How to simplify boolean formulas using mathematica.

```
In[4]:= f = Or [h1 == 11&&h0 ≠ 11&&h1 == 10&&h0 ≠ 10&&h0 ≠ h1,
    h0 == 11&&h0 ≠ 10&&h0 == h1,
    h1 == 11&&h0 ≠ 11&&h1 ≠ 10&&h0 ≠ 10&&h0 ≠ h1];

FindInstance[f, {h0, h1, 10, 11}, Booleans]

Out[5]= { {h0 → True, h1 → False, 10 → False, 11 → False} }

BooleanMinimize[f]

Out[6]= (h0 == h1&&h0 ≠ 10&&h0 == 11) || (h0 ≠ h1&&h0 ≠ 10&&h0 ≠ 11&&h1 == 11)

In[7]:= FullSimplify[f]

Out[7]= (h0 == h1 || h0 ≠ 11) &&h0 ≠ 10&&h0 ≠ h1, h1 == 11)

In[8]:= f = Or [h1 == 11&&h0 == 10&&h0 ≠ h1, h1 == 11&&h0 == h1];

FullSimplify[f]

Out[9]= h0 == 10&&h1 == 11
```

How to count using mathematica. The first cell counts a formula without projection. sharpSat reports an exact count after 37 seconds, where *Mathematica* run out of memory after a few minutes (process is killed by the kernel). The second cell counts a formula with projection. See the cnfToMath.py script for more details on how to convert from the DIMACS CNF file to a *Mathematica* expression.

```
In[62]:= booleanExpr = << "~/workspace/bvcount/inputs/s-rsa-1.smt2 .cnf.m ";
    (*booleanExpr = << "~/workspace/bvcount/inputs/test.m "*)
    SatisfiabilityCoun[booleanExpr] // AbsoluteTiming

In[62]:=
    booleanExpr = << "~/workspace/bvcount/inputs/s-rsa-10.smt2 .cnf.m ";
    projection = << "~/workspace/bvcount/inputs/s-rsa-10.smt2 .cnf.proj.m ";
    SatisfiabilityCoun[booleanExpr, projection] // AbsoluteTiming</pre>
```

As you can see, SatisfiabilityCount doesn't work when we specify a projection set distinct from the set of all boolean variables in the formula.

```
\label{eq:confor} $$\inf_{[65]=} $ SatisfiabilityCounfor[x && y && z, x || y], \{x,y\}]$$ Out[65]= $ SatisfiabilityCounf(x && y && z) || x || y, \{x,y\}]$$
```

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 $\label{eq:local_local_local_local} $$ \ln[66]:= $$ SatisfiabilityCountor[x && y && z, x || y], \{x,y,z\}]$$

Out[66]= 6