

# Written Homework

## Written Homework

**Problem 1** Consider the function

$$f(x, y, z) = \frac{4}{\sqrt{9 - x^2 - y^2 - z^2}}.$$

- (a) What is the domain of  $f$ ? Describe this domain as a region in  $\mathbb{R}^3$ .
- (b) What is the range of  $f$ ?

**Problem 2** Consider the function

$$f(x) = x^2 + y^2 - 4.$$

- (a) Draw at least five level curves of  $f$ .
- (b) Use these level curves to sketch the graph of  $f$ .

**Problem 3** Draw the graph of the surface in  $\mathbb{R}^3$  determined by the equation

$$x = y^2/4 - z^2/9.$$

Use level curves and/or sections to justify why your drawing is correct.

## Professional Problem

**Problem 4** (a) Consider the function  $g : \mathbb{R}^3 \rightarrow \mathbb{R}$  given by

$$g(x, y, z) = x^2 + y^2.$$

Draw at least three level surfaces of  $g$ , which will be surface in  $\mathbb{R}^3$ . What do you notice about these level surfaces?

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Learning outcomes:  
Author(s):

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- (b) Suppose you have a function  $g : \mathbb{R}^3 \rightarrow \mathbb{R}$ , such that  $g$  depends on  $x$  and  $y$ , but does not depend on  $z$ . What can you say about the level surfaces of  $g$ ?
  - (c) Suppose you have a function  $g : \mathbb{R}^3 \rightarrow \mathbb{R}$ , such that  $g$  depends on  $y$  and  $z$ , but does not depend on  $x$ . What can you say about the level surfaces of  $g$ ?
  - (d) Suppose you have a function  $g : \mathbb{R}^3 \rightarrow \mathbb{R}$ , such that  $g$  depends on  $x$ , but does not depend on  $y$  or  $z$ . What can you say about the level surfaces of  $g$ ?
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