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1 Graph

1.1 2SAT

```
// Os vertices pares indicam as proposicoes falsas
// Os vertices impares indicam as proposicoes verdadeiras
// Achar qual proposicao relativa a cada vertice, eh so dividiar
    vertice/2
// tamG = quantidade_proposicoes*2
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
int n, m, tamG;
vector<int> G[MAX], G_t[MAX], C[MAX];
stack<int> sta;
bool cor[MAX];
int componente[MAX], comp;
void preenche(int v)
    cor[v] = true;
    for(const int &u : G_t[v])
        if(!cor[u])
            preenche (u);
    sta.push(v);
void dfs(int v, int comp)
    componente[v] = comp;
```

```
dfs(u, comp);
void kosaraju()
    memset(cor, false, sizeof(cor));
    for(int i = 0; i < tamG; i++)
        if(!cor[i])
            preenche(i);
    memset(cor, false, sizeof(cor));
    comp = 1;
    while(!sta.empty())
        int u = sta.top();
        sta.pop();
        if(componente[u]) continue;
        dfs(u, comp);
        comp++;
// Id no grafo que representa a proposicao de numero P como verdadeira
int idTrue(int p)
    return (p << 1) + 1;
// Id no grafo que representa a proposicao de numero P como falsa.
int idFalse(int p)
    return (p << 1);
bool twoSat()
  kosaraju();
  for (int i = 0; i < tamG; i+=2)
  // Todo par de proposicoes (proposicao falsa, proposicao verdadeira)
  // Nao podem estar no mesmo componente
    if(componente[i] == componente[i + 1])
        return false;
  return true;
int addEdge(int u, int v)
    G[idFalse(u)].push_back(idTrue(v));
    G[idFalse(v)].push_back(idTrue(u));
    G[idTrue(u)].push_back(idFalse(v));
    G[idTrue(v)].push_back(idFalse(u));
    // montar grafo transposto para kosaraju nessa
    // aplicacao o grafo G sera igual ao transposto
    G_t[idFalse(u)].push_back(idTrue(v));
```

C[comp].push_back(v);
for(const int &u : G[v])
 if(!componente[u])

```
G_t[idFalse(v)].push_back(idTrue(u));
    G_t[idTrue(u)].push_back(idFalse(v));
    G_t[idTrue(v)].push_back(idFalse(u));
vector<int> g[MAX];
vector<int> ts;
int value[MAX];
void topSort(int v)
    cor[v] = true;
    for(int &u : G[v])
        if(!cor[u])
            topSort(u);
    ts.push_back(v);
void mountDAG()
    for (int v = 0; v < tamG; v++)
        for(int &u : G[v])
            if(componente[v] != componente[u])
                g[componente[v]].push_back(componente[u]);
    memset(cor, false, sizeof(cor));
    for (int v = 1; v < comp; v++)
        if(!cor[v])
            topSort(v);
    // nao inverter ts, pois precisamos da ordenacao
    // topologica ao contrario
// encontrar uma atribuicao (TREU ou FALSE) para as proposicoes
void assignment()
    if(!twoSat()) return;
   mountDAG();
    memset(value, -1, sizeof(value));
    for(int &v : ts)
        for(int &u : C[v])
            if (value [u >> 1] == -1) // u / 2 eh a proposicao
                value[u >> 1] = (u & 1 ? 1 : 0);
    for(int i = 0; i < (tamG >> 1); i++)
        cout << value[i] << ' ';
    puts("");
int main()
    cin >> n >> m;
    tamG = 2 * n;
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        addEdge(u, v);
    cout << twoSat() << '\n';</pre>
    assignment();
```

```
return 0;
```

1.2 BFS Zero One

```
// o peso das arestas eh 0 ou 1
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5:
const int 00 = 0x3f3f3f3f3f;
typedef pair<int, int> ii;
int n, m;
vector<ii> G[MAX];
int dist[MAX];
deque<int> dq;
void zeroOneBfs(int v)
    memset(dist, 63, sizeof(dist));
    dist[v] = 0;
    dq.push_back(v);
    while(!dq.empty())
        int u = dq.front();
        dq.pop_front();
        for(int i = 0; i < G[u].size(); i++)</pre>
            int w = G[u][i].first, d = G[u][i].second;
            if(dist[w] > dist[u] + d)
                dist[w] = dist[u] + d;
                if(!d) dq.push_front(w);
                else dq.push_back(w);
    for(int i = 0; i < n; i++)</pre>
        cout << dist[i] << ' ';
    puts("");
int main()
    cin >> n >> m;
    while (m--)
        int u, v, w;
        cin >> u >> v >> w; u--; v--;
        G[u].push_back({v, w});
        G[v].push_back({u, w});
    zeroOneBfs(0);
    return 0:
```

1.3 Binary Lifting

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int n, m, nivel[MAX], anc[MAX][30], MAX_LOG;
vector<int> G[MAX];
void dfs(int v, int p, int d)
    anc[v][0] = p;
    nivel[v] = d;
    if(d) MAX_LOG = max(MAX_LOG, (int)log2(d));
    for(const int &u : G[v])
        if(u != p)
            dfs(u, v, d + 1);
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k\&-k)], k -= k\&-k;
    return v;
int lca(int u. int v)
    if (nivel[u] < nivel[v]) v = walk(v, nivel[v]-nivel[u]);</pre>
    if(nivel[u] > nivel[v]) u = walk(u, nivel[u]-nivel[v]);
    if(u == v) return u;
    for(int i = MAX_LOG; i >= 0; i--)
        if(anc[u][i] != anc[v][i])
            u = anc[u][i];
            v = anc[v][i];
    return anc[u][0];
void build()
    memset (anc, -1, sizeof anc);
    nivel[0] = 0;
    dfs(0, -1, 0);
    for(int j = 1; j <= MAX LOG; j++)</pre>
        for(int i = 1; i <= n; i++)</pre>
            if(anc[i][j-1] != -1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
int main()
    int u, v;
    cin >> n >> m;
    while (m--)
        cin >> u >> v;
        u--; v--;
        G[u].push_back(v);
```

```
G[v].push_back(u);
    build();
    cin >> u >> v;
    cout << lca(u-1, v-1)+1 << ' n';
    return 0;
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5:
typedef pair<int, int> ii;
int n. m. max log:
vector<ii> G[MAX];
int anc[MAX][30], min_edge[MAX][30], depth[MAX];
void dfs(int v, int d, int p, int a)
    anc[v][0] = p;
    depth[v] = d;
    if(d) max_log = max(max_log, (int)log2(d));
    if(p != -1) min_edge[v][0] = a;
    for(int i = 0; i < G[v].size(); i++)
        int u = G[v][i].second, w = G[v][i].first;
        if(u != p)
            dfs(u, d + 1, v, w);
void build()
    memset(anc, -1, sizeof(anc));
    memset(min_edge, 63, sizeof(min_edge));
    dfs(0, 0, -1, -1);
    for(int j = 1; j <= max_log; j++)</pre>
        for(int i = 0; i < n; i++)</pre>
            if (anc[i][j-1] !=-1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
                min_edge[i][j] = min(min_edge[i][j-1], min_edge[anc[i
                     ][j-1]][j-1]);
        }
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k&-k)], k -= k&-k;
    return v;
int lca(int u, int v)
```

```
if(depth[u] > depth[v]) u = walk(u, depth[u]-depth[v]);
    if(depth[u] < depth[v]) v = walk(v, depth[v]-depth[u]);</pre>
    if(u == v) return u;
    for(int i = max_log; i >= 0; i--)
        if(anc[u][i] != anc[v][i])
            u = anc[u][i];
            v = anc[v][i];
    return anc[u][0];
int queryMinEdge(int u, int v)
    int LCA = lca(u, v);
    int ans = INT_MAX;
    int k = depth[u]-depth[LCA];
    while(k)
        ans = min(ans, min_edge[u][(int)log2(k&-k)]);
       u = walk(u, k\&-k);
        k = k - k;
    k = depth[v]-depth[LCA];
    while(k)
        ans = min(ans, min_edge[v][(int)log2(k&-k)]);
        v = walk(v, k\&-k);
        k = k - k;
    return ans;
int main()
    int u, v, w;
    cin >> n;
    for(int i = 0; i < n-1; i++)</pre>
        cin >> u >> v >> w;
        u--; v--;
        G[u].push_back({w, v});
        G[v].push_back({w, u});
    cin >> u >> v;
    build();
    cout << lca(u-1, v-1)+1 << ' n';
    cout << queryMinEdge(u-1, v-1) << '\n';
    return 0;
```

1.4 Boruvka MST

```
#include <bits/stdc++.h>
using namespace std;
int n, m;
vector<array<int, 3>> edge;
```

```
int pai[100100], sz[100100];
int find(int x)
    return pai[x] == x ? x : pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    y = find(y);
    if(x == y) return;
    if(sz[x] > sz[y]) swap(x, y);
    pai[x] = y;
    sz[y] += sz[x];
int main()
    scanf(" %d %d", &n, &m);
    for(int i = 0; i < m; i++)</pre>
        int u, v, w;
        scanf(" %d %d %d", &u, &v, &w); u--; v--;
        edge.push_back({w, v, u});
    for(int i = 0; i < n; i++)</pre>
        pai[i] = i, sz[i] = 1;
    int mst cost = 0;
    bool fl = true;
    while(fl)
        fl = false;
        vector<int> aux(n, -1);
        for(int i = 0; i < m; i++)</pre>
            int u = find(edge[i][1]), v = find(edge[i][2]), w = edge[i][1]
                ][0];
            if(u == v) continue;
            if(aux[u] == -1) aux[u] = i;
            else if(edge[aux[u]][0] > w) aux[u] = i;
            if(aux[v] == -1) aux[v] = i;
            else if (edge[aux[v]][0] > w) aux[v] = i;
        for(int i = 0; i < n; i++)</pre>
            if(aux[i] == -1) continue;
            int u = find(edge[aux[i]][1]), v = find(edge[aux[i]][2]);
            if(u == v) continue;
            // add_edge edge[aux[i]][1] --- edge[aux[i]][2] in the MST
            join(u, v);
            mst_cost += edge[aux[i]][0];
            fl = true;
    cout << mst_cost << '\n';</pre>
    return 0:
```

1.5 Center Of A Tree

```
#include <bits/stdc++.h>
const int MAX = 1e5;
using namespace std;
int n, degree[MAX];
vector<int> G[MAX];
bool vis[MAX];
int findCenter()
  queue<int> fila[2];
  for(int i = 0; i < n; i++)
    if(degree[i] == 1)
      fila[0].push(i);
  int cnt = 0, turn = 0;
  while (cnt + 2 < n)
    while(!fila[turn].empty())
      int u = fila[turn].front(); fila[turn].pop();
      vis[u] = true;
      cnt++;
      for(int i = 0; i < G[u].size(); i++)</pre>
        if(!vis[G[u][i]])
          degree[G[u][i]]--;
          if(degree[G[u][i]] == 1)
            fila[1-turn].push(G[u][i]);
    turn ^= 1;
  cout << "the set of central vertices\n";</pre>
  for (int i = 0; i < n; i++)
    if(!vis[i])
        cout << i + 1 << '\n';
int main()
    cin >> n;
  for(int i = 1; i < n; i++)</pre>
    int u, v;
    scanf("%d %d", &u, &v); u--; v--;
    G[u].push_back(v);
    G[v].push_back(u);
    degree[u]++;
    degree[v]++;
  findCenter();
  return 0;
```

1.6 Diameter And Center Of A Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int n:
vector<int> G[MAX];
int bfs(int v, vector<int> &dist)
    queue<int> q;
    q.push(v);
    dist[v] = 0;
    int lqv = -1;
    while(!q.empty())
        int u = q.front(); q.pop();
        lgv = u;
        for(int &w : G[u])
            if(dist[w] == -1)
                dist[w] = dist[u] + 1;
                q.push(w);
    return lqv;
void findCenterAndDiameter(int w)
    vector<int> dist1(n + 1, -1);
    vector<int> dist2(n + 1, -1);
  int v = bfs(w, dist1);
  int u = bfs(v, dist2);
  int d = dist2[u];
    dist1.assign(n + 1, -1);
    u = bfs(u, dist1);
    cout << "center ";</pre>
    for(int i = 0; i < n; i++)
        int d1 = dist1[i], d2 = dist2[i];
        if(d1 == d / 2 and d2 == d - d / 2 or d2 == d / 2 and d1 == d
            - d / 2)
        cout << i + 1 << ' ';
    cout << "\ndiameter " << d << '\n';</pre>
int main()
    cin >> n;
    for(int i = 1; i < n; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        G[u].push_back(v);
    G[v].push_back(u);
    findCenterAndDiameter(0);
```

```
return 0;
```

1.7 Dijkstra

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f3f;
const int MAX = 1e5:
typedef pair<int, int> ii;
int n, m;
int dist[MAX];
vector<ii> G[MAX];
int dijkstra(int v, int z)
    memset(dist, 63, sizeof(dist));
    dist[v] = 0;
    priority_queue<ii> pq;
    pq.push({0, v});
    while(!pq.empty())
        int u = pq.top().second;
        int d = -pq.top().first;
        pq.pop();
        if(d > dist[u]) continue;
        if(u == z) return d;
        for(int i = 0; i < G[u].size(); i++)</pre>
            int w = G[u][i].second, _d = G[u][i].first;
            if(dist[w] > d + _d)
                dist[w] = d + _d;
                pq.push({-dist[w], w});
    return 00;
int main()
    int u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        u--; v--;
        G[u].push_back({w, v});
        G[v].push_back({w, u});
    cin >> u >> v;
    cout << dijkstra(u-1, v-1) << '\n';
    return 0;
```

1.8 Dinic

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
const int 00 = 0x3f3f3f3f3f;
struct edge
    int v. f. c:
    edge(){}
    edge(int _v, int _f, int _c)
        v = _v, f = _f, c = _c;
};
vector<edge> edges;
vector<int> G[MAX];
int dist[MAX], work[MAX];
void add_edge(int u, int v, int cp, int rc){
  edges.push_back(edge(v, 0, cp));
  G[u].push_back(edges.size()-1);
  edges.push_back(edge(u, 0, rc));
  G[v].push_back(edges.size()-1);
bool bfs(int s, int t)
    memset(dist, -1, sizeof(dist));
    dist[s] = 0;
    queue<int> q;
    q.push(s);
    while(!q.empty())
        int u = q.front();
        q.pop();
        for(int e : G[u])
            if(dist[edges[e].v] == -1 and edges[e].c-edges[e].f > 0)
                q.push(edges[e].v);
                dist[edges[e].v] = dist[u] + 1;
    return dist[t] != -1;
int dfs(int s, int t, int f)
    if(s == t) return f;
    for(int &i = work[s]; i < G[s].size(); i++)</pre>
      int e = G[s][i];
        if(dist[edges[e].v] == dist[s] + 1 and edges[e].c-edges[e].f >
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                edges[e].f += a;
```

```
edges[e^1].f -= a;
                return a;
    return 0;
int MaxFlow(int s, int t)
    int mf = 0;
    while(bfs(s, t))
      memset(work, 0, sizeof(work));
        while(int a = dfs(s, t, 00))
            mf += a;
    return mf;
int main()
    int n, m, u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        add_edge(u-1, v-1, w, 0);
    cin >> u >> v;
    cout << MaxFlow(u-1, v-1) << '\n';
    return 0;
```

1.9 Erdos Gallai Theorem

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
int32_t main()
  int n;
  while(~scanf(" %lld", &n))
      vector<int> degree(n), pref(n + 2);
        for(int &i : degree)
            scanf (" %lld", &i);
      sort(degree.begin(), degree.end(), greater<int>());
      for(int i = 0; i < n; i++)</pre>
    pref[i + 1] = pref[i] + degree[i];
        bool fl = true;
        if(pref[n] & 1)
            fl = false;
        int j = n;
        for (int k = 1; k \le n and fl; k++)
            int L = pref[k];
            int R = k * (k - 1);
```

1.10 Eulirian Path

```
#include <bits/stdc++.h>
using namespace std;
int32_t main() {
   int n, m;
   cin >> n >> m;
   vector<vector<int>> g(n);
   vector<int> deg_in(n), deg_out(n);
   for(int i = 0; i < m; i++) {</pre>
      int u, v:
      cin >> u >> v; u--; v--;
      q[u].push_back(v);
      deg_in[v]++;
      deg_out[u]++;
   int s = -1, f = -1;
   for(int i = 0; i < n; ++i) {</pre>
      if (deg_in[i] - deg_out[i] == 0) continue;
      if(s == -1 and deg_out[i] - deg_in[i] == 1) s = i;
      else if(f == -1 and deg_in[i] - deg_out[i] == 1) f = i;
      else return cout << "NO\n", 0;</pre>
   if(s == -1 \text{ and } f == -1) s = 0;
   else if (s !=-1 and f ==-1 or s ==-1 and f !=-1) return cout <<
       "NO\n", 0;
   stack<int> st:
   st.push(s);
   vector<int> res;
   while(!st.empty()) {
      int v = st.top();
      if(q[v].empty()) {
         res.push_back(v);
         st.pop();
      } else {
         int u = q[v].back();
         g[v].pop_back();
         st.push(u);
   }
```

```
for(int i = 0; i < n; i++)
    if(g[i].empty() == false)
        return cout << "NO\n", 0;

reverse(res.begin(), res.end());

for(int w : res)
    cout << w + 1 << ' ';
    cout << endl;

return 0;
}</pre>
```

1.11 Floyd Sucessor Graph

```
#include <bits/stdc++.h>
using namespace std;
int n;
int table[10000][20];
//table[i][j] armazena o sucessor de distancia 2^j do vertice i
void build()
  for (int j = 1; (1 << j) <= n; j++)
    for(int i = 0; i < n; i++)</pre>
        if(table[i][j-1] != -1)
          table[i][j] = table[table[i][j-1]][j-1];
int succ(int u, int k)
  while (k)
    u = table[u][(int)log2(k&-k)];
    if(u == -1)
        return -1; // nao existe
    k = k - k;
  return u;
//algoritmo de Floyd para encontrar o tamanho de um ciclo
//alcancado a partir de um vertice u em um grafo sucessor
int Floyd(int u)
  int a = succ(u, 1);
  int b = succ(u, 2);
  //encontra um vertice no ciclo
  while(a != b)
    a = succ(a, 1);
    b = succ(b, 2);
    if (a == -1 or b == -1)
        return -1;// nao existe ciclo
```

```
//a e b vao ficar posicionados no inicio do ciclo
 a = u;
 while (a != b)
     a = succ(a, 1);
     b = succ(b, 1);
  //percorre todo o ciclo contando o seu tamanho
 b = succ(a, 1);
 int lenght = 1;
 while(a != b)
   b = succ(b, 1);
   lenght++;
 return lenght;
int main()
 int u, v, m;
 cin >> n >> m;
 memset(table, -1, sizeof(table));
 for(int i = 0; i < m; i++)
   cin >> u >> v; u--; v--;
   table[u][0] = v;
 build();
 cin >> u >> v;
 cout << "O sucessor de " << u << " com " << v <<
 " unidades a frente eh " << succ (u-1, v)+1 << '\n';
 cout << '\n';
 cin >> u;
 cout << "tamanho do ciclo iniciando em " << u <<
  ": " << Floyd(u-1) << '\n';
 return 0;
```

1.12 Ford Fulkerson

```
#include <bits/stdc++.h>
using namespace std;
typedef pair<int, int> ii;
const int 00 = 0x3f3f3f3f;
const int MAX = 1e4;

struct edge
{
   int v, f, c;
   edge() {}
   edge(int _v, int _f, int _c)
```

```
v = _v, f = _f, c = _c;
};
vector<edge> edges;
vector<int> G[MAX];
int tempo = 1, cor[MAX];
void add_edge(int u, int v, int cp, int rc)
    edges.push_back(edge(v, 0, cp));
    G[u].push_back(edges.size()-1);
    edges.push_back(edge(u, 0, rc));
    G[v].push_back(edges.size()-1);
int dfs(int s, int t, int f)
    if(s == t) return f;
    cor[s] = tempo;
    for(int e : G[s])
        if(cor[edges[e].v] < tempo and edges[e].c-edges[e].f > 0)
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                edges[e].f += a;
                edges[e^1].f -= a;
                return a;
    return 0;
int MaxFlow(int s, int t)
    int mf = 0;
    while(int a = dfs(s, t, 00))
        mf += a, tempo++;
    return mf;
int main()
    int n, m, w, u, v;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        add_edge(u-1, v-1, w, 0);
    cin >> u >> v;
    cout << MaxFlow(u-1, v-1) << '\n';
    return 0;
```

1.13 Fully Dynamic Connectivity Check If Two Vertices Are In The Same Component

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 131072;
const int 00 = 0x3f3f3f3f3f;
const double EPS = 1e-9;
#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first
#define se second
#define pb push_back
#define mt make_tuple
#define mp make_pair
#define all(vetor) vetor.begin(), vetor.end()
#define X real()
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11;
typedef long double ld:
//typedef pair<int, int> ii;
//typedef pair<int, ii> iii;
typedef complex<11> P11;
typedef complex<ld> Pld;
typedef pair<int, int> edge;
vector<edge> tree[4 * MAX], query[4 * MAX];;
int pai[MAX], sz[MAX];
stack<pair<int, int>> stk, size;
vector<int> ans;
int find(int x)
    if(pai[x] == x)
        return x;
    stk.push(mp(x, pai[x]));
    size.push(mp(x, sz[x]));
    return pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    y = find(y);
    if(x == y) return;
    if(sz[x] > sz[y])
        swap(x, y);
    stk.push(mp(x, pai[x]));
    size.push(mp(y, sz[y]));
    sz[y] += sz[x];
    pai[x] = y;
```

```
void rollback(int rollback_to) //desfaz todas as alteracaes no DSU,
\{//O(k) \text{ onde } k \text{ eh a quantidade de operações realizadas}
  while(rollback_to < stk.size())</pre>
    pai[stk.top().fi] = stk.top().se;
    stk.pop();
        sz[size.top().fi] = size.top().se;
        size.pop();
void add_edge(int node, int start, int end, int 1, int r, edge e)
    if(start == 1 and end == r)
        tree[node].push_back(e);
        return:
    if(1 >= r)
        return:
    int mid = (start + end) / 2;
    add_edge(2*node, start, mid, 1, min(mid, r), e);
    add_edge(2*node + 1, mid + 1, end, max(1, mid + 1), r, e);
void add_query(int node, int start, int end, int idx, edge e)
    if(start == end)
        query[node].push_back(e);
    else
        int mid = (start + end) / 2;
        if(idx <= mid)</pre>
            add_query(2*node, start, mid, idx, e);
        else
            add_query(2*node + 1, mid + 1, end, idx, e);
void processar(int node)
    for(auto it : tree[node])
        join(it.first, it.second);
void dfs(int node, int start, int end)
    int rollback to = stk.size();
    processar (node);
    if(start == end)
        for(auto v : query[node])
            bool rep = (find(v.first) == find(v.second));
            ans.push_back(rep);
    else
        int mid = (start + end) / 2;
```

```
dfs(2*node, start, mid);
        dfs(2*node + 1, mid + 1, end);
    rollback (rollback to);
int main()
    int n, q, o, u, v;
    cin >> n >> q;
    for(int i = 0; i <= n; i++)</pre>
        sz[i] = 1, pai[i] = i;
    int cur = 0;
    map<pair<int, int>, int> mapa;
    while (q--)
        cin >> o >> u >> v; u--; v--;
    if(u > v) swap(u, v);
        if(o == 1) // adicionar aresta
            mapa[mp(u, v)] = cur++;
        else if(o == 2)// remover aresta
            add_edge(1, 0, MAX-1, mapa[mp(u, v)], cur++, mp(u, v));
            mapa.erase(mp(u, v));
        else // verificar se dois vertices estao na mesma componente
            add_query(1, 0, MAX-1, cur++, mp(u, v));
    cur++;
    for(auto it : mapa)
        add_edge(1, 0, MAX-1, it.second, cur, it.first);
    dfs(1, 0, MAX-1);
    for(int i = 0; i < ans.size(); i++)</pre>
        cout << (ans[i] ? "Yes\n" : "No\n");</pre>
    return 0:
```

1.14 Fully Dynamic Connectivity Count Conected Components

```
#include <bits/stdc++.h>
using namespace std;

const int MAX = 131072;
const int OO = 0x3f3f3f3f3;
const double EPS = 1e-9;

#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first
#define se second
#define pb push_back
#define mt make_tuple
#define mp make_pair
#define all(vetor) vetor.begin(), vetor.end()
#define X real()</pre>
```

```
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11;
typedef long double ld;
//typedef pair<int, int> ii;
//typedef pair<int, ii> iii;
typedef complex<11> P11;
typedef complex<ld> Pld;
typedef pair<int, int> edge;
vector<edge> tree[4 * MAX];
vector<int> query[4 * MAX];
int pai[MAX], sz[MAX];
stack<pair<int, int>> stk, size;
stack<int> qtd;
vector<int> ans:
int rep;
int find(int x)
    if(pai[x] == x)
        return x;
    stk.push(mp(x, pai[x]));
    size.push(mp(x, sz[x]));
    qtd.push(rep);
    return pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    y = find(y);
    if(x == y) return;
    if(sz[x] > sz[y])
        swap(x, y);
    qtd.push(rep);
    stk.push(mp(x, pai[x]));
    size.push(mp(y, sz[y]));
    sz[y] += sz[x];
    pai[x] = y;
    rep--;
void rollback(int rollback_to) //desfaz todas as alteracoes no DSU,
\{//O(k) \text{ onde } k \text{ eh a quantidade de operações realizadas}\}
  while(rollback to < stk.size())</pre>
    pai[stk.top().fi] = stk.top().se;
    stk.pop();
        sz[size.top().fi] = size.top().se;
        size.pop();
        rep = qtd.top();
        qtd.pop();
void add_edge(int node, int start, int end, int 1, int r, edge e)
```

```
if(start == l and end == r)
        tree[node].push_back(e);
        return;
    if(1 >= r)
        return:
    int mid = (start + end) / 2;
    add_edge(2*node, start, mid, 1, min(mid, r), e);
    add_edge(2*node + 1, mid + 1, end, max(1, mid + 1), r, e);
void add_query(int node, int start, int end, int idx, int e)
    if(start == end)
        query[node].push_back(e);
    else
        int mid = (start + end) / 2;
        if(idx <= mid)</pre>
            add_query(2*node, start, mid, idx, e);
            add_query(2*node + 1, mid + 1, end, idx, e);
void processar(int node)
    for(auto it : tree[node])
        join(it.first, it.second);
void dfs(int node, int start, int end)
    int rollback_to = stk.size();
    processar (node);
    if(start == end)
        for(auto v : query[node])
            ans.push_back(rep);
    else
        int mid = (start + end) / 2;
        dfs(2*node, start, mid);
        dfs(2*node + 1, mid + 1, end);
    rollback (rollback_to);
int main()
    int n, q, u, v;
    cin >> n >> q;
    rep = n;
    for(int i = 0; i <= n; i++)</pre>
        sz[i] = 1, pai[i] = i;
    int cur = 0;
    map<pair<int, int>, int> mapa;
    while (q--)
```

```
char o;
    cin >> o;
    if(o != '?')
        cin >> u >> v; u--; v--;
  if(u > v) swap(u, v);
        if(o == '+')// adicionar aresta
            mapa[mp(u, v)] = cur++;
        else if(o == '-')// remover aresta
            add_edge(1, 0, MAX-1, mapa[mp(u, v)], cur++, mp(u, v))
            mapa.erase(mp(u, v));
    else // verificar se dois vertices estao na mesma componente
        add_query(1, 0, MAX-1, cur++, 1);
cur++;
for(auto it : mapa)
    add_edge(1, 0, MAX-1, it.second, cur, it.first);
dfs(1, 0, MAX-1);
for(int i = 0; i < ans.size(); i++)</pre>
    cout << ans[i] << '\n';
return 0;
```

1.15 Hopcroft Karp

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f3f;
int n, m;
vector<int> G[10000];
queue<int> q;
int pairU[10000], pairV[10000], dist[10000];
bool bfs()
    for(int u = 1; u <= m; u++)</pre>
        if(!pairU[u])
            dist[u] = 0;
            q.push(u);
        else dist[u] = 00;
    dist[0] = 00;
    while(!q.empty())
        int u = q.front();
        q.pop();
        if(dist[u] < dist[0])</pre>
            for(const int &v : G[u])
                if(dist[pairV[v]] == 00)
                     dist[pairV[v]] = dist[u] + 1;
                     q.push(pairV[v]);
```

```
return (dist[0] != 00);
bool dfs(int u)
    if(u)
    for(const int &v : G[u])
            if (dist[pairV[v]] == dist[u]+1)
                if (dfs(pairV[v]))
                    pairV[v] = u;
                    pairU[u] = v;
                    return true;
        dist[u] = 00;
        return false;
    return true;
int hopcroftKarp()
    memset(pairU, 0, sizeof(pairU));
    memset(pairV, 0, sizeof(pairV));
    int result = 0;
    while (bfs())
        for(int u = 1; u <= m; u++)
            if(!pairU[u] and dfs(u))
                result++;
    return result;
int main()
  n = m = 4;
 G[1].push_back(2);
  G[2].push_back(1);
 G[1].push_back(3);
  G[3].push_back(1);
 G[2].push_back(1);
  G[1].push_back(2);
 G[3].push_back(2);
  G[2].push_back(3);
  G[4].push_back(2);
  G[2].push_back(4);
  G[4].push_back(4);
  G[4].push_back(4);
  cout << hopcroftKarp() << '\n';
  return 0;
```

1.16 K Short Paths

#include <bits/stdc++.h>
using namespace std;

```
#define int long long
const int 00 = 0x3f3f3f3f3f3f3f3f3f;
const int MAX = 2000000;
typedef pair<int, int> ii;
int n, m, k;
vector<ii> G[MAX];
int cnt[MAX];
void dijkstra(int v) {
  priority_queue<ii> pq;
 pq.push({0, v});
  int c = 0;
  while(!pq.empty()) {
    int u = -pq.top().second;
   int d = -pq.top().first;
    pq.pop();
    cnt[u]++;
    if(cnt[u] > k) continue;
      if(u == n - 1) {
        cout << d << ' ';
      if(++c == k) { cout << '\n'; return; }</pre>
    for(auto [_d, w] : G[u])
      if(cnt[w] < k)
        pq.push({-(d + _d), -w});
int32_t main() {
  cin >> n >> m >> k;
  while (m--) {
   int u, v, w;
   cin >> u >> v >> w; u--; v--;
   G[u].push_back(\{w, v\});
  dijkstra(0);
  return 0;
```

1.17 Knapsack Dijkstra

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
#define ii pair<int, int>
#define fi first
#define se second

vector<ii>> G[105];
int dist[100000008];
vector<int> peso;

void dijkstra()
{
   memset(dist, 63, sizeof(dist));
   dist[0] = 0;
   priority_queue<ii>> pq;
```

```
pq.push({0, 0});
  while(!pq.empty())
    int u = pq.top().se;
    int d = -pq.top().fi;
    ; () qoq.pq
    if(d > dist[u]) continue;
    for(int i = 0; i < G[u].size(); i++)</pre>
      int w = G[u][i].fi, dd = G[u][i].se;
      if(dist[w] > dist[u] + dd)
        dist[w] = dist[u] + dd;
        pq.push({-dist[w], w});
  dist[0] = peso[0];
int32_t main()
  int n, e, d;
  cin >> n >> d >> e;
  // ler pesos
 peso = vector<int>{d, 2 * d, 5 * d, 10 * d, 20 * d, 50 * d, 100 * d,
   5 * e, 10 * e, 20 * e, 50 * e, 100 * e, 200 * e};
  // ordena pra pegar o menor valor
  sort(peso.begin(), peso.end());
  //montar grafo
  for(int i = 0; i < peso[0]; i++)</pre>
    for(int j = 0; j < peso.size(); j++)</pre>
      int x = (i + peso[j]) % peso[0];
      G[i].push_back({x, peso[j]});
    dist[i] eh o menor numero que eu consigo formar usando
    os meus objetos tal que dist[i] % peso[0] == i
  dijkstra();
    se dist[X % peso[0]] \le X eh possivel gerar um valor X
    utilizando os valores do array peso
    OBS: cada valor pode ser usado infinitas vezes
  return 0;
```

1.18 Kuhn MCBM

```
#include <bits/stdc++.h>
using namespace std;

int na, nb, m, tempo = 1;
int b[105];
int cor[105];
vector<int> G[105];
```

```
bool kuhn (int u)
  if(cor[u] == tempo)
    return 0;
  cor[u] = tempo;
//random_shuffle(G[u].begin(), G[u].end(), [](int x){ return rand() %
  for(const int &v : G[u])
    if(!b[v] or kuhn(b[v]))
      return b[v] = u;
  return 0;
int main()
  //srand(time(NULL));
  cin >> na >> nb >> m;
  while (m--)
    int u, v;
    cin >> u >> v;
    G[u].push back(v + na);
  tempo = 1;
  int ans = 0;
  for(int i = 1; i <= na; i++)
    ans += kuhn(i), tempo++;
  cout << "MCBM = " << ans << '\n';
  for(int i = nb + 1; i <= na + nb; i++)</pre>
    if(b[i])
      cout << b[i] << ' ' << i - na << '\n';
      return 0;
```

1.19 Lca With Square Root Decomposition

```
#include <bits/stdc++.h>
const int MAX = 50500;
using namespace std;
vector<int> G[MAX];
int nivel[MAX], pai[MAX], jump[MAX], n, blk_sz;
void dfs(int v, int d, int p)
    pai[v] = p;
    nivel[v] = d;
    (nivel[v] blk_sz == 0) ? jump[v] = pai[v] : jump[v] = jump[p];
    for(const int &u : G[v])
        if(u != p)
            dfs(u, d + 1, v);
int lcaTrivial(int u, int v)
    while(u != v)
        (nivel[u] > nivel[v]) ? u = pai[u] : v = pai[v];
    return u;
```

```
int lca(int u, int v)
    while(jump[u] != jump[v])
        (nivel[u] > nivel[v]) ? u = jump[u] : v = jump[v];
    return lcaTrivial(u, v);
void build()
    blk_sz = sqrt(n);
    dfs(0, 0, 0);
int main()
    int x, y;
    cin >> n;
    for (int i = 0; i < n-1; i++)
        cin >> x >> y;
        G[x-1].push_back(y-1);
        G[y-1].push_back(x-1);
    build();
    cin >> x >> y;
    cout << lca(x-1, y-1) + 1 << '\n';
    return 0;
```

1.20 Lca With Tree Linearization And Segment Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int pos[MAX];
int deft[MAX];
int segtree[5*MAX];
vector<int> tl;
vector<int> G[MAX];
void tree_linearization(int v, int p, int d)
 deft[v] = d;
  pos[v] = tl.size();
  tl.push_back(v);
  for(const int &u : G[v])
    if(u != p)
      tree_linearization(u, v, d + 1);
      tl.push_back(v);
void build(int node, int start, int end)
```

```
if(start == end)
    segtree[node] = tl[start];
  else
    int mid = (start+end)/2;
    build(2*node, start, mid);
    build(2*node+1, mid+1, end);
    if(deft[segtree[2*node]] < deft[segtree[2*node+1]])</pre>
      segtree[node] = segtree[2*node];
    else
      segtree[node] = segtree[2*node+1];
int lca(int node, int start, int end, int l, int r)
  if(l > end or r < start)</pre>
    return -1;
  if(1 <= start and end <= r)</pre>
    return segtree[node];
  int mid = (start+end)/2;
  int p1 = lca(2*node, start, mid, l, r);
  int p2 = lca(2*node+1, mid+1, end, l, r);
  if(p1 == -1) return p2;
  if(p2 == -1) return p1;
  return deft[p1] < deft[p2] ? p1 : p2;</pre>
/*int _lca(int a, int b)
  int ancestor = a, nivel = 0x3f3f3f3f;
  for (int i = pos[a]; i \le pos[b]; i++)
    if(deft[tl[i]] < nivel)</pre>
      ancestor = tl[i];
      nivel = deft[t1[i]];
  return ancestor;
int main()
  int n, u, v;
  cin >> n;
  for (int i = 0; i < n-1; i++)
    cin >> u >> v;
    G[u].push_back(v);
    G[v].push_back(u);
  tree_linearization(1, -1, 0);
  build(1, 0, tl.size()-1);
  for(int i = 1; i <= n; i++)
    cout << deft[i] << ' ';
  cout << '\n';
```

```
for(int i = 1; i <= n; i++)
    cout << pos[i] << ' ';
cout << '\n';
for(const int &p : tl)
    cout << p << ' ';
cout << '\n';
for(int i = 1; i <= 4*n; i++)
    cout << segtree[i] << ' ';
cout << '\n';*/
while(cin >> u >> v)
    cout << /*_lca(u, v) << ' ' <<*/
    lca(1, 0, tl.size()-1, pos[u], pos[v]) << '\n';
return 0;</pre>
```

1.21 Lca With Tree Linearization And Sparse Table

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
int n, m;
vector<int> G[MAX], tl;
int deft[MAX], SpT[27][MAX], pos[MAX];
void tree_linearization(int v, int p, int d)
 deft[v] = d;
 pos[v] = tl.size();
  tl.push_back(v);
  for(int &u : G[v])
    if(u != p)
      tree_linearization(u, v, d + 1);
      tl.push_back(v);
void build(int tam)
  for(int i = 0; (1 << i) <= tam; i++)
    for (int j = 0; j + (1 << i) <= tam; <math>j++)
      if(!i)
        SpT[i][j] = tl[j];
      else if (deft[SpT[i-1][j]] < deft[SpT[i-1][j+(1<<(i-1))]])
        SpT[i][j] = SpT[i-1][j];
      else
        SpT[i][j] = SpT[i-1][j+(1<<(i-1))];
int lca(int i, int j)
  int k = log2(j-i+1);
  if (deft[SpT[k][i]] < deft[SpT[k][j+1-(1<<k)]])</pre>
```

```
return SpT[k][i];
  else
    return SpT[k][j+1-(1<<k)];
int main()
    int u, v, q;
  cin >> n >> m;
  for(int i = 0; i < m; i++)</pre>
    cin >> u >> v:
    G[u].push_back(v);
    G[v].push_back(u);
  tree_linearization(1, -1, 0);
 build(tl.size());
  cin >> q;
  while (q--)
    cout << lca(min(pos[u], pos[v]), max(pos[u], pos[v])) << '\n';
  return 0;
```

1.22 Longest And Shortest Path In DAG

```
#include <bits/stdc++.h>
const int 00 = 0x3f3f3f3f;
const int MAX = 1e6;
using namespace std;
vector<pair<int, int>> G[MAX];
int dist1[MAX], dist2[MAX];
vector<int> ts;
bool cor[MAX];
void dfs(int v)
  cor[v] = true;
  for(pair<int, int> &w : G[v])
   if(!cor[w.first])
      dfs(w.first);
  ts.push_back(v);
// caminho de 0 a n-1
pair<int, int> longestAndShortestPathInDAG()
  for(int i = 0; i <= n; i++)
    dist1[i] = -00, dist2[i] = 00;
  dist1[0] = dist2[0] = 0;
```

```
int p = 0;
  while(p < (int)ts.size())</pre>
    int v = ts[p++];
    if(dist1[v] != -00)
      for (int i = 0; i < (int)G[v].size(); i++)
        int u = G[v][i].first, d = G[v][i].second;
        if(dist1[u] < dist1[v] + d)
          dist1[u] = dist1[v] + d;
    if(dist2[v] != 00)
      for (int i = 0; i < (int)G[v].size(); i++)
        int u = G[v][i].first, d = G[v][i].second;
        if(dist2[u] > dist2[v] + d)
          dist2[u] = dist2[v] + d;
  return {dist1[n-1], dist2[n-1]};
int main()
  cin >> n >> m;
  for(int i = 0; i < m; i++)</pre>
    int u, v, w;
    cin >> u >> v >> w; u--; v--;
    G[u].push_back(\{v, w\});
  for(int i = 0; i < n; i++)</pre>
    if(!cor[i])
      dfs(i);
  reverse(ts.begin(), ts.end());
  pair<int, int> ans = longestAndShortestPathInDAG();
  cout << "Longest Path " << ans.first << '\n';</pre>
  cout << "Shortest Path " << ans.second << '\n';</pre>
  return 0;
```

1.23 MCE MinimumEdgeCover

```
#include <bits/stdc++.h>
using namespace std;

vector<int> G[1000];
int b[1000], vis[1000], tempo;

bool kuhn(int v)
{
   if(vis[v] == tempo)
      return 0;
   vis[v] = tempo;
   for(const int &u : G[v])
      if(!b[u] or kuhn(b[u]))
      return b[u] = v;
   return 0;
}
```

```
int main()
  int n, m, e;
  cin >> n >> m >> e;
  while (e--)
    int u, v;
   cin >> u >> v;
    G[u].push_back(v + n);
  int ans = 0;
  tempo = 1;
  for(int i = 1; i <= n; i++)</pre>
    ans += kuhn(i), tempo++;
  //encontrar as arestas do Minimum Edge Cover
  vector<bool> covered(n + m + 10, false);
    vector<pair<int, int>> cover;
  for(int i = n + 1; i <= n + m; i++)</pre>
    if(b[i])
      covered[b[i]] = covered[i] = true;
      cover.push_back({b[i], i - n});
  for(int i = 1; i <= n; i++)</pre>
    bool is covered = covered[i];
    for(const int &u : G[i])
      if(!covered[u])
        is_covered = true;
        cover.push_back({i, u - n});
        covered[i] = covered[u] = true;
    if(!is_covered and !G[i].empty())
      cover.push_back({i, G[i].front() - n});
  cout << "MEC = " << cover.size() << '\n';</pre>
  for(int i = 0; i < cover.size(); i++)</pre>
    cout << cover[i].first << ' ' << cover[i].second << '\n';</pre>
    return 0;
```

1.24 MPC MinimumPathCover

```
#include <bits/stdc++.h>
using namespace std;

int n, m;
vector<int> G[1000], bip[1000], ts;
int vis[1000], b[1000], go[1000], tempo = 1;

bool kuhn(int v)
{
   if(vis[v] == tempo)
     return 0;
   vis[v] = tempo;
```

```
for(const int &u : bip[v])
    if(!b[u] or kuhn(b[u]))
      go[v] = u - n;
      return b[u] = v;
  return 0;
void topological_sort(int v)
  vis[v] = tempo;
  for(const int &u : G[v])
    if(vis[u] != tempo)
      topological_sort(u);
  ts.push_back(v);
int main()
  cin >> n >> m;
  while (m--)
    int u, v;
    cin >> u >> v;
    G[u].push_back(v);
    bip[u].push_back(v + n);
  int ans = 0;
  for(int i = 1; i <= n; i++)</pre>
    ans += kuhn(i), tempo++;
  for(int i = 1; i <= n; i++)</pre>
    if(vis[i] != tempo)
      topological_sort(i);
  reverse(ts.begin(), ts.end());
  tempo++;
  cout << n - ans << '\n';
  for(int i = 0; i < n; i++)</pre>
    int u = ts[i];
    if(vis[u] != tempo)
      while (u)
        vis[u] = tempo;
        cout << u << ' ';
        u = go[u];
      puts("");
    return 0;
```

1.25 MVC MinimumVertexCover

```
#include <bits/stdc++.h>
using namespace std;
```

```
vector<int> G[1000];
int b[1000], vis[1000], tempo;
bool be[1000];
set<int> r0, r1;
bool kuhn (int v)
  if(vis[v] == tempo)
    return 0;
  vis[v] = tempo;
  for(const int &u : G[v])
    if(!b[u] or kuhn(b[u]))
      return b[u] = v;
  return 0;
void MVC(int v)
  if(vis[v] == tempo)
    return;
  vis[v] = tempo;
  for(const int u : G[v])
    if(b[u] != v and b[u])
      rl.insert(u);
      vis[b[u]] = tempo;
int main()
  int n, m, e;
  cin >> n >> m >> e;
  while (e--)
    int u, v;
    cin >> u >> v;
    G[u].push_back(v);
  int ans = 0;
  tempo = 1;
  for(int i = 1; i <= n; i++)</pre>
    ans += kuhn(i), tempo++;
  for(int i = n + 1; i <= n + m; i++)</pre>
    if(b[i])
      be[i - n] = be[b[i]] = true;
  for(int i = 1; i <= n; i++)</pre>
    if(!be[i])
      MVC(i);
  for(int i = 1 ; i <= n; i++)</pre>
    if(vis[i] < tempo)</pre>
      r0.insert(i);
  cout << "MVC = "<< ans << '\n';
  cout << "tamanho lado esquerdo " << r0.size() << '\n';</pre>
  for(auto it = r0.begin(); it != r0.end(); it++)
    cout << *it << ' ';
  puts("");
  cout << "tamanho lado direito " << r1.size() << '\n';</pre>
  for(auto it = r1.begin(); it != r1.end(); it++)
    cout << *it - n << ' ';
  puts("");
```

```
return 0;
```

1.26 Maximum Clique

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
const int MAX = 43, C = 20;
int n, m, dp[1 << C];</pre>
11 G[MAX];
int maxClique()
  for (int i = 1; i < (1 << max(0, n - C)); i++)
    int x = i:
    for (int j = 0; j < max(0, n - C); j++)
     if((i >> j) & 1)
        x \&= G[j + C] >> C;
    if(x == i) dp[i] = __builtin_popcount(i);
  for (int i = 1; i < (1 << max(0, n - C)); i++)
    for (int j = 0; j < max(0, n - C); j++)
      if((i >> j) & 1)
        dp[i] = max(dp[i], dp[i ^ (1 << j)]);
  int ans = 0;
  for(int i = 0; i < (1 << min(C, n)); i++) {</pre>
    int x = i, y = (1 << max(0, n - C)) - 1;
    for(int j = 0; j < min(C, n); j++)</pre>
      if((i >> j) & 1)
        x \&= G[j], y \&= G[j] >> C;
    if(x == i)
        ans = max(ans, __builtin_popcount(i) + dp[y]);
  return ans;
int main()
    cin >> n >> m;
    while (m--)
        int u, v;
        cin >> u >> v; u--; v--;
        G[u] = (1LL << v);
        G[v] = (1LL << u);
    for(int i = 0; i < n; i++)</pre>
        G[i] = (1LL << i);
    cout << maxClique() << '\n';</pre>
  return 0;
```

1.27 Min Cost Max Flow

```
from IME Library
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
const int 00 = 0x3f3f3f3f3f;
struct edge {int v, f, w, c; };
// flw_lmt eh a quantidade de de fluxo que posso passar
// no maximo, alterar se necessario
// node_count eh o valor do maior vertice no grafo...
// inicializar node_count com numero de vertices no inicio...
int node_count, flw_lmt = 00, p[MAX];
vector<edge> edges;
vector<int> G[MAX];
// u--->v, custo w e capacidade c
void add_edge(int u, int v, int w, int c)
  int k = edges.size();
  node count = max(node count, u+1);
  node_count = max(node_count, v+1);
  G[u].push_back(k);
 G[v].push_back(k+1);
 edges.push_back({ v, 0, w, c });
  edges.push_back({ u, 0, -w, 0 });
void clear()
  flw_lmt = 00;
  for(int i = 0; i < node_count; ++i) G[i].clear();</pre>
  edges.clear();
 node count = 0:
bool SPFA(int s, int t)
  vector<int> dist(node_count, 00);
 vector<int> et (node_count, 0);
  deque<int> q;
  q.push_back(s), dist[s] = 0;
  while (!q.empty())
    int u = q.front(); q.pop_front();
    et[u] = 2;
    for(int i : G[u])
      edge &e = edges[i];
      int v = e.v;
      if (e.f < e.c and dist[v] > dist[u] + e.w)
        dist[v] = dist[u] + e.w;
        if (et[v] == 0) q.push_back(v);
        else if (et[v] == 2) q.push_front(v);
        et[v] = 1;
        p[v] = i;
```

```
return dist[t] != 00;
int min cost max flow(int s, int t)
 int mf = 0, cost = 0;
    while(SPFA(s, t) and mf < flw lmt)</pre>
    int inc = flw_lmt - mf;
    for (int u = t; u != s; u = edges[p[u]^1].v)
      edge &e = edges[p[u]];
      inc = min(inc, e.c - e.f);
    for (int u = t; u != s; u = edges[p[u]^1].v)
      edge &e = edges[p[u]], &rev = edges[p[u]^1];
      e.f += inc;
      rev.f -= inc;
      cost += inc * e.w;
       if (!inc) break;
       mf += inc;
 cout << "Max Flow " << mf << '\n';
 cout << "Min Cost " << cost << '\n';
 return cost;
int main()
 return 0;
```

1.28 Prim

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
const int 00 = 0x3f3f3f3f3f;
typedef pair<int, int> ii;
typedef pair<int, ii> iii;
int n, m;
vector<ii> G[MAX];
int dist[MAX], edge[MAX];
bool visit[MAX];
void prim(int s)
    memset(visit, 0, sizeof(visit));
    memset(dist, 63, sizeof(dist));
    dist[s] = 0;
    priority_queue<ii>> pq;
    pq.push({0, s});
    while(!pq.empty())
```

```
int u = pq.top().second;
        pq.pop();
        if(visit[u]) continue;
        for(int i = 0; i < G[u].size(); i++)</pre>
            int v = G[u][i].second, d = G[u][i].first;
            if(!visit[v] and dist[v] > d)
                dist[v] = d;
                edge[v] = u;
                pq.push({-d, v});
        visit[u] = true;
    int ans = 0;
   edge[s] = -2;
    for(int i = 0; i < n; i++)
        cout << edge[i]+1 << ' ';
        ans += dist[i];
   cout << '\n';
   cout << ans << '\n';
int main()
   int u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w; u--; v--;
        G[u].push_back({w, v});
        G[v].push_back({w, u});
   prim(0);
    return 0;
```

1.29 Tree Isomorfism

```
#include <bits/stdc++.h>
using namespace std;

const int ms = 100100;

int degree[ms], vis[ms];
int size[ms];
int n;

bool cmp(int a, int b)
{
  return size[a] < size[b];
}

void pre(vector<vector<int>> &edges, int on = 0)
```

```
size[on] = 1;
  for(auto to : edges[on])
    pre(edges, to);
    size[on] += size[to];
  sort(edges[on].begin(), edges[on].end(), cmp);
void solve(vector<vector<int>> &edges, string &str, int on = 0)
  str += 'D';
  for(int l = 0, r = 0; l < edges[on].size(); l = r) {</pre>
    while(r < edges[on].size() &&</pre>
      size[edges[on][l]] == size[edges[on][r]]) r++;
    if(r == 1 + 1)
      solve(edges, str, edges[on][1]);
      priority_queue<string> hp;
      for(int i = 1; i < r; i++) {</pre>
        string temp;
        solve(edges, temp, edges[on][i]);
        hp.push(temp);
      while (!hp.empty())
        str += hp.top();
        hp.pop();
  str += 'U';
// enraizar arvore
void mount(vector<vector<int>> &graph,
  vector<vector<int>> &G, int v = 0, int p = -1)
  for(int &u : G[v])
    if(u != p)
      graph[v].push_back(u);
      mount(graph, G, u, v);
// achar centro da arvore e enraizar no centro
void findCenterAndComputeStr(vector<vector<int>> &graph,
  vector<vector<int>> &G, string *str)
  memset(vis, 0, sizeof(vis));
  queue<int> fila[2];
  for(int i = 0; i < n; i++)</pre>
    if(degree[i] == 1)
      fila[0].push(i);
  int cnt = 0, turn = 0;
  while (cnt + 2 < n)
    while(!fila[turn].empty())
```

```
int u = fila[turn].front(); fila[turn].pop();
      vis[u] = true;
      cnt++;
      for(int i = 0; i < G[u].size(); i++)</pre>
        if(!vis[G[u][i]])
          degree[G[u][i]]--;
          if(degree[G[u][i]] == 1)
            fila[1-turn].push(G[u][i]);
   turn ^= 1;
  int k = 0;
  for(int i = 0; i < n; i++)</pre>
   if(vis[i]) continue;
   graph.clear();
   graph.resize(n + 1);
   mount (graph, G, i);
   pre(graph, i);
   solve(graph, str[k], i);
   k++;
int main()
 while(cin >> n)
   string str[2][2];
    for(int i = 0; i < 2; i++)
      vector<vector<int>> graph, G;
      G.resize(n + 1);
      memset (degree, 0, sizeof (degree));
      for (int j = 1; j < n; j++)
        int u, v;
        scanf(" %d %d", &u, &v); v--; u--;
        G[v].push_back(u);
        G[u].push_back(v);
        degree[v]++;
        degree[u]++;
      findCenterAndComputeStr(graph, G, str[i]);
   bool fl = (str[0][0] == str[1][0]) or (str[0][0] == str[1][1]);
   fl |= ((str[0][1] == str[1][0]) or (str[0][0] == str[1][1]));
   puts(fl ? "S" : "N");
 return 0;
```

2 Data Structures

2.1 BIT 1D

```
#include <bits/stdc++.h>
using namespace std;
int aux, n, arr[1000], BIT[1000];
// construir uma BIT a partir de um array em O(N)
void build() {
  for(int i = 1; i <= n; i++) {</pre>
    BIT[i] += arr[i];
    if(i + (i \& -i) \le n)
      BIT[i + (i \& -i)] += BIT[i];
// construir o array que gera a BIT a partir de uma BIT em O(N)
void buildArrav() {
  for(int i = n; i >= 1; i--)
    if(i + (i \& -i) \le n)
      BIT[i + (i \& -i)] -= BIT[i];
int sum(int x) {
    int s = 0;
    while (x) s += BIT[x], x -= x\&-x;
    return s;
void update(int x, int value) {
    while (x \le n) BIT [x] += value, x += x\&-x;
int main() {
    cin >> n;
    for(int i = 1; i <= n; i++) {</pre>
        cin >> aux;
        update(i, aux);
    int a, b;
    cin >> a >> b;
    cout << sum(b) -sum(a-1) << ' \n';
    return 0;
```

2.2 BIT 2D

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = le3;
int n, aux, BIT[MAX][MAX];
void update(int x, int y, int value)
```

```
for (int i = x; i \le n; i += i \& -i)
    for (int j = y; j \le n; j += j\&-j)
      BIT[i][j] += value;
int query(int x, int y)
  int sum = 0;
  for (int i = x; i > 0; i -= i\&-i)
    for (int j = y; j > 0; j = j\&-j)
      sum += BIT[i][j];
  return sum;
int queryInRectangle(int x1, int y1, int x2, int y2)
 int sum = 0;
 sum += query (max(x1, x2), max(y1, y2));
  sum -= query (max (x1, x2), min (y1, y2) - 1);
  sum -= query (min (x1, x2) - 1, max (y1, y2));
  sum += query(min(x1, x2) - 1, min(y1, y2) - 1);
  return sum;
int main()
  cin >> n;
  for(int i = 1; i <= n; i++)</pre>
   for(int j = 1; j <= n; j++)
      cin >> aux, update(i, j, aux);
  int x1, y1, x2, y2;
  while(cin >> x1 >> y1 >> x2 >> y2)
    cout << queryInRectangle(x1, y1, x2, y2) << '\n';</pre>
  return 0;
```

2.3 BIT Range Sum And Range Update

```
#include <bits/stdc++.h>
const int MAX = 1e5;

using namespace std;

struct BIT {
   int N;
   int BIT1[MAX];
   int BIT2[MAX];
   int BIT2[MAX];

BIT(int M) {
    N = M;
   }

   void add(int *b, int pos, int x) {
     while(pos <= N) b[pos] += x, pos += pos&-pos;
   }

   void range_add(int 1, int r, int x) {</pre>
```

```
add(BIT1, l, x);
    add(BIT1, r + 1, -x);
    add(BIT2, 1, x * (1 - 1));
    add(BIT2, r + 1, -x * r);
  int sum(int *b, int pos) {
    int s = 0;
    while(pos) s += b[pos], pos -= pos&-pos;
    return s;
  int prefix_sum(int pos) {
    return sum(BIT1, pos) * pos - sum(BIT2, pos);
  int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(l - 1);
};
int main() {
  int n, q;
  cin >> n >> q;
  BIT B(n);
  while(q--) {
    int o, 1, r, x;
    cin >> o >> l >> r;
    if(0 == 1) {
      cout << B.range_sum(1, r) << '\n';
      cin >> x;
       B.range_add(l, r, x);
  return 0;
```

2.4 Centroid Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

int n, m, Centroid_Tree[MAX], Size[MAX];
vector<int> G[MAX], cTree[MAX];
bool cut[MAX];

int dfs(int v, int p)
{
   int s = 1;
   for(const int &u : G[v])
      if(!cut[u] and u != p)
      s += dfs(u, v);
   return Size[v] = s;
}
```

```
int Find_Centroid(int v, int p, int tot)
  int next, cnt = 0;
  for(const int &u : G[v])
    if(!cut[u] and u != p and cnt < Size[u])</pre>
      cnt = Size[u];
      next = u;
  if(cnt > tot/2) return Find_Centroid(next, v, tot);
  return v:
void build(int v, int p)
  dfs(v, -1);
  int u = Find_Centroid(v, -1, Size[v]);
  cut[u] = true;
  Centroid_Tree[u] = p;
  if(p !=-1)
      cTree[u].push_back(p);
      cTree[p].push_back(u);
  for(const int &w : G[u])
    if(!cut[w])
      build(w, u);
int main()
    int u, v;
 memset(Centroid_Tree, -1, sizeof Centroid_Tree);
    cin >> n >> m;
    while (m--)
      cin >> u >> v;
      u--; v--;
    G[u].push_back(v);
    G[v].push_back(u);
  build(0, -1);
    for(int i = 0; i < n; i++)</pre>
        cout << i+1 << ": ";
        for(int &w : cTree[i])
            cout << w+1 << ' ';
        cout << '\n';
    }
  return 0;
```

2.5 Color Update

```
#include <bits/stdc++.h>
using namespace std;
#define bug(x) cout << #x << " >>>>>> " << x << '\n'</pre>
```

```
#define _ << " , " <<
#define INF 0x3f3f3f3f3f
#define ii pair<int, int>
#define fi first
#define se second
struct Color {
  int x;
  Color(int _x) : x(_x) {}
  Color() : x(-1) {}
  bool operator<(const Color &c) const {</pre>
    return x < c.x;
} ;
#define iic pair<pair<int, int>, Color>
#define defaut_color Color(-1)
struct ColorUpdate {
  set<iic> intervals:
  ColorUpdate(int begin = -INF, int end = INF) {
    intervals.insert( { {begin, end}, defaut_color } );
  void paint(int 1, int r, Color c = defaut color) {
    if(l > r) return;
    auto a = prev(intervals.upper_bound({{1, INF}, INF}));
    auto b = prev(intervals.upper_bound({{r, INF}, INF}));
    int l1 = a->fi.fi, r1 = l - 1;
    Color c1 = a \rightarrow se:
    int 12 = r + 1, r2 = b->fi.se;
    Color c2 = b \rightarrow se;
    intervals.erase(a, next(b));
    if(l1 <= r1) intervals.insert({{l1, r1}, c1});</pre>
    if(12 <= r2) intervals.insert({{12, r2}, c2});</pre>
    if(l <= r) intervals.insert({{l, r}, c});</pre>
    // printall();
  Color get_color_of(int x) {
    return prev(intervals.upper_bound({{x, INF}, INF}))->se;
  // true if x is in some interval
  bool find(int x) {
    auto a = intervals.upper_bound({{x, INF}, INF});
    if(a == intervals.begin()) return false;
    if(a->fi.fi > x or a->fi.se < x) return false;</pre>
    return true;
  ii get_interval_of(int x) {
    if(!find(x)) return {-INF, INF};
```

```
return prev(intervals.upper_bound({{x, INF}, INF}))->fi;
  ii get_interval_of(int l, int r) {
    if(!find(l)) return {-INF, INF};
    ii i = get interval of(1);
    if(i.fi <= r and r <= i.se) return i;</pre>
    return {-INF, INF};
  // x will be on the left side
  void cut_at(int x) {
    if(!find(x)) return;
    auto a = prev(intervals.upper_bound({{x, INF}, INF}));
    Color c = a -> se;
    int 11 = a->fi.fi, r1 = x;
    int 12 = x + 1, r2 = a -> fi.se;
    intervals.erase(a);
    if(l1 <= r1) intervals.insert({{l1, r1}, c});</pre>
    if(12 <= r2) intervals.insert({{12, r2}, c});</pre>
  void remove_interval(int 1, int r) {
    cut at (1 - 1);
    cut_at(r);
    auto a = prev(intervals.upper_bound({{l, INF}, INF}));
    auto b = prev(intervals.upper_bound({{r, INF}, INF}));
    intervals.erase(a, next(b));
  void remove_at(int x) {
    remove_interval(x, x);
  void p_interval(iic i) {
    cout << "elements from " << i.fi.fi << " to " << i.fi.se;</pre>
    cout << " have color " << i.se.x << endl;</pre>
  void printall() {
    cout << "\n\n\nColor Of The Elements:\n";</pre>
    for(auto it : intervals)
      p_interval(it);
    cout << endl << endl;</pre>
};
int32_t main() {
  ios_base::sync_with_stdio(false);
  cin.tie(nullptr);
  ColorUpdate C(1, 100);
```

```
for(int i = 3; i <= 50; i += 10)
    C.cut_at(i);

C.remove_interval(16, 57);

C.remove_at(100);
C.remove_at(1);
C.remove_at(2);
C.remove_at(3);

C.cut_at(20);

C.printall();

return 0;</pre>
```

2.6 DSU With Partial Persistence

```
int n, pai[MAX], sz[MAX], his[MAX], tempo;
void init()
  tempo = 0;
 for(int i = 0; i < n; i++)</pre>
    pai[i] = i, sz[i] = 1, his[i] = 0;
int find(int x, int t)
  if(pai[x] == x) return x;
  if(his[x] > t) return x;
  return find(pai[x], t);
void join(int u, int v)
  tempo++;
  u = find(u, tempo);
  v = find(v, tempo);
  if(sz[u] > sz[v]) swap(u, v);
  pai[u] = v;
  his[u] = tempo;
  sz[v] += sz[u];
```

2.7 Dynamic Segment Tree With Lazy Propagation

```
#include <bits/stdc++.h>
using namespace std;

struct Node
{
   int l, r, value;
};

vector<Node> tree;
vector<int> lazy;
```

```
int init()
  tree.clear();
  lazy.clear();
 tree.emplace back();
  lazy.push_back(0);
void createL(int node)
  tree[node].l = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void createR(int node)
  tree[node].r = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void calc(int node)
  tree[node].value = 0;
  if(tree[node].1) tree[node].value += tree[tree[node].1].value;
  if(tree[node].r) tree[node].value += tree[tree[node].r].value;
void push(int node, int start, int end)
  tree[node].value = lazy[node] * (end - start + 1);
  if(start != end)
    if(tree[node].l == 0) createL(node);
    if(tree[node].r == 0) createR(node);
    lazy[tree[node].l] = lazy[node]; // +=
    lazy[tree[node].r] = lazy[node]; // +=
  lazy[node] = 0;
void update (int node, int start, int end, int l, int r, int value)
 if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return;
  if(l <= start and end <= r)</pre>
    tree[node].value = value * (end - start + 1); // +=
    if(start != end)
      if(tree[node].l == 0) createL(node);
      if(tree[node].r == 0) createR(node);
      lazy[tree[node].l] = value; // +=
      lazy[tree[node].r] = value; // +=
```

```
else
    int mid = (start + end) / 2;
    if(tree[node].l == 0) createL(node);
    update(tree[node].1, start, mid, 1, r, value);
    if(tree[node].r == 0) createR(node);
    update(tree[node].r, mid + 1, end, 1, r, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return 0;
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
int main()
  int n, q;
  cin >> n >> q;
  init();
  for(int i = 0; i < n; i++)</pre>
    int x;
    cin >> x:
    update (0, 0, n - 1, i, i, x);
  while (q--)
    int o, l, r, x;
    cin >> o >> l >> r;
    if(0 == 1)
      cin >> x;
      update (0, 0, n - 1, 1 - 1, r - 1, x);
      cout << query (0, 0, n - 1, 1 - 1, r - 1) <math><< ' \ '';
  return 0;
```

2.8 Dynamic Segment Tree With Vector

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
```

```
struct Node
  int 1, r, value;
vector<Node> tree;
int init()
  tree.emplace_back();
void calc (int node)
  tree[node].value = 0;
  if(tree[node].l) tree[node].value += tree[tree[node].l].value;
 if(tree[node].r) tree[node].value += tree[tree[node].r].value;
void update(int node, int start, int end, int idx, int value)
  if(start == end)
    tree[node].value = value;
  else
    int mid = (start + end) / 2;
    if(start <= idx and idx <= mid)</pre>
      if(tree[node].l == 0)
        tree[node].l = tree.size();
        tree.emplace_back();
      update(tree[node].l, start, mid, idx, value);
    else
      if(tree[node].r == 0)
        tree[node].r = tree.size();
        tree.emplace_back();
      update(tree[node].r, mid + 1, end, idx, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(l > end or r < start) return 0;</pre>
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
int main()
```

```
int n, q;

cin >> n >> q;
init();
while(q--)
{
  int o, l, r;
    cin >> o >> l >> r;
    if(o == 1) update(0, 0, n - 1, l - 1, r);
    else cout << query(0, 0, n - 1, l - 1, r - 1) << '\n';
}

return 0;</pre>
```

2.9 Heavy Light Decomposition Path And Subtree Queries

```
no intervalo [ in[v], out[v] ) do array A
temos a subarvore de v. Para fazer consultas
basta usar a segtree.
no intervalo [ in[nxt[v]], in[v] ] temos os vertices no
caminho de nxt[v] ate v, Em que nxt[v] esta no inicio da
cadeia da HLD. e o caminho de nxt[v] ate v faz parte da
cadeia que comeca em nxt[v].
Assim, podemos processar queries rapidamente em caminhos
e subarvores usando a mesma segment tree.
Bonus: para uma query de mudanca de raiz: se a raiz atual
for v e a consulta for na subarvore de u, entao, se u for
ancestral de v a resposta eh a consulta da arvore
total menos a consulta da subarvore enraizada pelo filho
de u que en ancestral de v, caso contrario a consulta en
normal como se a raiz da arvore nunca tivesse mudado.
obs: Para encontrar o filho de u que eh ancestral de v
podemos usar binary lifting, da mesma forma que usamos
para calcular lca.
*/
#include <bits/stdc++.h>
using namespace std;
const int MAX = 5 * 1e5;
int n:
vector<int> Adj[MAX], G[MAX], A;
int in[MAX], out[MAX], rin[MAX], sz[MAX], nxt[MAX], arr[MAX], t = 0;
int st[MAX], lazy[MAX], val_vertex[MAX], depth[MAX], father[MAX];
void mount (int v = 0, int p = -1)
  for(int &u : Adj[v])
   if(u != p)
      G[v].push_back(u);
      mount(u, v);
```

```
void dfs_sz(int v = 0, int p = 0, int d = 0)
    sz[v] = 1;
    depth[v] = d;
    father[v] = p;
    for(int &u: G[v])
      if(u == p) continue;
        dfs_sz(u, v, d + 1);
        sz[v] += sz[u];
        if(sz[u] > sz[G[v][0]])
            swap(u, G[v][0]);
void dfs_hld(int v = 0, int p = -1)
    in[v] = t++;
  rin[in[v]] = v;
    A.push_back(val_vertex[v]);
    for(int u: G[v])
      if(u == p) continue;
        nxt[u] = (u == G[v][0] ? nxt[v] : u);
        dfs_hld(u, v);
    out[v] = t;
void build(int node, int start, int end)
  if(start == end)
    st[node] = A[start];
  else
    int mid = (start + end) / 2;
    build(2 * node, start, mid);
   build(2 * node + 1, mid + 1, end);
    st[node] = st[2 * node] + st[2 * node + 1];
void update(int node, int start, int end, int l, int r, int value)
  if(lazy[node])
    st[node] += (end - start + 1) * lazy[node];
    if(start != end)
      lazy[2 * node] += lazy[node];
      lazy[2 * node + 1] += lazy[node];
    lazy[node] = 0;
  if(l > end or start > r)
    return;
  if(l <= start and end <= r)</pre>
    st[node] += value * (end - start + 1);
    if(start != end)
```

```
lazy[2 * node] += value;
      lazy[2 * node + 1] += value;
    return;
  int mid = (start + end) / 2;
  update(2 * node, start, mid, 1, r, value);
  update(2 * node + 1, mid + 1, end, 1, r, value);
  st[node] = st[2 * node] + st[2 * node + 1];
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
    st[node] += (end - start + 1) * lazy[node];
    if(start != end)
      lazv[2 * node] += lazv[node];
      lazy[2 * node + 1] += lazy[node];
    lazv[node] = 0;
  if(l > end or start > r)
    return 0:
  if(l <= start and end <= r)</pre>
    return st[node];
  int mid = (start + end) / 2;
  int q1 = query(2 * node, start, mid, 1, r);
  int q2 = query(2 * node + 1, mid + 1, end, 1, r);
  return q1 + q2;
int lca(int u, int v)
  while(nxt[u] != nxt[v])
    if(depth[nxt[u]] < depth[nxt[v]])</pre>
      v = father[nxt[v]];
      u = father[nxt[u]];
  return depth[u] < depth[v] ? u : v;</pre>
void update_up(int u, int l, int value)
  while(true)
    if(nxt[u] == nxt[l])
      update(1, 0, n - 1, in[1], in[u], value);
    update(1, 0, n - 1, in[nxt[u]], in[u], value);
    u = father[nxt[u]];
// atualiza o valor de cada vertice no caminho de
void updatePath(int u, int v, int value)//u para v.
```

```
int l = lca(u, v);
 update_up(u, l, value);
 update_up(v, 1, value);
 update(1, 0, n - 1, in[1], in[1], -value);
int query_up(int u, int 1)
 int ans = 0;
 while(true)
   if(nxt[u] == nxt[l])
      ans += query(1, 0, n - 1, in[1], in[u]);
     break:
   ans += query(1, 0, n - 1, in[nxt[u]], in[u]);
   u = father[nxt[u]];
 return ans;
//consulta a soma do valor de cada vertice no caminho
int queryPath(int u, int v)// de u para v.
 int l = lca(u, v), ans = 0;
 ans += query_up(u, 1);
 ans += query_up(v, 1);
 ans -= query(1, 0, n - 1, in[1], in[1]);
 return ans;
int main()
 int q;
 scanf(" %d %d", &n, &q);
 for(int i = 1; i < n; i++)</pre>
 {// ler a arvore em qualquer ordem
   int u, v;
   scanf(" %d %d", &u, &v); u--; v--;
   Adj[u].push_back(v);
   Adj[v].push_back(u);
 mount();// montar a arvore direcionada
 dfs sz();
 dfs_hld();
  // realizar consultas
 return 0;
```

2.10 Heavy Light Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
```

```
// Heavy-Light Decomposition
vector<int> adj[MAX];
int par[MAX], h[MAX];
int chainno, chain[MAX], head[MAX], chainpos[MAX],;
int chainsz[MAX], pos[MAX], arrsz;
int sc[MAX], sz[MAX];
void dfs(int u)
    sz[u] = 1, sc[u] = 0; // nodes 1-indexed (0-ind: sc[u]=-1)
    for(int v : adj[u])
        if(v != par[u])
            par[v] = u, h[v] = h[u]+1, dfs(v);
            sz[u] += sz[v];
            if(sz[sc[u]] < sz[v]) sc[u] = v; // 1-indexed (0-ind: sc[u])
                ]<0 or ...)
void hld(int u)
    if(!head[chainno]) head[chainno] = u; // 1-indexed
    chain[u] = chainno;
    chainpos[u] = chainsz[chainno];
    chainsz[chainno]++;
    pos[u] = ++arrsz;
    if(sc[u]) hld(sc[u]);
    for(int v : adj[u]) if(v != par[u] and v != sc[u]) chainno++, hld(
        v);
int lca(int u, int v)
    while(chain[u] != chain[v])
        if (h[head[chain[u]]] < h[head[chain[v]]]) swap(u, v);</pre>
        u = par[head[chain[u]]];
    if(h[u] > h[v]) swap(u, v);
    return u:
/*int query_up(int u, int v)
    if(u == v) return 0;
    int ans = -1;
    while(true)
        if(chain[u] == chain[v])
            if (u == v) break;
            ans = max(ans, query(1, 1, n, chainpos[v]+1, chainpos[u]))
            break;
        ans = max(ans, query(1, 1, n, chainpos[head[chain[u]]],
            chainpos[u]));
        u = par[head[chain[u]]];
```

```
return ans;
                                                                              void hld(int u)
int query(int u, int v)
                                                                                   if(!head[chainno]) head[chainno] = u; // 1-indexed
    int 1 = lca(u, v);
                                                                                   chain[u] = chainno;
    return max(query_up(u, 1), query_up(v, 1));
                                                                                   pos[u] = edge_counted;
                                                                                  A[edge_counted++] = weight[u];
                                                                                   if(sc[u]) hld(sc[u]);
int main()
                                                                                   for(int v : adj[u])
                                                                                       if(v != par[u] and v != sc[u])
    int n;
    cin >> n;
                                                                                           number_edge[{u, v}] = edge_counted;
    for(int i = 1; i < n; i++)</pre>
                                                                                           chainno++, hld(v);
        int u, v;
        cin >> u >> v;
        adj[u].push_back(v);
                                                                              int lca(int u, int v)
        adj[v].push_back(u);
                                                                                   while(chain[u] != chain[v])
    dfs(1);
    hld(1);
                                                                                       if(h[head[chain[u]]] < h[head[chain[v]]]) swap(u, v);</pre>
    for(int i = 1; i <= n; i++)</pre>
                                                                                       u = par[head[chain[u]]];
        cout << chain[i] << ' ';
    puts("");
                                                                                  if(h[u] > h[v]) swap(u, v);
    for(int i = 1; i <= n; i++)</pre>
                                                                                   return u;
        cout << chainpos[i] << ' ';</pre>
    puts("");
                                                                              void build(int node, int start, int end)
    return 0;
                                                                                   if(start == end)
                                                                                       st[node] = A[start];
                                                                                   else
//Heavy Light Decomposition para encontrar a major aresta no
// caminho de u para v em uma arvore
                                                                                       int mid = (start + end) / 2;
                                                                                      build(2 * node, start, mid);
#include <bits/stdc++.h>
                                                                                      build(2 * node + 1, mid + 1, end);
using namespace std;
                                                                                       st[node] = max(st[2 * node], st[2 * node + 1]);
const int MAX = 1e5;
// Heavy-Light Decomposition
vector<int> adj[MAX], W[MAX];
                                                                              int query(int node, int start, int end, int 1, int r)
int par[MAX], h[MAX];
map<pair<int, int>, int> number_edge;
                                                                                   if(l > end or start > r)
int chainno, chain[MAX], head[MAX], A[MAX], pos[MAX];
                                                                                       return -1;
int sc[MAX], sz[MAX], weight[MAX], st[MAX], edge_counted, n;
                                                                                  if(l <= start and end <= r)</pre>
                                                                                       return st[node];
                                                                                   int mid = (start + end) / 2;
void dfs(int u)
                                                                                   int g1 = guery(2 * node, start, mid, 1, r);
    sz[u] = 1, sc[u] = 0; // nodes 1-indexed (0-ind: sc[u]=-1)
                                                                                   int q2 = query(2 * node + 1, mid + 1, end, 1, r);
    for(int i = 0; i < adj[u].size(); i++)</pre>
                                                                                   return max(q1, q2);
        int v = adj[u][i], w = W[u][i];
        if(v != par[u])
                                                                              void update(int node, int start, int end, int idx, int value)
            weight[v] = w, par[v] = u, h[v] = h[u] + 1, dfs(v);
                                                                                   if(start == end)
            sz[u] += sz[v];
                                                                                       st[node] = A[idx] = value;
            if(sz[sc[u]] < sz[v]) sc[u] = v; // 1-indexed (0-ind: sc[u])
                                                                                   else
                1<0 or ...)
                                                                                       int mid = (start + end) / 2;
                                                                                       if(start <= idx and idx <= mid)</pre>
```

```
update(2 * node, start, mid, idx, value);
        else
            update(2 * node + 1, mid + 1, end, idx, value);
        st[node] = max(st[2 * node], st[2 * node + 1]);
int query_up(int u, int v)
    if(u == v) return 0;
    int ans = -1;
    while (true)
        if(chain[u] == chain[v])
            if(u == v) break;
            ans = max(ans, query(1, 0, n-1, pos[v] + 1, pos[u]));
        ans = max(ans, query(1, 0, n-1, pos[head[chain[u]]], pos[u]));
        u = par[head[chain[u]]];
    return ans;
int queryMaxEdge(int u, int v)
    int l = lca(u, v);
    return max(query_up(u, 1), query_up(v, 1));
void updateEdge(int u, int v, int value)
    int idx:
    if(number_edge.find({u, v}) != number_edge.end())
        idx = number_edge[{u, v}];
        idx = number_edge[{v, u}];
    update(1, 0, n-1, idx, value);
int main()
    for(int i = 1; i < n; i++)</pre>
        int u, v, w;
        cin >> u >> v >> w;
        adi[u].push back(v);
        adj[v].push_back(u);
        W[u].push_back(w);
        W[v].push_back(w);
    weight[1] = -1;
    dfs(1);
    hld(1);
    build(1, 0, n-1);
    int x, y, o;
    while(cin >> o >> x >> y)
        if(0 == 1)
```

```
cout << queryMaxEdge(x, y) << '\n';
else
{
    int w; cin >> w;
    updateEdge(x, y, w);
}
return 0;
}
```

2.11 Implicit Treap

```
#include <bits/stdc++.h>
using namespace std;
struct Node
  int valor, priority, size, sum;
  Node *1, *r;
  bool rev;
  Node (int _valor) : rev(false), sum(_valor), valor(_valor),
    priority((rand() << 16) ^ rand()), size(1), l(nullptr), r(nullptr)</pre>
  ~Node() { delete l; delete r; }
  void recalc()
    size = 1;
    sum = valor;
    if(1) size += 1->size, sum += 1->sum;
    if(r) size += r->size, sum += r->sum;
};
struct Treap
  int size(Node* t) { return t ? t->size : 0; }
  int size() const { return root ? root->size : 0; }
  Node* propagate (Node* t)
    if(t == nullptr) return t;
    if(t->rev)
      swap(t->1, t->r);
      if(t->l != nullptr) t->l->rev ^= 1;
      if(t->r != nullptr) t->r->rev ^= 1;
      t \rightarrow rev = 0;
    t->recalc();
    return t;
  int position(Node *t, int n)
    //nao esta na treap, botar valor que noa esta no array...
    if(t == nullptr) return -1;
    propagate(t);
    if(n == size(t->1) + 1) return t->valor;
```

```
else if(n <= size(t->l)) return position(t->l, n);
 else return position(t->r, n - size(t->l) - 1);
int at(int n)
 return position(root, n);
Node* merge(Node *1, Node *r)
 l = propagate(1);
 r = propagate(r);
 if(!1 or !r) return 1 ? 1 : r;
 if(l->priority < r->priority)
    1->r = merge(1->r, r);
   l->recalc();
    return 1;
  else
    r->1 = merge(1, r->1);
    r->recalc();
    return r;
void split (Node *v, int valor, Node *&1, Node *&r)
 v = propagate(v);
 l = r = nullptr;
 if(!v) return;
 if(size(v->1) < valor)</pre>
    split(v->r, valor - size(v->l) - 1, v->r, r);
    1 = v:
  }else
    split(v->1, valor, 1, v->1);
   r = v;
 v->recalc();
Node * root;
Treap() : root(nullptr) {}
~Treap() { delete root; }
void insert(int valor, int pos)
 Node * 1, * r;
 split(root, pos - 1, 1, r);
 root = merge(merge(l, new Node(valor)), r);
void erase(int valor)
 Node * 1, * m, * r;
 split(root, valor - 1, 1, m);
 split(m, 1, m, r);
```

```
delete m;
    root = merge(l, r);
  void reverse(int 1, int r)
    1--; r--;
    if(l > r) swap(l, r);
    Node *a, *b, *c, *d;
    split(root, l, a, d);
    split(d, r - l + 1, b, c);
    if(b) b->rev ^= 1;
    root = merge(a, merge(b, c));
  int query(int 1, int r)
    Node *a, *b, *c, *d;
    split(root, l - 1, a, b);
    split(b, r - l + 1, c, d);
    int ans = c->sum;
    root = merge(a, merge(c, d));
    return ans;
  /*void emOrdem(Node *node)
    if(node == nullptr) return;
    emOrdem (node->1);
    printf("%d ", node->valor);
    emOrdem(node->r);
  }*/
}treap;
int main()
  srand(time(0));
  for(int i = 1; i <= 6; i++)</pre>
    int x; cin >> x;
    cout << x << ' ';
    treap.insert(x, i);
  return 0;
```

2.12 LiChao Tree

```
#include <bits/stdc++.h>
using namespace std;
#define x real
#define y imag
typedef int ftype;
typedef complex<ftype> point;
const int 00 = 0x3f3f3f3f;
const int maxn = 2e5;

point line[4 * maxn];
```

```
void init()
    for(int i = 0; i < 4 * maxn; i++)</pre>
        line[i] = point(0, 00);
ftype dot(point a, point b)
    return (conj(a) * b).x();
ftype f(point a, ftype x)
    return dot(a, {x, 1});
void add_line(point nw, int v = 1, int l = 0, int r = maxn)
    int m = (1 + r) / 2;
    bool lef = f(nw, 1) < f(line[v], 1);
    bool mid = f(nw, m) < f(line[v], m);</pre>
    if (mid)
        swap(line[v], nw);
    if(r - 1 == 1)
        return;
    else if(lef != mid)
        add_line(nw, 2 * v, l, m);
        add_line(nw, 2 * v + 1, m, r);
int get (int x, int v = 1, int l = 0, int r = maxn)
    int m = (1 + r) / 2;
    if(r - 1 == 1)
        return f(line[v], x);
    else if (x < m)
        return min(f(line[v], x), get(x, 2 * v, 1, m));
    else
        return min(f(line[v], x), get(x, 2 * v + 1, m, r));
int main()
    init();
    point a(2, 4);
    point b(1, 3);
    add_line(a);
    add_line(b);
    cout << get(2) << '\n';
    return 0;
```

```
#include <bits/stdc++.h>
using namespace std;
struct MaxQueue
  int plus = 0;
  deque<pair<int, int>> dq;
  bool empty()
    return (int)dq.size() == 0;
  void clear()
    plus = 0;
    dq.clear();
  void add(int x)
  { // somar x em cada elemento da fila
    plus += x;
  int max()
    return dq.begin()->first + plus;
  void push (int x)
    x -= plus;
    int amt = 0;
    while (dq.size() and dq.back().first <= x)</pre>
     amt += dq.back().second + 1, dq.pop_back();
    dq.push_back({ x, amt });
  void pop()
    if (dq.empty()) return;
    if (!dq.front().second) dq.pop_front();
    else dq.front().second--;
};
int main()
  int n, aux;
  MaxOueue O;
  cin >> n;
  for(int i = 0; i < n; i++)
    int aux;
    cin >> aux;
    Q.push(aux);
    cout << "max " << Q.max() << '\n';
  return 0;
```

2.14 Merge Sort Tree Iterative

```
#include <bits/stdc++.h>
using namespace std;
#define 00 0x3f3f3f3f
struct MergeSortTree
  int n;
  vector<vector<int>> tree;
  MergeSortTree(vector<int> &a)
    n = a.size();
    tree.resize(n << 1);
    for(int i = 0; i < n; i++)
     tree[i + n] = vector<int>{a[i]};
    build();
  void build()
    for (int i = n - 1; i > 0; --i)
      int L = i << 1;</pre>
      int R = (i << 1) | 1;
      int l = 0, r = 0, sz = tree[L].size() + tree[R].size();
      tree[i].resize(sz);
      tree[L].push_back(00);
      tree[R].push_back(00);
      for(int j = 0; j < sz; j++)
        if(tree[L][l] < tree[R][r])
          tree[i][j] = tree[L][l++];
        else
          tree[i][j] = tree[R][r++];
      tree[L].pop_back();
      tree[R].pop_back();
  int queryMax(int 1, int r, int x)
    if(1 >= r) return 0;
    int res = 0;
    for(1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
      if(1 & 1)
        auto it = upper_bound(tree[1].begin(), tree[1].end(), x);
        int p = it - tree[l].begin();
        if(it != tree[l].end())
          int p = it - tree[l].begin();
          res += (int)tree[l].size() - p;
        1++;
```

```
if(r & 1)
        auto it = upper_bound(tree[r].begin(), tree[r].end(), x);
        if(it != tree[r].end())
          int p = it - tree[r].begin();
          res += (int)tree[r].size() - p;
    return res;
  int queryMin(int 1, int r, int x)
    if(1 >= r) return 0;
    int res = 0;
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
      if(1 & 1)
        auto it = lower_bound(tree[1].begin(), tree[1].end(), x);
        if(it == tree[l].end()) res += tree[l].size();
        else res += it - tree[l].begin();
      if(r & 1)
        auto it = lower_bound(tree[r].begin(), tree[r].end(), x);
       if(it == tree[r].end()) res += tree[r].size();
        else res += it - tree[r].begin();
    return res:
};
int32_t main()
  int n;
  scanf(" %d", &n);
  vector<int> v(n);
  for(int &w : v) cin >> w;
  MergeSortTree T(v);
  // query(1, r, x)
                        [1, r)
  return 0;
```

2.15 Merge Sort Tree Range Order Statistics Queries

```
#include <bits/stdc++.h>
using namespace std;

int n;
vector<int> tree[100000];
vector<pair<int, int>> arr;
```

```
void build(int node, int start, int end)
    if(start == end)
        tree[node].push_back(arr[start].second);
        int mid = (start + end) / 2;
        build(2 * node, start, mid);
        build(2 * node + 1, mid + 1, end);
        merge(tree[2 * node].begin(), tree[2 * node].end(),
            tree[2 * node + 1].begin(), tree[2 * node + 1].end(),
            back_inserter(tree[node]));
int query(int node, int start, int end, int 1, int r, int k)
    if(start == end)
        return arr[start].first;
    int M = upper_bound(tree[2 * node].begin(), tree[2 * node].end(),
       - lower_bound(tree[2 * node].begin(), tree[2 * node].end(), 1);
    int mid = (start + end) / 2;
    if(M >= k)
        return query(2 * node, start, mid, 1, r, k);
        return query (2 * node + 1, mid + 1, end, 1, r, k - M);
int main()
    cin >> n;
    int aux;
    for(int i = 0; i < n; i++)</pre>
        cin >> aux;
        arr.push_back({aux, i});
    sort(arr.begin(), arr.end());
    build(1, 0, n-1);
    int 1, r, k;
    while(cin >> 1 >> r >> k)
        cout << query(1, 0, n-1, 1-1, r-1, k) << '\n';
    return 0;
```

2.16 Merge Sort Tree With Set

```
/*
encontra o menor numero na range [L, R] que eh maior
ou igual a K. build eh O(NlogNlogN) e query eh O(logNlogN)
e o erasee eh O(logNlogN).
*/
#define ii pair<int, int>
#define value first
```

```
#define index second
const int MAX = 1e6;
int n, m;
vector<array<int, 3>> B, A;
set<ii> tree[MAX];
void build(int node, int start, int end)
    if(start == end)
        tree[node] = set<ii>{ii(A[start][1], start)};
        int mid = (start + end) / 2;
       build(2*node, start, mid);
       build(2*node + 1, mid + 1, end);
      for(auto &it : tree[2 * node])
        tree[node].insert(it);
      for(auto &it : tree[2 * node + 1])
        tree[node].insert(it);
ii query(int node, int start, int end, int l, int r, int k)
    if(start > r or end < 1)</pre>
       return ii(-1, -1);
    if(1 <= start and end <= r)</pre>
      auto it = tree[node].upper_bound({k, n + 1});
      ii q = \{-1, -1\};
       if(it != tree[node].begin()) q = *--it;
        return q;
    int mid = (start + end) / 2;
    ii p1 = query(2 * node, start, mid, 1, r, k);
    ii p2 = query(2 * node + 1, mid + 1, end, l, r, k);
  return p1.value <= p2.value ? p2 : p1;</pre>
void erasee(int node, int start, int end, ii p)
  if(tree[node].count(p) == 0) return;
  if(start == end)
   tree[node].erase(p);
    return;
  int mid = (start + end) / 2;
 erasee(2 * node, start, mid, p);
  erasee (2 * node + 1, mid + 1, end, p);
  tree[node].erase(p);
```

2.17 Merge Sort Tree

O nome eh Merge Sort Tree pois o array armazenado em um Node da Segment Tree eh igual ao gerado pelo algoritmo

```
de ordenacao Merge Sort no Node correspondente da
 arvore de recursao.
*/
#include <bits/stdc++.h>
using namespace std;
const int MAX = 131072;
vector<int> a[MAX], tree[MAX];
void build(int node, int start, int end)
    if(start == end)
        tree[node] = a[start];
    else
        int mid = (start + end) / 2;
        build(2*node, start, mid);
        build(2*node + 1, mid + 1, end);
        merge(tree[2*node].begin(), tree[2*node].end(),
            tree [2*node + 1].begin(), tree [2*node + 1].end()
            , back_inserter(tree[node]));
int query(int node, int start, int end, int 1, int r, int k)
    if(start > r or end < 1)</pre>
        return 0;
    if(l <= start and end <= r)</pre>
        return upper_bound(tree[node].begin(), tree[node].end(), k)
                - tree[node].begin();
    int mid = (start + end) / 2;
    int p1 = query(2*node, start, mid, 1, r, k);
    int p2 = query (2*node + 1, mid + 1, end, 1, r, k);
    return p1 + p2;
int main()
    int n, aux;
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> aux;
        a[i].push_back(aux);
    build(1, 0, n-1);
    int 1, r, k;
    cin >> 1 >> r >> k;
//quantidade de elementos menores ou iguais a k na range [1 - r].
    cout << query(1, 0, n-1, 1-1, r-1, k) << '\n';
    return 0;
```

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5+10;
int bit[MAX], arr[MAX];
int bitSearch(int v)
  int sum = 0, pos = 0, LOGN = log2 (MAX - 2);
  for(int i = LOGN; i >= 0; i--)
    if(pos + (1 << i) < MAX and sum + bit[pos + (1 << i)] < v)
      sum += bit[pos + (1 << i)];
     pos += (1 << i);
  return pos + 1;
  // pos + 1, pq pos eh a maior posicao cuja soma do prefixo ate
  // ela eh menor que V
// essa funcao retorna o indice J no array em que a soma do
// prefixo [1, J] eh o lower_bound para V
// inserir os elemento na BIT com add(i, arr[i]), para todo i em [1, n
int query(int idx)// soma de um prefixo
  int sum = 0;
  for(; idx > 0; idx -= idx&-idx) sum += bit[idx];
  return sum;
void add(int idx, int k)
  for(int i = idx; i < MAX; i += i&-i) bit[i] += k;</pre>
int smallerCount(int v)
  return query(v);
int count(int v)
  return query(v) - query(v - 1);
int greaterCount(int v)
  return query (MAX - 3) - query (v - 1);
int orderOfKey(int v)
  return smallerCount(v);
int kth(int k)
  return bitSearch(k);
```

```
int main()
{
   int n;

   cin >> n;
   for(int i = 1; i <= n; i++)
   {
      cin >> arr[i];
      add(arr[i], 1);
   }
   cout << smallerCount(3) << '\n';
   cout << count(3) << '\n';
   cout << greaterCount(3) << '\n';
   cout << kth(2) << '\n';
   cout << orderOfKey(4) << '\n';
   return 0;
}</pre>
```

2.19 PBDS

```
#include <bits/stdc++.h>
// Common file
#include <ext/pb_ds/assoc_container.hpp>
// Including tree_order_statistics_node_update
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
typedef tree<int, null_type, less<int>,
    rb_tree_tag, tree_order_statistics_node_update> ordered_set;
int main()
   ordered_set X;
   X.insert(2):
   X.insert(13);
   X.insert(5);
   X.insert(2);
   cout << *X.find_by_order(0) << '\n';</pre>
   cout << X.order_of_key(1) << '\n';
   return 0;
```

```
#include <bits/stdc++.h>
// Common file
#include <ext/pb_ds/assoc_container.hpp>
// Including tree_order_statistics_node_update
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
#define vi vector<int>
#define var pair<int,int>
#define ordered_multiset tree<var, null_type, less<var>
```

```
, rb_tree_tag, tree_order_statistics_node_update>
int id = 0; map<int, vi> ids;
void insere(ordered_multiset &s, int x)
    s.insert({x, ++id});
    ids[x].push_back(id);
void apaga(ordered_multiset &s, int x)
  if(ids[x].empty()) return;
    s.erase({x, ids[x].back()});
    ids[x].pop_back();
int kth(ordered_multiset &s, int x)
    return s.find_by_order(x)->first;
int smallerCount(ordered_multiset &s, int x)
    return s.order_of_key({x, 0});
int count(ordered_multiset &s, int x)
    return smallerCount(s, x + 1) - smallerCount(s, x);
ordered_multiset::iterator find(ordered_multiset &s, int x)
  if(ids[x].empty())
    return s.end();
    return s.find({x, ids[x].back()});
int main()
    ordered multiset X:
    // usar funcoes ...
    return 0;
```

2.20 Persistent Segment Tree Without Vector

```
#include <bits/stdc++.h>
using namespace std;

#define _ << " , " <<
    #define bug(x) cout << #x << " >>>>>> " << x << endl;
#define fastio ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0);

const int MAX = 800100;
const int LOG_MAX = 30;</pre>
```

```
struct PersistentSegmentTree {
   int n; // the queries will be performed in the range [0, n-1]
  int L[LOG_MAX * MAX]; // L[node] is the left child of node
   int R[LOG_MAX * MAX]; // R[node] is the right child of node
  int tree[LOG_MAX * MAX]; // tree[node] is the value stored in the
   int root[MAX]; // stores the root of each version
   int next_vertex; // next index for a vertex
   int version count; // number of different versions of the tree
  void calc(int node) {
      int sum = 0;
      if(L[node]) sum += tree[L[node]];
     if(R[node]) sum += tree[R[node]];
      tree[node] = sum;
  void update (int prev, int node, int start, int end, int idx, int
       value) {
      if(start == end)
        tree[node] = tree[prev] + value;
      else {
         int mid = (start + end) / 2;
         if(start <= idx and idx <= mid) {</pre>
            R[node] = R[prev];
            if(L[node] == 0) L[node] = next_vertex++;
            update(L[prev], L[node], start, mid, idx, value);
         } else {
            L[node] = L[prev];
            if(R[node] == 0) R[node] = next vertex++;
            update(R[prev], R[node], mid + 1, end, idx, value);
         calc(node);
   int query(int node, int start, int end, int l, int r) {
      if(l > end or r < start) return 0;</pre>
      if(l <= start and end <= r) return tree[node];</pre>
      int mid = (start + end) / 2, q1 = 0, q2 = 0;
      if(L[node]) g1 = query(L[node], start, mid, 1, r);
      if(R[node]) q2 = query(R[node], mid + 1, end, 1, r);
      return q1 + q2;
   void init(int _n) {
      root[0] = 0;
      next vertex = 1;
     version_count = 1;
     n = _n;
   int update(int idx, int value) {
      root[version_count] = next_vertex++;
      update(root[version_count - 1], root[version_count], 0, n - 1,
          idx, value);
      version count++;
      return version_count - 1;
  int query(int version, int 1, int r) {
      return query(root[version], 0, n - 1, 1, r);
};
```

```
int n, q;
PersistentSegmentTree PST;
int32_t main() {
   fastio
   cin >> n >> q;
   PST.init(n);
   map<int, int> lst;
   vector<int> root(n);
   for(int i = 0; i < n; ++i) {</pre>
      int x;
      cin >> x;
      int 1 = -1:
      if(lst.count(x)) l = lst[x];
      if(1 != -1) PST.update(1, -1);
      root[i] = PST.update(i, 1);
      lst[x] = i;
   while(q--) {
      int 1, r;
      cin >> 1 >> r; 1--; r--;
      cout << PST.query(root[r], l, r) << '\n';</pre>
   return 0;
```

2.21 Persistent Segment Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

struct Node
{
   int l, r, value;
};

vector<Node> tree;
vector<int> root;

void init()
{
   tree.emplace_back();
   root.push_back(0);
}

void calc(int node)
{
   tree[node].value = 0;
   if(tree[node].l) tree[node].value += tree[tree[node].l].value;
   if(tree[node].r) tree[node].value += tree[tree[node].r].value;
```

```
void update (int prev, int node, int start, int end, int idx, int value
  if(start == end)
    tree[node].value = value;
  else
    int mid = (start + end) / 2;
    if(start <= idx and idx <= mid)</pre>
      tree[node].r = tree[prev].r;
      if(tree[node].1 == 0)
        tree[node].l = tree.size();
        tree.emplace_back();
      update(tree[prev].l, tree[node].l, start, mid, idx, value);
    else
      tree[node].l = tree[prev].l;
      if(tree[node].r == 0)
        tree[node].r = tree.size();
        tree.emplace_back();
      update(tree[prev].r, tree[node].r, mid + 1, end, idx, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(l > end or r < start) return 0;</pre>
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
int main()
 int n, q;
  cin >> n >> q;
  init();
  while (q--)
    int o, 1, r;
    cin >> o >> l >> r;
    if(0 == 1)
      int prev = root.back();
      root.push_back(tree.size());
      tree.emplace_back();
      update(prev, root.back(), 0, n - 1, l - 1, r);
```

```
else
{
    int version;
    scanf(" %d", &version);
    cout << query(root[version], 0, n - 1, 1 - 1, r - 1) << '\n';
    }
}
return 0;
}</pre>
```

2.22 Segment Tree Iterative

return 0;

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
int tree[MAX << 1], n;</pre>
void build()
  for(int i = n - 1; i > 0; --i) tree[i] = tree[i << 1] + tree[i << 1</pre>
      | 11;
void update(int p, int value)
  for(tree[p += n] = value; p > 1; p >>= 1) tree[p >> 1] = tree[p] +
      tree[p ^ 1];
int query(int 1, int r)
  int res = 0;
  for(1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
    if(l & 1) res += tree[l++];
    if(r & 1) res += tree[--r];
  return res;
int main()
  cin >> n;
  for(int i = 0; i < n; i++)
   cin >> tree[i + n];
  build();
  int q, 1, r, o;
  cin >> q;
  while (q--)
    cin >> o >> l >> r;
    if(0 == 1)
      cout << query(1 - 1, r) << '\n'; // soma de [1, r)
      update(1 - 1, r); // atualiza a posicoo l pra r
```

2.23 Segment Tree Tree 2D

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
int n, leaf;
int arr[MAX][MAX];
int ST[4*MAX][4*MAX];
void buildLeaf(int k, int node, int l, int r)
 if(1 == r)
   ST[k][node] = arr[leaf][l];
  else
    int mid = (l + r) / 2;
    buildLeaf(k, 2*node, 1, mid);
    buildLeaf(k, 2*node + 1, mid + 1, r);
    ST[k][node] = ST[k][2*node] + ST[k][2*node+1];
void build(int node, int 1, int r)
  if(1 == r)
   buildLeaf(node, 1, 0, n-1), leaf++;
  else
    int mid = (l + r) / 2;
    build(2*node, 1, mid);
    build(2*node + 1, mid + 1, r);
    for(int i = 1; i < 4*n; i++)
      ST[node][i] = ST[2*node][i] + ST[2*node+1][i];
int queryNode(int k, int node, int 1, int r, int cx, int cy)
  if(1 > cy or r < cx)
    return 0;
  if(cx <= 1 and r <= cy)
   return ST[k][node];
  int mid = (1 + r) / 2;
  int ans = queryNode(k, 2*node, 1, mid, cx, cy);
  ans += queryNode(k, 2*node + 1, mid + 1, r, cx, cy);
  return ans:
int query (int node, int 1, int r, int 1x, int 1y, int cx, int cy)
  if(1 > ly or r < lx)
    return 0;
  if(lx \le l and r \le ly)
   return queryNode (node, 1, 0, n-1, cx, cy);
  int mid = (1 + r) / 2;
  int ans = query(2*node, 1, mid, 1x, 1y, cx, cy);
  ans += query (2*node + 1, mid + 1, r, lx, ly, cx, cy);
```

```
return ans;
void updateNode(int k, int node, int l, int r, int x, int y, int value
  if(1 == r)
   ST[k][node] = arr[x][y] = value;
    int mid = (1 + r) / 2;
    if(1 <= y and y <= mid)</pre>
      updateNode(k, 2*node, 1, mid, x, y, value);
      updateNode(k, 2*node + 1, mid + 1, r, x, y, value);
    ST[k][node] = ST[k][2*node] + ST[k][2*node + 1];
void update(int node, int 1, int r, int x, int y, int value)
  if(1 == r)
   updateNode(node, 1, 0, n-1, x, y, value);
    int mid = (1 + r) / 2;
    if(1 \le x \text{ and } x \le mid)
      update(2*node, 1, mid, x, y, value);
      update (2*node + 1, mid + 1, r, x, y, value);
    for (int i = 1; i < 4*n; i++)
      ST[node][i] = ST[2*node][i] + ST[2*node+1][i];
int main()
  cin >> n;
  for(int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
      cin >> arr[i][j];
  build(1, 0, n-1);
  int o, a, b, c, d;
  while(cin >> o)
    cin >> a >> b >> c;
    if(0 == 1)
      update(1, 0, n-1, a-1, b-1, c);
      cout << query(1, 0, n-1, a-1, b-1, c-1, d-1) << '\n';
  return 0;
```

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
#define esq node << 1LL
#define dir (node << 1) | 1LL
struct SegmentTree {
  vector<int> tree, lazy;
  int size;
 void build(int node, int start, int end, vector<int> &a) {
   if(start == end) {
      tree[node] = a[start];
      return;
   int mid = (start + end) >> 1;
   build(esg, start, mid, a);
   build(dir, mid + 1, end, a);
   tree[node] = tree[esq] + tree[dir];
  SegmentTree() {}
  SegmentTree(int n) {
   size = n;
   tree.resize(size << 2);
   lazv.resize(size << 2);
  void init(vector<int> &a) {
   build(1, 0, size -1, a);
  // += add in the interval
  void push(int node, int start, int end) {
   tree[node] += lazy[node] * (end - start + 1);
   if(start != end) {
     lazy[esq] += lazy[node];
     lazy[dir] += lazy[node];
   lazy[node] = 0;
  int query(int node, int start, int end, int 1, int r) {
   if(lazy[node]) push(node, start, end);
   if(l > end or start > r or l > r) return 0;
   if(l <= start and end <= r) return tree[node];</pre>
   int mid = (start + end) >> 1;
   int q1 = query(esq, start, mid, l, r);
   int q2 = query(dir, mid + 1, end, 1, r);
   return q1 + q2;
  int query(int 1, int r) {
   return query (1, 0, size - 1, 1, r);
  void update(int node, int start, int end, int l, int r, int v) {
   if(lazy[node]) push(node, start, end);
```

```
if(l > end or start > r or l > r) return;
    if(l <= start and end <= r)</pre>
      lazy[node] += v;
      push (node, start, end);
      return;
    int mid = (start + end) >> 1;
    update(esq, start, mid, l, r, v);
    update(dir, mid + 1, end, l, r, v);
    tree[node] = tree[esq] + tree[dir];
  void update(int 1, int r, int v) {
    update(1, 0, size - 1, 1, r, v);
};
int32_t main() {
  ios_base::sync_with_stdio(false);
  cin.tie(nullptr);
  int n;
  cin >> n;
  SegmentTree T(n);
  return 0;
```

2.25 Sparse Table RMQ

```
#include <bits/stdc++.h>
#define maxn 100000
#define maxnlog 20
using namespace std;
const double EPS = 1e-6;
int n, q, Sparse_Table[maxnlog][maxn];
void build()
  for(int i = 1; (1 << i) <= n; i++)</pre>
    for (int j = 0; j + (1 << i) <= n; <math>j++)
      Sparse_Table[i][j] = max(Sparse_Table[i-1][j],
        Sparse_Table[i-1][j+(1 << (i-1))]);
int range_query(int i, int j)
  int sz = log2(i-i+1):
  return max(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
int main()
  scanf("%d %d", &n, &q);
  for(int i = 0; i < n; i++)</pre>
```

```
scanf("%d", &Sparse_Table[0][i]);
build();
for(int i = 0; i < q; i++)
{
  int a, b;
  scanf("%d %d", &a, &b);
  cout << range_query(a,b) << endl;
}
return 0;</pre>
```

2.26 Treap

```
#include <bits/stdc++.h>
using namespace std;
struct Node
  int valor, priority, size, maior;
 Node *1, *r;
 Node(int _valor) : valor(_valor), priority((rand() << 16)</pre>
  ^ rand()), size(1), l(nullptr), r(nullptr), maior(_valor) {}
  "Node() { delete 1: delete r: }
  void recalc()
   size = 1:
   maior = valor:
   if (1) size += 1->size, maior = max(maior, 1->maior);
    if (r) size += r->size, maior = max(maior, r->maior);
};
struct Treap
  Node* merge (Node *1, Node *r)
    if(!1 or !r) return 1 ? 1 : r;
    // Se a prioridade esquerda eh menor.
    if(l->priority < r->priority)
      1->r = merge(1->r, r);
     l->recalc();
      return 1;
     // Se a prioridade direita eh maior ou igual.
    else
      r->1 = merge(1, r->1);
      r->recalc();
      return r:
// Valores maiores ou iquais a "valor" ficarao no r, e os demais no 1.
  void split (Node *v, int valor, Node *&l, Node *&r)
```

```
l = r = nullptr;
  if(!v) return;
  // Se o valor for maior, ir para direita
  if(v->valor < valor)</pre>
    split(v->r, valor, v->r, r);
   1 = v;
    // Se o valor for menor ou iqual ir para esquerda.
  }else
    split(v->1, valor, 1, v->1);
    r = v:
  v->recalc();
bool find (Node *v, int valor)
  if(!v) return false;
  if( v->valor == valor ) return true;
  if( v->valor < valor ) return find(v->r, valor);
  if( v->valor > valor ) return find(v->1, valor);
int smallestCount(Node *v, int valor)
  if(!v) return 0;
  // Se for menor ou iqual adicionar + 1.
  if(v->valor == valor) return (v->l ? v->l->size : 0);
  if(v->valor < valor) return 1 + (v->l ? v->l->size : 0)
    + smallestCount(v->r, valor);
  if(v->valor > valor) return smallestCount(v->1, valor);
Node* kth(Node *v, int posicao)
  if(!v) return nullptr;
  int esquerda = (v->1? v->1->size: 0);
  if(posicao-esquerda == 1) return v;
  if(posicao-esquerda > 1) return kth(v->r, posicao-esquerda-1);
  if (posicao-esquerda < 1) return kth(v->1, posicao);
// Sendo i e j os indices no array ordenado
// Talvez deh problemas de i e j estiverem fora do range.
int query(int i, int j)
  Node *1, *q, *r;
  split(root, kth(root, i+1)->valor, l, q);
  split(q, kth(q, j+1-i) \rightarrow valor+1, q, r);
  int x = q->maior;
  root = merge(l, merge(q,r));
  return x;
Node * root;
Treap() : root(nullptr) {}
~Treap() { delete root; }
// Se existe um elemento com o valor
```

```
bool find(int valor)
 return find(root, valor);
// Quantidade de elementos menores que o valor
int smallestCount(int valor)
 return smallestCount(root, valor);
// Retorna o k-th menor elemento
Node * kth(int posicao) {
 return kth(root, posicao);
// Insere o valor mesmo se ja exista outro com valor iqual
void insert(int valor)
 Node * 1, * r;
 split(root, valor, l, r);
 root = merge(merge(l, new Node(valor)), r);
// Apaga todos os elementos que possuem o valor.
void erase(int valor)
 Node * 1, * m, * r;
 split (root, valor, 1, m);
 split(m, valor + 1, m, r);
 delete m;
  root = merge(l, r);
// Quantos valores existem menor que "valor"
int menoresQue(int valor)
 Node * 1, * r;
 split(root, valor, l, r);
 int res = (1? 1->size: 0);
 root = merge(l,r);
 return res;
// splitSmallest eh uma funcao que esta na implicit treap
// Retorna a consulta dos primeiros "quantidade" valor
int top(int quantidade)
 Node *1, *r;
 splitSmallest(root, quantidade, 1, r);
 int valor = (1 ? 1->maior : 0);
 root = merge(l,r);
 return valor;
// Remover os d menores
void removeSmallest(int d)
 Node *1, *r;
 splitSmallest(root, d, l, r);
 root = r;
 if(1) delete 1;
// Remover todos menos os d menores
```

```
void limit (int d)
    Node * 1, * r;
    splitSmallest(root, d, l, r);
    root = 1;
    if(r) delete r;
  int size() const { return root ? root->size : 0; }
}treap;
int n, a;
char op;
int main()
    srand(time(0));
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
    cin >> op >> a;
    if(op == 'I')
      if(!treap.find(a))
        treap.insert(a);
    else if(op == 'D' )
      treap.erase(a);
    else if(op == 'C' )
      cout << treap.smallestCount(a) << '\n';</pre>
    else if(op == 'K' )
      Node *v = treap.kth(a);
      if(v == nullptr) cout << "invalid" << '\n';</pre>
      else cout << v->valor << '\n';</pre>
  return 0;
```

2.27 TreeIsomorfismWithMap

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;

int n, ID, degree[MAX];
map<map<int, int>, int> formato;
bool vis[MAX];

void init()
{
    formato.clear();
    ID = 1;
}

int dfs(int v, int p, vector<vector<int>>> &G)
{
    if((int)G[v].size() == 1)
```

```
return 1;
    map<int, int> ids;
    for(int &u : G[v])
        if(u == p) continue;
        int x = dfs(u, v, G);
        ids[x]++;
    if(formato.count(ids) <= 0)</pre>
        formato[ids] = ++ID;
    return formato[ids];
inline void findCenterAndComputeID(vector<vector<int>> &G, vector<int>
    memset(vis, 0, sizeof(vis));
    queue<int> fila[2];
    for(int i = 0; i < n; i++)
        if(degree[i] == 1)
            fila[0].push(i);
    int cnt = 0, turn = 0;
    while (cnt + 2 < n)
        while(!fila[turn].empty())
            int u = fila[turn].front(); fila[turn].pop();
            vis[u] = true;
            cnt++;
            for(int i = 0; i < G[u].size(); i++)</pre>
                 if(!vis[G[u][i]])
                     degree[G[u][i]]--;
                     if (degree[G[u][i]] == 1) fila[1-turn].push(G[u][i
                         ]);
        turn ^= 1;
    for(int i = 0; i < n; i++)</pre>
        if(vis[i]) continue;
        val.push_back(dfs(i, -1, G));
int32_t main()
    while(cin >> n)
        init();
        vector<int> val[2];
        for (int j = 0; j < 2; j++)
            memset(degree, 0, sizeof(degree));
            vector<vector<int>> G(n + 1);
            for(int i = 1; i < n; i++)</pre>
                int u, v;
                scanf(" %d %d", &u, &v); u--; v--;
                G[u].push_back(v);
```

2.28 TreeIsomorfismWithPolynomialHashing

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long
const int MAX = 1e5 + 10;
const 11 A = 911382323;
const 11 B = 972663749;
int n, ID, degree[MAX];
map<11, 11> formato;
bool vis[MAX];
inline ll norm(ll a)
    return a > B ? a = a % B : a;
inline ll add(ll a, ll b)
    a = norm(a); b = norm(b);
    return norm(a + b);
inline ll prod(ll a, ll b)
    a = norm(a); b = norm(b);
    return norm(a * b);
inline ll pol_hash(vector<ll> &v)
    11 p = 1, ans = 0;
    for(ll &w : v)
    ans = add(ans, prod(p, w));
    p = prod(p, A);
  return norm(ans);
11 dfs(int v, int p, vector<vector<int>> &G)
```

```
if((int)G[v].size() == 1)
        return 1:
    vector<ll> ids;
    for(int &u : G[v])
        if(u == p) continue;
        11 x = dfs(u, v, G);
        ids.push_back(x);
    sort(ids.begin(), ids.end());
  ll ph = pol_hash(ids);
  if(formato.count(ph) <= 0) formato[ph] = ++ID;</pre>
    return formato[ph];
inline void findCenterAndComputeID(vector<vector<int>> &G, vector<11>
    &val)
    memset(vis, 0, sizeof(vis));
    queue<int> fila[2];
    for(int i = 0; i < n; i++)</pre>
        if(degree[i] == 1)
            fila[0].push(i);
    int cnt = 0, turn = 0;
    while (cnt + 2 < n)
        while(!fila[turn].empty())
            int u = fila[turn].front(); fila[turn].pop();
            vis[u] = true;
            for(int i = 0; i < G[u].size(); i++)</pre>
                if(!vis[G[u][i]])
                     degree[G[u][i]]--;
                     if (degree[G[u][i]] == 1) fila[1-turn].push(G[u][i
                         1);
        turn ^= 1:
    for(int i = 0; i < n; i++)</pre>
        if(vis[i]) continue;
        val.push_back(dfs(i, -1, G));
int32 t main()
    while(cin >> n)
    formato.clear();
    ID = 1;
        vector<ll> val[2];
        for (int j = 0; j < 2; j++)
            memset(degree, 0, sizeof(degree));
            vector<vector<int>> G(n + 1);
            for(int i = 1; i < n; i++)</pre>
```

2.29 Two Stacks Trick

```
const int 00 = 0x3f3f3f3f3f;
struct Stack {
    vector<int> s, smax = \{-00\}, smin = \{00\};
    void push(int x) {
        s.push_back(x);
        smax.push_back(max(smax.back(), x));
        smin.push_back(min(smin.back(), x));
    int pop() {
        int x = s.back();
        s.pop_back();
        smax.pop_back();
        smin.pop_back();
        return x;
    int min_() {
        return smin.back();
    int max () {
        return smax.back();
    bool empty() {
        return s.empty();
};
Stack s1, s2;
void push(int x) {
    s2.push(x):
void pop() {
    if(s1.empty()) {
        while(!s2.empty())
            s1.push(s2.pop());
```

```
s1.pop();
}
int min_() {
    return min(s1.min_(), s2.min_());
}
int max_() {
    return max(s1.max_(), s2.max_());
}
```

2.30 Wavelet Tree

```
#include <bits/stdc++.h>
using namespace std;
const int N = 100100;
const int MAX = 30 * N;
// MAX = N * log(maxX - minX)
// Queries in O(log(maxX - minX))
struct WaveletTree
  int arr[N], aux[N];
  int lo[MAX], hi[MAX];
  vector<int> freq[MAX];
  int lef[MAX], riq[MAX];
  int nextNode;
  WaveletTree(vector<int> a, int minX, int maxX)
    int sz = a.size();
    for(int i = 0; i < sz; i++)</pre>
      arr[i] = a[i];
   nextNode = 1;
    build(0, 0, sz, minX, maxX);
  int stable_partition(int s, int e, int mid)
    int pivot = 0;
    for(int i = s; i < e; i++)</pre>
      aux[i] = arr[i], pivot += (arr[i] \le mid);
    int l = s, r = s + pivot;
    for(int i = s; i < e; i++)</pre>
      if(aux[i] <= mid)</pre>
        arr[l++] = aux[i];
      else
        arr[r++] = aux[i];
    return 1:
  void build(int node, int s, int e, int minX, int maxX)
    lo[node] = minX, hi[node] = maxX;
    if(lo[node] == hi[node] or s >= e) return;
    int mid = (minX + maxX - 1) / 2;
    freq[node].resize(e - s + 1);
    freq[node][0] = 0;
```

```
for(int i = s; i < e; i++)</pre>
    freq[node][i - s + 1] = freq[node][i - s] + (arr[i] <= mid);
  int pivot = stable_partition(s, e, mid);
  lef[node] = nextNode++, rig[node] = nextNode++;
 build(lef[node], s, pivot, minX, mid);
 build(rig[node], pivot, e, mid + 1, maxX);
int went_right(int node, int i)
 return i - freq[node][i];
// less than ou equal to x in range [1, r]
int lte(int 1, int r, int x, int node = 0)
 if(l > r or x < lo[node]) return 0;</pre>
 if(hi[node] <= x) return r - l + 1;</pre>
 int 11 = freq[node][1 - 1] + 1, r1 = freq[node][r];
 int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
  return lte(11, r1, x, lef[node]) + lte(12, r2, x, rig[node]);
// greater than ou equal to x in range [l, r]
int gte(int 1, int r, int x, int node = 0)
 if(l > r or x > hi[node]) return 0;
 if(lo[node] >= x) return r - l + 1;
 int l1 = freq[node][l - 1] + 1, r1 = freq[node][r];
  int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
  return gte(11, r1, x, lef[node]) + gte(12, r2, x, rig[node]);
// counting numbers equal to x in range [l, r]
int count(int 1, int r, int x, int node = 0)
  if(l > r or lo[node] > x or hi[node] < x) return 0;</pre>
  if(lo[node] == hi[node] and lo[node] == x) return r - l + 1;
  int 11 = freq[node][1 - 1] + 1, r1 = freq[node][r];
  int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
  return count(l1, r1, x, lef[node]) + count(l2, r2, x, rig[node]);
// find kth number in range [l, r]
int kth(int 1, int r, int k, int node = 0)
 if(1 > r) return 0;
 if(lo[node] == hi[node]) return lo[node];
 int inLeft = freq[node][r] - freq[node][l - 1];
```

```
int 11 = freq[node][1 - 1] + 1, r1 = freq[node][r];
   if (k <= inLeft) return kth(11, r1, k, lef[node]);
   int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
   return kth(12, r2, k - inLeft, rig[node]);
   }
};

int main()
{
   vector<int> a = {2, 5, 3, 2, 4, 2};
   WaveletTree T(a, 0, 9);
   cout << T.lte(3, 5, 3) << '\n';
   cout << T.gte(3, 5, 3) << '\n';
   cout << T.count(1, 6, 2) << '\n';
   cout << T.kth(1, 6, 5) << '\n';
   return 0;
}</pre>
```

3 Dynamic Programming

3.1 Coin Problem Topdown Dp

```
#include <bits/stdc++.h>
using namespace std;
using namespace std;
vector<int> coin;
int memo[1000000];
int solve(int troco)
  if(troco < 0)
    return (1 << 25);
  if (memo[troco] != -1)
    return memo[troco];
  if(troco == 0)
    return 0;
  int ans = (1 << 25);
  for(int i = 0; i < coin.size(); i++)</pre>
    ans = min(ans, 1 + solve(troco - coin[i]));
  return memo[troco] = ans;
void ans(int troco)
  if(troco < 0)
    return;
  if(troco == 0)
    return;
  for(int i = 0; i < coin.size(); i++)</pre>
    if(solve(troco - coin[i]) + 1 == memo[troco])
```

```
cout << coin[i] << ' ';
    ans(troco - coin[i]);
    break;
}

int main()
{
    memset(memo, -1, sizeof(memo));
    int n, troco;
    cin >> n >> troco;
    coin.resize(n);
    for(int &w : coin)
        cin >> w;
    cout << solve(troco) << '\n';
    ans(troco);
    puts("");

    return 0;
}</pre>
```

3.2 Digit DP Sum Of Digits In Range

```
#include "bits/stdc++.h"
using namespace std;
int dp[20][200][2];
int digitDP(int idx, int sum, int can, vector<int> &digit)
{// idx eh o indice atual, sum a soma dos digitos ate idx,
//e can uma flag para indicar se pode colocar
//qualquer valor a partir daqui
  if(idx == (int)digit.size())
    return sum;
  if(dp[idx][sum][can] != -1)
    return dp[idx][sum][can];
  int ans = 0;
  for(int i = 0; i < 10; i++)
    if(can or i <= digit[idx])</pre>
      ans += digitDP(idx + 1, sum + i,
        can or i < digit[idx], digit);
  return dp[idx][sum][can] = ans;
int query(int x) // responde a consulta de 0 ate x
 memset(dp, -1, sizeof(dp));
    vector<int> digit;
    while (x)
        digit.push_back(x%10);
        x /= 10:
    reverse(digit.begin(), digit.end());
    return digitDP(0, 0, 0, digit);
int main()
    int q, a, b;
```

```
cin >> q;
while(q--)
{
  cin >> a >> b;
  cout << query(b) - query(a - 1) << '\n';
}
  return 0;
}</pre>
```

3.3 Edit Distance With DP

```
#include <bits/stdc++.h>
using namespace std;
string a, b;
int PD[2008][2008];
int solve(int i, int j)
  if(!i) return j;
  if(!j) return i;
  if (PD[i][j] !=-1)
   return PD[i][j];
  // substituir um caracter se for preciso
  int ans1 = solve(i - 1, j - 1) + (a[i] != b[j]);
  //apagar o caracter da string i
  int ans2 = solve(i - 1, j) + 1;
  //apagar o caracter da string j
  int ans3 = solve(i, j - 1) + 1;
  return PD[i][j] = min(ans1, min(ans2, ans3));
int main()
  int q;
  cin >> q;
  while (q--)
    memset (PD, -1, sizeof (PD));
   cin >> a >> b;
   a = "#" + a;
    b = "#" + b;
    cout << solve(a.size()-1, b.size()-1) << '\n';
  return 0;
```

3.4 Kadane 2D

```
#include <bits/stdc++.h>
using namespace std;
int pd[100][100], A[100][100];
int main()
{
   int n, m;
```

```
cin >> n >> m;
for(int i = 1; i <= n; i++)
    for(int j = 1; j <= m; j++)
        cin >> A[i][j], pd[i][j] = pd[i][j - 1] + A[i][j];
int ans = 0;
for(int i = 1; i <= n; i++)
    for(int j = i + 1; j <= m; j++)
    {
        int sum = 0;
        for(int k = 1; k <= n; k++)
        {
            sum += pd[k][j] - pd[k][i - 1];
            if(sum < 0) sum = 0;
            ans = max(ans, sum);
        }
    }
    cout << ans << '\n';
    return 0;
}</pre>
```

3.5 Kadane 3D

```
#include <bits/stdc++.h>
using namespace std;
int A, B, C;
int par[22][22][22], pd[22][22][22];
int main()
 cin >> A >> B >> C;
  for(int i = 1; i <= A; i++)</pre>
    for(int j = 1; j <= B; j++)
      for(int k = 1; k <= C; k++)
        cin >> par[i][j][k];
  for(int i = 1; i <= A; i++)</pre>
    for(int j = 1; j <= B; j++)
      for (int k = 1; k \le C; k++)
        pd[i][j][k] = pd[i][j-1][k] + pd[i][j][k-1]
           - pd[i][j-1][k-1] + par[i][j][k];
  int ans = -(1 << 25);
  for(int h1 = 1; h1 <= C; h1++)
  for(int h2 = h1; h2 <= C; h2++)
  for(int 11 = 1; 11 <= B; 11++)
    for(int 12 = 11; 12 <= B; 12++)
      int sum = -(1 << 25);
      for(int i = 1; i <= A; i++)</pre>
        int s = pd[i][12][h2] - pd[i][11 - 1][h2]
        - pd[i][12][h1 - 1] + pd[i][11 - 1][h1 - 1];
        sum = max(sum + s, s);
        ans = max(ans, sum);
  cout << ans << '\n';
```

```
return 0;
```

3.6 Knapsack With Copies SqrtN Memory

```
#include <bits/stdc++.h>
using namespace std:
#define bug(x) cout << #x << " >>>>>> " << x << '\n'
#define _ << " , " <<
//#define int long long
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
#define ii pair<int, int>
#define fi first
#define se second
#define UNTIL(t) while (clock() < (t) * CLOCKS PER SEC)
const int MAX = 20002; //2 * 10^5
const int MOD = 1000000007; //10^9 + 7
const int 00 = 0x3f3f3f3f; // 0x3f3f3f3f;
const double EPS = 1e-9; //10^-9
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
int n, S;
int B[205];
int C[205];
int V[35001;
int W[3500];
int ID[3500]:
int id = 1;
int dp[MAX];
int linha[70][MAX], T[70][MAX];
int L[70];
void add(int j)
  int sum = 0:
  for (int k = 0; sum + (1 << k) <= C[j]; sum += (1 << k), k++)
   V[id] = B[j] * (1 << k);
    W[id] = (1 << k);
   ID[id] = j;
    id++;
  int r = C[j] - sum;
  if(r > 0)
    V[id] = B[j] * r;
    W[id] = r;
    ID[id] = j;
    id++;
int32_t main()
  cin >> n:
  for(int i = 1; i <= n; i++) cin >> B[i];
  for(int i = 1; i <= n; i++) cin >> C[i];
  for(int i = 1; i <= n; i++) add(i);</pre>
  cin >> S;
```

```
for(int j = 1; j <= S; j++)
  dp[i] = 00;
int cnt = 0, k = -1, sq = max(10, (int) sqrt(id * 1.));
for(int i = 1; i < id; i++)
  if(cnt % sq == 0)
    cnt = 0;
    k++;
    for(int j = 0; j <= S; j++)</pre>
    linha[k][j] = dp[j];
    L[k] = i - 1;
  for(int j = S; j >= V[i]; j--)
    dp[j] = Min(dp[j - V[i]] + W[i], dp[j]);
  cnt++;
int last_raw = id - 1, s = S;
vector<int> note(n + 1);
while(last_raw >= 1)
  int first raw = last raw - 1;
  while(first_raw > L[k])
    first raw--;
  for(int j = 0; j <= S; j++)
   T[0][j] = linha[k][j];
  for(int i = 1; i <= last_raw - first_raw; i++)</pre>
    for(int i = 0; i \le S; i++)
      if(j >= V[i + first_raw])
        T[i][j] = Min(T[i-1][j], T[i-1][j-V[i+first_raw]] +
            W[i + first_raw]);
      else
        T[i][j] = T[i - 1][j];
  for(int i = last_raw - first_raw; i > 0; i--)
    if(T[i][s] != T[i - 1][s])
     note[ID[i + first raw]] += W[i + first raw];
      s -= V[i + first raw];
  last raw = first raw;
  k--;
int number_of_notes = 0;
for(int &w : note)
 number_of_notes += w;
cout << number_of_notes << '\n';</pre>
for(int i = 1; i <= n; i++)
  cout << note[i] << ' ';
puts("");
```

```
return 0;
```

3.7 Knapsack Zero One Without Value

```
// Knapsack 0 - 1 sem valor em O((N*W) / word)
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[10000];
bitset<10000> T[100];
bool knapsack()
 T[0][0] = 1;
  for(int i = 1; i <= n; i++)</pre>
    T[i] = ((T[i-1] << weight[i-1]) | T[i-1]);
  return T[n][W];
void retrieve()
  vector<int> ans;
  for (int i = n; i > 0; i--)
    if(W >= weight[i - 1]  and T[i - 1][W - weight[i - 1]])
      ans.push_back(i - 1);
      W \rightarrow = weight[i - 1];
  for(int &w : ans) cout << weight[w] << ' '; puts("");</pre>
int main()
  cin >> n;
  for(int i = 0; i < n; i++)
   cin >> weight[i];
  cin >> W:
  cout << knapsack() << '\n';</pre>
  retrieve();
  return 0:
```

3.8 Knapsack0-kSemValor

```
// Knapsack 0 - k sem valor em O((N*W*LogK) / word)
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[10000], K[10000];
bitset<10000> T[100];
bool knapsack()
```

```
T[0][0] = 1;
  for(int i = 1; i <= n; i++)</pre>
    int s = K[i - 1];
    T[i] = T[i - 1];
    for (int p = 1; p \le s; s -= p, p *= 2)
     T[i] = ((T[i] << (weight[i - 1] * p)) | T[i]);
      T[i] \mid = ((T[i] << (weight[i - 1] * s)) \mid T[i]);
  return T[n][W];
void retrieve()
  vector<pair<int, int>> ans;
  for (int i = n; i > 0; i--)
    int s = K[i - 1], atd = 0;
    for(int p = 1; p <= s; p *= 2)
    if(W \ge weight[i - 1] * p and T[i - 1][W - weight[i - 1] * p])
      W \rightarrow weight[i - 1] * p, qtd += p, s -= p;
    if(W \ge weight[i - 1] * s and T[i - 1][W - weight[i - 1] * s])
      W = s * weight[i - 1], qtd += s;
    if(qtd) ans.push_back({qtd, i - 1});
  }//first eh q quantidade de pesos i - 1
  for(pair<int, int> &w : ans)
    cout << w.first << ' ' << weight[w.second] << '\n';</pre>
int main()
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
    cin >> weight[i];
  for(int i = 0; i < n; i++)</pre>
    cin >> K[i];
  cin >> W;
  cout << (knapsack() ? "possible\n" : "impossible\n");</pre>
  retrieve();
  return 0;
```

3.9 KnapsackErrichto

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
const int 00 = 0x3f3f3f3f3f3f3f3f3f3f;

int n, w, maxi;
int value[120], weight[120];
int dp[100040];

int32_t main()
{
   cin >> n >> w;
   for(int i = 0; i < n; i++)
      cin >> weight[i] >> value[i];
```

3.10 KnapsackWithCopies

```
// O(S * sqrt(SumKi))
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
int freq[50];
vector<int> value, weight;
int memo[5000][5000];
// Decompor o numero em uma soma de potencias
//de 2 de tal forma que qualquer numero entre 0 e k
// pode ser formado usando os numeros da decomposicao.
void decomp(int k, int w, int v)
  int i = 1:
  freq[1] = k;
  while (true)
    int m = (freq[i] - 1) / 2;
    if(freq[i] - m * 2 == 0) break;
    freq[i] -= 2 * m;
    freq[2 * i] += m;
    i++;
  for (int i = 0; i < 32; i++)
    while(freg[i]--)
      value.push_back(i * v);
      weight.push_back(i * w);
    freq[i] = 0;
int solve(int id, int W)
  if (memo[id][W] !=-1)
    return memo[id][W];
  if(id == value.size() or !W)
    return memo[id][W] = 0;
  int ans = 0;
  if(weight[id] > W)
    ans = solve(id + 1, W);
    ans = max(value[id] + solve(id + 1, W)
      - weight[id]), solve(id + 1, W));
```

```
return memo[id][W] = ans;
}
int main()
{
  int n, w, v, k, S;
  memset(memo, -1, sizeof(memo));
  cin >> n >> S;
  for(int i = 0; i < n; i++)
  {
    cin >> v >> w >> k;
    decomp(k, w, v);
  }
  cout << solve(0, S) << '\n';
  return 0;
}</pre>
```

3.11 KnapsackwithPDtopdown

```
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[2005], value[2005];
int memo[2005][2005];
int solve(int id, int W)
  if (memo[id][W] !=-1)
   return memo[id][W];
  if(id == n or !W)
    return memo[id][W] = 0;
  int ans = 0;
  if(weight[id] > W)
    ans = solve(id + 1, W);
    ans = max(value[id] + solve(id + 1,
      W - weight[id]), solve(id + 1, W));
  return memo[id][W] = ans;
void ans(int id, int W)
  if(id == n or !W)
 if(solve(id + 1, W) == memo[id][W])
    ans(id + 1, W);
  else
    cout << id << ' ';
    ans(id + 1, W - weight[id]);
int main()
  memset (memo, -1, sizeof (memo));
  cin >> n >> W;
  for(int i = 0; i < n; i++)</pre>
    cin >> weight[i] >> value[i];
```

```
cout << solve(0, W) << '\n';
cout << "Objetos escolhidos 0 - indexdos\n";
ans(0, W);
puts("");

return 0;
}</pre>
```

3.12 Longest Common Subsequece And Edit Distance

```
#include <bits/stdc++.h>
using namespace std;
// longest common substring
int pd[1000][1000];
int LCS(string a, string b)
    for(int i = 1; i <= a.size(); i++)</pre>
        for(int j = 1; j <= b.size(); j++)</pre>
            if(a[i-1] == b[j-1])
                pd[i][j] = pd[i-1][j-1] + 1;
                pd[i][j] = max(pd[i][j-1], pd[i-1][j]);
    return pd[a.size()][b.size()];
int main()
    string a, b;
    cin >> a >> b;
    int lcs = LCS(a, b);
    cout << lcs << '\n';
    cout << "Edit Distance: " << a.size()+b.size()-2*lcs << '\n';</pre>
    return 0;
```

3.13 Longest Increasing Subsequence

```
#include <bits/stdc++.h>
using namespace std;

void lis(vector<int> &arr)
{
  vector<int> pilha;
  int pai[1000], pos[1000];
  for(int i = 0; i < arr.size(); i++)
  {
    int p = int(upper_bound(pilha.begin(),
        pilha.end(), arr[i]) - pilha.begin());
    if(p == pilha.size())
        pilha.push_back(arr[i]);
  else
        pilha[p] = arr[i];</pre>
```

```
pos[p] = i;
    if(!p)
      pai[i] = -1;
      pai[i] = pos[p - 1];
 vector<int> L;
  int aux = pos[pilha.size() - 1];
  cout << pilha.size() << '\n';</pre>
  while (aux !=-1)
   L.push_back(arr[aux]);
    aux = pai[aux];
 reverse(L.begin(), L.end());
 for(const int &w : L)
   cout << w << ' ';
 cout << '\n';
int main()
 int n;
 vector<int> arr(n);
 for(int &w : arr)
   cin >> w;
 lis(arr);
 return 0;
```

3.14 Subset Sum

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6 + 10;
int n, x, weight[1005];
bool pd[MAX];
int ans[MAX];
void printAns(int m)
  cout << ans[m] << ' ';
 if(m - ans[m] > 0)
    printAns(m - ans[m]);
int main()
  cin >> n >> x:
  int sum = 0;
  for(int i = 0; i < n; i++) cin >> weight[i], sum += weight[i];
  pd[0] = 1;
  for (int j = 0; j < n; j++)
    for(int i = sum; i >= 0; i--)
      if(pd[i] and !pd[i + weight[j]])
```

```
ans[i + weight[j]] = weight[j];
    pd[i + weight[j]] = 1;
}

printAns(x);
puts("");

return 0;
}
```

3.15 Traveling Salesman Problem Bottom Up Dp

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
int n:
double dist[20][20];
double pd[1 << 17][20];
int tsp(int ori)
  memset (pd, 63, sizeof (pd));
  for(int i = 0; i < n; i++)</pre>
    if(i != ori)
      pd[1 << i][i] = dist[ori][i];
  for (int k = 0; k < (1 << n); k++)
  for(int i = 0; i < n; i++)</pre>
  if(k & (1 << i))
    for (int j = 0; j < n; j++)
      if((k \& (1 << j)) and i != j)
      pd[k][j] = min(pd[k][j], pd[k ^ (1 << j)][i] + dist[i][j]);
  return pd[(1 << n) - 1][ori];
int main()
  // inicializar dist, dist[i][j] quarda a distancia de i para j no
      grafo
  // chamar tsp
  return 0;
```

3.16 Traveling Salesman Problem Topdown Dp

```
#include <bits/stdc++.h>
using namespace std;
int dist[22][22], m;
int memo[20][1 << 20];
int solve(int id, int mask) {
  if(((1 << m) - 1) == mask)
    return dist[id][0];
  if(memo[id][mask] != -1)
    return memo[id][mask];
  int ans = INT_MAX;</pre>
```

```
for(int i = 0; i < m; i++)
   if((mask & (1 << i)) == 0)
      ans = min(ans, dist[id][i] + solve(i, mask | (1 << i)));
   return memo[id][mask] = ans;
}
int main() {
   memset(memo, -1, sizeof(memo));
   //inicializa a matriz dist com as distancias
   //de todo mundo pra todo mundo..
   cout << solve(0, 1) << '\n';
   return 0;
}</pre>
```

4 String

4.1 Aho Corasick

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
int p[MAX], f[MAX], nxt[MAX][26], ch[MAX];
int tsz = 1; // size of the trie
int cnt[MAX]; // used to know number of matches
const int S = 2e3+5;
bitset<MAX> elem[S];
// S eh tamanho da maior das N strings que sao
// pradroes para buscar no texto
void init()
    tsz = 1;
    memset(f, 0, sizeof(f));
    memset(nxt, 0, sizeof(nxt));
    memset(cnt, 0, sizeof(cnt));
    for (int i = 0; i < MAX; i++)</pre>
      elem[i].reset();
void add(const string &s, int x)
  // the first element of the trie is the root
    int cur = 1;
    for(int i = 0; s[i]; ++i)
        int j = s[i] - 'a';
        if(!nxt[cur][j])
            tsz++;
            p[tsz] = cur;
            ch[tsz] = j;
            nxt[cur][j] = tsz;
        cur = nxt[cur][j];
```

```
cnt[cur]++;
    elem[cur].set(x);
void build()
    queue<int> q;
    for(int i = 0; i < 26; ++i)
        nxt[0][i] = 1;
        if(nxt[1][i])
            q.push(nxt[1][i]);
    while(!q.empty())
        int v = q.front(); q.pop();
        int u = f[p[v]];
        while (u and !nxt[u][ch[v]]) u = f[u];
        f[v] = nxt[u][ch[v]];
        cnt[v] += cnt[f[v]];
        for (int i = 0; i < 26; ++i)
            if(nxt[v][i])
                q.push(nxt[v][i]);
bitset<MAX> match(const string &s)
    int ans = 0;
    // Numero de matches
    bitset<MAX> found;
    // Usado pra saber quais strings matches
   int x = 1;
    for(int i = 0; i < s.size(); ++i)</pre>
        int t = s[i] - 'a';
        while(x and !nxt[x][t])
            x = f[x];
        x = nxt[x][t];
        ans += cnt[x];
        found |= elem[x];
    return found;
int main()
    int n;
    string s;
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> s;
        add(s, i);
    build();
    cin >> s;
    bitset<MAX> ans = match(s);
    for(int i = 0; i < n; i++)</pre>
        cout << ans[i] << '\n';
        // 1 se a i-esima string lida
```

```
// aparece no texto, 0 cc
 return 0;
    #include <bits/stdc++.h>
using namespace std;
const int K = 60:
struct Vertex {
  int next[K];
  bool leaf = false;
  int p = -1;
  char c;
  int link = -1:
  int go[K];
  bitset<1005> S;
  Vertex(int _p=-1, char _c = '$') : p(_p), c(_c) {
     fill(begin(next), end(next), -1);
     fill(begin(go), end(go), -1);
};
vector<Vertex> t;
void init() {
  t.clear();
  t.resize(1);
void add(string &s, int i) {
  int v = 0;
  for(char ch : s) {
     int c = ch - 'A';
     if(t[v].next[c] == -1) {
        t[v].next[c] = t.size();
        t.push_back(Vertex(v, ch));
     v = t[v].next[c];
  t[v].leaf = true;
  t[v].S[i] = 1;
int go(int v, char ch);
int get_link(int v) {
  if(t[v].link == -1) {
     if(v == 0 or t[v].p == 0)
        t[v].link = 0;
        t[v].link = go(get_link(t[v].p), t[v].c);
  return t[v].link;
int go(int v, char ch) {
```

```
int c = ch - 'A';
  if(t[v].go[c] == -1) {
      if(t[v].next[c] != -1)
         t[v].go[c] = t[v].next[c];
      else
         t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
   return t[v].go[c];
int32_t main() {
  ios_base::sync_with_stdio(false);
  cin.tie(nullptr);
  int caso:
  cin >> caso:
   while (caso--)
      init();
      string s:
      int n;
      cin >> s >> n;
      bitset<1005> S;
      for(int i = 0; i < n; i++) {</pre>
         string a;
         cin >> a;
         add(a, i);
      int v = 0;
      for(char &c : s) {
         v = qo(v, c);
         S \mid = t[v].S;
      for(int i = 0; i < n; i++)</pre>
         cout << (S[i] ? 'y' : 'n') << '\n';
  return 0:
```

4.2 Dynamic Trie

```
#include <bits/stdc++.h>
using namespace std;

struct TrieNode
{
    map<int, TrieNode*> childreen;
    bool isLeaf;
    TrieNode()
    {
        isLeaf = false;
    }
};

void inserir(TrieNode *root, string s)
{
    TrieNode *node = root;
    for(int i = 0; i < s.size(); i++)
    {
        int index = s[i] - 'a';
}</pre>
```

```
if(node->childreen.find(index) == node->childreen.end())
      node->childreen[index] = new TrieNode();
    node = node->childreen[index];
  node->isLeaf = true;
bool buscar(TrieNode *root, string s)
  TrieNode *node = root;
  for(int i = 0; i < s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(node->childreen.find(index) == node->childreen.end())
      return false:
    node = node->childreen[index];
  return node->isLeaf;
bool remover(TrieNode *node, string s, int level)
  if(node != nullptr)
    if(s.size() == level)
      if(node->isLeaf)
       node->isLeaf = false;
        return !node->childreen.size();
    else
      int index = s[level] - 'a';
      if (remover (node->childreen[index], s, level+1))
        delete node->childreen[index];
        node->childreen.erase(index);
        return !node->childreen.size();
  return false:
int main()
  TrieNode *root = new TrieNode();
  inserir(root, "abc");
  inserir(root, "abd");
  inserir(root, "cfa");
  remover(root, "abc", 0);
  printf(buscar(root, "abc") ? "yes\n" : "no\n");
  printf(buscar(root, "abd") ? "yes\n" : "no\n");
  return 0;
```

4.3 KMP

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;
int n, m;
// n eh o tamanho do texto e m eh o
// tamanho do padrao
int arr[MAX];
// array que guarda o tamanho do maior
// prefixo proprio que tambem eh sufixo
string t, p; // t eh o texto e p eh o padrao
void build() // kMP Preprocess
    int i = 0, j = 1;
    while(j < m)</pre>
        if(p[i] == p[j])
            arr[j] = ++i;
        else
            i = 0;
            if(p[i] == p[j])
                arr[j] = ++i;
        j++;
int matching() // KMP search
    int i = 0, j = 0;
    while (j < n)
        if(p[i] == t[j]) i++, j++;
        else if(i) i = arr[i - 1];
        else i++:
        if(i == m)
            return j - m;
    // a substring P inicia na posicao j - m em T
    return -1; // P nao eh substring de T
int main()
    cin >> t >> p;
    n = (int)t.size();
    m = (int)p.size();
    build();
    cout << matching() << '\n';</pre>
    return 0;
```

4.4 LIS LDS

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
```

```
int n;
int LI[MAX], LD[MAX];
vector<int> arr;
int LIS() {
    for(int i = 0; i < n; i++)</pre>
        LI[i] = 1;
    for(int i = n - 1; i >= 0; i--)
        for (int j = 0; j < i; j++)
            if(arr[j] < arr[i])
                 LI[j] = max(LI[j], LI[i] + 1);
int LDS() {
    reverse(arr.begin(), arr.end());
    for(int i = 0; i < n; i++)</pre>
        LD[i] = 1;
    vector<int> pilha:
    for(int i = 0; i < n; i++) {</pre>
        int p = (int) (lower_bound(pilha.begin(),
          pilha.end(), arr[i]) - pilha.begin());
        if(p == pilha.size())
            pilha.push_back(arr[i]);
        else
            pilha[p] = arr[i];
        LD[i] = p + 1;
int main() {
    cin >> n; arr.resize(n);
    for(int i = 0; i < n; i++) cin >> arr[i];
    LIS();
    LDS();
    for(int i = 0; i < n; i++)</pre>
      cout << LI[i] << ' '; puts("");
    for(int i = 0; i < n; i++)</pre>
      cout << LD[n - i - 1] << ' '; puts("");
  return 0;
```

4.5 Longest Common Substring

```
#include <stdio.h>
#include <string.h>
int pd[10000][10000];
int max(int a, int b)
{
   return a > b ? a : b;
}
int solve(char *a, char *b)
{
```

```
int i, j, ans = 0;
  int t1 = strlen(a), t2 = strlen(b);
  for(i = 1; i < t1; i++)
  for (j = 1; j < t2; j++)
   if(a[i-1] == b[j-1])
     pd[i][j] = pd[i-1][j-1] + 1,
        ans = max(ans, pd[i][j]);
    else
      pd[i][j] = 0;
  return ans;
int main()
 char s1[55], s2[55];
 while (fgets (s1, 54, stdin) != NULL
   && fgets(s2, 54, stdin) != NULL)
   printf("%d\n", solve(s1, s2));
  return 0;
```

4.6 Manacher

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 100:
int lps[2*MAX+5];
char s[MAX];
int manacher()
    int n = strlen(s);
    string p(2*n+3, '#');
    p[0] = '^{'};
    for(int i = 0; i < n; i++)</pre>
        p[2*(i+1)] = s[i];
    p[2*n+2] = '$';
    int k = 0, r = 0, m = 0;
    int l = p.length();
    for(int i = 1; i < 1; i++)</pre>
        int o = 2 * k - i;
        lps[i] = (r > i) ? min(r-i, lps[o]) : 0;
        while (p[i + 1 + lps[i]] == p[i - 1 - lps[i]])
            lps[i]++;
        if(i + lps[i] > r) k = i, r = i + lps[i];
        m = max(m, lps[i]);
    /*for(int i = 1; i \le 2 * n + 1; i++)
        cout << lps[i] << ' ';
    puts(""); */
    return m;
int main()
    cin >> s;
```

```
cout << manacher() << '\n';
return 0;</pre>
```

4.7 SA

```
* Code frin Competitive Programming 3
#include <algorithm>
#include <cstdio>
#include <cstring>
using namespace std;
typedef pair<int, int> ii;
#define MAX N 100010
                                            // second approach: O(n
    log n)
char T[MAX N];
                                // the input string, up to 100K
    characters
int n;
                                             // the length of input
    string
int RA[MAX_N], tempRA[MAX_N];
                                  // rank array and temporary rank
int SA[MAX_N], tempSA[MAX_N];
                               // suffix array and temporary suffix
    array
int c[MAX N];
                                                 // for counting/radix
    sort
char P[MAX N];
                               // the pattern string (for string
    matching)
int m;
                                            // the length of pattern
    string
int Phi[MAX N];
                                    // for computing longest common
    prefix
int PLCP[MAX N];
int LCP[MAX_N]; // LCP[i] stores the LCP between previous suffix T+SA
                                              // and current suffix T+
                                                  SA[i]
bool cmp(int a, int b) { return strcmp(T + a, T + b) < 0; }</pre>
    compare
void constructSA_slow() {
                                      // cannot go beyond 1000
    characters
  for (int i = 0; i < n; i++) SA[i] = i; // initial SA: {0, 1, 2, ...,
  sort(SA, SA + n, cmp); // sort: O(n log n) * compare: O(n) = O(n^2)
      log n)
                                                                    11
void countingSort(int k) {
  int i, sum, maxi = max(300, n); // up to 255 ASCII chars or length
       of n
  memset(c, 0, sizeof c);
                                                  // clear frequency
     table
```

```
for (i = 0; i < n; i++) // count the frequency of each integer</pre>
    rank
  c[i + k < n ? RA[i + k] : 0]++;
 for (i = sum = 0; i < maxi; i++) {</pre>
  int t = c[i]; c[i] = sum; sum += t;
 for (i = 0; i < n; i++) // shuffle the suffix array if
  necessarv
 tempSA[c[SA[i]+k < n ? RA[SA[i]+k] : 0]++] = SA[i];
 for (i = 0; i < n; i++) // update the suffix
  array SA
  SA[i] = tempSA[i];
characters
 int i. k. r:
 for (i = 0; i < n; i++) SA[i] = i;  // initial SA: {0, 1, 2, ...,</pre>
 for (k = 1; k < n; k <<= 1) { // repeat sorting process log n
  countingSort(k); // actually radix sort: sort based on the second
  item
  tempRA[SA[0]] = r = 0; // re-ranking; start from rank
    r = 0
   for (i = 1; i < n; i++) // compare adjacent
    suffixes
    tempRA[SA[i]] = // if same pair => same rank r; otherwise,
    increase r
    (RA[SA[i]] == RA[SA[i-1]] && RA[SA[i]+k] == RA[SA[i-1]+k]) ? r :
      ++r:
  for (i = 0; i < n; i++)
                                  // update the rank
    arrav RA
   RA[i] = tempRA[i];
  if (RA[SA[n-1]] == n-1) break; // nice optimization
     trick
void computeLCP_slow() {
 LCP[0] = 0;
                                          // default
   value
 definition
  int L = 0;
                                      // always reset L
    to 0
  while (T[SA[i] + L] == T[SA[i-1] + L]) L++; // same L-th char
  , L++
  LCP[i] = L;
void computeLCP() {
 int i, L;
                                         // default
 Phi[SA[0]] = -1;
   value
 for (i = 1; i < n; i++)
                      // compute Phi in
    0(n)
  Phi[SA[i]] = SA[i-1]; // remember which suffix is behind this
```

```
suffix
 0(n)
  if (Phi[i] == -1) { PLCP[i] = 0; continue; } // special
  while (T[i + L] == T[Phi[i] + L]) L++; // L increased max n
   times
  PLCP[i] = L;
  L = max(L-1, 0);
                              // L decreased max n
    times
                                  // compute LCP in
 for (i = 0; i < n; i++)
   0(n)
  LCP[i] = PLCP[SA[i]]; // put the permuted LCP to the correct
    position
ii stringMatching() {
                   // string matching in O(m
  log n)
 int lo = 0, hi = n-1, mid = lo;  // valid matching =
  [0..n-1]
 while (lo < hi) {</pre>
                                    // find lower
  bound
                       // this is round
  mid = (lo + hi) / 2;
    down
  int res = strncmp(T + SA[mid], P, m); // try to find P in suffix
  if (res >= 0) hi = mid;  // prune upper half (notice the >=
    sign)
  including mid
                         // observe '=' in "res >= 0"
    above
 if (strncmp(T + SA[lo], P, m) != 0) return ii(-1, -1);  // if not
    found
 ii ans; ans.first = lo;
 lo = 0; hi = n - 1; mid = lo;
 bound
  mid = (lo + hi) / 2;
  int res = strncmp(T + SA[mid], P, m);
  if (res > 0) hi = mid:
                                     // prune upper
     half
   including mid
                   // (notice the selected branch when res
   == 0)
 ans.second = hi;
 return ans;
} // return lower/upperbound as first/second item of the pair,
 respectively
ii LRS() { // returns a pair (the LRS length and its
 index)
int i, idx = 0, maxLCP = -1;
for (i = 1; i < n; i++)
                                 // O(n), start from
  i = 1
 if (LCP[i] > maxLCP)
 maxLCP = LCP[i], idx = i;
```

```
return ii(maxLCP, idx);
int owner(int idx) { return (idx < n-m-1) ? 1 : 2; }</pre>
ii LCS() {
                           // returns a pair (the LCS length and its
    index)
  int i, idx = 0, maxLCP = -1;
  for (i = 1; i < n; i++)
                                                  // O(n), start from
     i = 1
   if (owner(SA[i]) != owner(SA[i-1]) && LCP[i] > maxLCP)
     maxLCP = LCP[i], idx = i;
 return ii(maxLCP, idx);
int main() {
 //printf("Enter a string T below, we will compute its Suffix Array:\
 strcpy(T, "GATAGACA");
 n = (int)strlen(T);
 T[n++] = ' $';
 // if '\n' is read, uncomment the next line
  //T[n-1] = '$'; T[n] = 0;
  constructSA_slow();
                                                             // O(n^2
      log n)
 printf("The Suffix Array of string T = '%s' is
   shown below (O(n^2 \log n) \text{ version}): n", T);
 printf("i\tSA[i]\tSuffix\n");
  for (int i = 0; i < n; i++) printf("%2d\t%2d\t%s\n", i, SA[i], T +
      SA[i]);
                                                               // O(n
  constructSA():
 printf("\nThe Suffix Array of string T = '%s' is
    shown below (O(n log n) version):\n", T);
  printf("i\tSA[i]\tSuffix\n");
  for (int i = 0; i < n; i++) printf("%2d\t%2d\t%s\n", i, SA[i], T +
  computeLCP();
       O(n)
  // LRS demo
                                // find the LRS of the first input
  ii ans = LRS();
      string
  char lrsans[MAX N];
  strncpy(lrsans, T + SA[ans.second], ans.first);
 printf("\nThe LRS is '%s' with length = %d\n\n", lrsans, ans.first);
  // stringMatching demo
  //printf("\nNow, enter a string P below, we will try to find P in T
      :\n");
  strcpv(P, "A");
 m = (int)strlen(P);
  // if '\n' is read, uncomment the next line
  //P[m-1] = 0; m--;
  ii pos = stringMatching();
  if (pos.first != -1 && pos.second != -1) {
   printf("%s is found SA[%d..%d] of %s\n", P, pos.first, pos.second,
         T);
```

```
printf("They are:\n");
  for (int i = pos.first; i <= pos.second; i++)</pre>
    printf(" %s\n", T + SA[i]);
} else printf("%s is not found in %s\n", P, T);
//printf("\nRemember, T = ' ss' \setminus NNow, enter another string P: \setminus n", T);
// T already has '$' at the back
strcpy(P, "CATA");
m = (int)strlen(P);
// if '\n' is read, uncomment the next line
//P[m-1] = 0; m--;
strcat(T, P);
    append P
strcat(T, "#");
                                                    // add '$' at the
     back
n = (int)strlen(T);
                                                                11
    update n
// reconstruct SA of the combined strings
constructSA();
                                                              // O(n
    log n)
                                                                     11
computeLCP();
printf("\nThe LCP information of 'T+P' = '%s':\n", T);
printf("i\tSA[i]\tLCP[i]\tOwner\tSuffix\n");
for (int i = 0; i < n; i++)
  printf("%2d\t%2d\t%2d\t%2d\t%s\n", i, SA[i], LCP[i], owner(SA[i]),
ans = LCS();
                      // find the longest common substring between T
    and P
char lcsans[MAX_N];
strncpy(lcsans, T + SA[ans.second], ans.first);
printf("\nThe LCS is '%s' with length = %d\n", lcsans, ans.first);
return 0;
```

4.8 Suffix Array And Applications

```
#include <bits/stdc++.h>
using namespace std;

string s;
vector<int> sa, c, lcp;

// O(n)
void countSort()
{
  int n = sa.size();
  vector<int> buc(n), new_sa(n);
  for(int &w : sa)
    buc[c[w]]++;
  for(int i = 1; i < n; i++)
    buc[i] += buc[i - 1];
  for(int i = n - 1; i >= 0; i--)
    new_sa[ --buc[ c[sa[i]] ] ] = sa[i];
  sa = new_sa;
```

```
// O(|s| * log|s|)
void buildSuffixArray()
                                                                                   int mid = (b + e) / 2;
                                                                                   int r = cmp(sa[mid], p);
  int n = s.size();
                                                                                  if(!r)
  sa.resize(n);
                                                                                    e = mid - 1, ans = mid;
                                                                                   else if (r == -1)
  c.resize(n);
                                                                                    e = mid - 1;
  for (int i = 0; i < n; i++)
    sa[i] = i, c[i] = s[i];
                                                                                   else
  sort(sa.begin(), sa.end(), [&](int a, int b)
                                                                                    b = mid + 1;
      return c[a] < c[b];</pre>
                                                                                if(s.substr(sa[ans], p.size()) != p)
                                                                                  return -1:
    });
  c[sa[0]] = 0;
                                                                                return ans;
  for(int i = 1; i < n; i++)</pre>
    if(s[sa[i - 1]] == s[sa[i]])
      c[sa[i]] = c[sa[i - 1]];
                                                                              // posicao no suffix array do sufixo mais
                                                                              // a direita que contem p como prefixo
    else
      c[sa[i]] = c[sa[i - 1]] + 1;
                                                                              // O(|p| * log|s|)
  int k = 0:
                                                                              int upper_bound(string &p)
  while ((1 << k) < n)
                                                                                int b = 0, e = (int) sa.size() - 1, ans = 0;
    for(int i = 0; i < n; i++)</pre>
                                                                                while(b <= e)
      sa[i] = (sa[i] - (1 << k) + n) % n;
    countSort();
                                                                                   int mid = (b + e) / 2;
    vector<int> new_c(n);
                                                                                   int r = cmp(sa[mid], p);
    new_c[sa[0]] = 0;
                                                                                   if(!r)
    for(int i = 1; i < n; i++)</pre>
                                                                                    b = mid + 1, ans = mid;
                                                                                   else if (r == -1)
      pair<int, int> prev = \{c[sa[i-1]], c[(sa[i-1] + (1 << k)) \}
                                                                                    e = mid - 1;
                                                                                   else
      pair<int, int> cur = {c[sa[i]], c[(sa[i] + (1 << k)) % n]};
                                                                                    b = mid + 1;
      if (prev == cur) new_c[sa[i]] = new_c[sa[i - 1]];
      else new_c[sa[i]] = new_c[sa[i-1]] + 1;
                                                                                 if(s.substr(sa[ans], p.size()) != p)
                                                                                  return -1;
                                                                                return ans;
    c = new_c;
    k++;
                                                                              // numero de ocorrencias da string p
                                                                              // como substrina de s
// 0: padrao esta no sufixo
                                                                              // O(|p| * log|s|)
// 1: o padrao eh lexicograficamente maior que o sufixo k
                                                                              int count (string &p)
//-1: o padrao eh lexicograficamente menor que o sufixo k
// O(|p|)
                                                                                int 1 = lower_bound(p);
                                                                                int u = upper bound(p);
int cmp(int k, string &p)
                                                                                if (1 == -1 \text{ or } u == -1)
  for(int i = 0; i < p.size(); i++)</pre>
                                                                                   return 0;
                                                                                return u - 1 + 1;
   if(i + k >= s.size()) return 1;
   if(s[i + k] < p[i]) return 1;
                                                                              // construcao do array lcp
    if(s[i + k] > p[i]) return -1;
                                                                              // lcp[i] eh o maior prefixo comum
                                                                              // aos sufixos i e i - 1 do suffix array
  return 0;
                                                                              // O(n)
                                                                              void buildLcp()
// posicao no suffix array do sufixo mais
// a esquerda que contem p como prefixo
                                                                                int n = s.size();
// O(|p| * log|s|)
                                                                                lcp.resize(n);
int lower_bound(string &p)
                                                                                int k = 0:
                                                                                for (int i = 0; i < n - 1; i++)
  int b = 0, e = (int)sa.size() - 1, ans = 0;
```

while (b \leq e)

```
// pi eh a posicao no suffix array do
  // sufixo que comeca na posicao i da strig
    int pi = c[i];
    int j = sa[pi - 1];
    while (s[i + k] == s[j + k]) k++;
    lcp[pi] = k;
    k = max(k - 1, 0);
// conta a quantidade de substrings
// diferentes na string s
// O(IsI)
long long numberOfDifSubStr()
  long long n = s.size();
  long long ans = n * (n - 1) / 2;
  for(int i = 0; i < n; i++)</pre>
   ans -= lcp[i];
  return ans;
// encontra a maior substring comum a s e p
// O(|s + p|) depois de construir suffix array
void longestCommonSubstring(string p)
  int n = s.size();
  int m = p.size();
  int ans = -1, j = 1;
  s = s + "$" + p + "#";
 buildSuffixArrav();
  buildLcp();
  for(int i = 1; i < sa.size(); i++)</pre>
    int p = sa[i - 1] < n ? 1 : -1;
    int q = sa[i] < n ? 1 : -1;</pre>
    if(p * q < 0 and ans < lcp[i])
      ans = lcp[i], j = i;
  int a = sa[j];
  int b = sa[j - 1];
  string lcs;
  while (a < s.size()) and b < s.size() and s[a] == s[b])
    lcs.push back(s[a]);
    a++, b++;
  cout << ans << '\n';
  cout << lcs << '\n';
int32_t main()
  string p;
  cin >> s >> p;
```

```
// o tamanho do maior prefixo comum entre dois
// sufixos que estao nas posicoes a e b do
// suffix array eh igual ao menor valor no
// intervalo [a+1, b] do array lcp

// descomentar as linhas abaixo para todas as
// funcoes, exceto para longestCommonSubstring

// s.push_back('$');
// buildSuffixArray();
// buildLcp();

longestCommonSubstring(p);

return 0;
}
```

4.9 Suffix Array

```
#include <bits/stdc++.h>
using namespace std;
string txt; // texto
string pat; // padrao
int n; // tamanho do texto
int chave[100]; // chave para comparacao dos sufixos
int vs[100]; // vetor de sufixos
int ord[100]; // ordem de um sufixo (qual classe ele pertence)
int lcp[100]; // maior prefixo comum
bool comp(int a, int b)
    return chave[a] < chave[b];</pre>
void constroi() // O(N*Log(N) *Log(N))
    for(int i = 0; i < n; i++)</pre>
        vs[i] = i;
        chave[i] = txt[i] - 'a' + 1;
    sort (vs, vs+n, comp);
    for(int i = 0; i++)
        int classes = 0;
        for(int j = 0; j < n; j++)</pre>
            ord[vs[j]] = j > 0 and chave[vs[j]]
              == chave[vs[j-1]] ? ord[vs[j-1]] : ++classes;
        if(classes == n) break;
        for (int j = 0; j < n; j++)
            chave[j] = ord[j] * (classes+1);
            chave[j] += j+(1<<i) < n ? ord[j+(1<<i)] : 0;
        sort(vs, vs+n, comp);
int strcompara(int pos)
```

```
{// retorna 0 se o padrao esta no sufixo, maior que zero se o padrao
//lexicograficamente maior que o sufixo, e menor que 0 se o padrao
//eh lexicograficamente menor que o sufixo
    for(int i = 0; i < pat.size(); i++)</pre>
        if(i+pos >= n)
            return 1;
        else if(pat[i] != txt[i+pos])
            return pat[i] - txt[i+pos];
    return 0;
bool search() // O(Size(Pat) *Log(N))
    int b = 0, e = n - 1, m, aux;
    while(b <= e)</pre>
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            return true:
        else if(aux > 0)
            b = m + 1;
        else
            e = m - 1;
    return false;
// numero de vezes que o padrao aparece no texto. O(Size(Pat)*Log(N))
int numberOfOcur()
    int b = 0, e = n - 1, m, aux, l = INT_MAX, r = INT_MIN;
    while(b <= e)</pre>
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            l = min(l, m);
            e = m - 1;
        else if(aux > 0)
            b = m + 1;
        else
            e = m - 1;
    b = 0, e = n - 1;
    while(b <= e)</pre>
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            r = max(r, m);
            b = m + 1;
        else if (aux > 0)
            b = m + 1;
        else
            e = m - 1;
```

```
return abs(r-l+1);
// kasai em O(NloqN) pra construir o LCP (longest common prefix)
void kasai()
    vector<int> invSuff(n, 0);
    for(int i = 0; i < n; i++)
        invSuff[vs[i]] = i;
    int k = 0;
    for(int i = 0; i < n; i++)
        if(invSuff[i] == n-1)
            k = 0;
            continue;
        int i = vs[invSuff[i]+1];
        while (i + k < n \text{ and } j + k < n \text{ and } txt[i + k] == txt[j + k])
        lcp[invSuff[i]] = k;
        if(k > 0)
            k--;
void printAll()
    cout << "Vetor de sufixos:\n";
    for(int i = 0; i < n; i++)</pre>
        cout << vs[i] << ' ';
    cout << '\n';
    cout << "Sufixos em ordem:\n";</pre>
    for(int i = 0; i < n; i++)</pre>
        cout << txt.substr(vs[i]) << '\n';</pre>
  Dado um array LCP onde LCP[i] armazena o tamanho do maior prefixo
  em comum entre os sufixos i e i + 1 da suffix array
  , entao para achar o maior prefixo em comum entre dois sufixos que
   estao nas posicoes a e b da suffix array, corresponde a achar
   o menor valor no intervalo [a, b-1] no LCP array.
  Outra aplicacao eh dada uma string, para contar quantas substrings
   diferentes ela tem basta contar quantas tem no total ( ((n + 1) * n
    possiveis substrings) e remover todos os valores de LCP do total.
*/
int main()
    cin >> txt;
   n = txt.size();
    constroi();
    printAll();
    cout << '\n':
    cin >> pat;
```

4.10 Trie Static

#include <bits/stdc++.h>

```
using namespace std;
// as posicoes de 0 ate 25 representam as letras
// de a ate z do alfabeto.
// a posicao 26 armazena quantas strings terminam
// nesse vertice.
// a posicao 27 armazena quantas strings passam
// nesse vertice.
int trie[8000000][30], CUR = 1;
// fl eh zero se for uma operacao de inserir
// fl eh um se for uma operacao de buscar
int add(string &s, int fl)
  int root = 0;
  for(char &c : s)
   if(trie[root][c - 'a'] == 0)
      if(fl) return 0;
      trie[root][c - 'a'] = CUR++;
   if(!fl) trie[root][27]++;
   root = trie[root][c - 'a'];
  if(fl) return trie[root][26];
  trie[root][26]++;
  return 1;
void sub(string &s)
  int root = 0;
  for(char &c : s)
   if(trie[root][c - 'a'] and trie[root][27])
      trie[root][27]--:
      root = trie[root][c - 'a'];
  trie[root][26]--;
int main()
```

```
int q;
cin >> q;
while(q--)
{
   int o;
   string s;
   cin >> o >> s;
   if(o == 1) add(s, 0);
   else if(o == 2) puts(add(s, 1) ? "existe" : "nao existe");
   else sub(s);
}
return 0;
}
```

4.11 Trie With Vector

```
#include <bits/stdc++.h>
using namespace std;
struct TrieNode
  int child[26], size, cnt;
  TrieNode()
    memset(child, 0, sizeof(child));
    size = cnt = 0;
};
vector<TrieNode> trie;
void init()
  trie.clear();
  trie.push_back(TrieNode());
void add(string s)
  int root = 0;
  for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(trie[root].child[index] == 0)
      trie[root].child[index] = trie.size();
      trie.push_back(TrieNode());
    root = trie[root].child[index];
    trie[root].size++;
  trie[root].cnt++;
void sub(string s)
  int root = 0;
```

```
for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    root = trie[root].child[index];
    trie[root].size--;
  trie[root].cnt--;
int query(string s)
  int root = 0:
  for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(!trie[trie[root].child[index]].size)
      return false:
    root = trie[root].child[index];
  return trie[root].cnt;
int main()
  string s;
  int o;
  init();
  while(cin >> o >> s)
    if(o == 1) add(s);
    else if (o == 2) sub (s);
    else cout << query(s) << '\n';</pre>
  return 0;
```

4.12 Trie

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;

int trie[MAX] [26], cnt[MAX], tsz = 1;
bool leaf[MAX];

void insert(string s)
{
   int cur = 1;
   cnt[cur]++;
   for(int i = 0; i < s.size(); i++)
   {
      int a = s[i] - 'a';
      if(!trie[cur][a]) trie[cur][a] = ++tsz;
      cur = trie[cur][a];
      cnt[cur]++;
   }
   leaf[cur] = true;
}</pre>
```

```
bool find(string s)
    int cur = 1;
    for(int i = 0; i < s.size(); i++)</pre>
        int a = s[i] - 'a';
        if(!trie[cur][a] or !cnt[cur])
             return false;
        cur = trie[cur][a];
    return leaf[cur] and cnt[cur];
int remove(string s)
    int cur = 1;
    for(int i = 0; i < s.size(); i++)</pre>
        int a = s[i] - 'a';
        cnt[cur]--;
        cur = trie[cur][a];
    leaf[cur] = false;
    cnt[cur]--;
int main()
    string s;
    int n, o;
    while(cin >> o >> s)
        if(0 == 1)
             cout << (find(s) ? "found\n" : "not found\n");</pre>
        else if (\circ == 2)
             insert(s);
        else
             remove(s);
  return 0;
```

4.13 Z Function

```
#include "bits/stdc++.h"
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
using namespace std;
const int MAX = 1e5;

vector<int> Z(string &s)
{
  int n = s.size(), x = 0, y = 0;
  vector<int> z(n);
  for(int i = 1; i < n; i++)
  {
    z[i] = Max(0, Min(z[i - x], y - i + 1));
    while(i + z[i] < n and s[z[i]] == s[i + z[i]])
    x = i, y = i + z[i], z[i]++;</pre>
```

```
}
return z;
}
int main()
{
  string txt, pattern;
  cin >> txt >> pattern;
  string s = pattern + "#" + txt;
  vector<int> z = Z(s);
  for(int &w : z)
    cout << w << ' ';
  cout << '\n';
  return 0;
}</pre>
```

5 Math

5.1 Baby Step Giant Step

// a ^ kcongb mod m

```
int value[1000008];
int cor[1000008], tempo = 1;
// com vetor o modulo deve ser <= 10^7 fica O(sqrt(m))</pre>
inline int discreteLogarithm(int a, int b, int m) {
    tempo++;
  a %= m; b %= m;
    int n = (int) sqrt(m + .0) + 1, an = 1;
  for(int i = 1; i <= n; i++) an = (an * 1LL * a) % m;</pre>
    for(int i = 1, cur = an; i <= n; i++) {</pre>
      if(cor[cur] < tempo) value[cur] = i, cor[cur] = tempo;</pre>
        cur = (cur * 1LL * an) % m;
    for(int j = 0, cur = b; j \le n; j++) {
        if(cor[cur] == tempo) {
            int ans = value[cur] * n - j;
            if(ans < m)
                return ans;
    cur = (cur * 1LL * a) % m;
  return -1;
// com mapa o modulo pode ser ateh <= 10^12 fica O(sqrt(m) * log(m))
int discreteLogarithm(int a, int b, int m)
  a %= m; b %= m;
    int n = (int) sqrt(m + .0) + 1, an = 1;
  for (int i = 1; i \le n; i++) an = (an * a) % m;
    unordered_map<int, int> value;
    for(int i = 1, cur = an; i <= n; i++) {
      if(!value.count(cur)) value[cur] = i;
        cur = (cur * an) % m;
```

```
}
for(int j = 0, cur = b; j <= n; j++) {
    if(value[cur]) {
        int ans = value[cur] * n - j;
        if(ans < m)
            return ans;
    }
    cur = (cur * a) % m;
}
    return -1;
}
</pre>
```

5.2 Catalan Numbers

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
const long long MOD = 1000000000;
int catalan[MAX];
void init()
    catalan[0] = catalan[1] = 1;
    for(int i = 2; i <= 1000; i++)
        for (int j = 0; j < i; j++)
            catalan[i] += (catalan[j] * catalan[i-j-1]) % MOD;
            if(catalan[i] >= MOD)
                catalan[i] -= MOD;
int main()
  init();
  int n;
  while(cin >> n)
    printf("%d\n", catalan[n]);
  return 0;
```

5.3 Chinese Remainder Theorem

```
//codar em Python para evitar problemas de overflow
// O(Tlog(lcm(n1*n2*..)))
//https://codeforces.com/blog/entry/61290

#include<bits/stdc++.h>
using namespace std;
const int MAX = 20;
#define 11 long long

11 GCD(l1 a, l1 b) { return (b == 0) ? a : GCD(b, a % b); }
```

```
inline 11 LCM(11 a, 11 b) { return a / GCD(a, b) * b; }
inline 11 normalize(11 x, 11 mod) { x \% = mod; if (x < 0) x += mod;
    return x; }
struct GCD type { ll x, v, d; };
GCD_type ex_GCD(ll a, ll b)
    if (b == 0) return {1, 0, a};
    GCD_type pom = ex_GCD(b, a % b);
    return {pom.y, pom.x - a / b * pom.y, pom.d};
int t:
ll a[MAX], n[MAX], ans, lcm;
int main()
    cin >> t;
    for(int i = 1; i <= t; i++)</pre>
        cin >> a[i] >> n[i], normalize(a[i], n[i]);
    ans = a[1];
    lcm = n[1];
    for(int i = 2; i <= t; i++)
        auto pom = ex_GCD(lcm, n[i]);
        11 \times 1 = pom.x;
        11 d = pom.d;
        if((a[i] - ans) % d != 0) return cerr << "No solutions" <</pre>
        ans = normalize(ans + x1 * (a[i] - ans) / d % (n[i] / d) * lcm
      lcm * n[i] / d);
        lcm = LCM(lcm, n[i]);
        // you can save time by replacing above lcm * n[i] /d
        // by lcm = lcm * n[i] / d
    cout << ans << " " << lcm << endl;
    return 0;
```

5.4 Conversion Base

```
#include <bits/stdc++.h>
using namespace std;
int a,b; char sa[10000]; char sb[10000];

void rev(char s[])
{
   int 1 = strlen(s);
   for(int i = 0; i < l - l - i; i++)
        swap(s[i], s[l - l - i]);
}

void multi(char s[], int k)
{
   int i, c = 0, d;</pre>
```

```
for (i=0; s[i]; i++)
   d = (s[i] - '0') * k + c;
   c = d / b; d %= b;
   s[i] = '0' + d;
  while (c)
   s[i] = '0' + (c % b); i++;
   c /= b;
  s[i] = ' \setminus 0';
void add(char s[], int k)
 int i, c = k, d;
  for(i = 0; s[i]; i++)
   d = (s[i] - '0') + c;
   c = d / b; d %= b;
   s[i] = '0' + d;
  while (c)
   s[i] = '0' + (c % b); i++;
   c /= b;
  s[i]='\0';
void trans(char s[])
  for(int i = 0; s[i]; i++)
    char \& c = s[i];
    if(c >= 'A' \&\& c <= 'Z') c = '0' + 10 + (c - 'A');
    if(c >= 'a' \&\& c <= 'z') c = '0' + 36 + (c - 'a');
void itrans(char s[])
  for(int i = 0; s[i]; i++)
    char& c = s[i]; int d = c - '0';
    if(d >= 10 \&\& d <= 35) c = 'A' + (d - 10);
    if(d >= 36) c = 'a' + (d - 36);
int main()
//digitos \{0-9, A-Z, a-z\}
  int q; cin>>q;
  int i, j;
  while (q)
    q--;
    cin >> a >> b >> sa; sb[0] = '0'; sb[1] = '\0';
```

```
// a e b sao dados na base 10
// sa eh dado na base a
// converter sa da base a pra base b
cout << a << " " << sa << '\n';
trans(sa);
for(i = 0; sa[i]; i++)
{
    multi(sb, a);
    add(sb, sa[i] - '0');
}
rev(sb);
itrans(sb);
// sb eh a na base b
cout << b << " " << sb << '\n';
puts("");
}
return 0;</pre>
```

5.5 Counting Number Of Times That A Digit Appears Until N

```
1l digits(int n, int d)
{
    ll res = 0, pot = 1, rem = 0;
    while (n)
    {
        int x = n%10;
        n /= 10;
        if (x > d) res += (n+1)*pot;
        else res += n*pot;
        if (x == d) res += rem+1;
        if (d == 0) res -= pot;
        rem += pot * x;
        pot *= 10;
    }
    return res;
}
```

5.6 Fast Fourier Transform

```
#include <bits/stdc++.h>
using namespace std;

typedef complex<double> ftype;
const double pi = acos(-1);
const int maxn = 1 << 22;
ftype w[maxn];

void init()
{
   for(int i = 0; i < maxn; i++)
        w[i] = polar(1., 2 * pi / maxn * i);
}

template<typename T>
```

```
void fft(T *in, ftype *out, int n, int k = 1)
    if(n == 1)
        *out = *in;
        return;
    int t = maxn / n;
    n >>= 1;
    fft(in, out, n, 2 * k);
    fft(in + k, out + n, n, 2 * k);
    for (int i = 0, j = 0; i < n; i++, j += t)
        ftype t = w[j] * out[i + n];
        out[i + n] = out[i] - t;
        out[i] += t;
vector<ftype> evaluate(vector<int> p)
    while (__builtin_popcount (p.size()) != 1)
        p.push_back(0);
    vector<ftype> res(p.size());
    fft(p.data(), res.data(), p.size());
    return res;
vector<int> interpolate(vector<ftype> p)
    int n = p.size();
    vector<ftype> inv(n);
    fft(p.data(), inv.data(), n);
    vector<int> res(n);
    for(int i = 0; i < n; i++)</pre>
        res[i] = round(real(inv[i]) / n);
    reverse(begin(res) + 1, end(res));
    return res;
void align(vector<int> &a, vector<int> &b)
    int n = a.size() + b.size() - 1;
    while(a.size() < n)</pre>
        a.push_back(0);
    while(b.size() < n)</pre>
        b.push_back(0);
vector<int> poly_multiply(vector<int> a, vector<int> b)
    align(a, b);
    auto A = evaluate(a);
    auto B = evaluate(b);
    for(int i = 0; i < A.size(); i++)</pre>
        A[i] \star = B[i];
    return interpolate (A);
const int base = 10;
vector<int> normalize(vector<int> c)
```

```
cin >> t;
    int carry = 0;
                                                                                  while (t--)
    for (auto &it: c)
                                                                                  string s1, s2;
                                                                                  cin >> s1 >> s2;// le os dois numeros como strings
        it += carry;
        carry = it / base;
                                                                                  if(s1 == "0" or s2 == "0")
        it %= base;
                                                                                    puts("0");
    while(carry)
                                                                                    continue;
        c.push_back(carry % base);
                                                                                  vector < int > A = faz(s1), B = faz(s2);
        carry /= base;
                                                                                  A = normalize(A);
                                                                                  B = normalize(B);
                                                                                  reverse(A.begin(), A.end());
    return c;
                                                                                  reverse(B.begin(), B.end());
vector<int> multiply(vector<int> a, vector<int> b)
                                                                                  auto C = multiply(A, B);
    return normalize(poly_multiply(a, b));
                                                                                  while(C.back() == 0)
                                                                                        C.pop_back();
                                                                                  reverse(C.begin(), C.end());
vector<int> faz(string s)
                                                                                  for(int &c: C)
                                                                                    cout << c;
  vector<int> ans;
                                                                                  puts("");
  for (char &c : s)
   ans.push_back(c-'0');
 return ans;
                                                                                  init();
                                                                                    vector<int> a = \{3, 4\}, b = \{2, 3\};
string multAB(string s1, string s2)
                                                                                  auto C = poly_multiply(a, b);
                                                                                  int k = int(a.size() + b.size()) - 1;
  if(s1 == "0" or s2 == "0")
                                                                                  for (int i = 0; i < k; i++)
                                                                                      cout << C[i] << "X^" << k-i-1 << (i < k-1 ? " + " : "\n");
    return "0";
  bool sinall;
  if(s1[0] == '-' and s2[0] == '-' or s1[0] != '-' and s2[0] != '-')
    sinall = true;
                                                                                  return 0;
  else
    sinall = false;
  if(s1[0] == '-') s1[0] = '0';
  if(s2[0] == '-') s2[0] = '0';
  vector < int > A = faz(s1), B = faz(s2);
 A = normalize(A);
  B = normalize(B);
  reverse(A.begin(), A.end());
                                                                              #include <bits/stdc++.h>
  reverse(B.begin(), B.end());
  auto C = multiply(A, B);
  while(C.back() == 0)
                                                                              using namespace std;
      C.pop_back();
  reverse(C.begin(), C.end());
                                                                              typedef long double ld;
                                                                              const double PI = acos(-1);
  string ans;
  ans += (!sinall ? "-" : "");
  for(int &c: C)
                                                                              struct T
    ans += char(c + '0');
  return ans;
                                                                                ld x, y;
                                                                                T() : x(0), y(0) {}
                                                                                T(1d a, 1d b=0) : x(a), y(b) {}
int main()
                                                                                T operator/=(ld k) { x/=k; y/=k; return (*this); }
  int t;
                                                                                T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
    init();
                                                                                T operator+(T a) const { return T(x+a.x, y+a.y); }
                                                                                T operator-(T a) const { return T(x-a.x, y-a.y); }
```

```
a[1 << 23], b[1 << 23];
void fft(T* a, int n, int s)
  for (int i=0, j=0; i<n; i++)</pre>
    if (i>j) swap(a[i], a[j]);
    for (int l=n/2; (j^=1) < 1; l>>=1);
  for(int i = 1; (1<<i) <= n; i++)</pre>
    int M = 1 << i;</pre>
    int K = M >> 1;
    T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
    for(int j = 0; j < n; j += M)
      T w = T(1, 0);
      for (int 1 = j; 1 < K + j; ++1)
        T t = w*a[1 + K];
        a[1 + K] = a[1]-t;
        a[l] = a[l] + t;
        w = wn * w;
void multiply(T* a, T* b, int n)
  fft(a,n,1);
  fft(b,n,1);
  for (int i = 0; i < n; i++)</pre>
   a[i] = a[i] * b[i];
  fft(a,n,-1);
  for (int i = 0; i < n; i++)</pre>
    a[i] /= n;
int main()
  int n, na, nb, c;
  cin >> na >> nb;
  n = na + nb;
  while (n&(n-1))
    n++;
  for (int i = n - na; i < n; i++)
    cin >> c;
    a[i] = T(c);
  for (int i = n - nb; i < n; i++)
    cin >> c;
    b[i] = T(c);
  multiply(a, b, n);
  for (int i = 0; i < n - 1; i++)
    cout << int(a[i].x + 0.5) << "X^"
     << n - 2 - i << (i < n - 2 ? " + " : "");
  puts("");
```

```
/*
   3 2
   1 0 0
   2.3
   0X^6 + 0X^5 + 0X^4 + 2X^3 + 3X^2 + 0X^1 + 0X^0
  return 0;
//contar quantos subarrays de soma diferentes existem usando FFT
#include <bits/stdc++.h>
using namespace std;
typedef long double ld;
const long double PI = acos(-1);
struct T
 ld x, y;
  T() : x(0), y(0) \{ \}
  T(1d a, 1d b=0) : x(a), y(b) {}
 T operator/=(ld k) { x/=k; y/=k; return (*this); }
  T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
 T operator+(T a) const { return T(x+a.x, y+a.y); }
  T operator-(T a) const { return T(x-a.x, y-a.y); }
} a[16777219], b[16777219];
int pd[16777219];
void fft(T* a, int n, int s)
  for(int i=0, j=0; i<n; i++)
    if (i>j) swap(a[i], a[j]);
    for (int l=n/2; (j^=1) < 1; l>>=1);
  for(int i = 1; (1<<i) <= n; i++)</pre>
    int M = 1 << i;</pre>
    int K = M >> 1;
    T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
    for (int j = 0; j < n; j += M)
      T w = T(1, 0);
      for(int 1 = j; 1 < K + j; ++1)</pre>
        T t = w*a[l + K];
        a[1 + K] = a[1]-t;
        a[1] = a[1] + t;
        w = wn *w;
```

```
void multiply(T* a, T* b, int n)
  fft(a,n,1);
  fft(b,n,1);
  for (int i = 0; i < n; i++)
   a[i] = a[i] * b[i];
  fft(a,n,-1);
  for (int i = 0; i < n; i++)
    a[i] /= n;
int main()
  int k;
  cin >> k:
  for(int i = 1; i <= k; i++)</pre>
   int aux;
   cin >> aux;
    pd[i] = pd[i - 1] + aux;
  if(k >= 10000)
    for(int i = 0; i <= k; i++)</pre>
      a[pd[i] + pd[k]].x = 1;
      b[pd[k] - pd[i]].x = 1;
    int n = pd[k] + pd[k];
    n = 2 * n;
    while(n & (n - 1))
     n++;
    multiply(a, b, n);
    int ans = 0;
    for(int i = 0; i <= n; i++)</pre>
      if (int (a[i].x + 0.5) > 0 and (i - 2 * pd[k]) > 0)
        ans++;
    cout << ans << '\n';
  else
    int cnt = 0;
    unordered_set<int> ans1;
    for(int i = 1; i <= k; i++)</pre>
      for(int j = i; j <= k; j++)
        if(ans1.find(pd[j] - pd[i - 1]) == ans1.end())
          ansl.insert(pd[j] - pd[i - 1]);
          cnt++;
    cout << cnt << '\n';
  // quantidade de subarrays com soma diferente
  return 0;
```

```
#include <bits/stdc++.h>
using namespace std;
typedef long double ld;
const double PI = acos(-1);
struct T
  ld x, y;
  T() : x(0), y(0) \{ \}
  T(1d a, 1d b=0) : x(a), y(b) {}
  T operator/=(ld k) { x/=k; y/=k; return (*this); }
  T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
  T operator+(T a) const { return T(x+a.x, y+a.y);
  T operator-(T a) const { return T(x-a.x, y-a.y); }
a[1 << 20], b[1 << 20];
void fft(T* a, int n, int s)
  for (int i=0, j=0; i<n; i++)</pre>
    if (i>j) swap(a[i], a[j]);
    for (int l=n/2; (j^=1) < 1; l>=1);
  for(int i = 1; (1<<i) <= n; i++)</pre>
    int M = 1 << i;</pre>
    int K = M >> 1;
    T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
    for (int j = 0; j < n; j += M)
      T w = T(1, 0);
      for (int 1 = j; 1 < K + j; ++1)
        T t = w * a[1 + K];
        a[1 + K] = a[1]-t;
        a[1] = a[1] + t;
        w = wn *w;
    }
void multiply (T* a, T* b, int n)
  fft(a,n,1);
  fft(b,n,1);
  for (int i = 0; i < n; i++)</pre>
   a[i] = a[i] * b[i];
  fft(a,n,-1);
  for (int i = 0; i < n; i++)</pre>
    a[i] /= n;
```

```
int carry = 0;
    for(auto &it: c)
        it += carry;
        carry = it / base;
        it %= base;
    while(carry)
        c.push_back(carry % base);
        carry /= base;
    return c;
vector<int> faz(string s)
  vector<int> ans:
  for (char &c : s)
    ans.push_back(c-'0');
  return ans;
string mul(string s1, string s2)
  vector<int> A = normalize(faz(s1));
  vector<int> B = normalize(faz(s2));
  int na = A.size(), nb = B.size();
  int n = na + nb;
  while (n&(n-1))
   n++;
  reverse(A.begin(), A.end());
  reverse(B.begin(), B.end());
  while(A.size() < n) A.push_back(0);</pre>
  while(B.size() < n) B.push_back(0);</pre>
  reverse(A.begin(), A.end());
  reverse(B.begin(), B.end());
  for(int i = 0; i < n; i++)</pre>
    a[i] = T(A[i]);
  for(int i = 0; i < n; i++)</pre>
   b[i] = T(B[i]);
  multiply(a, b, n);
  vector<int> r;
  for (int i = 0; i < n - 1; i++)
    r.push_back(a[i].x + 0.5);
  reverse(r.begin(), r.end());
  r = normalize(r);
  while(r.back() == 0)
          r.pop_back();
```

```
reverse(r.begin(), r.end());
string ans;
for(int &c: r)
   ans.push_back(c + '0');
return ans;
}
int main()
{
   return 0;
}
```

5.7 Gaussian Elimination For Max Subset Xor

```
#include <bits/stdc++.h>
using namespace std;
#define ull unsigned long long
int MSB(ull n)
    int cnt = 0;
    while(n)
        cnt++;
        n >>= 1;
    return cnt;
int main()
    int n;
    cin >> n;
    ull a[n];
    for(int i = 0; i < n; i++)</pre>
        cin >> a[i];
    int lengths[n];
    for(int i = 0; i < n; i++)
        lengths[i] = MSB(a[i]);
    //eh um array que armazena os coeficientes
    //das equacoes
    vector<ull> buckets[65];
    //para a Gaussian Elimination, semelhante
    //a linha da matriz em algebra linear
    for(int i = 0; i < n; i++)</pre>
        buckets[lengths[i]].push_back(a[i]);
    ull modified_array[100], m_index = 0;
    // Gaussian Elimination
    for (int i = 64; i > 0; i--)
        if(buckets[i].size())
            modified_array[m_index++] = buckets[i][0];
```

```
for(int j = 1; j < buckets[i].size(); j++)
{
      ull temp = buckets[i][0] ^ buckets[i][j];
      int len = MSB(temp);
      buckets[len].push_back(temp);
    }

ull ans = 0;
for(int i = 0; i < m_index; i++)
    if(ans < (ans ^ modified_array[i]))
      ans = (ans ^ modified_array[i]);
cout << ans << '\n';

return 0;
}</pre>
```

5.8 Karatsuba

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<long long> vll;
vll karatsubaMultiply(const vll &a, const vll &b) {
  int n = a.size();
  vll res(n + n):
  if (n <= 32) {
      for (int i = 0; i < n; i++)</pre>
      for (int j = 0; j < n; j++)
          res[i + j] += a[i] * b[j];
      return res;
  int k = n \gg 1:
  vll a1(a.begin(), a.begin() + k);
  vll a2(a.begin() + k, a.end());
  vll b1(b.begin(), b.begin() + k);
  vll b2(b.begin() + k, b.end());
  vll a1b1 = karatsubaMultiply(a1, b1);
  vll a2b2 = karatsubaMultiply(a2, b2);
  for (int i = 0; i < k; i++)
      a2[i] += a1[i];
  for (int i = 0; i < k; i++)
      b2[i] += b1[i];
  vll r = karatsubaMultiply(a2, b2);
  for(int i = 0; i < (int) alb1.size(); i++)</pre>
      r[i] -= a1b1[i];
  for(int i = 0; i < (int) a2b2.size(); i++)</pre>
      r[i] -= a2b2[i];
  for(int i = 0; i < (int) r.size(); i++)</pre>
      res[i + k] += r[i];
  for(int i = 0; i < (int) alb1.size(); i++)</pre>
      res[i] += alb1[i];
  for(int i = 0; i < (int) a2b2.size(); i++)</pre>
      res[i + n] += a2b2[i];
```

```
return res;
}
int main()
{
  v11 a = {8, 7, 5};
  v11 b = {12};

  v11 c = karatsubaMultiply(a, b);

  for(auto it : c) cout << it << ' '; puts("");
  return 0;
}</pre>
```

5.9 Matrix Exponentiation

```
#include <bits/stdc++.h>
using namespace std;
#define matrix vector<vector<int>>
matrix init(int n, int m, int value = 0)
    return vector<vector<int>>>(n, vector<int>(m, value));
void printtt(const matrix &M)
    for(int i = 0; i < M.size(); i++)</pre>
        for(int j = 0; j < M[0].size(); j++)</pre>
            cout << M[i][j] << ' ';
        puts("");
matrix multiply (const matrix &A, const matrix &B)
    matrix C = init(A.size(), B[0].size());
    for(int i = 0; i < A.size(); i++)</pre>
        for(int j = 0; j < B[i].size(); j++)</pre>
             for(int k = 0; k < B.size(); k++)</pre>
                 C[i][j] += A[i][k] * B[k][j];
    return C;
matrix exp(matrix M, int k)
    matrix I = init(M.size(), M[0].size());
    for(int i = 0; i < M.size(); i++) I[i][i] = 1;</pre>
        if (k \& 1) I = multiply(I, M), k--;
        else M = multiply(M, M), k \neq 2;
    return I;
int determinantOfMatrix(matrix mat)
  int n = mat.size();
```

```
int num1, num2, det = 1, index, total = 1;
    int temp[n + 1];
    for(int i = 0; i < n; i++)</pre>
        index = i;
        while (mat[index][i] == 0 and index < n)</pre>
            index++;
        if(index == n)
            continue;
    if(index != i)
            for (int j = 0; j < n; j++)
                swap(mat[index][j], mat[i][j]);
            det = det*pow(-1, index-i);
    for (int j = 0; j < n; j++)
      temp[j] = mat[i][j];
    for (int j = i+1; j < n; j++)
      num1 = temp[i];
      num2 = mat[j][i];
      for (int k = 0; k < n; k++)
       mat[j][k] = (num1 * mat[j][k]) - (num2 * temp[k]);
      total = total * num1;
    for (int i = 0; i < n; i++)
        det = det * mat[i][i];
    return (det/total);
int32_t main()
    int n, m;
    cin >> n >> m;
    matrix A = init(n, m);
    for(int i = 0; i < n; i++)</pre>
        for (int j = 0; j < m; j++)
            cin >> A[i][j];
    matrix C = \exp(A, 7);
    printtt(C);
    return 0;
```

5.10 Miller Rabin

```
#include <bits/stdc++.h>
using namespace std;
#define ll long long

ll add(ll a, ll b, ll c)
{
    ll ans = (a + b) % c;
        if(ans < 0) ans += c;
        return ans;
}</pre>
```

```
ll mulmod(ll a, ll b, ll c)
  11 \text{ ans} = 0;
  while (b)
    if(b \& 1) ans = add(ans, a, c);
    a = add(a, a, c);
    b /= 2;
  return ans;
ll fexp(ll a, ll b, ll c)
  ll ans = 1;
  while (b)
    if(b \& 1) ans = mulmod(ans, a, c);
   a = mulmod(a, a, c):
    b /= 2;
  return ans;
bool miller(ll a, ll n)
    if (a >= n) return true;
    11 s = 0, d = n - 1;
    while (d%2 == 0 \text{ and } d) d >>= 1, s++;
    ll x = fexp(a, d, n);
    if(x == 1 or x == n - 1) return true;
    for (int r = 0; r < s; r++, x = mulmod(x, x, n))
        if (x == 1) return false;
        if (x == n-1) return true;
    return false:
bool isprime(ll n)
    int base[] = {2, 3, 5, 7, 11,
       13, 17, 19, 23, 29, 31, 37};
    for(int i = 0; i < 12; i++)</pre>
        if(!miller(base[i], n))
            return false;
    return true;
int32_t main()
    11 n;
    cin >> n;
    cout << (isprime(n) ? "PRIME\n"</pre>
      : "NOT PRIME\n");
    return 0;
```

5.11 Mobius

```
-mi(n) = 0 se n tem como divisor um outro numero
natural ao quadrado
-mi(n) = 1 se n nao tem como divisor um outro
numero natural ao quadrado
e eh decomposto em uma quantidade par de
numeros primos
-mi(n) = -1 se n nao tem como divisor um outro
numero natural ao quadrado
e eh decomposto em uma quantidade impar de
numeros primos
*/
#include "bits/stdc++.h"
using namespace std;
const int MAX = 1e6;
bool np[MAX];
int mob[MAX];
void mobius()
  for(int i = 1; i < MAX; i++)</pre>
    mob[i] = 1;
  for(int i = 2; i < MAX; i++)</pre>
    if(np[i]) continue;
    for(int j = i; j < MAX; j += i)</pre>
      np[j] = true;
      mob[j] \star = -1;
      if((j / i) % i == 0)
        mob[j] = 0;
int main()
 mobius();
    for(int i = 2; i <= 10; i++)
      cout << i << ' ' << mob[i] << '\n';
  puts("");
  return 0;
```

5.12 Mod Gaussian Elimination

```
#include<bits/stdc++.h>
using namespace std;
//#define int long long
#define pb push_back
#define inf 0x3f3f3f3f
```

```
int MOD = 1000000007LL;
inline int prod(int a, int b)
  return ((((a % MOD) * 1LL * (b % MOD)) % MOD) + MOD) % MOD;
inline int sub(int a, int b)
  return ((((a % MOD) - (b % MOD)) % MOD) + MOD) % MOD;
inline int expMod(int x, int e)
  int ans = 1;
  while (e > 0)
   if(e & 1LL) ans = prod(ans, x), e--;
    else x = prod(x, x), e \neq 2;
  return ans;
inline int inv(int x)
  return expMod(x, MOD - 2);
inline int gauss (vector<vector<int>> a, int mod)
 MOD = mod;
    int n = (int) a.size();
    int m = (int) a[0].size();
    vector<int> where (m, -1);
    for (int col = 0, row = 0; col < m and row < n; ++col)
        int sel = row;
        for(int i = row; i < n; ++i)
            if(abs(a[i][col]) > abs(a[sel][col]))
                sel = i:
        if(a[sel][col] == 0)
            continue;
        for(int i = col; i < m; ++i)</pre>
            swap(a[sel][i], a[row][i]);
        where [col] = row;
        for(int i = row + 1; i < n; ++i)</pre>
            int c = prod(a[i][col], inv(a[row][col]));
            for (int j = col; j < m; ++j)
            a[i][j] = sub(a[i][j], prod(a[row][j], c));
        ++row;
  int ans = 0;
    for(int i = 0; i < m; ++i)
        if(where[i] !=-1)
            ans++;
    return n - ans;
```

```
int32 t main()
 int n, m, a, k, t, caso = 1;
 cin >> t;
 while (t--)
   scanf(" %d %d %d", &n, &m, &k);
   vector<vector<int>> A(n, vector<int>(n));
   while (m--)
      int u, v;
      scanf(" %d %d", &u, &v), u--; v--;
      A[u][v] = A[v][u] = 1;
     if (u != v) A[u][v] = A[v][u] = k - 1;
    for(int i = 0; i < n; i++) A[i][i] = 1;</pre>
   int ans = gauss(A, k);
   MOD = 1000000007LL;
   printf("Case %d: %d\n", caso++, expMod(k, ans));
 return 0;
```

5.13 Modular Arithmetic

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
const int MOD = 1000000007LL;
int normalize(int x)
 x = x % MOD;
 if(x < 0) x += MOD;
 return x;
int add(int a, int b)
  return normalize(normalize(a) + normalize(b));
int prod(int a, int b)
 return normalize(normalize(a) * normalize(b));
int sub(int a, int b)
 return normalize(normalize(a) - normalize(b));
int expMod(int x, int e)
  int ans = 1;
  while (e > 0)
```

```
if(e & 1LL) ans = prod(ans, x), e--;
    else x = prod(x, x), e \neq 2;
  return normalize(ans);
int inv(int x)
  return expMod(x, MOD - 2);
int extended_euclidean(int a, int b, int& x, int& y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    int x1, y1;
    int d = extended_euclidean(b, a % b, x1, y1);
    x = y1;
   y = x1 - y1 * (a / b);
    return d;
int inv(int a, int m) {
  int x, y;
  int g = extended_euclidean(a, m, x, y);
  if (q != 1) return -1; // nao tem inverso
  return ((x % m) + m) % m;
```

5.14 Mulmod Trick

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;

ll mulmod(ll a, ll b, ll m)
{
    ll q = ll((long double)a*b/m);
    ll r = a * b - m * q;
    while(r < 0) r += m;
    while(r >= m) r -= m;
    return r;
}

int main()
{
    ll a, b, c;
    cout << mulmod(a, b, c) << '\n';
    return 0;
}</pre>
```

5.15 Pollard Rho

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long
ll llrand()
 11 \text{ tmp} = \text{rand();}
  return (tmp << 31) | rand();
ll add(ll a, ll b, ll c)
  ll ans = (a + b) % c;
    if(ans < 0) ans += c;
    return ans;
ll mulmod(ll a, ll b, ll c)
  11 \text{ ans} = 0;
  while (b)
    if(b & 1) ans = add(ans, a, c);
    a = add(a, a, c);
    b /= 2;
  return ans;
ll rho(ll n)
    if(n % 2 == 0) return 2;
    11 d = n;
    while(d == n)
        ll c = llrand() % n, x = llrand() % n, y = x;
        do
            x = add(mulmod(x, x, n), c, n);
            y = add(mulmod(y, y, n), c, n);
            y = add(mulmod(y, y, n), c, n);
            d = \underline{gcd(abs(x - y), n)};
        }while(d == 1);
    return d;
// Miller-Rabin AOUI
vector<ll> fac;
void factors(ll n) // encontrar os fatores primos de N
{// Usar Miller-Rabin para testar se N eh primo
    if(n == 1) return;
    if(isprime(n)) { fac.push_back(n); return; }
    11 d = rho(n);
    factors(d);
    factors(n / d);
int32_t main()
```

```
srand(time(NULL));
ll n;
cin >> n;
cout << rho(n) << '\n';
return 0;
}</pre>
```

6 Geometry

6.1 Andrew Algorithm Convex Hull

```
#include <bits/stdc++.h>
using namespace std;
#define X first
#define Y second
typedef pair<int, int> ii;
int cross(ii O, ii A, ii B)
    return (((A.X - O.X) * (B.Y - O.Y)) - ((A.Y - O.Y) * (B.X - O.X)))
vector<ii> ConvexHull(vector<ii> P)
  if(P.size() <= 1) return P;</pre>
    vector<ii> H(2*P.size());
    int k = 0;
    sort(P.begin(), P.end());
    //lower hull
    for(int i = 0; i < P.size(); i++)</pre>
        while (k \ge 2 \text{ and } cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    //upper hull
    for(int i = P.size()-2, l = k + 1; i >= 0; i--)
        while (k \ge 1 \text{ and } cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    H.resize(k-1):
    return H;
int main()
    int n, x, y;
    vector<ii>> P:
    cin >> n:
    while (n--)
        cin >> x >> v;
        P.push_back(\{x, y\});
```

```
vector<ii> H = ConvexHull(P);

for(int i = 0; i < H.size(); i++)
        cout << H[i].X << ' ' << H[i].Y << '\n';

return 0;
}</pre>
```

#include <bits/stdc++.h>

6.2 Build Two Lines That Go Through All Points Of A Set

```
using namespace std;
const int MAX = 1e6 + 10;
typedef long long 11;
struct Point
    11 x, y;
    Point(ll _x, ll _y) : x(_x), y(_y) {}
    Point() {}
    Point operator-(const Point& p)
        return Point (x - p.x, y - p.y);
    11 operator* (const Point& p)
        return (x * p.y) - (y * p.x);
} ;
int n:
int visit[MAX];
Point point [MAX];
bool inLine(int a, int b, int c)
    return ((point[a] - point[c]) * (point[b] - point[c])) == 0LL;
bool check(int a, int b) // traca a reta AB e verifica se todos os
//pontos que nao estao em AB estao contidos em uma mesma reta
    memset(visit, 0, sizeof(visit));
    visit[a] = visit[b] = 1;
    for(int i = 0; i < n; i++)</pre>
        if(!visit[i] and inLine(a, b, i))
            visit[i] = 1;// marco todos os pontos que estao na reta AB
    vector<int> c:
    for(int i = 0; i < n and c.size() < 2; i++)</pre>
        if(!visit[i])
            c.push_back(i);// procuro dois pontos que nao estao na
                reta AB
    if(c.size() < 2) return true;</pre>
    visit[c[0]] = visit[c[1]] = 1;
    for(int i = 0; i < n; i++)</pre>
        if(!visit[i])
        { // checo se o ponto que nao esta na reta AB esta na reta
            COC1
```

```
if(inLine(c[0], c[1], i))
                  visit[i] = 1;
             else
                  return false;
    return true;
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
         cin >> point[i].x >> point[i].y;
    if(n <= 2) return cout << "YES\n", 0;</pre>
    int k = 2:
    while (k < n \text{ and } inLine(0, 1, k)) k++;
    if(k == n) return cout << "YES\n", 0;</pre>
    cout << ((check(0, 1) or check(0, k)</pre>
      or check(1, k)) ? "YES\n" : "NO\n");
    return 0;
```

6.3 Check If A Point Is Inside A Convex Polygon

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
#define ii pair<int, int>
#define fi first
#define se second
int n:
vector<ii>> P:
ii operator-(ii a, ii b)
    return {a.fi - b.fi, a.se - b.se};
int operator*(ii a, ii b)
    return a.fi * b.se - a.se * b.fi;
void setFirstPoint()
    int pos = 0;
    for(int i = 0; i < n; i++)</pre>
        if(P[i].fi < P[pos].fi or P[i].fi == P[pos].fi and P[i].se < P</pre>
            [pos].se)
            pos = i;
    rotate(P.begin(), P.begin() + pos, P.end());
bool pointInTriangle(ii a, ii b, ii c, ii p)
    int s1 = abs((a - c) * (b - c));
    int s2 = abs((a - p) * (b - p)) + abs((b - p) * (c - p)) +
       abs((c - p) * (a - p));
```

```
return s1 == s2;//mesma area
int dist(ii a, ii b)
    return (a.fi - b.fi) * (a.fi - b.fi) + (a.se - b.se) * (a.se - b.
        se);
// O(logN) per query
bool pointInConvexPolygon(ii p)
    //adicionar = desconsidera pontos na borda
    if((P[1] - P[0]) * (p - P[0]) < 0)
        return false;
    //adicionar = desconsidera pontos na borda
    if((p - P[0]) * (P[n - 1] - P[0]) < 0)
        return false;
    //o ponto esta em cima do segento P[0], P[n-1]
    if((p - P[0]) * (P[n - 1] - P[0]) == 0)
        return dist(P[0], p) <= dist(P[0], P[n-1]) and dist(P[n-1])
            1], p) \leq dist(P[0], P[n - 1]);
    //o ponto esta em cima do segento P[0], P[1]
    if((P[1] - P[0]) * (p - P[0]) == 0)
        return dist(P[0], p) <= dist(P[0], P[1]) and dist(P[1], p) <=
             dist(P[0], P[1]);
    // se o ponto esta entre os segmentos P[0], P[n]
    int 1 = 0, e = n - 1, ans = 0;
    while(1 <= e)
        int m = 1 + (e - 1) / 2;
        if((P[m] - P[0]) * (p - P[0]) >= 0) 1 = m + 1, ans = m;
        else e = m - 1;
    return pointInTriangle(P[ans], P[ans + 1], P[0], p);
int32_t main()
    int q, x, y;
    cin >> n >> q;
    for(int i = 0; i < n; i++)</pre>
    {//poligono no sentido anti-horario
        cin >> x >> y;
        P.push_back(\{x, y\});
    setFirstPoint();
    while (q--)
        cin >> x >> y;
        cout << (pointInConvexPolygon({x, y}) ? "Dentro" : "Fora") <<</pre>
            '\n';
    return 0;
```

6.4 Convex Hull Trick

```
using namespace std;
#define type int
const int MAX = 1e5;
const int 00 = 0x3f3f3f3f3f;
struct line
  type m, b;
  line(type _m, type _b) { m = _m, b = _b; }
int pointer;//Keeps track of the best line from previous query
vector<line> hull;//store hull
//Returns true if line 13 is always better than line 12
bool bad(int 11, int 12, int 13)
    intersection(11,12) has x-coordinate (b1-b2)/(m2-m1)
  intersection (11,13) has x-coordinate (b1-b3)/(m3-m1)
  set the former greater than the latter, and cross-multiply to
    eliminate division
    */
  line L1 = hull[11], L2 = hull[12], L3 = hull[13];
  return (L3.b-L1.b) * (L1.m-L2.m) < (L2.b-L1.b) * (L1.m-L3.m);
//Adds a new line
void add(type m, type b)
    if(hull.size() > 0 and hull.back().m == m) return;
    //First, let's add it to the end
    hull.emplace_back(m, b);
    //If the penultimate is now made irrelevant between the
        antepenultimate
    //and the ultimate, remove it. Repeat as many times as necessary
    while(hull.size()>=3 and bad(hull.size()-3,hull.size()-2,hull.size
        ()-1))
        hull.erase(hull.end()-2);
//Returns y value of a function i
type eval(int i, type x)
  return hull[i].m * x + hull[i].b;
//Returns the minimum y-coordinate of any intersection
//between a given vertical line and the lower envelope
//O(N) for all queries (queries are in ascending order of x)
type query(type x)
{
    if(pointer >= hull.size())
        pointer = hull.size() - 1;
    while(pointer < hull.size()-1 and eval(pointer+1, x) < eval(</pre>
        pointer, x))
    pointer++;
    return eval (pointer, x);
```

```
//between a given vertical line and the lower envelope
//O(LogN) time (queries are in any order of x)
type binarySearch(type x)
 int b = 0, e = hull.size() - 1;
 while(b < e)</pre>
   int mid = (b + e) / 2;
   if(eval(mid+1, x) < eval(mid, x)) b = mid + 1;
   else e = mid;
 return eval(b, x);
   Maximum Y coordenate query, we have two options:
   1) Maximum Y-coordenate query: multiply m and b by -1 and
   make minimum Y-corrdenate query...
   2) Order lines by increasing m if m is not equal, otherwise by
        decreasing b
       in the function query and binary Search change < to >
            eval(pointer+1, x) < eval(pointer, x)
            eval(pointer+1, x) > eval(pointer, x)
int main()
 int n;
   cin >> n;
    //Order lines by decreasing m if m is not equal, otherwise by
        increasing b
    for(int i = 0; i < n; i++)</pre>
        int m, b;
        cin >> m >> b:
        add(m, b);
   int a:
   cin >> q;
   vector<int> queries(q);//queries are in ascending order of x - run
   for(int &w : queries)
   cin >> w;
  //processing queries in ascending order of x
  for(int &w : queries)
   cout << query(w) << '\n';
 while (cin >> x) //queries are in any order of x - run in O(log N)
   cout << binarySearch(x) << '\n';</pre>
   return 0;
```

6.5 Distance Between Nearest Pair Of Points

```
#include <bits/stdc++.h>
using namespace std;
```

```
const int MAX = 1e4;
const double EPS = 1e7;
typedef pair<double, double> ii;
vector<ii> v;
set<ii>> sv, sx;
int n;
int main()
    double x, y;
    cin >> n:
    for(int i = 0; i < n; i++)</pre>
        cin >> x >> y;
        v.push_back({x, y});
    sort(v.begin(), v.end());
    double d = 0x3f3f3f3f3f;
    for(int i = 0; i < n; i++)</pre>
        x = v[i].first, y = v[i].second;
        while(!sx.empty())
            ii p = *(sx.begin());
            if(p.first + d < x)
                sy.erase({p.second, p.first});
                sx.erase(p);
            else
                break;
        auto it = sy.lower_bound({int(floor(y-d))-1, 0});
        while(it != sy.end() and it->first < y + d + 1)</pre>
            d = min(d, hypot(x - it->second, y - it->first));
            it++;
        sy.insert({y, x});
        sx.insert({x, y});
    cout << d << '\n';
    return 0;
```

6.6 Dynamic Convex Hull Trick

```
#include <bits/stdc++.h>
using namespace std;
#define type __int128
#define int __int128
#define gc getchar
#define pc putchar
#define Min(a, b) (a > b ? b : a)
inline void scanint(int &k)
{
   bool sinal = true;
```

```
register char c;
    k = 0:
    for(c = gc(); sinal and (c < '0' or c > '9'); c = qc())
      if(c == '-')
        sinal = false;
    for (; c >= '0') and c <= '9'; c = qc()
       k = (k \ll 3) + (k \ll 1) + c - '0';
  if(!sinal) k = -k;
inline void printint(int n)
  if (n < 0) pc ('-');
 n = abs(n);
  int rev = n, cnt = 0;
  if(!n)
    pc('0');
   pc('\n');
    return;
  while(!(rev % 10))
    cnt++, rev /= 10;
  rev = 0;
  while (n)
    rev = (rev << 3) + (rev << 1) + n % 10, n /= 10;
  while (rev)
    pc(rev % 10 + '0'), rev /= 10;
  while (cnt--)
    pc('0');
 pc('\n');
struct line
 type m, b;
  line(type _m, type _b) { m = _m, b = _b; }
    line() { m = 0, b = 0; }
};
bool bad(int 11, int 12, int 13, vector<line> &hull)
  line L1 = hull[11], L2 = hull[12], L3 = hull[13];
  return (L3.b-L1.b) * (L1.m-L2.m) < (L2.b-L1.b) * (L1.m-L3.m);
void add(type m, type b, vector<line> &hull)
    if(hull.size() > 0 and hull.back().m == m) return;
    hull.emplace_back(m, b);
    while(hull.size()>=3 and bad(hull.size()-3,hull.size()-2,hull.size
        ()-1, hull))
        hull.erase(hull.end()-2);
type eval(int i, type x, vector<line> &hull)
 return hull[i].m * x + hull[i].b;
```

```
type binarySearch(type x, vector<line> &hull)
  int b = 0, e = hull.size() - 1;
  while(b < e)</pre>
    int mid = (b + e) / 2;
    if(eval(mid+1, x, hull) < eval(mid, x, hull)) b = mid + 1;
    else e = mid;
  return eval(b, x, hull);
//#########DAOUI PRA BAIXO EH O SUCESSO##################
vector<line> merge(vector<line> a, vector<line> b)
    if(a.size() < b.size()) swap(a, b);</pre>
    for(int i = 0; i < b.size(); i++)</pre>
        a.push back(b[i]);
    sort(a.begin(), a.end(), [](line c, line d)
     { return c.m == d.m ? c.b < d.b : c.m > d.m; });
    b.clear();
    for(int i = 0; i < a.size(); i++)</pre>
        add(a[i].m, a[i].b, b);
    return b;
vector<vector<line>> groups;
void add(line 1)
    vector<line> g = {1};
    while(!groups.empty() and groups.back().size() <= g.size())</pre>
        q = merge(q, groups.back());
        groups.pop_back();
    groups.push_back(g);
type query(int x)
    int ans = 0;
    for(int i = 0; i < groups.size(); i++)</pre>
        ans = Min(ans, binarySearch(x, groups[i]));
    return -ans;
int32 t main()
  int n, q;
  scanint(n);
  scanint (q);
    vector<line> cyc(n + 1);
    while (q--)
        int t, T;
        scanint(t);
        scanint(T);
```

```
if(t % 2 == 1)
{
    int N, C;
    scanint(C);
    scanint(N);
    int b = - N * T + cyc[C].m * T + cyc[C].b;
    //cout << N << ' ' << b << '\n';
    add(line(-N, -b));
    cyc[C] = line(N, b);
}
else
    printint(query(T));
}
return 0;</pre>
```

6.7 Enclosing Circle R2

```
#include <cstdio>
#include <cmath>
int n;
double x[1005], y[1005], X, Y, d, e;
double dist(double a, double b) {
  return a*a + b*b;
int main() {
  scanf("%d", &n);
  for (int i = 0; i < n; i++) {
    scanf("%lf%lf", &x[i], &y[i]);
    X += x[i]; Y += y[i];
  X /= n; Y /= n;
  double P = 0.1;
  for (int i = 0; i < 30000; i++) {</pre>
   int f = 0;
    d = dist(X - x[0], Y - y[0]);
    for (int j = 1; j < n; j++) {
      e = dist(X - x[j], Y - y[j]);
      if (d < e) { d = e; f = j; }
    X += (x[f] - X) *P;
   Y += (y[f] - Y) *P;
    P *= 0.999;
  printf("%.31f %.31f\n%.31f", X, Y, sqrt(d));
```

6.8 Enclosing Circle R3

```
#include <cstdio>
#include <cmath>
int n;
double x[105], y[105], z[105], X, Y, Z, d, e;
double dist(double a, double b, double c) {
   return a*a + b*b + c*c;
}
int main() {
```

```
scanf("%d", &n);
for (int i = 0; i < n; i++) {
  scanf("%lf%lf%lf", &x[i], &y[i], &z[i]);
  X += x[i];
  Y += y[i];
  Z += z[i];
X /= n; Y /= n; Z /= n;
double P = 0.1;
for (int i = 0; i < 70000; i++) {</pre>
  int f = 0;
  d = dist(X - x[0], Y - y[0], Z - z[0]);
  for (int j = 1; j < n; j++) {</pre>
    e = dist(X - x[j], Y - y[j], Z - z[j]);
    if (d < e) {
      d = e;
      f = \dot{j};
  X += (x[f] - X) *P;
  Y += (y[f] - Y) *P;
  Z += (z[f] - Z) *P;
  P *= 0.998;
printf("%.101f %.101f %.101f", X, Y, Z);
```

6.9 Geometry Stan

```
struct PT {
  double x, y;
  PT() {}
  PT(double x, double y) : x(x), y(y) {}
  PT(const PT &p) : x(p.x), y(p.y) {}
  PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
  PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
  PT operator * (double c) const { return PT(x*c, y*c); }
  PT operator / (double c) const { return PT(x/c, y/c); }
  bool operator == (PT p) const {
    return (fabs(x-p.x) < EPS && (fabs(y-p.y) < EPS)); };
  bool operator < (PT p) const {</pre>
    if(fabs(x-p.x) > EPS) return x<p.x; return y<p.y; };</pre>
};
// dot(p,q) = length(p) * length(q) * cos(angle between p and q)
double dot(PT p, PT q) { return p.x*q.x+p.v*q.v; }
double dist2(PT p, PT q) { return dot(p-q,p-q); }
double dist(PT p, PT q) { return sqrt(dist2(p,q)); }
double mdist(PT p, PT q) { return fabs(p.x-q.x)+fabs(p.y-q.y); }
double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
ostream & operator << (ostream & os, const PT & p) {return os << "("<< p.x << ",
    "<<p.y<<")";}
// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.v.p.x); }
PT RotateCW90(PT p) { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
  return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// returns angle aob in rad
double angle (PT a, PT o, PT b) {
  return acos(dot(a-o,b-o)/sqrt(dot(a-o,a-o)*dot(b-o,b-o)));
```

```
// returns true if point r is on the left side of line pq
bool ccw(PT p, PT q, PT r) {
  return cross(p,q)+cross(q,r)+cross(r,p) > 0;
// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
 return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
 double r = dot(b-a,b-a);
  if (fabs(r) < EPS) return a;</pre>
 r = dot(c-a, b-a)/r;
  if (r < 0) return a;</pre>
 if (r > 1) return b;
 return a + (b-a) *r;
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane (double x, double y, double z,
double a, double b, double c, double d) {
  return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
  return fabs(cross(b-a, c-d)) < EPS;
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
    && fabs(cross(a-b, a-c)) < EPS
    && fabs(cross(c-d, c-a)) < EPS;
// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
  if (LinesCollinear(a, b, c, d)) {
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
    if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
      return false;
    return true;
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true:
// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
 b=b-a; d=c-d; c=c-a;
  assert (dot (b, b) > EPS && dot (d, d) > EPS);
 return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
```

```
PT ComputeCircleCenter(PT a, PT b, PT c) {
  b = (a+b)/2:
  c = (a+c)/2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
  bool c = 0:
 for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1)%p.size();
    if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
     p[i]q > v.p & v.p = v.[i]q
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y)
          i].y))
        c = !c;
  return c;
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT g) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) <</pre>
      return true;
  return false:
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
 vector<PT> ret:
 b = b-a;
 a = a-c;
 double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret;
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
 vector<PT> ret;
  double d = sgrt(dist2(a, b));
 if (d > r+R || d+min(r, R) < max(r, R)) return ret;</pre>
 double x = (d*d-R*R+r*r)/(2*d);
  double y = sqrt(r*r-x*x);
 PT v = (b-a)/d;
 ret.push_back(a+v*x + RotateCCW90(v)*y);
 if (v > 0)
    ret.push_back(a+v*x - RotateCCW90(v)*y);
```

```
return ret;
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs (ComputeSignedArea(p));
// gravity center
PT ComputeCentroid(const vector<PT> &p) {
 PT c(0,0);
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
   int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  return c / scale;
// tests whether or not a given polygon (in CW or CCW order) is simple
// segments do not intersect
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++) {</pre>
    for (int k = i+1; k < p.size(); k++) {</pre>
      int j = (i+1) % p.size();
      int 1 = (k+1) % p.size();
      if (i == 1 || j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false:
  return true;
// compute two center's of circle given two points a and b
// and a radius r
pair<PT, PT> CumputeTwoCircleCenter(PT a, PT b, double R)
  if(dist(a, b) < EPS)</pre>
    return {a, b};
 PT middle = (a + b) / 2;
 PT v = RotateCCW90 (middle - a);
  v = v / sqrt(dot(v, v));
  double l = 0, r = 100, escalar;
  for (int i = 0; i < 100; i++)
    double mid = (1 + r) / 2;
    PT u = v * mid + middle:
    if(dist(a, u) \le R + EPS)
     l = mid, escalar = mid;
    else
```

```
r = mid;
}

PT c1 = v * escalar + middle;
PT c2 = v * (-escalar) + middle;
return {c1, c2};
}
```

6.10 Graham Scan

```
#include <bits/stdc++.h>
using namespace std;
#define ii pair<int, int>
#define fi first
#define se second
vector<ii>> P;
ii operator-(ii a, ii b)
    return ii(a.fi - b.fi, a.se - b.se);
ii operator+(ii a, ii b)
    return ii(a.fi + b.fi, a.se + b.se);
int operator*(ii a, ii b)
    return a.fi * b.se - a.se * b.fi;
int dist(ii a, ii b)
    return (a.fi - b.fi) * (a.fi - b.fi) + (a.se - b.se) * (a.se - b
        .se);
bool cmp(ii a, ii b)
    int cross = (a - P[0]) * (b - P[0]);
    if(!cross) return dist(P[0], a) > dist(P[0], b);
    return cross > 0;
void setFirstPoint()
    for(int i = 1; i < P.size(); i++)</pre>
        if(P[i].fi < P[0].fi or P[i].fi == P[0].fi and P[i].se < P[0].</pre>
            swap(P[0], P[i]);
vector<ii> GrahamScan()
    setFirstPoint();
    sort(P.begin() + 1, P.end(),cmp);
    vector<ii>> H(P.size() * 2);
```

```
int k = 0;
    for(int i = 0; i < P.size(); i++)</pre>
    { //crsso <= 0 para remover os pontos colineares
        while (k > 2 \text{ and } (H[k-1] - H[k-2]) * (P[i] - H[k-1]) < 0)
            k--:
        H[k++] = P[i];
    H.resize(k);
    return H;
int main()
    int n;
    cin >> n:
    for(int i = 0; i < n; i++)</pre>
        ii p;
        cin >> p.fi >> p.se;
        P.push_back(p);
    vector<ii>> H = GrahamScan();
    for(int i = 0; i < H.size(); i++)</pre>
        cout << H[i].fi << ' ' << H[i].se << '\n';
    return 0;
```

6.11 Maximum Dot Product

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
#define X first
#define Y second
const int 00 = 0x3f3f3f3f3f3f3f3f3f;
typedef pair<int, int> ii;
int cross(ii O, ii A, ii B)
    return (((A.X - O.X) * (B.Y - O.Y)) - ((A.Y - O.Y) * (B.X - O.X)))
int dot(ii a, ii b)
    return a.X * b.X + a.Y * b.Y;
vector<ii> ConvexHull(vector<ii> P)
    if(P.size() <= 1) return P;</pre>
    vector<ii>> H(2*P.size());
    int k = 0:
    sort(P.begin(), P.end());
    for(int i = 0; i < P.size(); i++)</pre>
        while (k \ge 2 \text{ and } cross(H[k-2], H[k-1], P[i]) \le 0) k--;
        H[k++] = P[i];
    for (int i = P.size()-2, l = k + 1; i >= 0; i--)
```

```
while (k \ge 1 \text{ and } cross(H[k-2], H[k-1], P[i]) \le 0) k--;
       H[k++] = P[i];
    H.resize(k-1);
    return H;
vector<ii> merge (vector<ii> H1, vector<ii> H2)
    for(auto &it : H2) H1.push_back(it);
    return ConvexHull(H1):
int maxConcavityUp(int b, int e, vector<ii> &H, ii p)
    if(b > e) return -00;
    return max(dot(H[b], p), dot(H[e], p));
int maxConcavityDown(int b, int e, vector<ii> &H, ii p)
    if(b > e) return -00;
    b--;
    while (e - b > 1)
      int m = b + (e - b) / 2;
      if(dot(H[m], p) > dot(H[m + 1], p))
      else
          b = m;
    return dot(H[e], p);
int maximumDot(vector<ii> &H, ii p)
    bool growing = dot(H[0], p) \le dot(H[1], p);
    if (growing)
      int b = 0, e = H.size() - 1, w = -1;
      while(b \le e)
          int m = (b + e) / 2;
          if(dot(H[0], p) <= dot(H[m], p))
              b = m + 1, w = m;
          else
              e = m - 1;
      return max(maxConcavityUp(w, H.size() - 1, H, p),
         maxConcavityDown(0, w, H, p));
      //cout << "caso #1\n0" << w << "concavidade para baixo\n"
             << w + 1 << ' ' << H.size() - 1 << " concavidade para
          cima\n";
    else
      int b = 0, e = H.size() - 1, w = -1;
      while(b <= e)</pre>
          int m = (b + e) / 2;
```

```
if(dot(H[0], p) >= dot(H[m], p))
              b = m + 1, w = m;
          else
              e = m - 1;
      //cout << "caso #2 \n0 " << w << " concavidade para cima \n"
             << w + 1 << ' ' << H.size() - 1 << " cocavidade para
          baixo\n";
      return max(maxConcavityUp(0, w, H, p),
        maxConcavityDown(w, H.size() - 1, H, p));
vector<vector<ii>>> st;
void add(ii p)
    vector < ii > q = \{p\};
    while(!st.empty() and st.back().size() <= g.size())</pre>
        q = merge(q, st.back());
        st.pop_back();
    st.push_back(g);
int query(ii p)
    int ans = -00;
    for(int i = 0; i < st.size(); i++)</pre>
        ans = max(ans, maximumDot(st[i], p));
    return ans;
int32_t main()
    int n, q;
    scanf(" %lld", &n);
    for(int i = 0; i < n; i++)
        int x, y;
        scanf(" %lld %lld", &x, &y);
        add(\{x, y\});
    scanf(" %lld", &q);
    while (q--)
        char s[10];
        int x, y;
        scanf(" %s %lld %lld", s, &x, &y);
        if(s[0] == 'a') add({x, y});
        else printf("%lld\n", query(\{x, y\}));
    return 0;
```

6.12 Radial Sort

```
#include <bits/stdc++.h>
```

```
using namespace std;
#define type int
#define point pair<type, type>
#define X first
#define Y second
point operator-(point a, point b)
    return {a.X - b.X, a.Y - b.Y};
type operator* (point a, point b)
    return a.X * b.Y - a.Y * b.X;
int n;
vector<point> P;
point R;
int dist(point a, point b)
    return (a.X - b.X) * (a.X - b.X) + (a.Y - b.Y) * (a.Y - b.Y);
bool cmp (point a, point b)
    if((a - R).Y * (b - R).Y <= 0) return a.Y > R.Y;
    int c = (a - R) * (b - R);
    if(c == 0) return dist(R, a) <= dist(R, b);</pre>
    return c > 0;
int main()
    cin >> n >> R.X >> R.Y;
    for(int i = 0; i < n; i++)</pre>
        type x, y;
        cin >> x >> y;
        P.push_back({x, y});
    sort(P.begin(), P.end(), cmp);
    for(point p : P) cout << p.X << ' ' << p.Y << '\n';</pre>
    return 0;
```

6.13 Segment Intersection

```
#define ll long long
#define Pll complex<ll>
#define Y imag()
#define X real()

bool intersec(Pll a, Pll b, Pll c, Pll d)
{
   if(cross(c - a, c - b) * cross(d - a, d - b) <= 0 and cross(a - c, a - d) * cross(b - c, b - d) <= 0)
   return true;</pre>
```

return false;

7 Miscellaneous

7.1 Big Num Product

```
string mul(string a, string b)
 while (a.size() > b.size()) b = "0" + b;
 while(a.size() < b.size()) a = "0" + a;</pre>
 a = "00" + a;
 b = "00" + b;
 int ans = 0, n = a.size(), carry = 0;
 vector<int> num(2 * n. 0);
  for (int i = n - 1; i >= 0; i--)
    for(int i = n - 1; i >= 0; i--)
      int di = a[i] - '0';
      int dj = b[j] - '0';
      num[i + j + 1] += (di * dj) + carry;
      carry = (num[i + j + 1] / 10);
      num[i + j + 1] %= 10;
  string r;
  for (int i = 0, fl = 0; i < 2 * n; i++)
   if(num[i]) fl = 1;
   if(fl) r.push_back(num[i] + '0');
  return r;
```

7.2 Count Divisors

```
#include <bits/stdc++.h>
using namespace std;

long long add(long long a, long long b, long long c)
{
    long long ans = (a + b) % c;
        if(ans < 0) ans += c;
        return ans;
}

long long mulmod(long long a, long long b, long long c)
{
    long long ans = 0;
    while(b)
    {
        if(b & 1) ans = add(ans, a, c);
        a = add(a, a, c);
        b /= 2;
    }
    return ans;
}

long long fexp(long long a, long long b, long long c)</pre>
```

```
long long ans = 1;
  while (b)
    if(b & 1) ans = mulmod(ans, a, c);
    a = mulmod(a, a, c);
    b /= 2;
  return ans;
bool miller (long long a, long long n)
    if (a >= n) return true;
    long long s = 0, d = n - 1;
    while (d%2 == 0 \text{ and } d) d >>= 1, s++;
    long long x = fexp(a, d, n);
    if(x == 1 or x == n - 1) return true;
    for (int r = 0; r < s; r++, x = mulmod(x, x, n))
        if (x == 1) return false;
        if (x == n-1) return true;
    return false;
bool isprime (long long n)
  if(n < 2) return false;</pre>
    int base[] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
    for(int i = 0; i < 12; i++)
        if(!miller(base[i], n))
            return false:
    return true;
vector<int> prime;
bitset<10000000> composite;
void sieve()
  for(int i = 2; i < 10000000; i++)</pre>
    if(!composite[i])
      prime.push_back(i);
      for(int j = 2; i * j < 10000000; j++)
        composite[i * j] = 1;
long long countDivisors(long long n)
  int idx = 1;
  long long ans = 1, p = prime[0];
  while (p * p * p <= n)
    int cnt = 1;
    while(n % p == 0)
     n \neq p, cnt++;
    ans *= cnt;
    p = prime[idx++];
```

```
}
if(n == 1) return ans;
if(isprime(n)) ans *= 2;
else
{
   long long sq = sqrt(n);
   if(sq * sq == n)
        ans *= 3;
   else if(n != 1)
        ans *= 4;
}
return ans;
}

int main()
{
   long long n;
   cin >> n;
   sieve();
   cout << countDivisors(n) << '\n';
   return 0;
}
</pre>
```

7.3 Count Sort

```
#include <bits/stdc++.h>
using namespace std;
int n, m;
int arr[100];
int cnt[10000];
int aux[100];
void count_sort()
    for(int i = 0; i < n; i++)</pre>
        cnt[arr[i]]++;
    for(int i = 1; i <= m; i++)</pre>
        cnt[i] += cnt[i-1];
    for(int i = 0; i < n; i++)
        aux[--cnt[arr[i]]] = arr[i];
    memcpy(arr, aux, n*sizeof(int));
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> arr[i], m = max(arr[i], m);
    count_sort();
    for(int i = 0; i < n; i++)
      cout << arr[i] << ' '; cout << '\n';
    return 0;
```

7.4 Counting Different Elements In A Path With Mo

```
//COT - Count on a tree (SPOJ)
//Em cada vertice existe um valor
//A resposta para uma query eh quantos valores
//distintos existem no caminho de u a v
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;
typedef long long 11;
struct Ouerv
    int x, y, l, r, lc, res;
};
int n, q, max_log, tempo, blk, ans;
vector<int> G[MAX];
int value[MAX], pos[MAX], anc[MAX][25], depth[MAX];
int tl[MAX], ST[MAX], EN[MAX], freq[MAX], node[MAX];
Query Q[MAX];
ll arr[MAX];
void dfs(int v, int p, int d)
    anc[v][0] = p;
    depth[v] = d:
    tl[tempo] = v;
    ST[v] = tempo++;
    if(d) max_log = max(max_log, (int)log2(d));
    for(const int &u : G[v])
        if(u != p)
            dfs(u, v, d + 1);
    tl[tempo] = v;
    EN[v] = tempo++;
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k&-k)], k -= k&-k;
    return v;
int lca(int u, int v)
    if(depth[u] > depth[v]) u = walk(u, depth[u] - depth[v]);
    if(depth[u] < depth[v]) v = walk(v, depth[v] - depth[u]);</pre>
    if(u == v) return u;
    for(int i = max_log; i >= 0; i--)
        if(anc[u][i] != anc[v][i])
            u = anc[u][i]:
            v = anc[v][i];
    return anc[u][0];
void build()
```

```
memset(anc, -1, sizeof(anc));
    dfs(0, -1, 0);
    for(int j = 1; j <= max_log; j++)</pre>
        for(int i = 0; i < n; i++)
            if (anc[i][j-1] != -1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
inline void mo(int i)
    int u = tl[i];
    if(node[u] and --freq[value[u]] == 0) ans--;
    else if(!node[u] and ++freq[value[u]] == 1) ans++;
    node[u] ^= 1;
bool compare (int a, int b)
    if(O[a].1/blk != O[b].1/blk)
        return Q[a].1 < Q[b].1;
    return Q[a].r > Q[b].r;
int main()
    scanf("%d %d", &n, &q);
    for (int i = 0; i < n; i++) //values
        scanf("%d", &arr[i]), pos[i] = i;
    sort(pos, pos + n, [](ll a, ll b){return arr[a] < arr[b];});
    for (int i = 0, j = 1; i < n; i++)
        if(!i)
            value[pos[i]] = j++;
        else if(arr[pos[i]] != arr[pos[i-1]])
            value[pos[i]] = j++;
        else value[pos[i]] = value[pos[i-1]];
    for(int i = 0; i < n-1; i++)</pre>
        int u, v;
        scanf("%d %d", &u, &v); u--; v--;
        G[u].push_back(v);
        G[v].push_back(u);
    build();
    for(int i = 0; i < q; i++)
        int u, v;
        scanf("%d %d", &u, &v); u--; v--;
        if(ST[u] > ST[v]) swap(u, v);
        Q[i].lc = lca(u, v);
        Q[i].x = u, Q[i].y = v;
        if(u == O[i].lc)
            Q[i].l = ST[u], Q[i].r = ST[v];
        else
            Q[i].l = EN[u], Q[i].r = ST[v];
        pos[i] = i;
    blk = sqrt(tempo);
```

```
sort (pos, pos + q, compare);
int curL = 0, curR = 0;
for(int i = 0; i < q; i++)</pre>
    int L = Q[pos[i]].l, R = Q[pos[i]].r;
    while(curL < L)</pre>
        mo(curL++);
    while (curL > L)
        mo(--curL);
    while (curR < R + 1)
        mo(curR++);
    while (curR > R + 1)
        mo(--curR);
    if(Q[pos[i]].x != Q[pos[i]].lc)
        mo(ST[Q[pos[i]].lc]);
    Q[pos[i]].res = ans;
    if(Q[pos[i]].x != Q[pos[i]].lc)
        mo(ST[Q[pos[i]].lc]);
for(int i = 0; i < q; i++)
    printf("%d\n", Q[i].res);
return 0;
```

7.5 Custom Hash Function Unordered Map Or Set

```
#include <bits/stdc++.h>
using namespace std;
struct custom hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    size_t operator()(uint64_t x) const {
        static const uint64 t FIXED RANDOM = chrono::steady clock::now
            ().time_since_epoch().count();
        return splitmix64(x + FIXED RANDOM);
};
//teste
const int N = 2e5:
void insert_numbers(long long x)
    clock_t begin = clock();
    unordered_map<long long, int, custom_hash> numbers;
    for (int i = 1; i <= N; i++)</pre>
        numbers[i * x] = i;
    long long sum = 0;
```

7.6 Divide Conquer Optimization

```
#include <bits/stdc++.h>
using namespace std;
#define maxn 20005
#define maxnlog 22
const long long 00 = 0x3f3f3f3f3f3f3f3f3f;
struct SparseTableDS
 int Sparse_Table[maxnlog][maxn];
 bool maxi:
 int n;
  void build()
   for(int i = 1; (1 << i) <= n; i++)
      for (int j = 0; j + (1 << i) <= n; <math>j++)
          Sparse_Table[i][j] = max(Sparse_Table[i-1][j],
            Sparse_Table[i-1][j+(1 << (i-1))]);
          Sparse_Table[i][j] = min(Sparse_Table[i-1][j],
              Sparse_Table[i-1][j+(1 << (i-1))]);
  int query(int i, int j)
   int sz = log2(j-i+1);
   if(maxi)
      return max(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
   return min(Sparse_Table[sz][i], Sparse_Table[sz][j+1-(1 << sz)]);</pre>
  void init(bool fl, vector<int> &arr)
   maxi = fl;
   if(!maxi) memset(Sparse_Table, 63, sizeof(Sparse_Table));
   n = arr.size();
   for(int i = 0; i < n; i++)</pre>
```

```
Sparse_Table[0][i] = arr[i];
    build();
};
int n, k;
SparseTableDS maxi, mini;
long long dp_before[maxn];
long long dp_cur[maxn];
int get(int 1, int r)
  int a = maxi.query(l, r);
  int b = mini.query(l, r);
  return abs(a - b);
void compute(int 1, int r, int opt1, int optr)
  if(l > r) return;
  int mid = (1 + r) >> 1;
  int best = 0;
  int opt = optl;
  for(int k = optl; k < min(mid, optr + 1); k++)</pre>
    if(best < dp_before[k] + get(k + 1, mid))</pre>
     best = dp_before[k] + get(k + 1, mid);
      opt = k;
  dp_cur[mid] = best;
    compute(l, mid - 1, optl, opt);
    compute (mid + 1, r, opt, optr);
int32_t main()
  cin >> n >> k;
 vector<int> arr(n);
  for(int &w : arr) scanf(" %d", &w);
 maxi.init(true, arr);
  mini.init(false, arr);
  for(int i = 0; i < n; i++)</pre>
    dp cur[i] = qet(0, i);
  for(int i = 2; i <= k; i++)</pre>
    for (int j = 0; j < n; j++)
      dp_before[j] = dp_cur[j];
      dp_cur[j] = 0;
    compute(i - 2, n - 1, i - 2, n - 1);
```

```
cout << dp_cur[n - 1] << endl;
return 0;
}</pre>
```

7.7 FastIO

```
#include <bits/stdc++.h>
using namespace std;
#define gc getchar_unlocked
#define pc putchar_unlocked
inline void scanint(int &k)
 bool sinal = true;
    register char c;
    k = 0;
    for (c = gc(); sinal and (c < '0' or c > '9'); c = gc())
      if(c == '-')
        sinal = false;
    for(; c \ge '0' and c \le '9'; c = gc())
        k = (k \ll 3) + (k \ll 1) + c - '0';
  if(!sinal) k = -k;
inline void printint(int n)
  if (n < 0) pc ('-');
  n = abs(n);
  int rev = n, cnt = 0;
  if(!n)
    pc('0');
    pc('\n');
    return;
  while(!(rev % 10))
    cnt++, rev /= 10;
  rev = 0;
  while (n)
    rev = (rev << 3) + (rev << 1) + n % 10, n /= 10;
  while (rev)
    pc(rev % 10 + '0'), rev /= 10;
  while (cnt--)
   pc('0');
 pc('\n');
inline void scanstr(string &k)
    register char c;
  k = "";
    for(c = qc(); c < 'a' or c > 'z'; c = qc());
    for(; c \ge 'a' and c \le 'z'; c = qc()) k.push_back(c);
inline void printstr(string &k)
  for(char &c : k) putchar(c);
```

```
putchar('\n');
}
int main()
{
  int k;
  scanint(k);
  printint(k);

  return 0;
}
```

7.8 Fence Problem With Max Flow

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
const int 00 = 0x3f3f3f3f;
int SOURCE, SINK;
struct edge
    int v, f, c;
    edge(){}
    edge(int _v, int _f, int _c)
        v = _v, f = _f, c = _c;
};
vector<edge> edges;
vector<int> G[MAX];
int dist[MAX], work[MAX];
void add_edge(int u, int v, int cp, int rc){
  edges.push_back(edge(v, 0, cp));
  G[u].push_back(edges.size()-1);
  edges.push_back(edge(u, 0, rc));
  G[v].push_back(edges.size()-1);
bool bfs(int s, int t)
    memset(dist, -1, sizeof(dist));
    dist[s] = 0;
    queue<int> q;
    q.push(s);
    while(!q.empty())
        int u = q.front();
        q.pop();
        for(int e : G[u])
            if(dist[edges[e].v] == -1 and edges[e].c-edges[e].f > 0)
                q.push (edges[e].v);
                dist[edges[e].v] = dist[u] + 1;
    return dist[t] != -1;
```

```
int dfs(int s, int t, int f)
    if(s == t) return f;
    for(int &i = work[s]; i < G[s].size(); i++)</pre>
      int e = G[s][i];
        if(dist[edges[e].v] == dist[s] + 1 and edges[e].c-edges[e].f >
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                )))
                edges[e].f += a;
                edges[e^1].f -= a;
                return a;
    return 0;
int MaxFlow(int s, int t)
    int mf = 0;
    while (bfs(s, t))
      memset (work, 0, sizeof (work));
        while(int a = dfs(s, t, 00))
            mf += a;
    return mf;
int n, m, a, b;
int dx[] = \{1, 0, -1, 0\};
int dy[] = \{0, -1, 0, 1\};
char ANS[60][60];
bool cor[MAX];
bool check(int x, int y)
  return x >= 0 and x < n and y >= 0 and y < m;
int vertexIn(int i, int j)
  return i * m + j;
int vertexOut(int i, int j)
  return i * m + j + n * m + 1;
void mountANS(int v)
  cor[v] = true;
  for(int &e : G[v])
    if(cor[edges[e].v]) continue;
    if(edges[e].c - edges[e].f > 0)
      mountANS (edges [e].v);
```

```
int main()
 memset(ANS, '.', sizeof(ANS));
 cin >> n >> m >> a >> b; a--; b--;
 SOURCE = 2 * n * m + 2;
 SINK = 2 * n * m + 3;
  for(int i = 0; i < n; i++)</pre>
    for (int j = 0; j < m; j++)
      int cost;
      cin >> cost;
      if(a == i and b == j) cost = 00;
      add_edge(vertexIn(i, j), vertexOut(i, j), cost, 0);
      if(cost == 00) add_edge(vertexOut(i, j), SINK, 00, 0);
      for(int k = 0; k < 4; k++)
       int x = i + dx[k], y = j + dy[k];
        if(check(x, y))
          add_edge(vertexOut(i, j),
            vertexIn(x, y), 00, 0);
      if(!i or !j or i == n - 1 or j == m - 1)
        add_edge(SOURCE, vertexIn(i, j), 00, 0);
  cout << MaxFlow(SOURCE, SINK) << '\n';</pre>
 mountANS (SOURCE);
 for (int i = 0; i < n * m; i++)
    for(int &e : G[i])
      if(!(e & 1) and cor[i] and !cor[edges[e].v])
        ANS[i / m][i % m] = 'X';
 for(int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
      cout << ANS[i][j];
    puts("");
    return 0;
```

7.9 Gen Random Tree

```
#include <bits/stdc++.h>
using namespace std;
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());

int rand(int a, int b) {
    return a + rng() % (b - a + 1);
}

int main() {
    int n = rand(4, 20);
    cout << n << endl;
    vector<pair<int,int>> edges;
    for(int i = 2; i <= n; i++)
        edges.emplace_back(rand(1, i - 1), i);

// re-naming vertices</pre>
```

```
vector<int> perm(n + 1); // re-naming vertices
for(int i = 1; i <= n; ++i)
    perm[i] = i;

// random order of labels
shuffle(perm.begin() + 1, perm.end(), rng);
// random order of edges
shuffle(edges.begin(), edges.end(), rng);

for(auto [u, v] : edges) {
    // random order of two vertices
        if(rng() % 2) swap(u, v);
        cout << perm[u] << ' ' << perm[v] << endl;
}
return 0;</pre>
```

7.10 Histogram

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
int n, vet[1000000];
11 histogram()
  stack<ll> s;
  11 \text{ ans} = 0, tp, cur;
  int i = 0;
  while(i < n or !s.empty())</pre>
    if(i < n and (s.empty() or vet[s.top()] <= vet[i]))</pre>
      s.push(i++);
    else
      tp = s.top();
      s.pop();
      cur = vet[tp] * (s.empty() ? i : i - s.top() - 1);
      if (ans < cur)
        ans = cur;
  return ans;
int main()
  while(cin >> n and n)
    for(int i = 0; i < n; i++)</pre>
      cin >> vet[i];
    cout << histogram() << '\n';</pre>
    return 0;
```

7.11 Inclusion Exclusion

```
contar a quantidade de numeros na range [1, b]
  que sao multiplos de pelo menos um numero na range [1, a]
#include <bits/stdc++.h>
using namespace std;
#define bug(x) cout << #x << " >>>>>> " << x << '\n'
#define _ << " , " <<
#define int long long
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
#define ii pair<int, int>
#define fi first
#define se second
#define SZ(v) (int)v.size()
#define UNTIL(t) while (clock() < (t) * CLOCKS_PER_SEC)
const long long MAX = (long long) 1e15; \frac{10^5}{}
const int MOD = 1000000007; //10^9 + 7
const int 00 = 0x3f3f3f3f; //3f3f3f3f;
const double EPS = 1e-9; //10^-9
mt19937 rnq(chrono::steady_clock::now().time_since_epoch().count());
vector<int> prime = {3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43,
    47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 101, 103, 107, 109,
    113, 127};
vector<vector<ii>>> lista:
void add(int id)
  vector<ii> aux:
  for (int k = 0; k < id; k++)
    int i = SZ(lista[k]) - 1;
    while(i >= 0 and MAX / lista[k][i].fi / prime[id] == 0) i--;
    for(int j = 0; j <= i; j++)
      aux.push_back({lista[k][j].fi * prime[id], !lista[k][j].se});
  aux.push_back({prime[id], 1});
  sort(aux.begin(), aux.end());
  lista.push back(aux);
int32 t main()
  for (int i = 0; i < SZ (prime); i++)
    add(i);
  int t:
  scanf(" %lld", &t);
  while (t--)
    int a, b;
    scanf(" %lld %lld", &a, &b);
```

```
int ans = b / 2;
int cnt_p = 0;

for(int &w : prime) cnt_p += (w <= a);

for(int i = 0; i < cnt_p; i++)
{
    for(int j = 0; j < SZ(lista[i]); j++)
    {
        if(lista[i][j].fi > b) break;
        if(lista[i][j].se) ans += (b / lista[i][j].fi + 1) / 2;
        else ans -= (b / lista[i][j].fi + 1) / 2;
    }
}
printf("%lld\n", ans);
}

return 0;
}
```

7.12 Index Compression

```
#include <bits/stdc++.h>
const int MAX = 1e6 + 10;
using namespace std;
int n, arr[MAX], pos[MAX], newArr[MAX], realValue[MAX];
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> arr[i], pos[i] = i;
    sort(pos, pos + n, [](int i, int j){ return arr[i] < arr[j]; });</pre>
    int id = 1;
    for(int i = 0; i < n; i++)
    if(!i) newArr[pos[i]] = id, realValue[id] = arr[pos[i]];
    else if(arr[pos[i-1]] == arr[pos[i]]) newArr[pos[i]] = newArr[pos[
    else newArr[pos[i]] = ++id, realValue[id] = arr[pos[i]];
    for(int i = 0; i < n; i++)</pre>
        cout << arr[i] << ' ' << newArr[i] <<
           ' ' << realValue[newArr[i]] << '\n';
    return 0;
```

7.13 Karp Rabin

```
... S[N-1] *A^0) mod B
*/
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
typedef long long 11;
11 A = 911382323, B = 972663749;
ll h1[MAX], h2[MAX], p[MAX];
int arr[MAX];
string s;
ll buildH(ll *H, int k)
    if(k == 0)
        return H[0] = s[0];
    return H[k] = (buildH(H, k - 1) *A + s[k]) % B;
11 buildP(int k)
    if(k == 0)
        return p[0] = 1;
    return p[k] = (buildP(k - 1) *A) % B;
ll vhash(ll *H, int a, int b)
    if(a == 0)
        return H[b];
    ll ans = (H[b] - H[a - 1] * p[b - a + 1]) % B;
    if(ans < 0)
        ans += B;
    return ans;
bool slidingWindow(int k)
    if(k < 0 or k > s.size()) return false;
    for(int i = 0; i + k - 1 < s.size(); i++)</pre>
        if (vhash (h1, i, i + k - 1) == vhash (h2, s.size()
           -(i+k-1)-1, s.size() -(i+k-1)-2+k)
            return true; // A substring [i, i + k - 1] eh palindromo
    return false;
int buscab()
    int tam = 0;
    for(int i = 0; i < s.size(); i++)</pre>
        arr[i] = 2*i + 1, tam++;
    int b = 0, e = tam, m, ans = 0;
    while(b <= e)</pre>
        m = (b + e) / 2;
        slidingWindow(arr[m]) ? b = m + 1, ans = arr[m] : e = m - 1;
    tam = 0:
    for(int i = 0; i < s.size(); i++)</pre>
```

```
arr[i] = 2*i, tam++;
    b = 0, e = tam;
    while(b <= e)</pre>
        m = (b + e) / 2;
        slidingWindow(arr[m]) ? b = m + 1,
          ans = max(arr[m], ans) : e = m - 1;
    return ans;
int main()
    cin >> s;
   buildH(h1, s.size()-1);
    reverse(s.begin(), s.end());
   buildH(h2, s.size()-1);
    buildP(s.size()-1);
    reverse(s.begin(), s.end());
    cout << buscab() << '\n';</pre>
    return 0;
```

7.14 Knapsack With Backtraking

```
#include <bits/stdc++.h>
using namespace std;
#define pii pair<int, int>
#define fi first
#define se second
#define pb push_back
int n,c;
vector<pii> v;
int res,aux;
double c2,aux2;
void bt(int i){
  if(i == n) return;
  aux2 = 0; c2 = c;
  for(int j=i; j<n && c2; j++){</pre>
    if(v[j].fi <= c2){
      c2 -= v[j].fi; aux2 += v[j].se;
    } else {
      aux2 += (v[j].se*c2)/v[j].fi;
      c2 = 0;
  if(aux2 + aux <= res) return;</pre>
  if(v[i].fi <= c){</pre>
    c -= v[i].fi;
    aux += v[i].se;
    if(aux > res) res = aux;
    bt(i+1);
    aux -= v[i].se;
    c += v[i].fi;
```

```
bt(i+1);
}
int32_t main() {
  ios::sync_with_stdio(false);cin.tie(0);

  cin>>n>c;
  for(int i = 0; i < n; i++)
  {
    int wei,value; cin>>wei>>value;
    v.pb({wei,value});
  }

  sort(v.begin(), v.end(), [](pii a, pii b) {
    return (a.se+0.0)/a.fi > (b.se+0.0)/b.fi;
  });

  bt(0);
  cout<<res<<endl;
  return 0;
}</pre>
```

7.15 Knuth Optimization

```
#include <bits/stdc++.h>
using namespace std;
// Knuth Optimization
int pf[6000], n;
int dp[6000][6000];
int sum(int 1, int r)
  return pf[r] - pf[l - 1];
int solve(int 1, int r)
  if(1 > r) return 0;
  if (dp[l][r] != -1) return dp[l][r];
  int ans = (1 << 30);
  for(int i = 1; i <= r; i++)</pre>
    ans = min(ans, sum(1, r) + solve(1, i - 1) + solve(i + 1, r));
  return dp[l][r] = ans;
#define ii pair<int, int>
#define fi first
#define se second
ii DP[6000][6000];
//Point(1, r - 1) \le Point(1, r) \le Point(1 + 1, r)
ii knuth(int 1, int r)
  if(1 == r) return {sum(1, r), 1};
```

```
if (DP[1][r] != ii(-1, -1)) return DP[1][r];
  int lef = knuth(l, r - 1).se;
  int rig = knuth(l + 1, r).se;
  int point = 1, ans = (1 << 30);</pre>
  for(int i = lef; i <= rig; i++)</pre>
    int cur = sum(1, r);
    if(i - 1 >= 1) cur += knuth(1, i - 1).fi;
    if(i + 1 \le r) cur += knuth(i + 1, r).fi;
    if(cur < ans) ans = cur, point = i;</pre>
  return DP[1][r] = {ans, point};
int main()
 memset (dp, -1, sizeof(dp));
  cin >> n;
  //for(int i = 1; i \le n; i++)
    //cin >> pf[i], pf[i] += pf[i - 1];
  //cout << solve(1, n) << endl;
  memset (DP, -1, sizeof (DP));
  cout << knuth(1, n).fi << endl;</pre>
  return 0;
```

7.16 Lontest Substring That Is A Correct Bracket Sequence

```
#include <bits/stdc++.h>
using namespace std;
#define 00 0x3f3f3f3f
#define gc getchar
#define pc putchar
#define offset 1000000
string str;
int Sparse_Table[22][1000002], n;
vector<int> forest[2000002];
int pf[1000002], cnt[1000002];
inline void build()
  for (int i = 1; (1 << i) < n; i++)</pre>
    for (int j = 0; j + (1 << i) < n; j++)
      Sparse_Table[i][j] = min(Sparse_Table[i-1][j],
        Sparse_Table[i-1][j+(1 << (i-1))]);
inline int range_query(int i, int j)
  int sz = log2(j-i+1);
  return min(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
inline int countNumberOfElementEqualToXinLR(int 1, int r, int x)
```

```
int p1 = lower_bound(forest[x + offset].begin(), forest[x + offset].
      end(), 1) - forest[x + offset].begin();
  int p2 = upper_bound(forest[x + offset].begin(), forest[x + offset].
      end(), r) - forest[x + offset].begin() - 1;
  if (p1 > p2) return -1;
  return p2 - p1 + 1;
inline int nxt(int i, int x)
  int b = i, e = n - 1, ans = -1;
  while(b <= e)</pre>
    int m = (b + e) >> 1;
    int v = range_query(i, m);
    if(v >= x) ans = m, b = m + 1;
    else e = m - 1;
  return ans:
inline int queryIndex(int 1, int r, int x)
  int b = 1, e = r, ans = -1;
  while(b <= e)
    int m = (b + e) >> 1;
    if(countNumberOfElementEqualToXinLR(m, r, x) > 0) ans = m, b = m +
    else e = m - 1;
  return ans;
inline void scanstr(string &k)
    register char c:
  k = "";
    for(c = qc(); c != '(' and c != ')'; c = qc());
    for(; c \ge ' (' \text{ and } c \le ')'; c = qc()) k.push_back(c);
int main()
  scanstr(str);
  n = str.size() + 1;
  for(int i = 1; i < n; i++)</pre>
    pf[i] = pf[i - 1] + (str[i - 1] == '(' ? 1 : -1);
    Sparse_Table[0][i] = pf[i];
    forest[pf[i] + offset].push_back(i);
  build();
  int ans = 0;
  cnt[0] = 1;
  for(int i = 1; i < n; i++)</pre>
    if(str[i - 1] != '(') continue;
    int e = nxt(i, pf[i] - 1);
    if(e < i) continue;</pre>
    int p = queryIndex(i, e, pf[i] - 1);
```

```
if(p < i) continue;
int l = p - i + 1;
cnt[l]++;
if(l > ans) ans = l;
}
printf("%d %d\n", ans, cnt[ans]);
return 0;
```

7.17 Maximum Subarray Xor

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
const int 00 = 0x3f3f3f3f;
const double EPS = 1e-9;
#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first.
#define se second
#define pb push_back
#define mt make_tuple
#define all(vetor) vetor.begin(), vetor.end()
#define X real()
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11;
typedef long double ld;
typedef pair<ll, ll> ii;
typedef pair<int, ii> iii;
typedef complex<11> P11;
typedef complex<ld> Pld;
struct TrieNode
    int value;
    TrieNode *children[2];
    TrieNode()
        value = 0;
        children[0] = children[1] = nullptr;
};
void insert(TrieNode *root, int n)
    TrieNode *aux = root;
    for(int i = 31; i >= 0; i--)
        bool b = (n & (1 << i));
        if(aux->children[b] == nullptr)
            aux->children[b] = new TrieNode();
        aux = aux->children[b];
    aux->value = n;
```

```
int query(TrieNode *root, int n)
    TrieNode *aux = root;
    for(int i = 31; i >= 0; i--)
        bool b = (n \& (1 << i));
        if(aux->children[1-b] != nullptr)
            aux = aux->children[1-b];
        else
            aux = aux->children[b];
    return n ^ aux->value;
void maxSubArrayXor(int *arr, int n)
    TrieNode *root = new TrieNode();
    insert(root, 0);
    int px = 0, ans = INT_MIN, r = -1;
    for(int i = 0; i < n; i++)
       px = px ^ arr[i];
        insert(root, px);
        int num = max(ans, query(root, px));
        if(num > ans)
           ans = num, r = i;
    int 1 = r, xo = 0;
    for(; 1 >= 0; 1--)
        xo ^= arr[1];
        if(xo == ans)
            break;
    cout << "O Xor maximo eh: " << ans << '\n';
    while(1 <= r)</pre>
       cout << arr[l++] << ' ';
    cout << '\n';
int main()
    int arr[MAX], n;
    cin >> n;
    REP(i, n) cin >> arr[i];
    maxSubArrayXor(arr, n);
  return 0;
```

7.18 Mo

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 3 * 1e5;
```

//com hash no braco

```
struct Query
    int 1, r, qt;
    vector<int> el;
};
Query q[MAX];
int n, m, blk, ans;
int arr[MAX], freq[MAX], qtd[MAX], pos[MAX];
vector<vector<int>> tab;
void add(int i)
    if(freq[arr[i]])
        qtd[freq[arr[i]]]--;
    freq[arr[i]]++;
    qtd[freq[arr[i]]]++;
    if(ans <= freq[arr[i]])</pre>
        ans = freq[arr[i]];
        tab[ans].push_back(arr[i]);
void sub(int i)
    qtd[freq[arr[i]]]--;
    if(!qtd[ans])
        for(int j = 0; j < tab[ans].size(); j++)</pre>
            if(tab[ans][j] == arr[i])
                 tab[ans].erase(tab[ans].begin() + j);
                break;
        ans--;
        tab[ans].push_back(arr[i]);
    freq[arr[i]]--;
    if(freq[arr[i]])
        qtd[freq[arr[i]]]++;
bool compare(int a, int b)
    if(q[a].1/blk != q[b].1/blk)
        return q[a].1 < q[b].1;
    return q[a].r < q[b].r;</pre>
int main()
    while(cin >> n >> m and n)
        blk = sqrt(n);
        for(int i = 0; i < n; i++)</pre>
            cin >> arr[i];
            arr[i] += 100000;
```

```
for(int i = 0; i < m; i++)</pre>
            cin >> q[i].l >> q[i].r, pos[i] = i;
        sort (pos, pos + m, compare);
        ans = 0;
        int curL = 0, curR = 0;
        int L, R;
        memset(freq, 0, sizeof(freq));
        memset(qtd, 0, sizeof(qtd));
        tab.clear();
        tab.resize(MAX);
        for (int j = 0; j < m; j++)
            L = q[pos[j]].l - 1;
            R = q[pos[j]].r - 1;
            while (curL < L)
                sub(curL++);
            while (curL > L)
                add (--curL);
            while (curR < R + 1)
                add(curR++);
            while (curR > R + 1)
                sub (--curR);
            q[pos[j]].qt = ans;
            q[pos[j]].el = tab[ans];
        for(int j = 0; j < m; j++)
            for(int i = 0; i < q[j].el.size(); i++)</pre>
                cout << q[j].el[i]-100000 << '\n';
    return 0;
//com unordered_multimap
#include <bits/stdc++.h>
using namespace std;
const int MAX = 3 * 1e5;
struct Query
    int 1, r, qt, morefrequent;
};
Query q[MAX];
int n, m, blk, ans;
int arr[MAX], freq[MAX], qtd[MAX], pos[MAX];
unordered_multimap<int, int> tab;
void add(int i)
    if(freq[arr[i]])
        qtd[freq[arr[i]]]--;
    freq[arr[i]]++;
    qtd[freq[arr[i]]]++;
    if(ans <= freq[arr[i]])</pre>
```

```
ans = freq[arr[i]];
        tab.insert({ans, arr[i]});
void sub(int i)
    qtd[freq[arr[i]]]--;
    if(!qtd[ans])
        int k = 0, sz = tab.bucket(ans);
        auto it = tab.find(ans);
        for(int j = 0; j < sz; j++)
            if(it->second == arr[i])
                tab.erase(it);
                 j = sz;
            else it++;
        tab.insert({ans, arr[i]});
    freq[arr[i]]--;
    if(freq[arr[i]])
        qtd[freq[arr[i]]]++;
bool compare(int a, int b)
    if(q[a].1/blk != q[b].1/blk)
        return q[a].1 < q[b].1;
    return q[a].r < q[b].r;</pre>
int main()
    while(cin >> n >> m and n)
        blk = sqrt(n);
        for(int i = 0; i < n; i++)</pre>
            cin >> arr[i];
            arr[i] += 100000;
        for(int i = 0; i < m; i++)</pre>
            cin >> q[i].l >> q[i].r, pos[i] = i;
        sort (pos, pos + m, compare);
        ans = 0;
        int curL = 0, curR = 0;
        int L, R;
        memset(freq, 0, sizeof(freq));
        memset(qtd, 0, sizeof(qtd));
        tab.clear();
        for (int j = 0; j < m; j++)
```

```
L = q[pos[j]].l - 1;
            R = q[pos[j]].r - 1;
            while (curL < L)
                sub(curL++);
            while (curl > I)
                add (--curL);
            while (curR < R + 1)
                add(curR++);
            while(curR > R + 1)
                sub(--curR);
            q[pos[j]].qt = ans;
            q[pos[j]].morefrequent = tab.find(ans)->second;
        for (int j = 0; j < m; j++)
                cout << q[j].morefrequent-100000 << '\n';</pre>
    return 0;
Mo em arvore parte 1
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
struct Query
    int 1, r, v;
};
int n, q;
int freg[MAX], inicio[MAX], fim[MAX], pos[MAX], value[MAX];
vector<int> tree_linearization, G[MAX];
Query Q[MAX];
int ans, blk:
void TreeLinearization(int v, int p)
    inicio[v] = tree_linearization.size();
    tree_linearization.push_back(v);
    for(const int &u : G[v])
        if(u != p)
            TreeLinearization(u, v);
    fim[v] = tree_linearization.size() - 1;
void add(int i)
    if(!freq[value[tree_linearization[i]]])
    freq[value[tree_linearization[i]]]++;
void sub(int i)
    freq[value[tree_linearization[i]]]--;
    if(!freq[value[tree_linearization[i]]])
        ans--;
```

```
bool compare(int a, int b)
    if(O[a].1/blk != O[b].1/blk)
        return Q[a].1/blk < Q[b].1/blk;</pre>
    return Q[a].r < Q[b].r;</pre>
int main()
    int u, v;
    cin >> n >> q;
    for(int i = 0; i < n; i++)</pre>
        cin >> value[i];
    for(int i = 0; i < n-1; i++)</pre>
        cin >> u >> v;
        u--; v--;
        G[u].push_back(v);
        G[v].push_back(u);
    TreeLinearization (0, -1);
    for(int i = 0; i < q; i++)
        cin >> u;
        u--;
        Q[i].l = inicio[u];
        Q[i].r = fim[u];
        pos[i] = i;
    blk = sqrt(n);
    sort (pos, pos+q, compare);
    int curL = 0, curR = 0;
    for(int i = 0; i < q; i++)
        int L = Q[pos[i]].l, R = Q[pos[i]].r;
        while(curL < L)</pre>
            sub(curL++);
        while(curL > L)
            add (--curL);
        while(curR < R + 1)</pre>
             add(curR++);
        while (curR > R + 1)
            sub(--curR);
        Q[pos[i]].v = ans;
    for(int i = 0; i < q; i++)
        cout << Q[i].v << '\n';
    return 0;
```

7.19 Odd Rectangles Area

You are given several axis-aligned rectangles. Compute the sum of the area of the regions that are covered by an odd number of rectangles.

```
input: The first line of input contains a single integer n (1<=n
    <=10^5), representing
the number of rectangles. Each of the next n lines contains four space
integers x1, y1, x2, and y2, each between 0 and 109, describing the
    coordinates of
a rectangle.
Output: Print, on one line, the total area covered by an odd number of
     rectangles
as an exact integer.
#include <bits/stdc++.h>
using namespace std;
struct Event
    int x1, x2, y, t;
    Event(int _x1, int _x2, int _y, int _t)
        x1 = _x1, x2 = _x2, y = _y, t = _t;
    Event(){}
};
struct Node
  int 1, r, value;
};
int n;
vector<Node> tree;
vector<int> lazy;
vector<Event> arr;
int init()
 tree.clear();
  lazy.clear();
  tree.emplace_back();
  lazy.push_back(0);
void createL(int node)
  tree[node].l = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void createR(int node)
  tree[node].r = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void calc(int node)
  tree[node].value = 0;
```

```
if(tree[node].l) tree[node].value += tree[tree[node].l].value;
  if(tree[node].r) tree[node].value += tree[tree[node].r].value;
void push(int node, int start, int end)
  tree[node].value = (end - start + 1) - tree[node].value;
  if(start != end)
    if(tree[node].l == 0) createL(node);
    if(tree[node].r == 0) createR(node);
   lazy[tree[node].l] ^= 1;
   lazy[tree[node].r] ^= 1;
  lazy[node] = 0;
void update(int node, int start, int end, int 1, int r)
  if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return;
  if(1 <= start and end <= r)</pre>
    push (node, start, end);
  else
    int mid = (start + end) / 2;
    if(tree[node].l == 0) createL(node);
    update(tree[node].1, start, mid, 1, r);
    if(tree[node].r == 0) createR(node);
    update(tree[node].r, mid + 1, end, 1, r);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return 0;
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
bool cmp (Event a, Event b)
    if(a.y != b.y) return a.y < b.y;</pre>
    return a.t < b.t;</pre>
int32_t main()
    scanf(" %d", &n);
```

```
for(int i = 0; i < n; i++)</pre>
    int x1, y1, x2, y2;
    scanf(" %d %d %d %d", &x1, &y1, &x2, &y2);
    int xmi = min(x1, x2);
    int ymi = min(y1, y2);
    int xma = max(x1, x2);
    int yma = max(y1, y2);
    xma--;
    //yma--;
    arr.emplace_back(xmi, xma, ymi, -1);
    arr.emplace_back(xmi, xma, yma, 1);
sort(arr.begin(), arr.end(), cmp);
long long Y = 0, ans = 0;
init();
for(int i = 0; i < arr.size(); i++)</pre>
    //cout << "op " << arr[i].t << '\n';
   long long s = query(0, 0, 1000000008, 0, 1000000007);
    long long aux = s * 1LL * (arr[i].y - Y);
    //cout << "this
                          " << aux << ' ' << arr[i].y1 << ' ' <<
        Y << ' ' << s << '\n';
    update(0, 0, 1000000008, arr[i].x1, arr[i].x2);
   Y = arr[i].y;
    ans += aux;
cout << ans << '\n';
return 0;
```

7.20 Quick Sort And Select

```
#include <bits/stdc++.h>
using namespace std;
int n, arr[10000];
int quickselect(int l, int r, int k)
    int j = 1 - 1;
    for(int i = 1; i < r; i++)</pre>
        if(arr[i] <= arr[r])
            swap(arr[++j], arr[i]);
    swap(arr[j+1], arr[r]);
    if(j+1 < k) return quickselect(j+2, r, k);</pre>
    else if(j+1 > k) return quickselect(l, j, k);
    return arr[j+1];
void quicksort(int 1, int r)
    int j = 1 - 1;
    for(int i = 1; i < r; i++)
        if(arr[i] <= arr[r])
            swap(arr[++j], arr[i]);
    swap(arr[j+1], arr[r]);
    if(1 < j)
        quicksort(1, j);
```

7.21 Rectangles Union Area

```
#include <bits/stdc++.h>
using namespace std;
#define ii pair<int, int>
#define fi first
#define se second
struct Event
    int x1, x2, y, t;
    Event(int _x1, int _x2, int _y, int _t)
        x1 = _x1, x2 = _x2, y = _y, t = _t;
    Event(){}
};
ii tree[5008001:
int lazy[500800];
int n:
vector<pair<ii, ii>> segments, rect;
int X1, Y1, X2, Y2, P;
ii calc(ii a, ii b)
  if(a.fi > b.fi) return b;
  else if(a.fi < b.fi) return a;</pre>
  return {a.fi, a.se + b.se};
void build(int node, int start, int end)
 if(start == end)
   tree[node] = \{0, 1\}, lazy[node] = 0;
    int mid = (start + end) / 2;
    build(2 * node, start, mid);
   build(2 * node + 1, mid + 1, end);
   tree[node] = calc(tree[2 * node], tree[2 * node + 1]);
    lazy[node] = 0;
```

```
void push(int node, int start, int end)
  tree[node].fi += lazy[node];
  if(start != end)
   lazv[2 * node] += lazv[node];
   lazy[2 * node + 1] += lazy[node];
  lazv[node] = 0;
void update(int node, int start, int end, int 1, int r, int v)
  if(lazy[node]) push(node, start, end);
  if(start > r or end < l) return;</pre>
  if(1 <= start and end <= r)</pre>
    lazy[node] += v;
    push (node, start, end);
    return;
  int mid = (start + end) / 2;
  update(2 * node, start, mid, 1, r, v);
  update(2 * node + 1, mid + 1, end, l, r, v);
  tree[node] = calc(tree[2 * node], tree[2 * node + 1]);
int query(int node, int start, int end)
  if(lazy[node]) push(node, start, end);
  return end - start + 1 - tree[node].se;
void mount(int r)
  rect.clear();
  for(auto &it : segments)
    int x1 = max(min(it.fi.fi, it.se.fi) - r, X1);
    int y1 = max(min(it.fi.se, it.se.se) - r, Y1);
    int x2 = min(max(it.fi.fi, it.se.fi) + r, X2);
    int y2 = min(max(it.fi.se, it.se.se) + r, Y2);
    x2--;
    rect.push_back({{x1, y1}, {x2, y2}});
bool cmp (Event a, Event b)
    if(a.y != b.y) return a.y < b.y;</pre>
    return a.t > b.t;
long long area(int r)
 mount(r);
  vector<Event> eve;
  for(auto &it : rect)
    eve.emplace_back(it.fi.fi, it.se.fi, it.fi.se, 1);
```

eve.emplace_back(it.fi.fi, it.se.fi, it.se.se, -1);

```
sort(eve.begin(), eve.end(), cmp);
  build(1, 0, 100001);
  long long Y = 0, ans = 0;
    for(int i = 0; i < eve.size(); i++)</pre>
        long long s = query(1, 0, 100001);
        long long aux = s * 1LL * (eve[i].y - Y);
        update(1, 0, 100001, eve[i].x1, eve[i].x2, eve[i].t);
        Y = eve[i].y;
        ans += aux;
    return ans;
int32_t main()
  scanf(" %d", &n);
  for(int i = 0; i < n; i++)</pre>
    int x1, y1, x2, y2;
    scanf(" %d %d %d %d", &x1, &y1, &x2, &y2);
    segments.push_back(\{\{x1, y1\}, \{x2, y2\}\});
  scanf(" %d %d %d %d %d", &P, &X1, &Y1, &X2, &Y2);
  long long tot = (X2 - X1) * 1LL * (Y2 - Y1);
  int b = 0, e = 100000, ans = 0;
  while(b <= e)</pre>
    int mid = (b + e) / 2;
    long long A = area(mid);
   if(P * 1LL * tot <= 100LL * A) ans = mid, e = mid - 1;
    else b = mid + 1;
  cout << ans << '\n';
    return 0;
```

7.22 Small To Large

```
https://codeforces.com/blog/entry/44351

// Small To Large (using map)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN*logN), (we are using map)

#include <bits/stdc++.h>
using namespace std;

const int MAX = 1e4 + 10;

vector<int> g[MAX];
int sz[MAX], col[MAX];
map<int, int> *cnt[MAX];
```

```
sz[v] = 1;
    for(auto u : g[v])
       if(u != p) {
            getsz(u, v); sz[v] += sz[u]; }
void dfs(int v, int p)
    int mx = -1, bigChild = -1;
    for(auto u : q[v])
       if(u != p)
           dfs(u, v);
           if(sz[u] > mx)
               mx = sz[u], bigChild = u;
    if (bigChild != -1)
        cnt[v] = cnt[bigChild];
        cnt[v] = new map<int, int> ();
    (*cnt[v])[ col[v] ] ++;
    for(auto u : g[v])
       if(u != p && u != bigChild)
           for(auto x : *cnt[u])
               (*cnt[v])[x.first] += x.second;
    //now (*cnt[v])[c] is the number of vertices in
    //subtree of vertex v that has color c. You can
    //answer the queries easily.
int32 t main()
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        q[u].push_back(v);
        q[v].push_back(u);
    getsz(0, -1);
    dfs(0, -1);
  return 0;
// dsu on tree (using vector)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
```

void getsz(int v, int p)

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
vector<int> q[MAX];
int sz[MAX], col[MAX];
vector<int> *vec[MAX];
int cnt[MAX];
void getsz(int v, int p)
    sz[v] = 1;
    for(auto u : q[v])
        if(u != p) {
            getsz(u, v); sz[v] += sz[u]; } }
void dfs(int v, int p, bool keep)
    int mx = -1, bigChild = -1;
    for(auto u : q[v])
       if(u != p && sz[u] > mx)
           mx = sz[u], bigChild = u;
    for(auto u : g[v])
       if(u != p && u != bigChild)
           dfs(u, v, 0);
    if (bigChild != -1)
        dfs(bigChild, v, 1), vec[v] = vec[bigChild];
    e1se
        vec[v] = new vector<int> ();
    vec[v]->push back(v);
    cnt[ col[v] ]++;
    for(auto u : q[v])
       if(u != p && u != bigChild)
           for(auto x : *vec[u]){
               cnt[ col[x] ]++;
               vec[v] -> push_back(x);
//now (*cnt[v])[c] is the number of vertices in subtree
//of vertex v that has color c. You can answer the gueries
//easily. note that in this step *vec[v] contains all of
//the subtree of vertex v.
    if(keep == 0)
        for(auto u : *vec[v])
            cnt[col[u]]--;
int32 t main()
    int n, m;
    cin >> n >> m;
    for (int i = 0; i < n; i++)
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        q[u].push_back(v);
        q[v].push_back(u);
```

```
getsz(0, -1);
    dfs(0, -1, 0);
  return 0;
// Small To Large (heavy-light decomposition style)
// Given a tree, every vertex has color. Ouery is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
vector<int> a[MAX];
int sz[MAX], col[MAX];
bool big[MAX];
int cnt[MAX];
void getsz(int v, int p)
    sz[v] = 1;
    for(auto u : g[v])
       if(u != p){
            getsz(u, v); sz[v] += sz[u]; } }
void add(int v, int p, int x)
    cnt[col[v]] += x;
    for(auto u: q[v])
       if(u != p && !biq[u])
            add(u, v, x);
void dfs(int v, int p, bool keep)
   int mx = -1, bigChild = -1;
    for(auto u : q[v])
       if(u != p && sz[u] > mx)
         mx = sz[u], bigChild = u;
    for(auto u : q[v])
       if(u != p && u != bigChild)
        // run a dfs on small childs and clear them from cnt
            dfs(u, v, 0);
    if (bigChild !=-1)
        // bigChild marked as big and not cleared from cnt
        dfs(bigChild, v, 1), big[bigChild] = 1;
    add(v, p, 1);
//now cnt[c] is the number of vertices in subtree of
//vertex v that has color c. You can answer the queries easily.
    if (bigChild !=-1)
       big[bigChild] = 0;
   if(keep == 0)
       add(v, p, -1);
int32_t main()
```

```
int n, m;
    cin >> n >> m;
    for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        q[u].push_back(v);
        q[v].push_back(u);
    getsz(0, -1);
    dfs(0, -1, 0);
  return 0;
// Small To Large (using nesting intervals)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
vector<int> g[MAX];
int sz[MAX], col[MAX];
int st[MAX], ft[MAX];
int cnt[MAX], ver[MAX];
int tempo = 0;
void getsz(int v, int p)
    sz[v] = 1;
    ver[tempo] = v;
    st[v] = tempo++;
    for(auto u : q[v])
        if(u != p) {
            getsz(u, v); sz[v] += sz[u]; 
    ft[v] = tempo++;
void dfs(int v, int p, bool keep)
    int mx = -1, bigChild = -1;
    for(auto u : g[v])
        if(u != p && sz[u] > mx)
         mx = sz[u], bigChild = u;
    for(auto u : q[v])
        if(u != p && u != bigChild)
            // run a dfs on small childs and
            // clear them from cnt
            dfs(u, v, 0);
    if (bigChild != -1)
        // bigChild marked as big and not cleared from cnt
        dfs(bigChild, v, 1);
```

```
for(auto u : g[v])
  if(u != p && u != bigChild)
      for(int p = st[u]; p < ft[u]; p++)</pre>
        cnt[ col[ ver[p] ] ]++;
    cnt[ col[v] ]++;
//now cnt[c] is the number of vertices in subtree of vertex
//v that has color c. You can answer the queries easily.
    if(v == 1) cout << cnt[2] << '\n';</pre>
    if(keep == 0)
        for(int p = st[v]; p < ft[v]; p++)</pre>
          cnt[ col[ ver[p] ] ]--;
int32_t main()
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        g[u].push_back(v);
        g[v].push_back(u);
    getsz(0, -1);
    dfs(0, -1, 0);
  return 0;
/*
But why it is ? You know that why dsu has time
(for g queries); the code uses the same method.
Merge smaller to greater.
If you have heard heavy-light decomposition you
will see that function add will go light edges
only, because of this, code works in time.
*/
```

7.23 Square Root Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

int n, blk_sz;
int arr[MAX], block[MAX];

void update(int idx, int val)
{
   int blockNumber = idx/blk_sz;
   block[blockNumber] += val - arr[idx];
   arr[idx] = val;
}
```

```
int query(int 1, int r)
    int sum = 0;
    while(1 < r and 1%blk_sz != 0 and 1 != 0)</pre>
        sum += arr[1], 1++;
    while(l+blk sz <= r)</pre>
        sum += block[1/blk_sz], 1 += blk_sz;
    while(1 <= r)</pre>
        sum += arr[1], 1++;
    return sum;
void build()
    int blk_idx = -1;
    blk_sz = sqrt(n);
    for(int i = 0; i < n; i++)</pre>
        if(i%blk sz == 0)
            blk_idx++;
        block[blk_idx] += arr[i];
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> arr[i];
    build();
    int o, 1, r;
    while (cin >> o >> 1 >> r and o)
        if(0 == 1)
             update(l-1, r);
        else
             cout << query(1-1, r-1) << '\n';
    return 0;
```

7.24 String Matching Hash Sqrtdecomp

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 100;

typedef long long ll;

#define ii pair<int, long long>
#define fi first
#define se second

11 A = 911382323, B = 972663749;
11 h[MAX], p[MAX];
string s;

11 buildP(int k)
{
   if(k == 0)
        return p[0] = 1;
```

```
return p[k] = (buildP(k - 1)*A) % B;
int main()
    ios_base::sync_with_stdio(false);
  cin.tie(NULL);
    cin >> s;
  buildP(s.size() + 10);
    int n = s.size();
    int sz = sqrt(n);
    unordered_set<ll> AAAA;
    vector<ii> BBBB:
  string aux;
    while(cin >> aux)
        long long value = 0, j = 0;
        while(j < aux.size())</pre>
            if(j == 0) value = aux[j];
            else value = (value * A + aux[j]) % B;
        if(aux.size() > sz)
            BBBB.push_back({aux.size(), value});
            AAAA.insert(value);
    sort(BBBB.begin(), BBBB.end());
  string ans;
  int j = 0, i = 0;
  while(i < s.size())</pre>
      ans.push_back(s[i]);
      if(j == 0) h[j] = s[i];
      else h[j] = (h[j-1] * A + s[i]) % B;
      int leng = -1;
      long long vh;
        for (int k = j; k \ge 0 and k \ge j - sz - 1 and leng < 0; k--)
            if(k == 0) vh = h[j];
            else
                vh = (h[j] - h[k - 1] * p[j - k + 1]) % B;
                if(vh < 0) vh += B;
            if (AAAA.count (vh))
                leng = j - k + 1;
            //length j - k + 1
```

```
if(leng == -1)
      for (int k = 0; k < BBBB.size(); k++)
          int a = j - BBBB[k].first + 1;
            if(a < 0) break;</pre>
          if(a == 0) vh = h[j];
            else
                vh = (h[j] - h[a - 1] * p[j - a + 1]) % B;
                if(vh < 0) vh += B;
            if(vh == BBBB[k].se)
                leng = BBBB[k].fi;
  if(leng != -1)
        j -= leng;
        while(leng--) ans.pop_back();
    ++j;
  i++;
cout << ans << '\n';
return 0;
```

8 Useful Scripts

8.1 Brute

```
#include <bits/stdc++.h>
using namespace std;
// implement the brute force here
int32_t main() {
    return 0;
}
```

8.2 Gen Tree2

```
// generating a tree in a not-so-stupid way (from Errichto)
#include <bits/stdc++.h>
using namespace std;
int rand(int a, int b) {
   return a + rand() % (b - a + 1);
```

```
int main(int argc, char* argv[]) {
   srand(atoi(argv[1]));
   int n = rand(2, 20);
   cout << n << '\n';
   vector<pair<int,int>> edges;
   for(int i = 2; i <= n; ++i)</pre>
      edges.emplace_back(rand(1, i - 1), i);
   vector<int> perm(n + 1); // re-naming vertices
   for(int i = 1; i <= n; ++i)</pre>
      perm[i] = i;
   random_shuffle(perm.begin() + 1, perm.end());
   random_shuffle(edges.begin(), edges.end()); // random order of
       edges
   for(pair<int, int> edge : edges) {
      int a = edge.first, b = edge.second;
      if(rand() % 2)
         swap(a, b); // random order of two vertices
      cout << perm[a] << ' ' << perm[b] << '\n';</pre>
   return 0;
```

8.3 Gen Tree

```
// generating a tree in a simple way (from Errichto)
#include <bits/stdc++.h>
using namespace std;

int rand(int a, int b) {
    return a + rand() % (b - a + 1);
}

int main(int argc, char* argv[]) {
    srand(atoi(argv[1]));
    int n = rand(2, 20);
    cout << n << '\n';
    for(int i = 2; i <= n; ++i)
        cout << rand(1, i - 1) << ' ' << i << '\n';
    return 0;
}</pre>
```

8.4 Gen

```
#include <bits/stdc++.h>
using namespace std;

int rand(int a, int b) {
    return a + rand() % (b - a + 1);
}
```

```
int main(int argc, char* argv[]) {
    // atoi(s) converts an array of chars to int
    srand(atoi(argv[1]));

int n = rand(1, 3), m = rand(1, 3);

cout << n << ' ' << m << endl;
    for(int i = 0; i < n; i++) {
        cout << rand(1, 5) << ' ';
    }
    cout << endl;
}

return 0;
}</pre>
```

8.5 Makefile

```
CXX = g++

CXXFLAGS = -fsanitize=address,undefined -fno-omit-frame-pointer -g -

Wall -Wshadow -std=c++17 -Wno-unused-result -Wno-sign-compare -Wno
-char-subscripts #-fuse-ld=gold
```

8.6 Sol

```
#include <bits/stdc++.h>
using namespace std;
// implement your solution here
int32_t main() {
   return 0;
}
```

8.7 Stress Test Animated

8.8 Stress With Checker

```
#!/bin/bash
make sol brute gen check
for ((i = 1; ; i++)) do
        ./qen $i > in
        ./sol < in > out
        ./brute < in > out2
        ./check > log
        expected=correct
        result=$(< check.txt)
        if [ "$expected" != "$result" ]; then
                echo "--> entrada:"
                cat in
                echo "--> saida sol"
                cat out
                echo "--> saida2 brute"
                cat out2
                break;
        fi
        echo $i
done
```

8.9 Stress

```
make sol brute gen
for ((i = 1; ; i++)) do
        ./gen $i > in
        ./sol < in > out
        ./brute < in > out2
        if (! cmp -s out out2) then
                echo "--> entrada:"
                cat in
                echo "--> saida sol"
                cat out
                echo "--> saida2 brute"
                cat out2
                break;
        fi
        echo $i
done
```