## **Graph Theory – Classifying Graphs**

Graph: collection of vertices and edges

**Path from x to y:** list of vertices in which successive vertices are connected by edges: SB-MK-F1

**Simple Path**: a path in a graph which does not have repeating vertices (e.g. SpongeBob-Gary-Karen).

**Cycle**: a simple path of edges and vertices wherein a vertex is reachable from itself (e.g. Gary-Patrick-Karen-Gary).

**Simple Graph**: doesn't contain multiple edges between nodes nor loops. A **simple directed graph** has no multiple arrows with same source and target nodes

**Connected graph**: path exists from every vertex to every other vertex

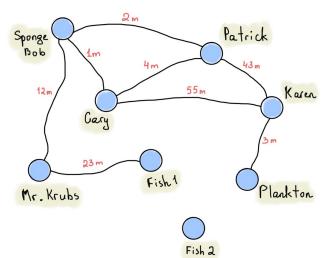
**Unconnected graph**: a graph that is not connected and is made up of connected components

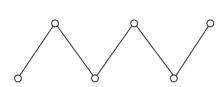
**Tree:** An undirected graph in which any two vertices are connected by exactly one path.

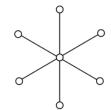
I.e. a connected acyclic undirected graph. I.e. a connected graph that does not contain even a single cycle.

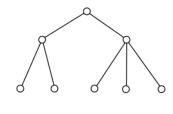


## A simple undirected weighted cyclic graph:

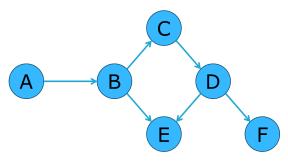








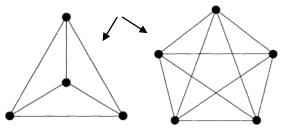
**Directed Acyclic Graph (DAG):** a directed graph with no cycles

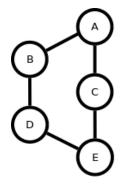


Cyclic Graph: A graph with at least one cycle.

Circular Graph: A graph that is a cycle.

Complete Graph: A simple graph in which each pair of distinct vertices are adjacent.





**Adjacency matrix:** matrix containing 1's and 0's indicating an existing directed edge between vertices. 1 = edge exists, 0 = edge does not exist