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1 Data Structures

1.1 BIT 1D

```
#include <bits/stdc++.h>
using namespace std;

int aux, n, arr[1000], BIT[1000];

// construir uma BIT a partir de um array em O(N)
void build() {
    for(int i = 1; i <= n; i++) {
        BIT[i] += arr[i];
        if(i + (i & -i) <= n)
            BIT[i + (i & -i)] += BIT[i];
    }
}

// construir o array que gera a BIT a partir de uma BIT em O(N)
void buildArray() {
    for(int i = n; i >= 1; i--)
        if(i + (i & -i) <= n)
            BIT[i + (i & -i)] -= BIT[i];
}

int sum(int x) {
    int s = 0;
    while(x) s += BIT[x], x -= x&-x;
    return s;
}
```

```
void update(int x, int value) {
    while(x <= n) BIT[x] += value, x += x&-x;
}

int main() {
    cin >> n;
    for(int i = 1; i <= n; i++) {
        cin >> aux;
        update(i, aux);
    }
    int a, b;
    cin >> a >> b;
    cout << sum(b) - sum(a-1) << '\n';

    return 0;
}
```

2 Dynamic Programming

2.1 Traveling Salesman Problem

```
#include <bits/stdc++.h>
using namespace std;

int dist[22][22], m;
int memo[20][1 << 20];

int solve(int id, int mask) {
    if(((1 << m) - 1) == mask)
        return dist[id][0];
    if(memo[id][mask] != -1)
        return memo[id][mask];
    int ans = INT_MAX;
    for(int i = 0; i < m; i++)
        if((mask & (1 << i)) == 0)
            ans = min(ans, dist[id][i] + solve(i, mask | (1 << i)));
    return memo[id][mask] = ans;
}

int main() {
    memset(memo, -1, sizeof(memo));
    //inicializa a matriz dist com as distancias
    //de todo mundo pra todo mundo..
    cout << solve(0, 1) << '\n';
    return 0;
}
```

3 Geometry

3.1 Convex Hull

```
#include <bits/stdc++.h>
using namespace std;
#define X first
#define Y second
```

```

typedef pair<int, int> ii;

int cross(ii O, ii A, ii B)
{
    return ((A.X - O.X) * (B.Y - O.Y)) - ((A.Y - O.Y) * (B.X - O.X));
}

vector<ii> ConvexHull(vector<ii> P)
{
    if(P.size() <= 1) return P;
    vector<ii> H(2*P.size());
    int k = 0;
    sort(P.begin(), P.end());
    //lower hull
    for(int i = 0; i < P.size(); i++)
    {
        while(k >= 2 and cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    }
    //upper hull
    for(int i = P.size()-2, l = k + 1; i >= 0; i--)
    {
        while(k >= l and cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    }
    H.resize(k-1);
    return H;
}

int main()
{
    int n, x, y;
    vector<ii> P;

    cin >> n;
    while(n--)
    {
        cin >> x >> y;
        P.push_back({x, y});
    }

    vector<ii> H = ConvexHull(P);

    for(int i = 0; i < H.size(); i++)
        cout << H[i].X << ' ' << H[i].Y << '\n';

    return 0;
}

```

4 Graph

4.1 Bipartite Matching

```

#include <bits/stdc++.h>
using namespace std;

int na, nb, m, tempo = 1;

```

```

int b[105];
int cor[105];
vector<int> G[105];

bool kuhn(int u)
{
    if(cor[u] == tempo)
        return 0;
    cor[u] = tempo;
    //random_shuffle(G[u].begin(), G[u].end(), [] (int x){ return rand() %
    x; });
    for(const int &v : G[u])
        if(!b[v] or kuhn(b[v]))
            return b[v] = u;
    return 0;
}

int main()
{
    //srand(time(NULL));
    cin >> na >> nb >> m;
    while(m--)
    {
        int u, v;
        cin >> u >> v;
        G[u].push_back(v + na);
    }
    tempo = 1;
    int ans = 0;
    for(int i = 1; i <= na; i++)
        ans += kuhn(i), tempo++;
    cout << "MCBM = " << ans << '\n';
    for(int i = nb + 1; i <= na + nb; i++)
        if(b[i])
            cout << b[i] << ' ' << i - na << '\n';

    return 0;
}

```

5 Math

5.1 Baby Step Giant Step

```

// a ^ kcong b mod m

int value[1000008];
int cor[1000008], tempo = 1;

// com vetor o modulo deve ser <= 10^7 fica O(sqrt(m))
inline int discreteLogarithm(int a, int b, int m) {
    tempo++;
    a %= m; b %= m;
    int n = (int)sqrt(m + .0) + 1, an = 1;
    for(int i = 1; i <= n; i++) an = (an * 1LL * a) % m;
    for(int i = 1, cur = an; i <= n; i++) {
        if(cor[cur] < tempo) value[cur] = i, cor[cur] = tempo;
        cur = (cur * 1LL * an) % m;
    }
}

```

```

    for(int j = 0, cur = b; j <= n; j++) {
        if(cor[cur] == tempo) {
            int ans = value[cur] * n - j;
            if(ans < m)
                return ans;
        }
        cur = (cur * 1LL * a) % m;
    }
    return -1;
}

// com mapa o modulo pode ser ateh <= 10^12 fica O(sqrt(m) * log(m))
int discreteLogarithm(int a, int b, int m)
{
    a %= m; b %= m;
    int n = (int)sqrt(m + .0) + 1, an = 1;
    for(int i = 1; i <= n; i++) an = (an * a) % m;
    unordered_map<int, int> value;
    for(int i = 1, cur = an; i <= n; i++) {
        if(!value.count(cur)) value[cur] = i;
        cur = (cur * an) % m;
    }
    for(int j = 0, cur = b; j <= n; j++) {
        if(value[cur]) {
            int ans = value[cur] * n - j;
            if(ans < m)
                return ans;
        }
        cur = (cur * a) % m;
    }
    return -1;
}

```

6 String

6.1 LIS - LDS

```

#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;

int n;
int LI[MAX], LD[MAX];
vector<int> arr;

int LIS() {
    for(int i = 0; i < n; i++)
        LI[i] = 1;
    for(int i = n - 1; i >= 0; i--)
        for(int j = 0; j < i; j++)
            if(arr[j] < arr[i])
                LI[j] = max(LI[j], LI[i] + 1);
}

int LDS() {
    reverse(arr.begin(), arr.end());
    for(int i = 0; i < n; i++)
        LD[i] = 1;
}

```

```

vector<int> pilha;
for(int i = 0; i < n; i++) {
    int p = (int)(lower_bound(pilha.begin(),
        pilha.end(), arr[i]) - pilha.begin());
    if(p == pilha.size())
        pilha.push_back(arr[i]);
    else
        pilha[p] = arr[i];
    LD[i] = p + 1;
}

int main() {
    cin >> n; arr.resize(n);
    for(int i = 0; i < n; i++) cin >> arr[i];

    LIS();
    LDS();

    for(int i = 0; i < n; i++)
        cout << LI[i] << ' '; puts("");
    for(int i = 0; i < n; i++)
        cout << LD[n - i - 1] << ' '; puts("");

    return 0;
}

```

7 Miscellaneous

7.1 BIT 1D

```

#include <bits/stdc++.h>
using namespace std;

int aux, n, arr[1000], BIT[1000];

// construir uma BIT a partir de um array em O(N)
void build() {
    for(int i = 1; i <= n; i++) {
        BIT[i] += arr[i];
        if(i + (i & -i) <= n)
            BIT[i + (i & -i)] += BIT[i];
    }
}

// construir o array que gera a BIT a partir de uma BIT em O(N)
void buildArray() {
    for(int i = n; i >= 1; i--)
        if(i + (i & -i) <= n)
            BIT[i + (i & -i)] -= BIT[i];
}

int sum(int x) {
    int s = 0;
    while(x) s += BIT[x], x -= x & -x;
    return s;
}

```

```
void update(int x, int value) {
    while(x <= n) BIT[x] += value, x += x&-x;
}

int main() {
    cin >> n;
    for(int i = 1; i <= n; i++) {
        cin >> aux;
        update(i, aux);
    }
}
```

```
int a, b;
cin >> a >> b;
cout << sum(b)-sum(a-1) << '\n';

return 0;
}
```

8 Other