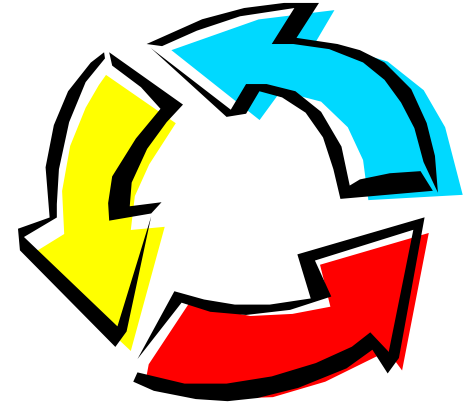


Recursion

Lab 09 and 10

Recursion



**Recursion occurs
when a method calls
itself.**

Recursion

```
public class RecursionOne
{
    public void run(int x)
    {
        out.println(x);
        run(x+1);
    }
    public static void main(String args[] )
    {
        RecursionOne test = new RecursionOne();
        test.run(1);
    }
}
```

Will it stop?



OUTPUT

1
2
3
4
5

.....

stack overflow

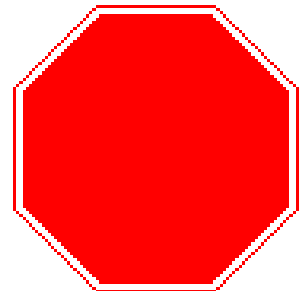
open

recursionone.java

Base Case

A recursive method must have a stop condition/ base case.

Recursive calls will continue until the stop condition is met.



Recursion 2

```
public class RecursionTwo
```

```
{
```

```
    public void run(int x )
```

```
    {
```

```
        out.println(x);
```

```
        if(x<5) ←
```

```
            run(x+1);
```

```
    }
```

```
    public static void main(String args[] )
```

```
    {
```

```
        RecursionTwo test = new RecursionTwo();
```

```
        test.run(1);
```

```
    }
```

```
}
```

base case
It will stop!

OUTPUT

1
2
3
4
5



Recursion 3

```
public class RecursionThree
```

```
{
```

```
    public void run(int x )
```

```
    {
```

```
        if(x<5)
```

← **base case**

```
            run(x+1);
```

```
            out.println(x);
```

```
    }
```

```
    public static void main(String args[] )
```

```
    {
```

```
        RecursionThree test = new RecursionThree ();
```

```
        test.run(1);
```

```
    }
```

```
}
```

OUTPUT

5

4

3

2

1

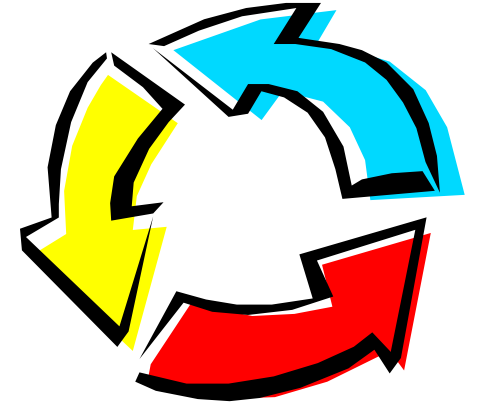


open

recursiontwo.java

recursionthree.java

Recursion



Recursion is basically a loop that is created using method calls.

```
class DoWhile
```

```
{
```

```
    public void run( )
```

```
    {
```

```
        int x=0;
```

```
        do{
```

```
            x++;
```

```
            out.println(x);
```

```
        }while(x<10);    //condition
```

```
    }
```

```
    public static void main(String args[] )
```

```
    {
```

```
        DoWhile test = new DoWhile();
```

```
        test.run( );
```

```
    }
```

```
}
```

do while

open dowhile.java

The Stack

When you call a method, an activation record for that method call is put on the stack with spots for all parameters/arguments being passed.

The Stack

AR1- method() call

The Stack

AR2- method() call

AR1- method() call

The Stack

AR3- method() call

AR2- method() call

AR1- method() call

The Stack

AR4- method() call

AR3- method() call

AR2- method() call

AR1- method() call

The Stack

AR3- method() call

AR2- method() call

AR1- method() call

The Stack

AR2- method() call

AR1- method() call

The Stack

As each call to the method completes, the instance of that method is removed from the stack.

AR1- method() call

Recursion 2

```
public class RecursionTwo
{
    public void run(int x )
    {
        out.println(x);
        if(x<5)
            run(x+1);
    }
    public static void main(String args[] )
    {
        RecursionTwo test = new RecursionTwo();
        test.run(1);
    }
}
```

base case
It will stop!

OUTPUT

1
2
3
4
5



Recursion 3

```
public class RecursionThree
{
    public void run(int x )
    {
        if(x<5) ← base case
            run(x+1);
            out.println(x);
    }
    public static void main(String args[] )
    {
        RecursionThree test = new RecursionThree();
        test.run(1);
    }
}
```

OUTPUT

5
4
3
2
1

Why does this output differ from recur2?



Tracing Recursive Code

```
int fun(int y)
{
    if(y<=1)
        return 1;
    else
        return fun(y-2) + y;
}
```

```
//test code in client class
out.println(test.fun(5));
```

AR3

y
1 return 1

AR2

y
3 return AR3 + 3 **4**

AR1

y
5 return AR2 + 5

9

Tracing Recursive Code

```
int fun( int x, int y)
{
    if( y < 1)
        return x;
    else
        return fun( x, y - 2) + x;
}
```

```
//test code in client class
out.println(test.fun(4,3));
```

AR3

x	y	
4	-1	return 4



AR2

x	y	
4	1	return AR3 + 4



8

AR1

x	y	
4	3	return AR2 + 4



12

open

recursionfour.java

recursionfive.java

Recursive Fun

```
int fun(int x, int y)
{
    if ( x == 0 )
        return x;
    else
        return x+fun(y-1,x);
}
```

OUTPUT

16

What would fun(4,4) return?

open

recursionsix.java

split recursion

tail recursion

```
public String recur(String s)
{
    int len = s.length();
    if(len>0)
        return recur(s.substring(0,len-1)) +
                    s.charAt(len-1);
    return "";
}
```

split recursion

tail recursion

```
public String recur(String s)
{
    int len = s.length();
    if(len>0)
        return s.charAt(len-1) +
               recur(s.substring(0,len-1));
    return "";
}
```

open

recursionseven.java

recursioneight.java

split recursion

tail recursion

The Stack

call out.println(recur("abc"))

```
public String recur(String s)
{
    int len = s.length();
    if(len>0)
        return recur(s.substring(0,len-1)) +
                    s.charAt(len-1);
    return "";
}
```

The Stack

call out.println(recur("abc"))

AR stands for activation record. An **AR** is placed on the stack every time a method is called.

AR1 – s="abc"
return AR2 + c

The Stack

AR2 – s="ab"
return AR3 + b

AR1 – s="abc"
return AR2 + c

The Stack

AR3 – s="a"
return AR4 + a

AR2 – s="ab"
return AR3 + b

AR1 – s="abc"
return AR2 + c

The Stack

AR4 – s=""
return ""

AR3 – s="a"
return AR4 + a

AR2 – s="ab"
return AR3 + b

AR1 – s="abc"
return AR2 + c

The Stack

AR3 – s="a"
return a

AR2 – s="ab"
return AR3 + b

AR1 – s="abc"
return AR2 + c

The Stack

AR2 – s="ab"
return ab

AR1 – s="abc"
return AR2 + c

The Stack

call out.println(recur("abc"))

OUTPUT

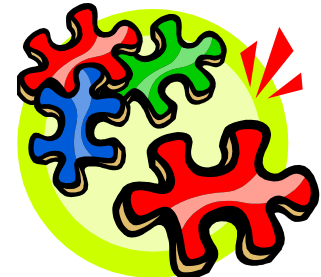
abc

AR1 – s="abc"
return abc

What is the point?

If recursion is just a loop, why would you just not use a loop?

Recursion is a way to take a block of code and spawn copies of that block over and over again. This helps break a large problem down into smaller pieces.



Counting Spots

If checking 0 0, you would find 5 @s are connected.

@	-	@	-	-	@	-	@	@	@
@	@	@	-	@	@	-	@	-	@
-	-	-	-	-	-	-	@	@	@
-	@	@	@	@	@	-	@	-	@
-	@	-	@	-	@	-	@	-	@
@	@	@	@	@	@	-	@	@	@
-	@	-	@	-	@	-	-	-	@
-	@	@	@	-	@	-	-	-	-
-	@	-	@	-	@	-	@	@	@
-	@	@	@	@	@	-	@	@	@

@ at spot [0,0]

@ at spot [0,2]

@ at spot [1,0]

@ at spot [1,1]

@ at spot [1,2]

The exact same checks
are made at each spot.

Counting Spots

**if (r and c are in bounds and
current spot is a @)**

mark spot as visited

bump up current count by one

recur up

recur down

recur left

recur right

**This same block of
code is recreated with
each recursive call.
The exact same code is
used to check many
different locations.**

Counting Spots

if (r and c are in bounds and
current spot is a @)

mark spot as visited

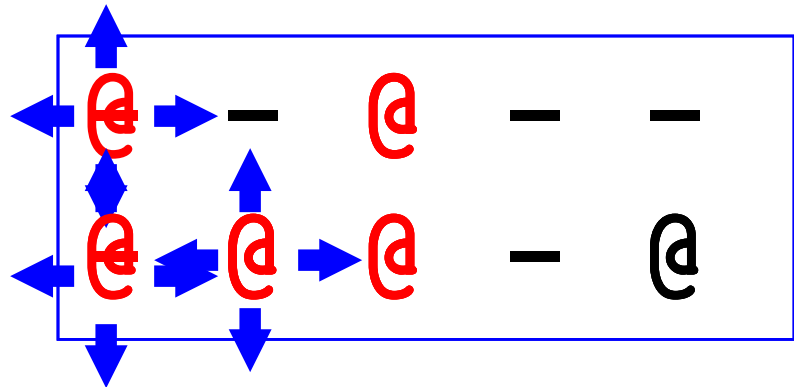
bump up current count by one

recur up

recur down

recur left

recur right



Start work on Lab 09

Advanced Recursion

Mazes

Mazes

Maze problems are very common programming problems.

```
* * * * *
* . . . . *
* . . * * *
* S . . . *
* . . . E *
* * * * *
```

. are paths

*** are walls**

In some cases, you are provided with a symbol for the start and a symbol for the exit.

Mazes

Maze problems are very common programming problems.

```
. * * * * *  
. . . . .  
* . . * . .  
* . * * * *  
* . * . . *  
* * . * . .
```

. are paths

*** are walls**

Other times, you start at 0,0 and must check to see if you can get to length-1, length-1.

Maze Solving

```
void search(int row, int col)
{
    if (row >= 0 && col >= 0 && row < maze.length &&
        col < maze[r].length && maze[row][col] == 1)
    {
        if (col == maze[r].length - 1) {
            exitFound = true;
        }
        else {
            maze[row][col] = 0; //marking
            search(row+1, col);
            search(row-1, col);
            search(row, col+1);
            search(row, col-1);
        }
    }
}
```

1	0	1	1	1
0	1	1	1	1
1	1	1	1	0
0	0	0	0	1
0	0	1	1	0

Marking / UnMarking

In some situations, you want to make changes to the maze temporarily. For instance, if you are trying to determine the shortest path, you have to find all paths and determine which path is the shortest. Each time to you search the maze for a path, the maze must be in its original state.

Marking / UnMarking

```
void search(int row, int col)
```

```
{
```

```
    if (row >= 0 && col >= 0 && row < maze.length &&  
        col < maze[r].length && maze[row][col] == 1)
```

```
    {
```

```
        if (col == maze[r].length - 1) {  
            exitFound = true;
```

```
        }
```

```
        else {
```

```
            maze[row][col] = 0;  //marking
```

```
            search(row+1, col);
```

```
            search(row-1, col);
```

```
            search(row, col+1);
```

```
            search(row, col-1);
```

```
            maze[row][col] = 1;  //unmarking ( set it back )
```

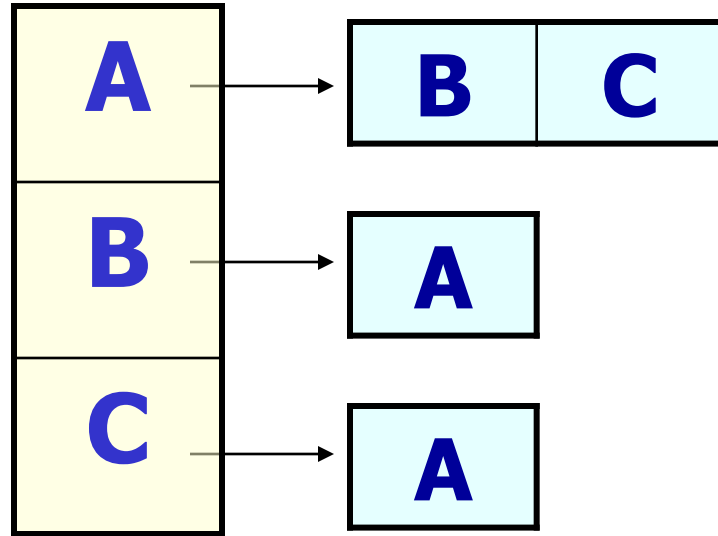
```
        }
```

```
    }
```

```
}
```

connections

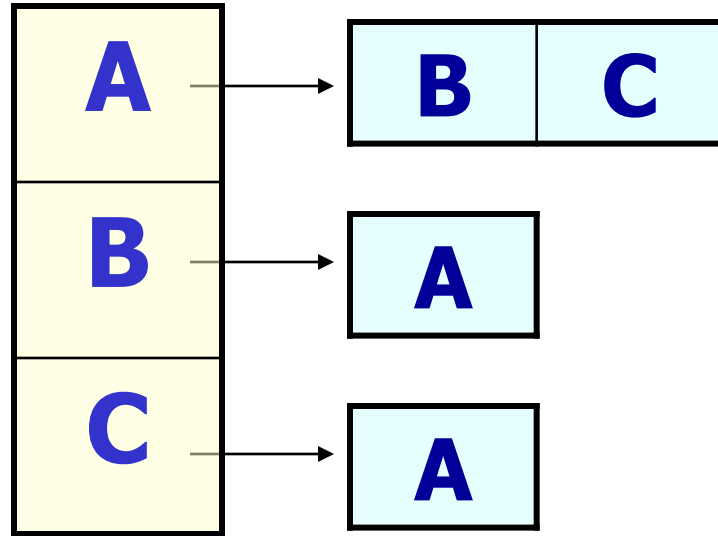
Connections



Connection problems require you to check for a path between 2 items.

Is A directly connected to C? YES

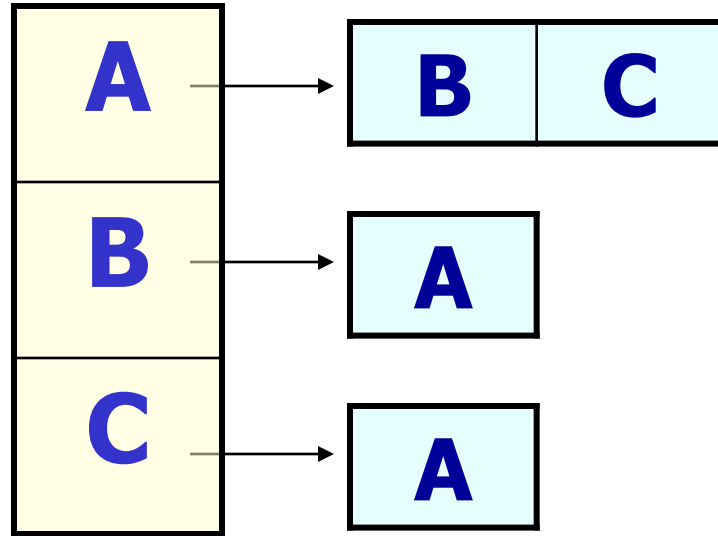
Connections



Connection problems require you to check for a path between 2 items.

Is B directly connected to C? NO

Connections



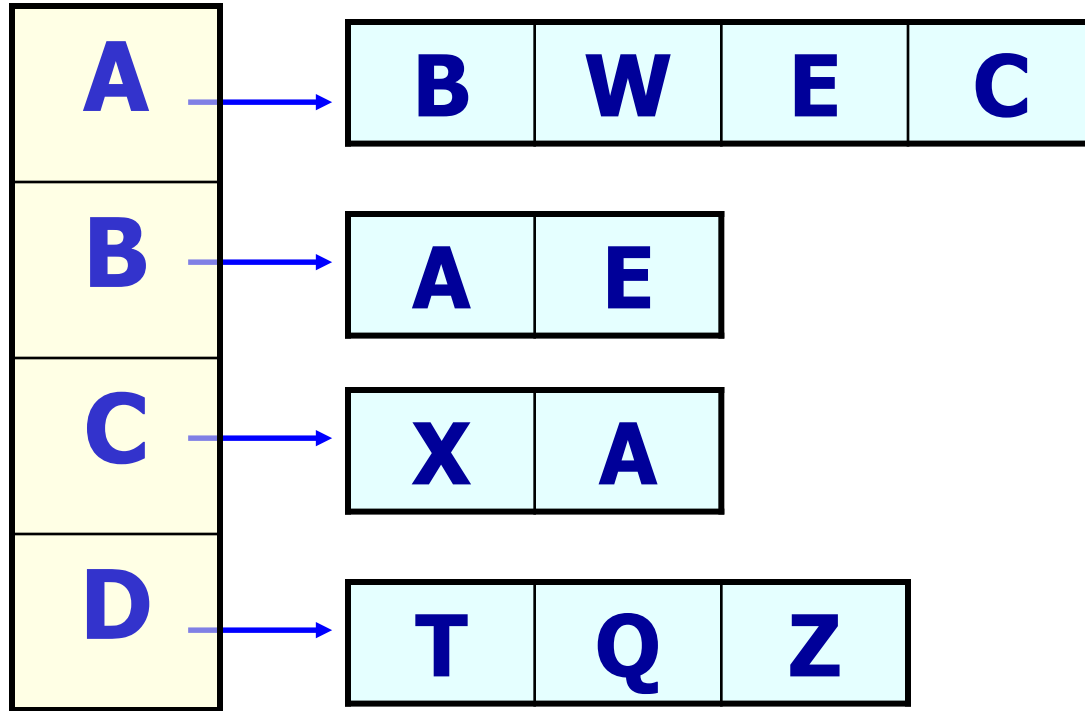
A is directly connected to B and C.

B is directly connected to A.

C is directly connected to A.

Is B connected to C? YES

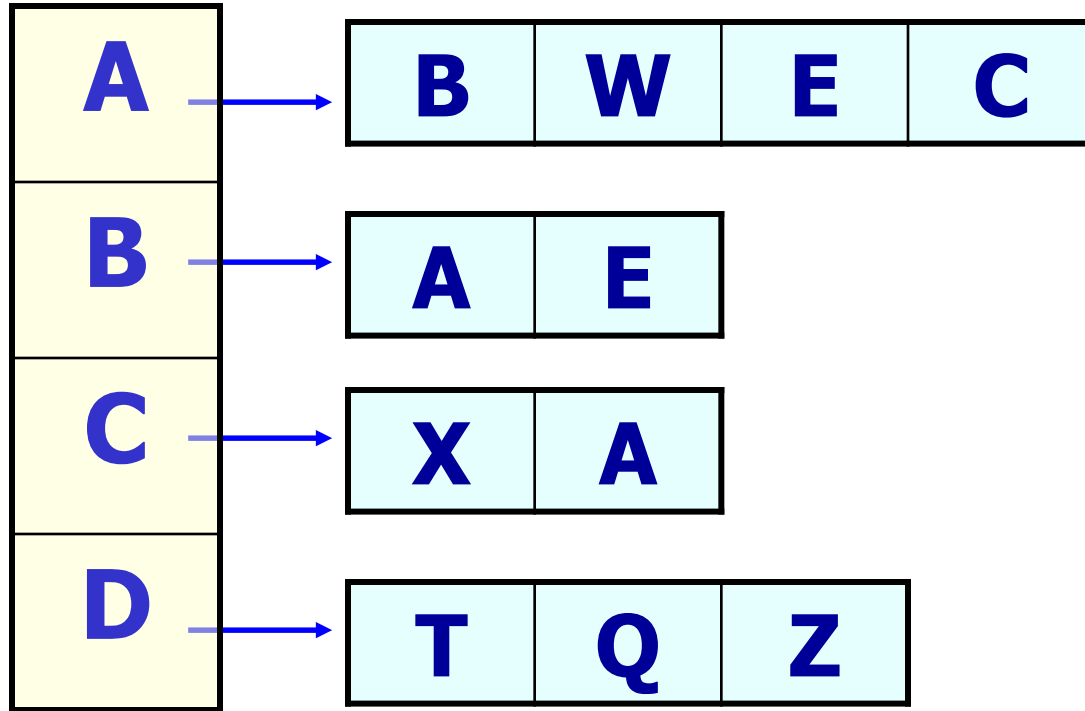
Connections



Is A connected to X? **YES**

Is A connected to Q? **NO**

Connections



```
TreeMap<Character, String> map;
```

```
TreeMap<Character, Set> map;
```

Connections

```
check(String one, String two, String list)
{
    if a direct connection exists between one and two
        we have a match
    else
    {
        get the current list of connections for one
        loop through all of the connections
        if you have not checked the current spot
            add current spot to list
            check to see a connection exists between spot
                and the destination ( recursive call )
    }
}
```


Start work on Lab 10