\pi - \alpha) = \operatorname{sen}\alpha$$

$$\frac{4}{4} + 1$$

$$\frac{n}{2} - 3 = \cos\left(\frac{41\pi}{2} + \alpha\right) = \cos\left(\frac{1\pi}{2} + \alpha\right) = -\operatorname{sen}\alpha$$

$$3 - \frac{n}{2} = \operatorname{sen}\alpha$$

$$\frac{6 - n}{2} = \operatorname{sen}\alpha$$

Luego:  $sen\alpha = sen\alpha$ 

$$\frac{n-1}{3}=\frac{6-n}{2}$$

$$2n - 2 = 18 - 3n$$

$$5n = 20$$

$$\cdot \cdot \cdot \mathbf{n} = \mathbf{4}$$

Calcule 
$$E = \cos\left(\frac{37\pi}{3}\right) + \tan\left(\frac{59\pi}{4}\right)$$

### **RESOLUCIÓN**

$$\mathsf{E} = \mathsf{cos}\!\left(\frac{37\pi}{3}\right) + \mathsf{tan}\!\left(\frac{59\pi}{4}\right)$$

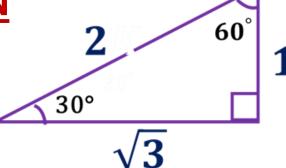
$$\mathsf{E} = \mathsf{cos}\!\left(\frac{1\pi}{3}\right) + \mathsf{tan}\!\left(\frac{3\pi}{4}\right)$$

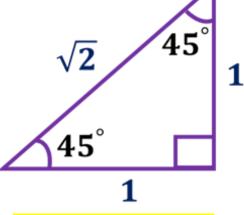
$$E = \cos 60^{\circ} + \tan 135^{\circ}$$

### IIC

$$E = \frac{1}{2} + \tan(180^{\circ} - 45^{\circ})$$

$$E = \frac{1}{2} + (-\tan 45^\circ) = \frac{1}{2} - 1$$





$$\stackrel{\cdot \cdot}{\cdot} E = -\frac{1}{2}$$

Para reducir arcos de la forma  $\left(\frac{a\pi}{b}\right)$ , donde a>2b

#### **Efectuamos:**

### Luego:

$$\mathsf{RT}\!\left(\,\frac{\mathsf{a}\pi}{\mathsf{b}}\,\right) = \mathsf{RT}\!\left(\,\frac{\mathsf{r}\pi}{\mathsf{b}}\,\right)$$

Siendo x + y = 1170°, reduzca : 
$$G = \frac{\tan y}{\cot x} + senx \cdot secy$$

## **RESOLUCIÓN**

Dato: 
$$x + y = 1170^{\circ}$$

$$\Rightarrow$$
 y = 1170° - x

RT(y) = RT[
$$3(360^\circ) + 90^\circ - x$$
]

$$RT(y) = RT[90^{\circ} - x]$$

$$RT(y) = CO - RT(x)$$

### Recordar:

$$RT[\frac{360^{\circ} \cdot k}{2} \pm \alpha] = RT(\pm \alpha)$$

$$RT \left\{ \frac{90^{\circ} \pm \theta}{270^{\circ} \pm \theta} \right\} = \pm Co\_RT(\theta)$$

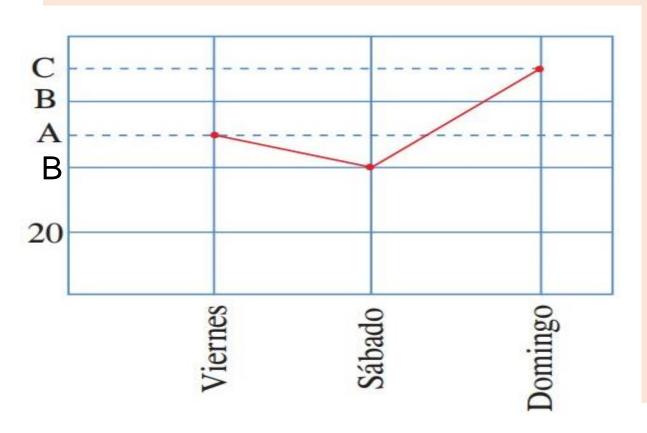
Luego: 
$$G = \frac{tany}{cotx} + senx.secy$$

$$G = \frac{\cot x}{\cot x} + \operatorname{senx.cscx}$$

$$G = 1 + 1$$

$$\cdot$$
 G = 2

La gráfica muestra las temperaturas ( en C° ), registradas al mediodía en la ciudad de Piura, los días viernes, sábado y domingo de la primera semana de febrero.



Donde: 
$$A = 16 \csc^2\left(\frac{81\pi}{4}\right)$$

$$B = 62 \operatorname{sen}\left(\frac{13\pi}{6}\right)$$

$$C = 18 \sec\left(\frac{19\pi}{3}\right)$$

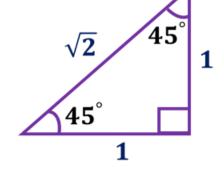
¿Cuál es el promedio de las temperaturas?

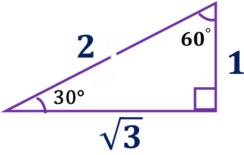
### **RESOLUCIÓN**

$$A = 16 \csc^2 \left(\frac{1\pi}{4}\right) = 16 \left(\sqrt{2}\right)^2 = 32$$

$$B = 62 \operatorname{sen}\left(\frac{1\pi}{6}\right) = 62\left(\frac{1}{2}\right) = 31$$

$$C = 18 \sec\left(\frac{1\pi}{3}\right) = 18(2) = 36$$





## Para reducir arcos de la forma $\left(\frac{a\pi}{b}\right)$ , donde a>2b

### **Efectuamos:**

### Luego:

$$\mathsf{RT}\!\left(\,\frac{\mathsf{a}\pi}{\mathsf{b}}\,\right) = \mathsf{RT}\!\left(\,\frac{\mathsf{r}\pi}{\mathsf{b}}\,\right)$$

**Luego : Promedio** = 
$$\left(\frac{32 + 31 + 36}{3}\right)^{0}$$
 C

$$\therefore$$
 Promedio = 33°C

