

Mahindra University Hyderabad

École Centrale School of Engineering

Minor II

Program: B.Tech. Branch: Computation & Mathematics Year: Second Semester: Spring

Subject: Optimization Techniques (MA 2210)

Date: 18/04/2024

Start Time: 10:00 AM

Time Duration: 1.5 Hours

Max. Marks: 20

Instructions:

- 1) All questions are compulsory.
- 2) Please start each answer on a separate page and ensure you clearly number the responses. Also, make sure to address all parts of each question together and in the correct order.
- 3) It is essential to provide an explanation of each step. Correct outcomes without any description will not be evaluated.
- 4) A calculator is allowed.

Q 01: Select the correct choice for the following questions with proper explanation. Correct choices without valid justification will not be considered. [01 × 05]

A) In a linear programming problem, the optimal value of the objective function is attained at the points

- i) Given by intersection of lines representing inequalities with axes only
- ii) Given by intersection of lines representing inequalities with the x -axis only
- iii) Given by corner points of the feasible region
- iv) At the origin
- v) None of these

B) The corner points of the feasible region determined by the system of linear constraints are $(0, 10)$, $(5, 5)$, $(15, 15)$, and $(0, 20)$. Let $z = px + qy$, where $p > 0$ and $q > 0$. The condition on p and q so that the maximum of z occurs at both points $(15, 15)$ and $(0, 20)$ is:

- i) $p = q$
- ii) $p = 2q$
- iii) $q = 2p$
- iv) $q = 3p$

C) Identify the type of the feasible region given by the set of following inequalities:

$$\left. \begin{array}{l} x - y \leq 1 \\ x - y \geq 2 \end{array} \right\}; \text{ and } x \geq 0 \text{ and } y \geq 0.$$

- i) A triangle
- ii) A rectangle
- iii) An unbounded region
- iv) An empty region

D) In a maximization linear programming problem, if at least one artificial variable is in the basis but not at zero level and the net evaluation $\Delta_j = (z_j - c_j)$ for each variable is non-negative, then we have

i) A feasible solution

ii) No feasible solution

iii) An unbounded solution

iv) An optimum solution

E) If an iso-profit line yielding the optimum solution coincides with a constraint line, then

i) The solution is unbounded

ii) The solution is infeasible

iii) The constraint that coincides is redundant

iv) None of the above

Q02: Obtain the dual of the following primal problem:

[03]

min $z_x = 3x_1 - 2x_2 + x_3$; subject to the constraints

$$\left. \begin{array}{l} 2x_1 - 3x_2 + x_3 \leq 5 \\ 4x_1 - 2x_2 \geq 9 \\ -8x_1 + 4x_2 + 3x_3 = 8 \end{array} \right\}; \text{ and}$$

$x_1 \geq 0, x_2 \geq 0$, and x_3 is unrestricted.

Q03: A milk plant manufactures two types of products, A and B, and sells them at a profit of ₹ 5 on type A and ₹ 3 on type B. Each product is processed on two machines, G and H. Type A requires one minute of processing time on G and two minutes on H. Type B requires one minute on G and one minute on H. Machine G is available for not more than one hour 40 minutes, while machine H is available for two hours 20 minutes during any working day. Formulate and solve the linear programming problem to maximize the profit.

[05]

Q04: Use the Simplex method to solve the following linear programming problem:

[07]

min $z = -6x_1 - 10x_2 - 4x_3$; subject to the constraints

$$\left. \begin{array}{l} x_1 + x_2 + x_3 \leq 1000 \\ x_1 + x_2 \leq 500 \\ x_1 + 2x_2 \leq 700 \end{array} \right\}; \text{ and}$$

$x_1 \geq 0, x_2 \geq 0$, and $x_3 \geq 0$.