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Motivation

Attention mode

Learning a bette graph Miscellaneous

Data

Results

Graph Neural Network Approaches to EHR Data

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Overview

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- Motivation
- Models
 - MPNNs
 - Attention models
 - Learning a better graph
 - Miscellaneous
- Data
- Results

Motivation

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Motivation

Survey information-theoretic approaches to structuring and learning from the same EHR dataset

- Learning from a graph structure
- Learning the structure itself
- Generating a better structure
- More complex organization/representation

General terminology

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- ullet Consider a graph $\mathcal{G} = \{\mathcal{V}, \mathcal{E}\}$
- ullet Nodes ${\mathcal V}$ represented by feature matrix ${\mathcal X}$, class vector ${\mathcal Y}$
- Adjacency matrix A
- Embeddings of feature vectors in latent space = H
- ullet Standard nonlinear activation function σ
- Trainable parameters W (and sometimes b)

HORDE

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Results

Construct a multi-modal EHR graph

- Graph contains multiple classes of node: patient, event, and concept
- Patients are connected to concepts and events that relate to their hospital visits
- Graph varies in time (discrete visit sequence)
- Edges $\mathcal{E} = \{\mathcal{E}_t\}_{t=0}^n$
- Time-invariant embeddings computed through MPNN process:

$$h_i^l = \sigma(\sum_{v_j \in \mathcal{V}_{inv}} rac{h_j^{l-1} \mathcal{W}_{inv}^l}{|\mathcal{N}(v_i)| \cdot |\mathcal{N}(v_j)|})$$

 Time-variant node embeddings updated using MPNN, then passed through LSTM

LSTM-GNN

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The majority of diseases and procedures occur relatively infrequently

- Connect similar cases in a graph of patients
- A becomes \mathcal{M} , a relatedness matrix

$$\mathcal{M}_{ij} = a \sum_{\mu=1}^{m} (\mathcal{D}_{i\mu} \mathcal{D}_{j\mu} (d_{\mu}^{-1} + c)) - \sum_{\mu=1}^{m} (\mathcal{D}_{i\mu} + \mathcal{D}_{j\mu})$$

- ullet $\mathcal D$ is a row matrix of diagnoses
- MPNN neighborhood is chosen using k most related neighbors
- Hyperparameters a, c, k

LSTM-GNN

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- X is divided into X_{var} and X_{inv} , time-variant and time-invariant
- Time-variant features are fed into LSTM, invariant to a GCN
- Embeddings concatenated and classified by a FCN

Attention models

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Adjacency matrix not known a priori

- Learn edges using the transformer architecture
- There are several self-attention mechanisms

GCT

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First application of the transformer to a graph

- A is naively initialized with conditional probabilities of co-occurrence
- \bullet Some connections are forbidden: operations at each step are multiplied by mask M

$$\hat{A}^{(j)} = \operatorname{softmax} \big(\frac{C^{(j-1)} W_Q^{(j)} (C^{(j-1)} W_K^{(j)})^T}{\sqrt{d}} \cdot M \big)$$

C represents output of last encoding

VGNN

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Key advance: variational

- Features passed through embedding: $X \rightarrow H$
- Model learns distribution $p(z_i | h_i)$
- Sample from $q(\hat{h}_i \mid z_i)$
- K-head attention predicts \widehat{A}
- Attention coefficients $e_{ij} = \sigma(a^T[Wh_i \mid\mid Wh_j])/\sqrt{dim(h_i)}$

$$\bullet \ A_{ij} = \frac{e \times p(e_{ij})}{\sum\limits_{p \in N(i)} e \times p(e_{ip})}$$

•
$$H^{(l+1)} = FFN [A^{(l)}(H^{(l)}W^{(l)} + b^{(l)})]$$

GRAM

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Results

Key advance: new hierarchical structure

- Concept nodes are placed in a DAG, where depth encodes specificity
- MPNN creates embeddings for concepts
- Visits are represented by a row matrix of concept vectors
- Sequence of visit embeddings passed through RNN, final output is a softmax disease prediction

GraphSMOTE

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Key advance: node interpolation

- GraphSAGE layer creates embeddings
- Add more nodes of a highly underrepresented class

$$h_{v'}^1 = (1 - \delta) \cdot h_v^1 + \delta \cdot h_{nn}^1,$$

Predict edges for new nodes:

$$E(u, v) = \operatorname{softmax}(\sigma(h_v^1 \cdot S \cdot h_u^1)),$$

Final embeddings are passed through one MPNN and one linear layer

RioGNN

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Key advance: iterative node deletion

Penalize dissimilar embeddings within a class using similarity

$$\mathcal{S}(u,v)=1-\mathcal{D}(u,v),$$

- We define a Markov Decision Process with an action space of node and edge deletions
- Reward function is the average similarity of a neighborhood
- After pruning, the model uses one MPNN layer to update embeddings
- Repeated over several layers
- Similarity is fed into loss

Walk-GNN

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Key advance: a new kind of recommender system

- Construct a knowledge graph of patient and concept nodes
- Agent walks along graph
- Define an MDP, state space $s_t = \{p_e, e_t, h_t\}$
- Action space $a_t = (r_{t+1}, e_{t+1})$ (walking to a new node).
- Reward function prioritizes walking to disease nodes that match diagnosis
- ullet Agent learns optimal walk policy π_t

EHR Datasets

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MODES

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Two main datasets used in medical ML

- MIMIC-III contains information over three years at Beth Israel Hospital
- ullet elCU contains information from same time period from 300+ ICUs across the US
- Deidentified, tagged patient records, including encounters, admission data, prescriptions, lab results and formal diagnoses
- Newer versions of the dataset include doctors' notes in natural language

Results

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Model	AUPRC
HORDE [1]	0.433
LSTM-GNN [2]	0.386
GCT [3]	0.581
VGNN [4]	0.603
GRAM [5]	0.575
RioGNN [7]	0.572*

^{*}Provided their own MIMIC matrix, not standard

Takeaways

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- Graph RL has huge potential in health record analysis
- New approaches continue to arise
- ML outperforms humans at constructing knowledge graphs
- No need to constrain to traditional MPNNs

References

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The End