

Magnetic properties

UNIT III

(1)

Introduction: Magnetic materials play an important role in Industrial & scientific research fields. Based on the response of materials in the external field, they are classified into 3 categories: Dia, Para, Ferromagnetic which are further classified into 5 important groups depending on the alignment of magnetic moments within the material. Thus they are known as.

1. Diamagnetic, 2. Paramagnetic, 3. Ferromagnetic
4. Antiferromagnetic, 5. Ferrimagnetic

Basic Definition:

Magnetism: The Attracting property exhibited by the magnet is known as magnetism.

Bohr Magnet: The magnetic moment contributed by an e^- with angular momentum $n=1$ is known as Bohr magneton.

$$\mu_B = \frac{eh}{2m} = 9.27 \times 10^{-24}$$

magnetic susceptibility: It is defined as the intensity of magnetization produced in the substance per unit magnetic field strength

$$\chi = \frac{M}{H}$$

magnetic permeability: measures degree to which the magnetic field can penetrate through the substance.

$$\mu = \frac{B}{H}$$

medium

$$\mu_0 = \frac{B_0}{H}$$

free space

Relative permeability (μ_r):- $\mu_r = \frac{\mu}{\mu_0}$, $M = H(\mu_r - 1)$

$$B = \mu_0 (H + M)$$

magnetic dipole moment: $M = IA$

magnetic field strength (H):- The force experienced by a unit north pole at any pt in the field is called magnetic field strength.

magnetic induction field strength & Magnetic flux density (B):- The no of magnetic lines of force passing through the unit area of cross section is called magnetic flux density

$$B = \frac{\Phi}{A}$$

classification of magnetic materials

The different types of magnetic materials are:

① Diamagnetic materials: These substances which when placed in magnetic field acquire weak magnetism opposite to the direction of the field known as diamagnetic materials

Properties

1. These materials are repelled by the magnets
2. When the diamagnetic materials is suspended in a uniform magnetic field (H) they set their longest axis at right \perp to field
3. In a non-uniform H, these substances move from stronger parts of the field to weaker parts

4. $B_{in} < B_{out}$



5. χ is -ve, $\chi = \frac{M}{H} = -1$

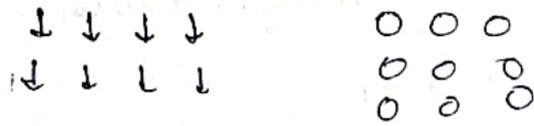
6. χ is independent of Temp.

7. $\mu_r < 1$

8. Diamagnetic do not have permanent dipoles

9. In an external field H , the orbital motion of e^- undergoes changes & the atoms acquire induced magnetic field is opp to field. (2)

The induced dipoles & magnetization vanishes as soon as field is removed.

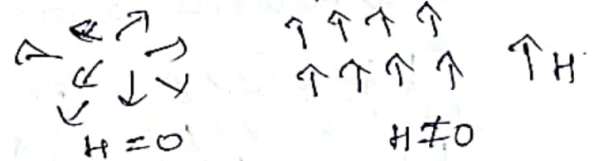


$H \neq 0$

$H = 0$

ex: Bismuth, Cu, gold, quartz, water, Alcohols, mercury
Paramagnetic materials: acquire weak magnetism

in the direction of the field.



Properties:

1. Paramagnetic materials have permanent dipoles
2. The dipoles are randomly oriented. Therefore the net magnetic moment is zero. In the presence of H dipoles are tending to align in the direction of the field.
3. χ is +ve & $\chi \propto \frac{1}{T}$
 $\chi = \frac{C}{T} > 1$
 \hookrightarrow Curie's const
4. $B_{in} > B_{out}$, Paramagnetic materials are attracted by magnets
5. $\mu_r > 1$ ex: Aluminium, Platinum, Cr, Mn, $CuSO_4$, etc

Ferromagnetic materials: substances which when placed in H become strongly magnetized in the direction of the field is known as ferromagnetic

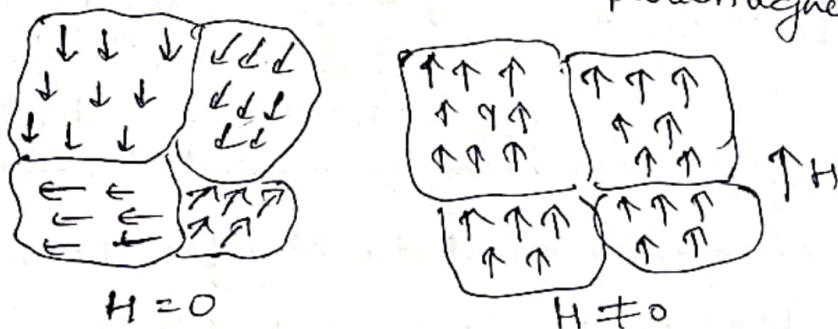
Properties

- 1 strongly attracted by magnets
- 2 $B_{in} \gg B_{out}$, $\mu_r \gg 1$

3. materials have permanent dipoles.
4. Dipoles are \parallel to each other within the domains
5. The net magnetic moment is zero due to intermolecular field
6. The spin magnetic moments of unpaired e^- are responsible for it. They have spontaneous magnetization.
7. χ is very large depends on Temp.

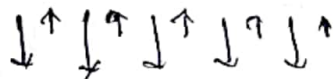
$$\chi = \frac{C}{T - \theta} \gg 1$$

When Temp increases its χ decreases & shows paramagnetic behaviour above the paramagnetic curve Temp θ .



ex: Iron, cobalt, nickel & no of alloys

Ferrimagnetic materials: The materials which consist of Anti parallel magnetic moments of different magnitude.



Properties: 1. strongly attracted by magnets

2. $B_m \gg B_{ext}$ $M_r \gg 1$

3. possess permanent dipoles

4. χ is very high & +ve for ferrimagnetic materials

$$5. \chi = \frac{C}{T \pm \theta}$$

ex: Pb Fe₁₂O₁₉, pyrrhotite Fe_{1-x}S.

Iron oxides with other elements as Al, Co, Ni

3

Antiferromagnetic materials: which consists of Antiparallel magnetic moments of equal magnitude

$\uparrow \downarrow \uparrow \downarrow \uparrow \downarrow \uparrow \downarrow$

- Properties:
1. These are attracted by magnets
 2. $B_{in} > B_{out}$ in Non uniform H , substances move from weaker parts to stronger parts
 3. $\chi = \frac{C}{T + \theta}$, $\theta_r > 1$ is very small
ex Alloys of Iron Fe Mn, NiO.

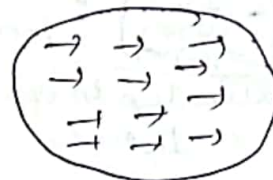
ferromagnetic domain theory

It states that ferromagnetic material consist of large no of small regions of spontaneous magnetisation called domains

- within each domain, the magnetic moments are



aligned parallel to one another $H=0$



$H \neq 0$

- the direction of magnetisation varies from domain to domain & thus M is zero when $H=0$
- when we apply an increasing H , initially, the areas of the domains which are parallel to field are increased. In the final saturation stage, the other domains are rotated parallel to field.
- the region of domain space is very small of order

process of magnetisation!

1. By motion of domain walls!

when small magnetic field is



$B=0$



weak B



Strong B

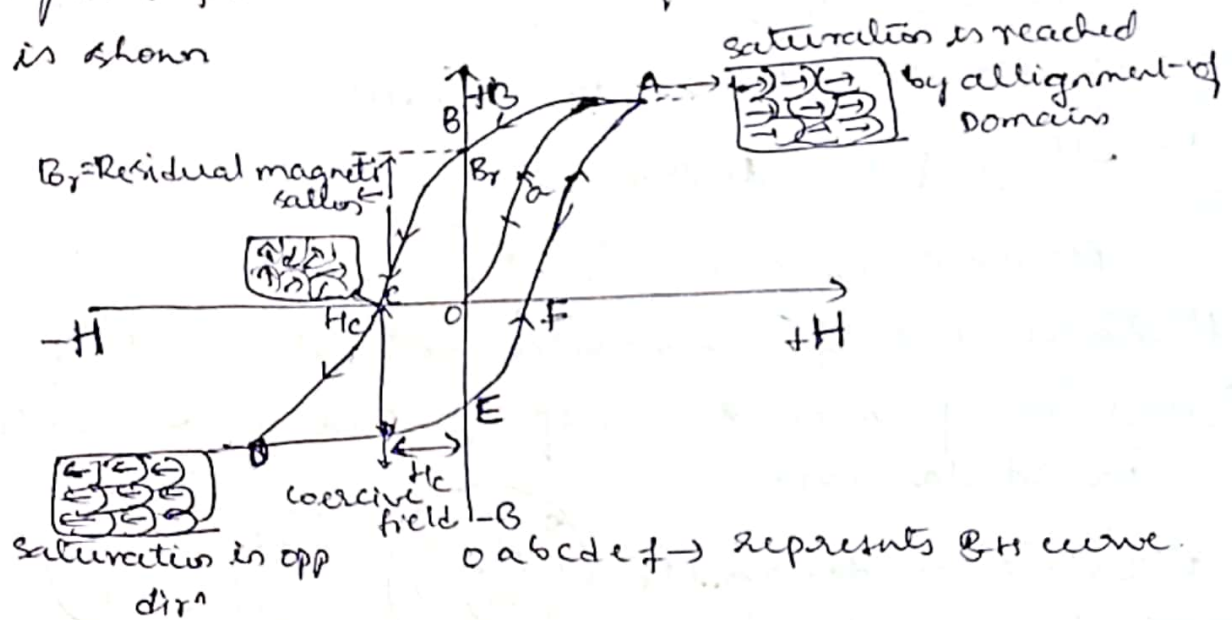
applied the domains of magnetisation either \parallel or nearly \parallel to field grow at the expense of others

By rotation of domains: domains rotates in the field dir.

Hysteresis on the basis of Domain Theory

Lagging of B behind H is called hysteresis.

When the specimen ferromagnetic material is placed in magnetic field. the variation of B with variation of H is shown



oa \rightarrow due to smaller reversible domain wall movement
ob \rightarrow due to small irreversible domain rotation.

When a field of small value H is applied, the domain walls are displaced & give rise to small magnetisation (oa) in graph.

At A all the domains aligned in the direction of H . no further enhancement is possible, therefore it attains saturation state.

NEXT, we decrease H & reduce it to zero. when $H=0$, $B \neq 0$. This represents the curve AB, is called Retentivity or Remanence. B_r (Residual magnetism). The domains are not completely randomized even though the external driving field has been removed.

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These domains are called irreversible domains.

This is due to small irreversible domain rotations.

Next, the ~~current~~ ^H in the solenoid is reversed & slowly increased. (This high reverse magnetic field can destroy the Retentivity). Certain domains are flipped until the net field inside stands nullified. This represents the curve BC. The value of H at C is called coercivity, H_c .

As the reversed H is increased in magnitude, we once again obtain saturation. The curve CD shows saturation.

Next H is reduced (curve DE) & reversed represents curve EF. It forms a cycle ABCDEF.

Thus the reversible & irreversible domain wall movements give rise to hysteresis in ferromagnetic materials.

NOTE! The curve OA, does not trace itself as H is reduced. For a given value of H, B is not unique it depends on previous history of the sample. This phenomenon is called Hysteresis.

Hysteresis Loss: When a ferromagnetic material is subjected to cycles of magnetisation, the domains of the material resist being turned first in one direction & then in the other direction. Energy is expended in the material to overcome this opposition; this loss in the form of heat is called hysteresis loss, effect is rise in Temp.

5. Hard and soft magnetic materials

Based on the area of hysteresis, ferro magnetic materials can be classified into soft and hard magnetic materials.

Soft magnetic materials

The magnetized materials which are easily magnetized and demagnetized are known as soft magnetic materials.

Properties:

Soft magnetic materials have small hysteresis loop area.

Soft magnetic materials have low hysteresis loss.

Soft magnetic materials have small retentivity values.

Soft magnetic materials have small coercivity values

Soft magnetic materials require low magnetic field for magnetization.

Soft magnetic materials have high values of susceptibility and permeability.

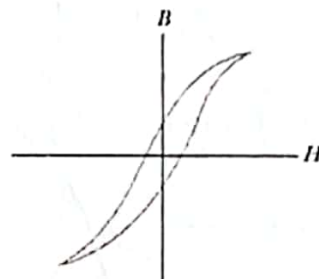
Examples:- Iron-silicon alloys, Nickel-iron alloys, Iron-cobalt alloys.

Applications:

They are used in electrical equipments and magnetic cores and transformers.

They are used in motors, relays and sensors.

They are used in microwave isolators.

**Hard magnetic materials**

The magnetized materials which are hard to magnetize and demagnetize are known as hard magnetic materials.

Properties:

Hard magnetic materials have large hysteresis loop area.

Hard magnetic materials have large hysteresis loss.

Hard magnetic materials have large retentivity values

Hard magnetic materials have large coercivity values

Hard magnetic materials require large magnetic field for magnetization

Hard magnetic materials have low values of susceptibility and permeability

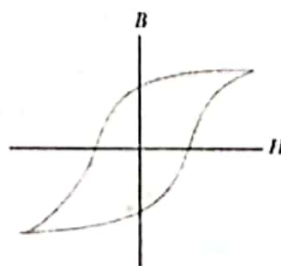
Examples:- carbon steel, tungsten steel, chromium steel.

Applications:

They are used into make permanent magnets.

They are used in dc meters and measuring devices.

They are used in speedometers and sensors in auto mobiles.



Dielectrics

Defn:

Dielectrics are non-conducting materials when kept in external field, they modify the electric field & themselves undergo some charges & start acting as stores of electric charges, such materials are dielectrics.

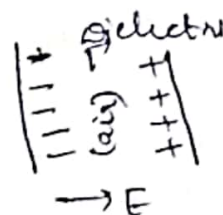
electrons are tightly bound to the nuclei of atoms as these are insulators. They have no (or negligible no of) charge carriers. However, when an external electric field is applied induced charges appear on the surface of the dielectric. The induced charges reduce the external electric field. The extent of effect depends on the nature of the dielectric. Dielectrics are so called because they can transmit electric field without actually conducting electricity.

Eg! glass, polymers, ceramics etc.

1) Dielectric material have dielectric constant.

$$K = \epsilon_r = \frac{\epsilon}{\epsilon_0} = \frac{C}{C_0}$$

$\xrightarrow{\text{Presence of dielectric}}$
 $\xrightarrow{\text{Absence of dielectric}}$

2)  \rightarrow capacitor is capable of storing charge hence electric energy, consists of two conducting surfaces separated by an insulating material.

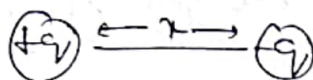
3) (K) dielectric const is independent of size & shape of dielectric material

4). Capacitance (ability of capacitor to store charges) depends on the presence of dielectrics

presence of dielectric $C = \frac{\epsilon_0 \epsilon_r A}{d}$
 or $C = \frac{\epsilon_0 K A}{d}$

in absence of dielectric $C_0 = \frac{\epsilon_0 A}{d}$

5). Electric dipole.



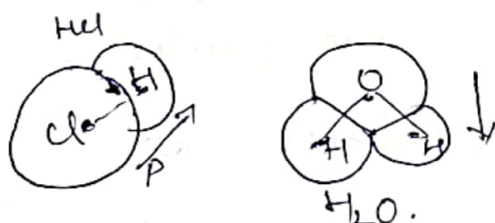
dipole moment $\mu = q \cdot r$

there are two types of dielectrics.

a) polar b) Non-polar.

a) Polar dielectrics: centres of +ve charge & the negative charge of each molecule do not coincide. \therefore molecules of polar dielectrics have permanent dipole moments such dielectrics are called polar dielectrics.

molecules like NH_3 , HCl & water, alcohol etc have asymmetric in shape. Due to finite separation b/w \oplus ve & \ominus ve charge centre, each molecule behave as electric dipole.



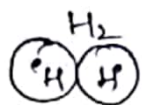
ϵ_r varies from 3-8.

even though these have permanent dipole moment due to random orientation ^{net} dipole moment decreases.

b) Non-polar dielectrics: centres of \oplus ve charge & \ominus ve charge coincide, therefore non-polar molecules possess do not possess permanent dipole moments. such dielectrics

are called Non-polar Dielectrics

eg: H_2 , CO_2 , N_2 , O_2 , CH_4 etc, in which \oplus & \ominus centres coincides makes zero separation, the dipole moment of such molecules is zero.

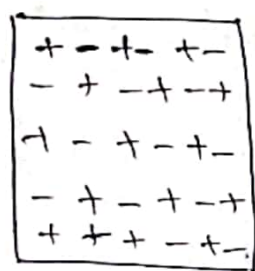


Symmetric molecules.

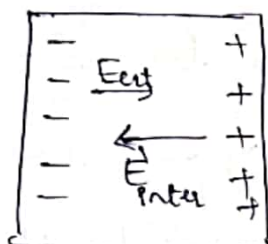
$$\epsilon_r = 1 \text{ to } 2.2$$

In the absence of ^{external} Electric field (\vec{E}) dipole moment is zero. However in the presence of \vec{E} , the polarization of the dielectric, (separation of \oplus & \ominus in the dirⁿ of \vec{E} , \ominus is in the opposite direction) takes place. These induced charges produce an Internal electric field that opposes the external electric field.

The result is that there is a reduction in external electric field within dielectric



$$E_{ext} = 0$$



$$E_{ext} \neq 0$$

Displacement of charges takes place

$$\text{Resultant } E = E_{ext} - E_{internal}$$

Polarization: The dipole moment developed per unit volume in a dielectric when placed in external electric field is called Polarization (P), also called Polarization density.

The induced dipole moment is in the direction of the field E , is proportional to the field strength.

$$\text{Polarization} = \frac{\text{Induced dipole moment}}{\text{volume}}$$

$$P = \frac{\mu}{V}$$

If N -Atoms are present

$$P = N\mu$$

[for unit volume $V=1$]

Induced dipole moment

$$\mu \propto \text{Ext. field}$$

$$\mu = \alpha E$$

where α is proportionality const called polarizability.

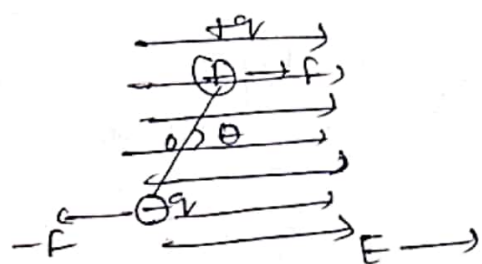
$$\therefore P = N\mu = N\alpha E$$

$$\langle P = N\alpha E \rangle$$

$$\text{or } P = \epsilon_0 \chi_e E$$

$\chi_e \rightarrow$ electric susceptibility

In case of polar molecules even though net dipole moment is present orientation random, when we apply uniform electric field experiences torque.

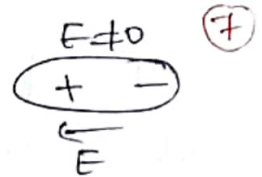
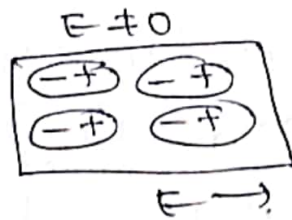
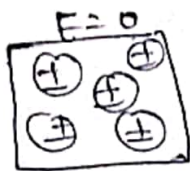


$$\text{Torque} = \mu E \sin \theta$$

θ is b/w μ & E

Types of Electric polarization

1) Electronic polarization:- Electronic polarization occurs due to the displacement of the \oplus ve charged nucleus & \ominus ve charged electrons of an atom in opposite direction of E .



$$P_e = N \alpha_e E_{ext}$$

$P_e \rightarrow$ electronic polarization

$\alpha_e \rightarrow$ electronic polarizability which is independent of Temp

WKT $P = \epsilon_0 (\epsilon_r - 1) E$

$$\epsilon_r - 1 = \frac{P}{\epsilon_0 E} \Rightarrow \epsilon_r = 1 + \frac{P}{\epsilon_0 E}$$

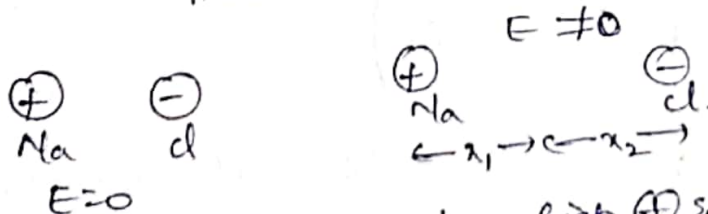
$$\epsilon_r = 1 + \frac{N \alpha_e E}{\epsilon_0 E}$$

$$\epsilon_r = 1 + \frac{N \alpha_e}{\epsilon_0}$$

$\alpha_e = 4\pi \epsilon_0 R^3 \rightarrow$ enclosed in a sphere of charge

or $P_e = N (4\pi \epsilon_0 R^3) E \rightarrow$ electronic polarization \rightarrow ①

2). Ionic/Atomic Polarization: occurs due to the displacement of cation & anion (\oplus & \ominus ions) in opposite direction by an electric field. occurs only in ionic solids.



x_1, x_2 is the distance to which \oplus & \ominus ions move apart from ϵ_r^m position

Interatomic distance changes when E is applied.

For the ion: restoring force $F \propto x_1$

$$F = \beta_1 x_1 \quad \left| \beta_1 = m\omega_0^2 \right.$$

(Kd)

$$eE = m\omega_0^2 x_1 \rightarrow (1) \Rightarrow x_1 = \frac{eE}{m\omega_0^2}$$

$$\text{Similarly } \ominus \text{ve ion } F = \beta_2 x_2 \quad \left| \beta_2 = M\omega_0^2 \right.$$

$$F = M\omega_0^2 x_2 \rightarrow (2) \Rightarrow x_2 = \frac{eE}{M\omega_0^2}$$

Add (1) & (2)

$$x_1 + x_2 = \frac{eE}{\omega_0^2} \left\{ \frac{1}{m} + \frac{1}{M} \right\}$$

$$\mu_p = e(x_1 + x_2)$$

Induced dipole moment = magnitude \times displacement

$$\mu_p = \frac{e^2 E}{\omega_0^2} \left\{ \frac{1}{m} + \frac{1}{M} \right\}$$

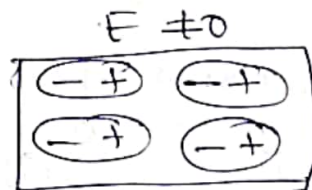
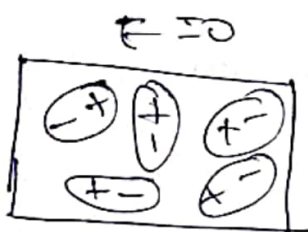
$$\mu_p = \chi_p E$$

\rightarrow for frequencies of constituent ions

$$\chi_p = \frac{e^2}{\omega_0^2} \left\{ \frac{1}{m} + \frac{1}{M} \right\}$$

$$P_p = N\chi_p E = N \frac{e^2}{\omega_0^2} \left\{ \frac{1}{m} + \frac{1}{M} \right\} E \rightarrow (2)$$

3) Orientation Polarization: arises due to presence of polar molecules in the dielectric medium.



when E is applied the portion align themselves in the direction of field & are in opposite direction, this kind of polarization is called as orientation polarization.

this depends on Temp. when T increases thermal energy tends to randomize alignment.

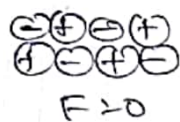
$$P_0 = N \kappa_0 \vec{E}$$

$$\kappa_0 = \frac{\mu^2}{3k_B T}$$

$$\therefore \langle P_0 = \frac{N \mu^2 E}{3k_B T} \rangle \rightarrow (3)$$

By Langevin's theory
net intensity of magnetisation

Space charge polarization: occurs due to diffusion of ions, along the electric field direction & giving rise to an redistribution of charges in dielectrics. This occurs only in ferroelectrics & semiconductors & will be very small



$E \neq 0$

$$P_s = N \kappa_s \vec{E} \rightarrow (4)$$

total Polarization:

$$\begin{aligned} P &= P_e + P_r + P_0 + P_s = N(\kappa_e + \kappa_1 + \kappa_0 + \kappa_s) \vec{E} \\ &= N \left[4\pi \epsilon_0 R^3 + \frac{e^2}{\omega_0^2} \left\{ \frac{1}{m} + \frac{1}{M} \right\} + \frac{\mu^2}{3k_B T} \right] \vec{E} \rightarrow (5) \end{aligned}$$

Clausius - Mossotti relation

Internal/Local field : when a dielectric is kept in an external field (E), two fields are exerted due to

- (i) External field (ii) Field created by the neighbouring dipoles

These long range coulomb force which are created due to the dipoles are called Local field or Internal field

Consider a Dielectric solid in an External field E ^{b/w 111 plates} dipoles are formed in the material.

The total polarization in dielectric is given by

$$P = P_e + P_i + P_o + P_s$$

Here we are considering a solid. $P_e \rightarrow$ electronic polarization is dominant

$$\therefore P = P_e = N \alpha_e E_f \rightarrow (1)$$

$N \rightarrow$ No. of atoms or molecules or dipoles per unit volume

$E_f \rightarrow$ Local electric field.

$$\text{WKT } E_f = E_{\text{external}} + \frac{P}{3\epsilon_0} \rightarrow (\text{field due to dipoles})$$

$$E_f = E_{\text{ext}} + \frac{P}{3\epsilon_0} \rightarrow (2)$$

$$\text{But } P = \epsilon_0 (\epsilon_r - 1) E$$

$$\therefore P = (\epsilon_0 \epsilon_r - \epsilon_0) E \Rightarrow (\epsilon - \epsilon_0) E$$

$$\therefore E = \frac{P}{\epsilon - \epsilon_0} \rightarrow (3)$$

Substitute (3) in (2)

$$E_f = \frac{P}{\epsilon - \epsilon_0} + \frac{P}{3\epsilon_0} \rightarrow (4)$$

Exm (1)

$$P = N\alpha_f E_f$$

(1)

$$E_{int} = \frac{P}{N\alpha}$$

Rewrite (1)

$$E_f = \frac{P}{\epsilon - \epsilon_0} + \frac{P}{3\epsilon_0}$$

$$\frac{P}{N\alpha} = \frac{P}{\epsilon - \epsilon_0} + \frac{P}{3\epsilon_0} \quad (\text{take LCM})$$

$$\frac{P}{N\alpha} = \frac{P(3\epsilon_0) + P(\epsilon - \epsilon_0)}{3\epsilon_0(\epsilon - \epsilon_0)}$$

$$\frac{P}{N\alpha} = \frac{P(3\epsilon_0 + \epsilon - \epsilon_0)}{3\epsilon_0(\epsilon - \epsilon_0)}$$

$$\frac{3\epsilon_0}{N\alpha} = \frac{2\epsilon_0 + \epsilon}{(\epsilon - \epsilon_0)}$$

$$\left(\epsilon = \underbrace{\epsilon_0}_{\text{free space}} \underbrace{\epsilon_r}_{\text{medium}} \right)$$

$$\frac{3\epsilon_0}{N\alpha} = \frac{2\epsilon_0 + \epsilon_0 \epsilon_r}{\epsilon_0 \epsilon_r - \epsilon_0}$$

$$\frac{3\epsilon_0}{N\alpha} = \frac{(2 + \epsilon_r) \cancel{\epsilon_0}}{(\epsilon_r - 1) \cancel{\epsilon_0}} \rightarrow (5)$$

Reverse the eqⁿ $\frac{N\alpha}{3\epsilon_0} = \frac{\epsilon_r - 1}{2 + \epsilon_r} \rightarrow (6)$

eqⁿ (6) represents Clausius Mosotti eqⁿ relates microscopic parameters (atomic polarizability) α with the microscopic dielectric const ϵ_r

FERROELECTRICS

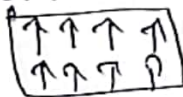
A new variety of characteristics, new classes of dielectric material called ferroelectric, piezoelectric & pyroelectric ceramics.

→ Ferroelectric materials are characterized by the presence spontaneous dielectric polarization

which does not need any external electric field to get them polarized. & direction of spontaneous polarization can be reversed by reversing the dirn of Electric field.

ex: Rochelle salt (Sodium Potassium Tetrates $\text{NaK}(\text{C}_4\text{H}_4\text{O}_6 \cdot 4\text{H}_2\text{O})$)

$$E=0$$
$$P \neq 0$$



→ There are pre-existing dipoles in these materials even in the absence of external electric field.

because there is minor deviation from crystallographic symmetry or inherent asymmetry in the crystal structure of these materials.

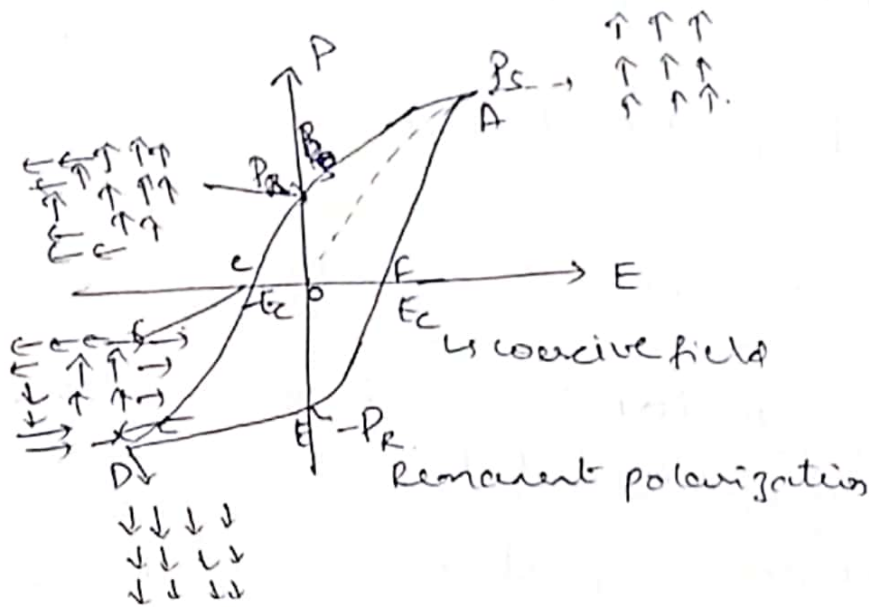
→ As a consequence of spontaneous polarization the mechanism of orientation polarization dominates over all other mechanisms

→ There are ex- of Non-linear dielectrics giving rise to ferroelectric hysteresis when polarization is plotted against electric field.

The polarization becomes maximum when all the domains become parallel to the direction of the applied field

→ The generation of current in response to the application of force is called piezoelectricity

ferroelectric hysteresis



At O. $E=0$, $P=0$,

At A $E_{max}=E$, $P=P_s$ (saturation polarization)

At B $E=0$, $P=P_r$ (Remanent polarization)

At C $E=-E_c$, $P=0$ E_c (coercive field)

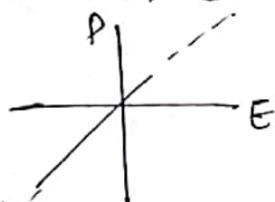
At D $E=-E_{max}$, $P=-P_s$

At E $E=0$, $P=-P_r$

At F $E=E_c$, $P=0$

It exhibits ferro-electric property below curie temp

Curie Temp (T_c) $\rightarrow T < T_c \Rightarrow$ ferroelectric material
 $\rightarrow T > T_c \Rightarrow$ Piezoelectric material



$$\gamma = \frac{c}{T - T_c}$$

Applications

- 1) Capacitors, Non-volatile memory
- 2) Electro-optic materials for data storage applications
- 3) Thermistors, oscillators & filters, light deflectors, modulators
- 4) Switches known as transchargers or transpolarizers
- 5) Piezoelectrics for ultrasound imaging & actuators