C	GEMP - UECE - ICPC Library Contents		3.3 Ed 3.4 Ka 3.5 Ka 3.6 Kr	git DP Sum Of Digits In Range lit Distance With DP	47 47 47 48
1	1.1 2SAT 1.2 BFS Zero One 1.3 Binary Lifting 1.4 Boruvka MST 1.5 Center Of A Tree 1.6 Diameter And Center Of A Tree 1.7 Dijkstra	2 2 3 3 5 5 6 6	3.8 Kr 3.9 Kr 3.10 Kr 3.11 Kr 3.12 Lo 3.13 Lo 3.14 Su 3.15 Tr	napsack Zero One Without Value napsack0-kSemValor napsackErrichto napsackWithCopies napsackwithPDtopdown nongest Common Subsequece And Edit Distance nongest Increasing Subsequence theset Sum raveling Salesman Problem Bottom Up Dp raveling Salesman Problem Topdown Dp	49 50 50 51 51 51
	1.18 Kuhn MCBM 1.19 Lca With Square Root Decomposition 1.20 Lca With Tree Linearization And Segment Tree 1.21 Lca With Tree Linearization And Sparse Table 1.22 Longest And Shortest Path In DAG	8 4 8 9 9 10 11 13 13 14 14 15 15 16 17 17	4.1 Ah 4.2 Dy 4.3 KM 4.4 LIG 4.5 Lo 4.6 Mi 4.7 SA 4.8 Su 4.9 Su 4.10 Tr 4.11 Tr 4.12 Tr	no Corasick	55 56 56 56 58 60 62
2	1.24 MPC MinimumPathCover 1.25 MVC MinimumVertexCover 1.26 Maximum Clique 1.27 Min Cost Max Flow 1.28 Prim 1.29 Tree Isomorfism	18 18 19 19 20 21 22 22 22 23 23 24 25 26 27	5.1 Ba 5.2 Ca 5.3 Ch 5.4 Co 5.5 Co 5.6 Fa 5.7 Ga 5.8 Ka 5.9 Mi 5.10 Mi 5.11 Mc 5.12 Mc 5.13 Mc	aby Step Giant Step tatalan Numbers ninese Remainder Theorem noversion Base ounting Number Of Times That A Digit Appears Until N ust Fourier Transform aussian Elimination For Max Subset Xor aratsuba atrix Exponentiation iller Rabin obius od Gaussian Elimination odular Arithmetic ulmod Trick ollard Rho	65 66 66
	2.10 Heavy Light Decomposition 2.11 Implicit Treap 2.12 LiChao Tree 2.13 Max Queue 2.14 Merge Sort Tree Iterative 2.15 Merge Sort Tree Range Order Statistics Queries 2.16 Merge Sort Tree With Set 2.17 Merge Sort Tree 2.18 Ordered Set With BIT 2.19 PBDS 2.20 Persistent Segment Tree 2.21 Segment Tree Iterative 2.22 Segment Tree Tree 2D 2.23 Segment Tree With Lazy Propagation 2.24 Sparse Table RMQ	29 31 32 33 33 34 35 35 36 37 37 38 38 39 40	6.1 Ar. 6.2 Bu 6.3 Ch 6.4 Co 6.5 Di 6.6 Dy 6.7 En 6.8 En 6.10 Gr 6.11 Me 6.12 Ra	etry idrew Algorithm Convex Hull iild Two Lines That Go Through All Points Of A Set neck If A Point Is Inside A Convex Polygon onvex Hull Trick stance Between Nearest Pair Of Points ynamic Convex Hull Trick closing Circle R2 nclosing Circle R3 sometry Stan raham Scan aximum Dot Product adial Sort gment Intersection	80 80 80 82 83 84
3	2.26 TreeİsomorfismWithMap 2.27 TreeİsomorfismWithPolynomialHashing 2.28 Two Stacks Trick 2.29 Wavelet Tree Dynamic Programming	41 42 43 44 45 46	7.1 Big 7.2 Co 7.3 Co 7.4 Co 7.5 Cu	llaneous g Num Product	87

	7.7	FastIO	89
	7.8	Fence Problem With Max Flow	89
	7.9	Gen Random Tree	90
	7.10	Histogram	91
	7.11	Inclusion Exclusion	91
	7.12	Index Compression	92
	7.13	Karp Rabin	92
	7.14	Knapsack With Backtraking	93
	7.15	Knuth Optimization	93
	7.16	Lontest Substring That Is A Correct Bracket Sequence	94
	7.17	Maximum Subarray Xor	95
	7.18	Mo	95
	7.19	Odd Rectangles Area	98
	7.20	Quick Sort And Select	99
	7.21	Rectangles Union Area	100
	7.22	Small To Large	101
	7.23	Square Root Decomposition	103
	7.24	String Matching Hash Sqrtdecomp	104
8	Usei	ful Scripts	105
_	8.1	Brute	105
	8.2	Gen	105
	8.3		105
	8.4		106
	8.5	Stress.sh	106

1 Graph

1.1 2SAT

```
// Os vertices pares indicam as proposicoes falsas
// Os vertices impares indicam as proposicoes verdadeiras
// Achar qual proposicao relativa a cada vertice, eh so dividiar
    vertice/2
// tamG = quantidade_proposicoes*2
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
int n, m, tamG;
vector<int> G[MAX], G_t[MAX], C[MAX];
stack<int> sta;
bool cor[MAX];
int componente[MAX], comp;
void preenche(int v)
    cor[v] = true;
    for(const int &u : G_t[v])
        if(!cor[u])
            preenche (u);
    sta.push(v);
void dfs(int v, int comp)
    componente[v] = comp;
    C[comp].push_back(v);
    for (const int &u : G[v])
        if(!componente[u])
            dfs(u, comp);
```

```
void kosaraju()
    memset(cor, false, sizeof(cor));
    for(int i = 0; i < tamG; i++)</pre>
        if(!cor[i])
            preenche(i);
    memset(cor, false, sizeof(cor));
    comp = 1;
    while(!sta.empty())
        int u = sta.top();
        sta.pop();
        if(componente[u]) continue;
        dfs(u, comp);
        comp++;
// Id no grafo que representa a proposicao de numero P como verdadeira
int idTrue(int p)
    return (p << 1) + 1;
// Id no grafo que representa a proposicao de numero P como falsa.
int idFalse(int p)
    return (p << 1);
bool twoSat()
  kosaraju();
  for (int i = 0; i < tamG; i+=2)
  // Todo par de proposicoes (proposicao falsa, proposicao verdadeira)
  // Nao podem estar no mesmo componente
    if(componente[i] == componente[i + 1])
        return false;
  return true;
int addEdge(int u, int v)
    G[idFalse(u)].push_back(idTrue(v));
    G[idFalse(v)].push_back(idTrue(u));
    G[idTrue(u)].push_back(idFalse(v));
    G[idTrue(v)].push_back(idFalse(u));
    // montar grafo transposto para kosaraju nessa
    // aplicacao o grafo G sera igual ao transposto
    G_t[idFalse(u)].push_back(idTrue(v));
    G_t[idFalse(v)].push_back(idTrue(u));
    G_t[idTrue(u)].push_back(idFalse(v));
    G_t[idTrue(v)].push_back(idFalse(u));
```

```
vector<int> g[MAX];
vector<int> ts;
int value[MAX];
void topSort(int v)
    cor[v] = true;
    for(int &u : G[v])
        if(!cor[u])
            topSort(u);
    ts.push_back(v);
void mountDAG()
    for (int v = 0; v < tamG; v++)
        for(int &u : G[v])
            if(componente[v] != componente[u])
                g[componente[v]].push_back(componente[u]);
    memset(cor, false, sizeof(cor));
    for (int v = 1; v < comp; v++)
        if(!cor[v])
            topSort(v);
    // nao inverter ts, pois precisamos da ordenacao
    // topologica ao contrario
// encontrar uma atribuicao (TREU ou FALSE) para as proposicoes
void assignment()
    if(!twoSat()) return;
    mountDAG();
    memset(value, -1, sizeof(value));
    for(int &v : ts)
        for(int &u : C[v])
            if (value [u >> 1] == -1) // u / 2 eh a proposicao
                value[u >> 1] = (u & 1 ? 1 : 0);
    for(int i = 0; i < (tamG >> 1); i++)
        cout << value[i] << ' ';
    puts("");
int main()
    cin >> n >> m;
    tamG = 2 * n;
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        addEdge(u, v);
    cout << twoSat() << '\n';</pre>
    assignment();
    return 0;
```

1.2 BFS Zero One

```
// o peso das arestas eh 0 ou 1
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
const int 00 = 0x3f3f3f3f3f;
typedef pair<int, int> ii;
int n, m;
vector<ii> G[MAX];
int dist[MAX];
deque<int> dq;
void zeroOneBfs(int v)
    memset(dist, 63, sizeof(dist));
    dist[v] = 0;
    dq.push_back(v);
    while(!dq.empty())
        int u = dq.front();
        dq.pop_front();
        for(int i = 0; i < G[u].size(); i++)</pre>
            int w = G[u][i].first, d = G[u][i].second;
            if(dist[w] > dist[u] + d)
                dist[w] = dist[u] + d;
                if(!d) dq.push_front(w);
                else dq.push_back(w);
    for(int i = 0; i < n; i++)</pre>
        cout << dist[i] << ' ';
    puts("");
int main()
    cin >> n >> m;
    while (m--)
        int u, v, w;
        cin >> u >> v >> w; u--; v--;
        G[u].push_back({v, w});
        G[v].push_back({u, w});
    zeroOneBfs(0);
    return 0;
```

1.3 Binary Lifting

```
using namespace std;
const int MAX = 1e5;
int n, m, nivel[MAX], anc[MAX][30], MAX_LOG;
vector<int> G[MAX];
void dfs(int v, int p, int d)
    anc[v][0] = p;
   nivel[v] = d;
    if(d) MAX_LOG = max(MAX_LOG, (int)log2(d));
    for(const int &u : G[v])
        if(u != p)
            dfs(u, v, d + 1);
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k_k-k)], k = k_k-k;
    return v;
int lca(int u, int v)
    if(nivel[u] < nivel[v]) v = walk(v, nivel[v]-nivel[u]);</pre>
    if(nivel[u] > nivel[v]) u = walk(u, nivel[u]-nivel[v]);
    if(u == v) return u;
    for(int i = MAX_LOG; i >= 0; i--)
        if(anc[u][i] != anc[v][i])
            u = anc[u][i];
            v = anc[v][i];
    return anc[u][0];
void build()
    memset (anc, -1, sizeof anc);
    nivel[0] = 0;
    dfs(0, -1, 0);
    for(int j = 1; j <= MAX_LOG; j++)</pre>
        for(int i = 1; i <= n; i++)</pre>
            if(anc[i][j-1] != -1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
int main()
    int u, v;
    cin >> n >> m;
    while (m--)
        cin >> u >> v;
        u--; v--;
        G[u].push_back(v);
        G[v].push_back(u);
    build();
    cin >> u >> v;
```

```
cout << lca(u-1, v-1)+1 << ' n';
    return 0;
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
typedef pair<int, int> ii;
int n, m, max_log;
vector<ii> G[MAX]:
int anc[MAX][30], min_edge[MAX][30], depth[MAX];
void dfs(int v, int d, int p, int a)
   anc[v][0] = p;
    depth[v] = d;
    if(d) max_log = max(max_log, (int)log2(d));
    if (p != -1) min edge [v][0] = a;
    for(int i = 0; i < G[v].size(); i++)</pre>
        int u = G[v][i].second, w = G[v][i].first;
       if(u != p)
           dfs(u, d + 1, v, w);
void build()
   memset(anc, -1, sizeof(anc));
   memset (min_edge, 63, sizeof (min_edge));
    dfs(0, 0, -1, -1);
    for(int j = 1; j <= max_log; j++)</pre>
        for(int i = 0; i < n; i++)</pre>
            if (anc[i][j-1] != -1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
                min_edge[i][j] = min(min_edge[i][j-1], min_edge[anc[i
                    ][j-1]][j-1]);
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k&-k)], k -= k&-k;
    return v;
int lca(int u, int v)
   if(depth[u] > depth[v]) u = walk(u, depth[u]-depth[v]);
   if (depth[u] < depth[v]) v = walk(v, depth[v]-depth[u]);</pre>
    if(u == v) return u;
    for(int i = max_log; i >= 0; i--)
```

```
if(anc[u][i] != anc[v][i])
            u = anc[u][i];
            v = anc[v][i];
    return anc[u][0];
int queryMinEdge(int u, int v)
    int LCA = lca(u, v);
    int ans = INT MAX;
    int k = depth[u]-depth[LCA];
    while(k)
        ans = min(ans, min_edge[u][(int)log2(k&-k)]);
        u = walk(u, k\&-k);
        k = k_{\&}-k_{:}
    k = depth[v]-depth[LCA];
    while(k)
        ans = min(ans, min_edge[v][(int)log2(k&-k)]);
        v = walk(v, k\&-k);
        k = k - k;
    return ans;
int main()
    int u, v, w;
    cin >> n:
    for(int i = 0; i < n-1; i++)</pre>
        cin >> u >> v >> w;
        u--; v--;
        G[u].push_back({w, v});
        G[v].push_back({w, u});
    cin >> u >> v:
   build();
    cout << lca (u-1, v-1)+1 << ' n';
    cout << queryMinEdge(u-1, v-1) << '\n';</pre>
    return 0;
```

1.4 Boruvka MST

```
#include <bits/stdc++.h>
using namespace std;
int n, m;
vector<array<int, 3>> edge;
int pai[100100], sz[100100];
int find(int x)
{
```

```
return pai[x] == x ? x : pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    y = find(y);
    if(x == y) return;
    if(sz[x] > sz[y]) swap(x, y);
    pai[x] = y;
    sz[y] += sz[x];
int main()
    scanf(" %d %d", &n, &m);
    for(int i = 0; i < m; i++)</pre>
        int u, v, w;
        scanf(" %d %d %d", &u, &v, &w); u--; v--;
        edge.push_back({w, v, u});
    for (int i = 0; i < n; i++)
        pai[i] = i, sz[i] = 1;
    int mst cost = 0;
    bool fl = true;
    while (fl)
        fl = false;
        vector<int> aux(n, -1);
        for(int i = 0; i < m; i++)</pre>
            int u = find(edge[i][1]), v = find(edge[i][2]), w = edge[i][1]
                ][0];
            if(u == v) continue;
            if(aux[u] == -1) aux[u] = i;
            else if(edge[aux[u]][0] > w) aux[u] = i;
            if(aux[v] == -1) aux[v] = i;
            else if (edge[aux[v]][0] > w) aux[v] = i;
        for(int i = 0; i < n; i++)</pre>
            if(aux[i] == -1) continue;
            int u = find(edge[aux[i]][1]), v = find(edge[aux[i]][2]);
            if(u == v) continue;
            // add_edge edge[aux[i]][1] --- edge[aux[i]][2] in the MST
            join(u, v);
            mst_cost += edge[aux[i]][0];
            fl = true;
    cout << mst_cost << '\n';</pre>
    return 0;
```

1.5 Center Of A Tree

```
#include <bits/stdc++.h>
const int MAX = 1e5;
```

```
using namespace std;
int n, degree[MAX];
vector<int> G[MAX];
bool vis[MAX];
int findCenter()
  queue<int> fila[2];
  for(int i = 0; i < n; i++)</pre>
    if(degree[i] == 1)
      fila[0].push(i);
  int cnt = 0, turn = 0;
  while (cnt + 2 < n)
    while(!fila[turn].empty())
      int u = fila[turn].front(); fila[turn].pop();
      vis[u] = true;
      cnt++;
      for(int i = 0; i < G[u].size(); i++)</pre>
        if(!vis[G[u][i]])
          degree[G[u][i]]--;
          if(degree[G[u][i]] == 1)
            fila[1-turn].push(G[u][i]);
    turn ^= 1;
  cout << "the set of central vertices\n";</pre>
  for(int i = 0; i < n; i++)</pre>
    if(!vis[i])
        cout << i + 1 << '\n';
int main()
    cin >> n;
  for(int i = 1; i < n; i++)</pre>
    int u, v;
    scanf("%d %d", &u, &v); u--; v--;
    G[u].push_back(v);
    G[v].push_back(u);
    degree[u]++;
    degree[v]++;
  findCenter();
  return 0;
```

1.6 Diameter And Center Of A Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int n;
```

```
vector<int> G[MAX];
int bfs(int v, vector<int> &dist)
    queue<int> q;
    q.push(v);
    dist[v] = 0;
    int lgv = -1;
    while(!q.empty())
        int u = q.front(); q.pop();
        lqv = u;
        for(int &w : G[u])
             if(dist[w] == -1)
                 dist[w] = dist[u] + 1;
                 q.push(w);
    return lqv;
void findCenterAndDiameter(int w)
    vector<int> dist1(n + 1, -1);
    vector<int> dist2(n + 1, -1);
  int v = bfs(w, dist1);
  int u = bfs(v, dist2);
  int d = dist2[u];
    dist1.assign(n + 1, -1);
    u = bfs(u, dist1);
    cout << "center ";</pre>
    for(int i = 0; i < n; i++)</pre>
        int d1 = dist1[i], d2 = dist2[i];
        if(d1 == d / 2 \text{ and } d2 == d - d / 2 \text{ or } d2 == d / 2 \text{ and } d1 == d
             - d / 2)
        cout << i + 1 << ' ';
    cout << "\ndiameter " << d << '\n';</pre>
int main()
    cin >> n;
    for(int i = 1; i < n; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        G[u].push_back(v);
    G[v].push_back(u);
    findCenterAndDiameter(0);
    return 0;
```

1.7 Dijkstra

#include <bits/stdc++.h>

```
using namespace std;
const int 00 = 0x3f3f3f3f;
const int MAX = 1e5;
typedef pair<int, int> ii;
int n, m;
int dist[MAX];
vector<ii> G[MAX];
int dijkstra(int v, int z)
    memset(dist, 63, sizeof(dist));
    dist[v] = 0;
    priority_queue<ii> pq;
    pq.push({0, v});
    while(!pq.empty())
        int u = pq.top().second;
        int d = -pq.top().first;
        pq.pop();
        if(d > dist[u]) continue;
        if(u == z) return d;
        for(int i = 0; i < G[u].size(); i++)</pre>
            int w = G[u][i].second, _d = G[u][i].first;
            if(dist[w] > d + _d)
                dist[w] = d + _d;
                pq.push({-dist[w], w});
    return 00;
int main()
    int u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        u--; v--;
        G[u].push_back({w, v});
        G[v].push_back({w, u});
    cin >> u >> v;
    cout << dijkstra(u-1, v-1) << '\n';
    return 0;
```

1.8 Dinic

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
const int OO = 0x3f3f3f3f3f;
```

```
struct edge
    int v, f, c;
    edge(){}
    edge(int _v, int _f, int _c)
       v = _v, f = _f, c = _c;
};
vector<edge> edges;
vector<int> G[MAX];
int dist[MAX], work[MAX];
void add_edge(int u, int v, int cp, int rc) {
  edges.push_back(edge(v, 0, cp));
 G[u].push_back(edges.size()-1);
  edges.push_back(edge(u, 0, rc));
  G[v].push_back(edges.size()-1);
bool bfs(int s, int t)
    memset(dist, -1, sizeof(dist));
    dist[s] = 0;
    queue<int> q;
    q.push(s);
    while(!q.empty())
        int u = q.front();
        q.pop();
        for(int e : G[u])
            if(dist[edges[e].v] == -1 and edges[e].c-edges[e].f > 0)
                q.push (edges[e].v);
                dist[edges[e].v] = dist[u] + 1;
    return dist[t] != -1;
int dfs(int s, int t, int f)
    if(s == t) return f;
    for(int &i = work[s]; i < G[s].size(); i++)</pre>
      int e = G[s][i];
        if(dist[edges[e].v] == dist[s] + 1 and edges[e].c-edges[e].f >
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                )))
                edges[e].f += a;
                edges[e^1].f -= a;
                return a;
    return 0;
```

```
int MaxFlow(int s, int t)
    int mf = 0;
    while(bfs(s, t))
      memset (work, 0, sizeof (work));
        while(int a = dfs(s, t, 00))
            mf += a;
    return mf;
int main()
    int n, m, u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        add_edge(u-1, v-1, w, 0);
    cin >> u >> v;
    cout \ll MaxFlow(u-1, v-1) \ll '\n';
    return 0;
```

1.9 Erdos Gallai Theorem

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
int32_t main()
  int n;
  while(~scanf(" %lld", &n))
      vector<int> degree(n), pref(n + 2);
        for(int &i : degree)
            scanf (" %lld", &i);
      sort(degree.begin(), degree.end(), greater<int>());
      for(int i = 0; i < n; i++)</pre>
    pref[i + 1] = pref[i] + degree[i];
        bool fl = true;
        if(pref[n] & 1)
            fl = false;
        int j = n;
        for (int k = 1; k \le n and f1; k++)
            int L = pref[k];
            int R = k * (k - 1);
            while (j > 0 \text{ and } degree[j - 1] < k)
                j--;
            int pos = max(j, k);
            R += pref[n] - pref[pos] + (pos - k) * k;
            if(L > R) fl = false;
        puts(fl ? "possivel" : "impossivel");
```

```
}
return 0;
```

1.10 Eulirian Path

```
#include <bits/stdc++.h>
using namespace std;
int32 t main() {
   int n, m;
   cin >> n >> m;
   vector<vector<int>> q(n);
   vector<int> deg_in(n), deg_out(n);
   for(int i = 0; i < m; i++) {</pre>
      int u, v;
      cin >> u >> v; u--; v--;
      g[u].push_back(v);
      deg_in[v]++;
      deg_out[u]++;
   int s = -1, f = -1;
   for(int i = 0; i < n; ++i) {</pre>
      if (deg_in[i] - deg_out[i] == 0) continue;
      if(s == -1 and deq_out[i] - deq_in[i] == 1) s = i;
      else if(f == -1 and deq_in[i] - deq_out[i] == 1) f = i;
      else return cout << "NO\n", 0;</pre>
   if (s == -1 and f == -1) s = 0;
   else if (s !=-1 and f ==-1 or s ==-1 and f !=-1) return cout <<
       "NO\n", 0;
   stack<int> st;
   st.push(s);
   vector<int> res;
   while(!st.emptv()) {
      int v = st.top();
      if(q[v].emptv()) {
         res.push_back(v);
         st.pop();
      } else {
         int u = g[v].back();
         q[v].pop_back();
         st.push(u);
   for(int i = 0; i < n; i++)</pre>
      if(g[i].empty() == false)
         return cout << "NO\n", 0;</pre>
   reverse(res.begin(), res.end());
```

```
for(int w : res)
    cout << w + 1 << ' ';
cout << endl;
return 0;</pre>
```

1.11 Floyd Sucessor Graph

```
#include <bits/stdc++.h>
using namespace std;
int n;
int table[10000][20];
//table[i][j] armazena o sucessor de distancia 2^j do vertice i
void build()
  for (int j = 1; (1 << j) <= n; j++)
    for(int i = 0; i < n; i++)
        if(table[i][j-1] != -1)
          table[i][j] = table[table[i][j-1]][j-1];
int succ(int u, int k)
  while(k)
    u = table[u][(int)log2(k&-k)];
    if(u == -1)
        return -1;// nao existe
    k = k - k;
  return u;
//algoritmo de Floyd para encontrar o tamanho de um ciclo
//alcancado a partir de um vertice u em um grafo sucessor
int Floyd(int u)
  int a = succ(u, 1);
  int b = succ(u, 2);
  //encontra um vertice no ciclo
  while(a != b)
   a = succ(a, 1);
   b = succ(b, 2);
    if (a == -1 or b == -1)
        return -1;// nao existe ciclo
  //a e b vao ficar posicionados no inicio do ciclo
  a = u;
  while(a != b)
      a = succ(a, 1);
      b = succ(b, 1);
```

```
//percorre todo o ciclo contando o seu tamanho
  b = succ(a, 1);
  int lenght = 1;
  while(a != b)
    b = succ(b, 1);
    lenght++;
  return lenght;
int main()
  int u, v, m;
  cin >> n >> m;
  memset(table, -1, sizeof(table));
  for(int i = 0; i < m; i++)
    cin >> u >> v; u--; v--;
   table[u][0] = v;
  build();
  cin >> u >> v;
  cout << "O sucessor de " << u << " com " << v <<
  " unidades a frente eh " << succ(u-1, v)+1 << '\n';
  cout << '\n';
  cin >> u:
  cout << "tamanho do ciclo iniciando em " << u <<
   ": " << Floyd(u-1) << '\n';
  return 0;
```

1.12 Ford Fulkerson

```
#include <bits/stdc++.h>
using namespace std;
typedef pair<int, int> ii;
const int 00 = 0x3f3f3f3f3f;
const int MAX = 1e4;

struct edge
{
   int v, f, c;
   edge(){}
   edge(int _v, int _f, int _c)
   {
      v = _v, f = _f, c = _c;
   }
};

vector<edge> edges;
vector<int> G[MAX];
```

```
int tempo = 1, cor[MAX];
void add_edge(int u, int v, int cp, int rc)
    edges.push_back(edge(v, 0, cp));
    G[u].push back(edges.size()-1);
    edges.push_back(edge(u, 0, rc));
    G[v].push_back(edges.size()-1);
int dfs(int s, int t, int f)
    if(s == t) return f;
    cor[s] = tempo;
    for(int e : G[s])
        if(cor[edges[e].v] < tempo and edges[e].c-edges[e].f > 0)
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                edges[e].f += a;
                edges[e^1].f -= a;
                return a;
    return 0;
int MaxFlow(int s, int t)
    int mf = 0;
    while(int a = dfs(s, t, 00))
        mf += a, tempo++;
    return mf;
int main()
    int n, m, w, u, v;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w;
        add_edge(u-1, v-1, w, 0);
    cin >> u >> v;
    cout \ll MaxFlow(u-1, v-1) \ll '\n';
    return 0;
```

1.13 Fully Dynamic Connectivity Check If Two Vertices Are In The Same Component

```
#include <bits/stdc++.h>
using namespace std;

const int MAX = 131072;
const int 00 = 0x3f3f3f3f3f;
const double EPS = 1e-9;
```

```
#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first
#define se second
#define pb push_back
#define mt make_tuple
#define mp make pair
#define all(vetor) vetor.begin(), vetor.end()
#define X real()
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11;
typedef long double ld;
//typedef pair<int, int> ii;
//typedef pair<int, ii> iii;
typedef complex<11> Pll:
typedef complex<ld> Pld;
typedef pair<int, int> edge;
vector<edge> tree[4 * MAX], query[4 * MAX];;
int pai[MAX], sz[MAX];
stack<pair<int, int>> stk, size;
vector<int> ans;
int find(int x)
    if(pai[x] == x)
        return x;
    stk.push(mp(x, pai[x]));
    size.push(mp(x, sz[x]));
    return pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    v = find(v):
    if(x == y) return;
    if(sz[x] > sz[y])
        swap(x, y);
    stk.push(mp(x, pai[x]));
    size.push(mp(y, sz[y]));
    sz[y] += sz[x];
    pai[x] = v;
void rollback(int rollback_to)//desfaz todas as alteracaes no DSU,
\{//O(k) \text{ onde } k \text{ eh a quantidade de operações realizadas}
  while(rollback to < stk.size())</pre>
    pai[stk.top().fi] = stk.top().se;
    stk.pop();
        sz[size.top().fi] = size.top().se;
        size.pop();
```

```
void add_edge(int node, int start, int end, int 1, int r, edge e)
    if(start == 1 and end == r)
        tree[node].push_back(e);
    if(1 >= r)
        return;
    int mid = (start + end) / 2;
    add_edge(2*node, start, mid, 1, min(mid, r), e);
    add_edge(2*node + 1, mid + 1, end, max(1, mid + 1), r, e);
void add_query(int node, int start, int end, int idx, edge e)
    if(start == end)
        query[node].push_back(e);
    else
        int mid = (start + end) / 2;
        if(idx <= mid)</pre>
            add_query(2*node, start, mid, idx, e);
        else
            add_query(2*node + 1, mid + 1, end, idx, e);
void processar(int node)
    for(auto it : tree[node])
        join(it.first, it.second);
void dfs(int node, int start, int end)
    int rollback_to = stk.size();
    processar (node);
    if(start == end)
        for(auto v : query[node])
            bool rep = (find(v.first) == find(v.second));
            ans.push_back(rep);
    else
        int mid = (start + end) / 2;
        dfs(2*node, start, mid);
        dfs(2*node + 1, mid + 1, end);
    rollback (rollback to);
int main()
    int n, q, o, u, v;
    cin >> n >> q;
```

```
for(int i = 0; i <= n; i++)</pre>
    sz[i] = 1, pai[i] = i;
int cur = 0;
map<pair<int, int>, int> mapa;
while (q--)
    cin >> o >> u >> v; u--; v--;
if(u > v) swap(u, v);
    if(o == 1)// adicionar aresta
        mapa[mp(u, v)] = cur++;
    else if(o == 2)// remover aresta
        add_edge(1, 0, MAX-1, mapa[mp(u, v)], cur++, mp(u, v));
        mapa.erase(mp(u, v));
    else // verificar se dois vertices estao na mesma componente
        add_query(1, 0, MAX-1, cur++, mp(u, v));
cur++;
for(auto it : mapa)
    add_edge(1, 0, MAX-1, it.second, cur, it.first);
dfs(1, 0, MAX-1);
for(int i = 0; i < ans.size(); i++)</pre>
    cout << (ans[i] ? "Yes\n" : "No\n");</pre>
return 0;
```

1.14 Fully Dynamic Connectivity Count Conected Components

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 131072;
const int 00 = 0x3f3f3f3f3f;
const double EPS = 1e-9;
#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first
#define se second
#define pb push back
#define mt make_tuple
#define mp make_pair
#define all(vetor) vetor.begin(), vetor.end()
#define X real()
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11:
typedef long double ld;
//typedef pair<int, int> ii;
//typedef pair<int, ii> iii;
typedef complex<11> P11;
typedef complex<ld> Pld;
```

```
typedef pair<int, int> edge;
vector<edge> tree[4 * MAX];
vector<int> query[4 * MAX];
int pai[MAX], sz[MAX];
stack<pair<int, int>> stk, size;
stack<int> qtd;
vector<int> ans;
int rep;
int find(int x)
    if(pai[x] == x)
        return x;
    stk.push(mp(x, pai[x]));
    size.push(mp(x, sz[x]));
    qtd.push(rep);
    return pai[x] = find(pai[x]);
void join(int x, int y)
    x = find(x);
    v = find(v);
    if(x == y) return;
    if(sz[x] > sz[y])
        swap(x, y);
    qtd.push(rep);
    stk.push(mp(x, pai[x]));
    size.push(mp(y, sz[y]));
    sz[y] += sz[x];
    pai[x] = y;
    rep--;
void rollback(int rollback_to)//desfaz todas as alteracoes no DSU,
\{//O(k) \text{ onde } k \text{ eh a quantidade de operações realizadas}
 while(rollback_to < stk.size())</pre>
    pai[stk.top().fi] = stk.top().se;
    stk.pop();
        sz[size.top().fi] = size.top().se;
        size.pop();
        rep = qtd.top();
        qtd.pop();
void add edge(int node, int start, int end, int 1, int r, edge e)
    if(start == 1 and end == r)
        tree[node].push_back(e);
    if(1 >= r)
        return;
    int mid = (start + end) / 2;
    add_edge(2*node, start, mid, 1, min(mid, r), e);
    add_edge(2*node + 1, mid + 1, end, max(1, mid + 1), r, e);
```

```
void add_query(int node, int start, int end, int idx, int e)
    if(start == end)
        query[node].push_back(e);
    else
        int mid = (start + end) / 2;
        if(idx <= mid)</pre>
            add_query(2*node, start, mid, idx, e);
        else
            add_query(2*node + 1, mid + 1, end, idx, e);
void processar(int node)
    for(auto it : tree[node])
        join(it.first, it.second);
void dfs(int node, int start, int end)
    int rollback to = stk.size();
    processar (node);
    if(start == end)
        for(auto v : query[node])
            ans.push_back(rep);
    else
        int mid = (start + end) / 2;
        dfs(2*node, start, mid);
        dfs(2*node + 1, mid + 1, end);
    rollback (rollback to);
int main()
    int n, q, u, v;
    cin >> n >> q;
    rep = n;
    for(int i = 0; i <= n; i++)</pre>
        sz[i] = 1, pai[i] = i;
    int cur = 0;
    map<pair<int, int>, int> mapa;
    while (q--)
        char o;
        cin >> o;
        if(o != '?')
            cin >> u >> v; u--; v--;
      if(u > v) swap(u, v);
            if(o == '+')// adicionar aresta
                mapa[mp(u, v)] = cur++;
            else if(o == '-')// remover aresta
                add\_edge(1, 0, MAX-1, mapa[mp(u, v)], cur++, mp(u, v))
```

1.15 Hopcroft Karp

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
int n, m;
vector<int> G[10000];
queue<int> q:
int pairU[10000], pairV[10000], dist[10000];
bool bfs()
    for(int u = 1; u <= m; u++)
        if(!pairU[u])
            dist[u] = 0;
            q.push(u);
        else dist[u] = 00;
    dist[0] = 00;
    while(!q.empty())
        int u = q.front();
        q.pop();
        if(dist[u] < dist[0])</pre>
            for(const int &v : G[u])
                if(dist[pairV[v]] == 00)
                    dist[pairV[v]] = dist[u] + 1;
                    q.push(pairV[v]);
    return (dist[0] != 00);
bool dfs(int u)
    if(u)
    for(const int &v : G[u])
            if(dist[pairV[v]] == dist[u]+1)
                if (dfs(pairV[v]))
```

```
pairV[v] = u;
                     pairU[u] = v;
                     return true;
        dist[u] = 00;
        return false;
    return true;
int hopcroftKarp()
    memset(pairU, 0, sizeof(pairU));
    memset(pairV, 0, sizeof(pairV));
    int result = 0;
    while(bfs())
        for (int u = 1; u \le m; u++)
            if(!pairU[u] and dfs(u))
                result++;
    return result;
int main()
  n = m = 4;
 G[1].push_back(2);
  G[2].push_back(1);
  G[1].push_back(3);
  G[3].push_back(1);
  G[2].push_back(1);
  G[1].push_back(2);
 G[3].push_back(2);
  G[2].push_back(3);
  G[4].push_back(2);
  G[2].push_back(4);
  G[4].push_back(4);
  G[4].push_back(4);
  cout << hopcroftKarp() << '\n';</pre>
  return 0;
```

1.16 K Short Paths

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
const int 00 = 0x3f3f3f3f3f3f3f3f3f3f;
const int MAX = 2000000;

typedef pair<int, int> ii;
int n, m, k;
vector<ii> G[MAX];
int cnt[MAX];
void dijkstra(int v) {
```

```
priority_queue<ii> pq;
  pq.push({0, v});
  int c = 0;
  while(!pq.empty()) {
    int u = -pq.top().second;
    int d = -pq.top().first;
    pq.pop();
    cnt[u]++;
    if(cnt[u] > k) continue;
      if(u == n - 1) {
        cout << d << ' ';
      if(++c == k) { cout << '\n'; return; }</pre>
    for(auto [_d, w] : G[u])
      if(cnt[w] < k)
        pq.push({-(d + _d), -w});
int32_t main() {
  cin >> n >> m >> k;
  while (m--) {
   int u, v, w;
    cin >> u >> v >> w; u--; v--;
   G[u].push_back({w, v});
  dijkstra(0);
  return 0;
```

1.17 Knapsack Dijkstra

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
#define ii pair<int, int>
#define fi first
#define se second
vector<ii>> G[105];
int dist[100000008];
vector<int> peso;
void dijkstra()
 memset(dist, 63, sizeof(dist));
  dist[0] = 0;
  priority_queue<ii> pq;
 pq.push({0, 0});
  while(!pq.empty())
    int u = pq.top().se;
    int d = -pq.top().fi;
    pq.pop();
    if(d > dist[u]) continue;
    for(int i = 0; i < G[u].size(); i++)</pre>
      int w = G[u][i].fi, dd = G[u][i].se;
      if(dist[w] > dist[u] + dd)
```

```
dist[w] = dist[u] + dd;
       pq.push({-dist[w], w});
    }
  dist[0] = peso[0];
int32_t main()
  int n, e, d;
  cin >> n >> d >> e;
  // ler pesos
 peso = vector<int>{d, 2 * d, 5 * d, 10 * d, 20 * d, 50 * d, 100 * d,
   5 * e, 10 * e, 20 * e, 50 * e, 100 * e, 200 * e};
  // ordena pra pegar o menor valor
  sort(peso.begin(), peso.end());
  //montar grafo
  for(int i = 0; i < peso[0]; i++)</pre>
    for(int j = 0; j < peso.size(); j++)</pre>
      int x = (i + peso[j]) % peso[0];
      G[i].push_back({x, peso[j]});
    dist[i] eh o menor numero que eu consigo formar usando
    os meus objetos tal que dist[i] % peso[0] == i
  dijkstra();
    se dist[X % peso[0]] \le X eh possivel gerar um valor X
    utilizando os valores do array peso
    OBS: cada valor pode ser usado infinitas vezes
  return 0;
```

1.18 Kuhn MCBM

```
#include <bits/stdc++.h>
using namespace std;
int na, nb, m, tempo = 1;
int b[105];
int cor[105];
vector<int> G[105];
bool kuhn (int u)
  if(cor[u] == tempo)
    return 0:
  cor[u] = tempo;
//random_shuffle(G[u].begin(), G[u].end(), [](int x){ return rand() %
    x; \});
  for(const int &v : G[u])
    if(!b[v] or kuhn(b[v]))
      return b[v] = u;
  return 0;
```

```
int main()
{
    //srand(time(NULL));
    cin >> na >> nb >> m;
    while(m--)
    {
        int u, v;
        cin >> u >> v;
        G[u].push_back(v + na);
    }
    tempo = 1;
    int ans = 0;
    for(int i = 1; i <= na; i++)
        ans += kuhn(i), tempo++;
    cout << "MCBM = " << ans << '\n';
    for(int i = nb + 1; i <= na + nb; i++)
        if(b[i])
        cout << b[i] << ' ' << i - na << '\n';
        return 0;
}</pre>
```

1.19 Lca With Square Root Decomposition

```
#include <bits/stdc++.h>
const int MAX = 50500;
using namespace std;
vector<int> G[MAX];
int nivel[MAX], pai[MAX], jump[MAX], n, blk_sz;
void dfs(int v, int d, int p)
    pai[v] = p;
    nivel[v] = d;
    (nivel[v] blk_sz == 0) ? jump[v] = pai[v] : jump[v] = jump[p];
    for(const int &u : G[v])
        if(u != p)
            dfs(u, d + 1, v);
int lcaTrivial(int u, int v)
    while(u != v)
        (nivel[u] > nivel[v]) ? u = pai[u] : v = pai[v];
    return u;
int lca(int u. int v)
    while(jump[u] != jump[v])
        (nivel[u] > nivel[v]) ? u = jump[u] : v = jump[v];
    return lcaTrivial(u, v);
void build()
```

```
{
    blk_sz = sqrt(n);
    dfs(0, 0, 0);
}
int main()
{
    int x, y;
    cin >> n;
    for(int i = 0; i < n-1; i++)
    {
        cin >> x >> y;
        G[x-1].push_back(y-1);
        G[y-1].push_back(x-1);
    }
    build();
    cin >> x >> y;
    cout << lca(x-1, y-1) + 1 << '\n';
    return 0;
}</pre>
```

1.20 Lca With Tree Linearization And Segment Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int pos[MAX];
int deft[MAX];
int seqtree[5*MAX];
vector<int> tl;
vector<int> G[MAX];
void tree_linearization(int v, int p, int d)
 deft[v] = d;
  pos[v] = tl.size();
  tl.push_back(v);
  for (const int &u : G[v])
    if(u != p)
      tree_linearization(u, v, d + 1);
      tl.push_back(v);
void build(int node, int start, int end)
  if (start == end)
    segtree[node] = tl[start];
  else
    int mid = (start+end)/2;
    build(2*node, start, mid);
    build(2*node+1, mid+1, end);
    if (deft[segtree[2*node]] < deft[segtree[2*node+1]])</pre>
      segtree[node] = segtree[2*node];
    else
      segtree[node] = segtree[2*node+1];
```

```
int lca(int node, int start, int end, int l, int r)
  if(l > end or r < start)</pre>
    return -1;
  if(l <= start and end <= r)</pre>
    return segtree[node];
  int mid = (start+end)/2;
  int p1 = lca(2*node, start, mid, l, r);
  int p2 = lca(2*node+1, mid+1, end, l, r);
  if (p1 == -1) return p2;
  if(p2 == -1) return p1;
  return deft[p1] < deft[p2] ? p1 : p2;</pre>
/*int _lca(int a, int b)
  int ancestor = a, nivel = 0x3f3f3f3f;
  for (int i = pos[a]; i \le pos[b]; i++)
    if(deft[tl[i]] < nivel)</pre>
      ancestor = tl[i];
      nivel = deft[tl[i]];
  return ancestor;
} */
int main()
  int n, u, v;
  cin >> n;
  for (int i = 0; i < n-1; i++)
    cin >> u >> v;
    G[u].push_back(v);
    G[v].push_back(u);
  tree_linearization(1, -1, 0);
  build(1, 0, tl.size()-1);
  for (int i = 1; i \le n; i++)
    cout << deft[i] << ' ';
  cout << '\n';
  for(int i = 1; i <= n; i++)
    cout << pos[i] << ' ';
  cout << '\n';
  for(const int &p : tl)
   cout << p << ' ';
  cout << '\n';
  for (int i = 1; i \le 4*n; i++)
   cout << segtree[i] << ' ';</pre>
  cout << '\n'; */
  while(cin >> u >> v)
```

```
cout << /*_lca(u, v) << ' ' <<*/
    lca(1, 0, tl.size()-1, pos[u], pos[v]) << '\n';
return 0;
}</pre>
```

1.21 Lca With Tree Linearization And Sparse Table

```
#include <bits/stdc++.h>
using namespace std:
const int MAX = 1e5 + 10;
int n, m;
vector<int> G[MAX], tl;
int deft[MAX], SpT[27][MAX], pos[MAX];
void tree_linearization(int v, int p, int d)
  deft[v] = d;
  pos[v] = tl.size();
  tl.push_back(v);
  for(int &u : G[v])
    if(u != p)
      tree_linearization(u, v, d + 1);
      tl.push_back(v);
void build(int tam)
  for(int i = 0; (1 << i) <= tam; i++)</pre>
    for(int j = 0; j + (1 << i) <= tam; <math>j++)
      if(!i)
        SpT[i][j] = tl[j];
      else if(deft[SpT[i-1][j]] < deft[SpT[i-1][j+(1<<(i-1))]])</pre>
        SpT[i][j] = SpT[i-1][j];
      else
        SpT[i][j] = SpT[i-1][j+(1<<(i-1))];
int lca(int i, int j)
  int k = log2(j-i+1);
  if (deft[SpT[k][i]] < deft[SpT[k][j+1-(1<<k)]])</pre>
    return SpT[k][i];
    return SpT[k][j+1-(1<<k)];
int main()
    int u, v, q;
  cin >> n >> m;
  for(int i = 0; i < m; i++)</pre>
```

```
{
    cin >> u >> v;
    G[u].push_back(v);
    G[v].push_back(u);
}

tree_linearization(1, -1, 0);
build(tl.size());

cin >> q;
while(q--)
{
    cin >> u >> v;
    cout << lca(min(pos[u], pos[v]), max(pos[u], pos[v])) << '\n';
}

return 0;
}</pre>
```

1.22 Longest And Shortest Path In DAG

```
#include <bits/stdc++.h>
const int 00 = 0x3f3f3f3f3f;
const int MAX = 1e6;
using namespace std;
int n, m;
vector<pair<int, int>> G[MAX];
int dist1[MAX], dist2[MAX];
vector<int> ts;
bool cor[MAX];
void dfs(int v)
  cor[v] = true;
  for(pair<int, int> &w : G[v])
    if(!cor[w.first])
      dfs(w.first);
  ts.push_back(v);
// caminho de 0 a n-1
pair<int, int> longestAndShortestPathInDAG()
  for(int i = 0; i <= n; i++)</pre>
    dist1[i] = -00, dist2[i] = 00;
  dist1[0] = dist2[0] = 0;
  int p = 0;
  while(p < (int)ts.size())</pre>
    int v = ts[p++];
    if(dist1[v] != -00)
      for (int i = 0; i < (int)G[v].size(); i++)
        int u = G[v][i].first, d = G[v][i].second;
        if(dist1[u] < dist1[v] + d)
          dist1[u] = dist1[v] + d;
```

```
if(dist2[v] != 00)
      for(int i = 0; i < (int)G[v].size(); i++)</pre>
        int u = G[v][i].first, d = G[v][i].second;
        if(dist2[u] > dist2[v] + d)
          dist2[u] = dist2[v] + d;
  return {dist1[n-1], dist2[n-1]};
int main()
  cin >> n >> m;
  for(int i = 0; i < m; i++)</pre>
    int u, v, w;
    cin >> u >> v >> w; u--; v--;
    G[u].push back({v, w});
  for(int i = 0; i < n; i++)</pre>
    if(!cor[i])
      dfs(i);
  reverse(ts.begin(), ts.end());
  pair<int, int> ans = longestAndShortestPathInDAG();
  cout << "Longest Path " << ans.first << '\n';</pre>
  cout << "Shortest Path " << ans.second << '\n';</pre>
  return 0;
```

1.23 MCE MinimumEdgeCover

```
#include <bits/stdc++.h>
using namespace std;
vector<int> G[1000];
int b[1000], vis[1000], tempo;
bool kuhn (int v)
  if(vis[v] == tempo)
    return 0;
  vis[v] = tempo;
  for(const int &u : G[v])
    if(!b[u] or kuhn(b[u]))
      return b[u] = v;
  return 0;
int main()
  int n, m, e;
  cin >> n >> m >> e;
  while (e--)
    int u, v;
    cin >> u >> v;
    G[u].push_back(v + n);
```

```
int ans = 0;
tempo = 1;
for(int i = 1; i <= n; i++)</pre>
 ans += kuhn(i), tempo++;
//encontrar as arestas do Minimum Edge Cover
vector<bool> covered(n + m + 10, false);
 vector<pair<int, int>> cover;
for(int i = n + 1; i <= n + m; i++)</pre>
 if(b[i])
    covered[b[i]] = covered[i] = true;
    cover.push_back({b[i], i - n});
for(int i = 1; i <= n; i++)</pre>
 bool is_covered = covered[i];
  for(const int &u : G[i])
    if(!covered[u])
      is covered = true;
      cover.push_back({i, u - n});
      covered[i] = covered[u] = true;
 if(!is_covered and !G[i].empty())
    cover.push_back({i, G[i].front() - n});
cout << "MEC = " << cover.size() << '\n';</pre>
for(int i = 0; i < cover.size(); i++)</pre>
 cout << cover[i].first << ' ' << cover[i].second << '\n';</pre>
 return 0;
```

1.24 MPC MinimumPathCover

```
#include <bits/stdc++.h>
using namespace std;

int n, m;
vector<int> G[1000], bip[1000], ts;
int vis[1000], b[1000], go[1000], tempo = 1;

bool kuhn(int v)
{
   if(vis[v] == tempo)
      return 0;
   vis[v] = tempo;
   for(const int &u : bip[v])
      if(!b[u] or kuhn(b[u]))
      {
        go[v] = u - n;
        return b[u] = v;
      }
   return 0;
}

void topological_sort(int v)
```

```
vis[v] = tempo;
  for(const int &u : G[v])
    if(vis[u] != tempo)
      topological_sort(u);
  ts.push_back(v);
int main()
  cin >> n >> m;
  while (m--)
    int u, v;
    cin >> u >> v;
    G[u].push_back(v);
    bip[u].push_back(v + n);
  int ans = 0;
  for(int i = 1; i <= n; i++)
    ans += kuhn(i), tempo++;
  for(int i = 1; i <= n; i++)</pre>
    if(vis[i] != tempo)
      topological_sort(i);
  reverse(ts.begin(), ts.end());
  tempo++;
  cout << n - ans << '\n';
  for(int i = 0; i < n; i++)</pre>
    int u = ts[i];
    if(vis[u] != tempo)
      while (u)
        vis[u] = tempo;
        cout << u << ' ';
        u = qo[u];
      puts("");
    return 0;
```

1.25 MVC MinimumVertexCover

```
#include <bits/stdc++.h>
using namespace std;

vector<int> G[1000];
int b[1000], vis[1000], tempo;
bool be[1000];
set<int> r0, r1;

bool kuhn(int v)
{
  if(vis[v] == tempo)
    return 0;
  vis[v] = tempo;
  for(const int &u : G[v])
```

```
if(!b[u] or kuhn(b[u]))
      return b[u] = v;
  return 0;
void MVC(int v)
  if(vis[v] == tempo)
    return;
  vis[v] = tempo;
  for(const int u : G[v])
    if(b[u] != v and b[u])
      rl.insert(u);
      vis[b[u]] = tempo;
int main()
  int n, m, e;
  cin >> n >> m >> e;
  while (e--)
    int u, v;
    cin >> u >> v;
    G[u].push back(v);
  int ans = 0;
  tempo = 1;
  for(int i = 1; i <= n; i++)</pre>
    ans += kuhn(i), tempo++;
  for(int i = n + 1; i <= n + m; i++)</pre>
    if(b[i])
      be[i - n] = be[b[i]] = true;
  for(int i = 1; i <= n; i++)</pre>
    if(!be[i])
      MVC(i);
  for(int i = 1 ; i <= n; i++)</pre>
    if(vis[i] < tempo)</pre>
      r0.insert(i);
  cout << "MVC = "<< ans << '\n';
  cout << "tamanho lado esquerdo " << r0.size() << '\n';</pre>
  for(auto it = r0.begin(); it != r0.end(); it++)
    cout << *it << ' ';
  puts("");
  cout << "tamanho lado direito " << r1.size() << '\n';</pre>
  for(auto it = r1.begin(); it != r1.end(); it++)
    cout << *it - n << ' ';
  puts("");
    return 0;
```

1.26 Maximum Clique

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
const int MAX = 43, C = 20;
```

```
int n, m, dp[1 << C];</pre>
11 G[MAX];
int maxClique()
  for (int i = 1; i < (1 << max(0, n - C)); i++)
    int x = i;
    for (int j = 0; j < max(0, n - C); j++)
     if((i >> j) & 1)
        x \&= G[j + C] >> C;
    if(x == i) dp[i] = __builtin_popcount(i);
  for (int i = 1; i < (1 << max(0, n - C)); i++)
    for (int j = 0; j < max(0, n - C); j++)
      if((i >> j) & 1)
        dp[i] = max(dp[i], dp[i ^ (1 << j)]);
  int ans = 0;
  for(int i = 0; i < (1 << min(C, n)); i++) {</pre>
    int x = i, y = (1 << max(0, n - C)) - 1;
    for (int j = 0; j < min(C, n); j++)
     if((i >> j) & 1)
        x \&= G[j], y \&= G[j] >> C;
    if(x == i)
        ans = max(ans, __builtin_popcount(i) + dp[y]);
  return ans;
int main()
    cin >> n >> m;
    while (m--)
        int u, v;
        cin >> u >> v; u--; v--;
        G[u] = (1LL << v);
        G[v] = (1LL << u);
    for(int i = 0; i < n; i++)</pre>
        G[i] = (1LL << i);
    cout << maxClique() << '\n';</pre>
  return 0;
```

1.27 Min Cost Max Flow

```
/*
  * from IME Library
  */
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
const int 00 = 0x3f3f3f3f;
struct edge {int v, f, w, c; };
```

```
// flw_lmt eh a quantidade de de fluxo que posso passar
// no maximo, alterar se necessario
// node count eh o valor do maior vertice no grafo...
// inicializar node_count com numero de vertices no inicio...
int node_count, flw_lmt = 00, p[MAX];
vector<edge> edges;
vector<int> G[MAX];
// u--->v, custo w e capacidade c
void add_edge(int u, int v, int w, int c)
  int k = edges.size();
 node_count = max(node_count, u+1);
  node_count = max(node_count, v+1);
 G[u].push_back(k);
  G[v].push_back(k+1);
 edges.push_back({ v, 0, w, c });
  edges.push_back({ u, 0, -w, 0 });
void clear()
  flw lmt = 00;
  for(int i = 0; i < node_count; ++i) G[i].clear();</pre>
  edges.clear();
  node_count = 0;
bool SPFA(int s, int t)
  vector<int> dist(node_count, 00);
  vector<int> et(node_count, 0);
  deque<int> q;
  q.push_back(s), dist[s] = 0;
  while (!q.empty())
    int u = q.front(); q.pop_front();
   et[u] = 2;
    for(int i : G[u])
      edge &e = edges[i];
      int v = e.v;
      if (e.f < e.c and dist[v] > dist[u] + e.w)
        dist[v] = dist[u] + e.w;
        if (et[v] == 0) q.push_back(v);
        else if (et[v] == 2) q.push_front(v);
        et[v] = 1;
        p[v] = i;
  return dist[t] != 00;
int min_cost_max_flow(int s, int t)
  int mf = 0, cost = 0;
    while(SPFA(s, t) and mf < flw_lmt)</pre>
    int inc = flw_lmt - mf;
```

1.28 Prim

```
#include <bits/stdc++.h>
using namespace std:
const int MAX = 1e5;
const int 00 = 0x3f3f3f3f3f;
typedef pair<int, int> ii;
typedef pair<int, ii> iii;
int n, m;
vector<ii> G[MAX];
int dist[MAX], edge[MAX];
bool visit[MAX];
void prim(int s)
    memset(visit, 0, sizeof(visit));
    memset(dist, 63, sizeof(dist));
    dist[s] = 0;
    priority_queue<ii> pq;
    pq.push({0, s});
    while(!pq.empty())
        int u = pq.top().second;
        pq.pop();
        if(visit[u]) continue;
        for(int i = 0; i < G[u].size(); i++)</pre>
            int v = G[u][i].second, d = G[u][i].first;
            if(!visit[v] and dist[v] > d)
                dist[v] = d;
                edge[v] = u;
```

```
pq.push({-d, v});
        visit[u] = true;
    int ans = 0;
    edge[s] = -2;
    for(int i = 0; i < n; i++)
        cout << edge[i]+1 << ' ';
        ans += dist[i];
    cout << '\n';
    cout << ans << '\n';
int main()
    int u, v, w;
    cin >> n >> m;
    while (m--)
        cin >> u >> v >> w; u--; v--;
        G[u].push_back(\{w, v\});
        G[v].push_back({w, u});
    prim(0);
    return 0;
```

1.29 Tree Isomorfism

```
#include <bits/stdc++.h>
using namespace std;

const int ms = 100100;

int degree[ms], vis[ms];
int size[ms];
int n;

bool cmp(int a, int b)
{
  return size[a] < size[b];
}

void pre(vector<vector<int>>> &edges, int on = 0)
{
  size[on] = 1;
  for(auto to : edges[on])
  {
    pre(edges, to);
    size[on] += size[to];
  }
  sort(edges[on].begin(), edges[on].end(), cmp);
}

void solve(vector<vector<int>>> &edges, string &str, int on = 0)
```

```
str += 'D';
  for(int l = 0, r = 0; l < edges[on].size(); l = r) {</pre>
    while(r < edges[on].size() &&</pre>
      size[edges[on][l]] == size[edges[on][r]]) r++;
    if(r == 1 + 1)
      solve(edges, str, edges[on][1]);
    else
      priority_queue<string> hp;
      for(int i = 1; i < r; i++) {</pre>
        string temp;
        solve(edges, temp, edges[on][i]);
        hp.push(temp);
      while (!hp.empty())
        str += hp.top();
        hp.pop();
  str += 'U';
// enraizar arvore
void mount(vector<vector<int>> &graph,
  vector<vector<int>> &G, int v = 0, int p = -1)
  for(int &u : G[v])
    if(u != p)
      graph[v].push_back(u);
      mount (graph, G, u, v);
// achar centro da arvore e enraizar no centro
void findCenterAndComputeStr(vector<vector<int>> &graph,
  vector<vector<int>> &G, string *str)
  memset(vis, 0, sizeof(vis));
  queue<int> fila[2];
  for(int i = 0; i < n; i++)</pre>
    if(degree[i] == 1)
      fila[0].push(i);
  int cnt = 0, turn = 0;
  while (cnt + 2 < n)
    while(!fila[turn].empty())
      int u = fila[turn].front(); fila[turn].pop();
      vis[u] = true;
      cnt++;
      for(int i = 0; i < G[u].size(); i++)</pre>
        if(!vis[G[u][i]])
          degree[G[u][i]]--;
          if(degree[G[u][i]] == 1)
            fila[1-turn].push(G[u][i]);
```

```
turn ^= 1;
  int k = 0;
  for (int i = 0; i < n; i++)
    if(vis[i]) continue;
    graph.clear();
    graph.resize(n + 1);
    mount(graph, G, i);
    pre(graph, i);
    solve(graph, str[k], i);
    k++;
int main()
  while(cin >> n)
    string str[2][2];
    for(int i = 0; i < 2; i++)
      vector<vector<int>> graph, G;
      G.resize(n + 1);
      memset(degree, 0, sizeof(degree));
      for (int j = 1; j < n; j++)
        int u, v;
        scanf(" %d %d", &u, &v); v--; u--;
        G[v].push_back(u);
        G[u].push_back(v);
        degree[v]++;
        degree[u]++;
      findCenterAndComputeStr(graph, G, str[i]);
    bool fl = (str[0][0] == str[1][0]) or (str[0][0] == str[1][1]);
    fl |= ((str[0][1] == str[1][0]) or (str[0][0] == str[1][1]));
    puts(fl ? "S" : "N");
  return 0;
```

2 Data Structures

2.1 BIT 1D

```
#include <bits/stdc++.h>
using namespace std;

int aux, n, arr[1000], BIT[1000];

// construir uma BIT a partir de um array em O(N)
void build() {
  for(int i = 1; i <= n; i++) {</pre>
```

```
BIT[i] += arr[i];
    if(i + (i \& -i) \le n)
      BIT[i + (i \& -i)] += BIT[i];
}
// construir o array que gera a BIT a partir de uma BIT em O(N)
void buildArray() {
  for(int i = n; i >= 1; i--)
    if(i + (i & -i) <= n)
      BIT[i + (i \& -i)] -= BIT[i];
int sum(int x) {
    int s = 0:
    while (x) s += BIT[x], x -= x\&-x;
    return s:
void update(int x, int value) {
    while (x \le n) BIT [x] += value, x += x\&-x;
int main() {
    cin >> n;
    for(int i = 1; i <= n; i++) {
        cin >> aux;
        update(i, aux);
    int a, b;
    cin >> a >> b;
    cout << sum(b) -sum(a-1) << ' \n';
    return 0;
```

2.2 BIT 2D

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
int n, aux, BIT[MAX][MAX];

void update(int x, int y, int value)
{
  for(int i = x; i <= n; i += i&-i)
    for(int j = y; j <= n; j += j&-j)
    BIT[i][j] += value;
}

int query(int x, int y)
{
  int sum = 0;
  for(int i = x; i > 0; i -= i&-i)
    for(int j = y; j > 0; j -= j&-j)
        sum += BIT[i][j];
  return sum;
}
```

```
int queryInRectangle(int x1, int y1, int x2, int y2)
  int sum = 0;
  sum += query (max(x1, x2), max(y1, y2));
  sum -= query (max (x1, x2), min (y1, y2) - 1);
  sum -= query(min(x1, x2) - 1, max(y1, y2));
  sum += query (min (x1, x2) - 1, min (y1, y2) - 1);
  return sum;
int main()
  cin >> n:
  for(int i = 1; i <= n; i++)</pre>
   for(int j = 1; j <= n; j++)</pre>
      cin >> aux, update(i, j, aux);
  int x1, y1, x2, y2;
  while(cin >> x1 >> y1 >> x2 >> y2)
    cout << queryInRectangle(x1, y1, x2, y2) << '\n';</pre>
  return 0;
```

2.3 BIT Range Sum And Range Update

```
#include <bits/stdc++.h>
const int MAX = 1e5;
using namespace std;
struct BIT {
  int N:
  int BIT1[MAX];
  int BIT2[MAX];
  BIT (int M) {
   N = M;
  void add(int *b, int pos, int x) {
    while(pos <= N) b[pos] += x, pos += pos&-pos;</pre>
  void range_add(int 1, int r, int x) {
   add(BIT1, l, x);
   add(BIT1, r + 1, -x);
    add(BIT2, 1, x * (1 - 1));
   add(BIT2, r + 1, -x * r);
  int sum(int *b, int pos) {
    int s = 0;
    while(pos) s += b[pos], pos -= pos&-pos;
    return s;
  int prefix_sum(int pos) {
    return sum(BIT1, pos) * pos - sum(BIT2, pos);
```

```
int range_sum(int 1, int r) {
    return prefix_sum(r) - prefix_sum(l - 1);
};
int main() {
  int n, q;
  cin >> n >> q;
  BIT B(n);
  while(q--) {
   int o, 1, r, x;
    cin >> o >> l >> r;
    if(0 == 1) {
      cout << B.range_sum(l, r) << '\n';</pre>
    } else {
      cin >> x;
        B.range_add(l, r, x);
  return 0;
```

2.4 Centroid Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;
int n, m, Centroid_Tree[MAX], Size[MAX];
vector<int> G[MAX], cTree[MAX];
bool cut[MAX];
int dfs(int v, int p)
  int s = 1;
  for(const int &u : G[v])
   if(!cut[u] and u != p)
      s += dfs(u, v);
  return Size[v] = s;
int Find_Centroid(int v, int p, int tot)
  int next, cnt = 0;
  for (const int &u : G[v])
    if(!cut[u] and u != p and cnt < Size[u])</pre>
      cnt = Size[u]:
      next = u;
  if(cnt > tot/2) return Find_Centroid(next, v, tot);
  return v;
void build(int v, int p)
```

```
dfs(v, -1);
  int u = Find_Centroid(v, -1, Size[v]);
  cut[u] = true;
  Centroid_Tree[u] = p;
  if (p ! = -1)
      cTree[u].push_back(p);
      cTree[p].push back(u);
  for(const int &w : G[u])
    if(!cut[w])
      build(w, u);
int main()
    int u, v;
  memset (Centroid Tree, -1, sizeof Centroid Tree);
    cin >> n >> m;
    while (m--)
      cin >> u >> v;
      u--; v--;
    G[u].push_back(v);
    G[v].push_back(u);
 build(0, -1);
    for (int i = 0; i < n; i++)
        cout << i+1 << ": ";
        for(int &w : cTree[i])
            cout << w+1 << ' ';
        cout << '\n';
  return 0:
```

2.5 Color Update

```
#include <bits/stdc++.h>
using namespace std;

#define bug(x) cout << #x << " >>>>>> " << x << '\n'
#define _ << " , " <<
    #define INF 0x3f3f3f3f

#define ii pair<int, int>
#define fi first
#define se second

struct Color {
   int x;
   Color(int _x) : x(_x) {}
   Color() : x(-1) {}
   bool operator<(const Color &c) const {
      return x < c.x;
   }
};</pre>
```

```
#define iic pair<pair<int, int>, Color>
#define defaut color Color(-1)
struct ColorUpdate {
 set<iic> intervals;
 ColorUpdate(int begin = -INF, int end = INF) {
    intervals.insert( { {begin, end}, defaut color } );
  void paint(int 1, int r, Color c = defaut_color) {
   if(1 > r) return;
    auto a = prev(intervals.upper_bound({{l, INF}, INF}));
   auto b = prev(intervals.upper_bound({{r, INF}, INF}));
   int l1 = a->fi.fi, r1 = l - 1;
   Color c1 = a \rightarrow se:
   int 12 = r + 1, r2 = b->fi.se;
   Color c2 = b \rightarrow se:
    intervals.erase(a, next(b));
   if(l1 <= r1) intervals.insert({{l1, r1}, c1});</pre>
   if(12 <= r2) intervals.insert({{12, r2}, c2});</pre>
   if(l <= r) intervals.insert({{l, r}, c});</pre>
   // printall();
 Color get color of (int x) {
    return prev(intervals.upper_bound({{x, INF}, INF}))->se;
  // true if x is in some interval
 bool find(int x) {
    auto a = intervals.upper_bound({{x, INF}, INF});
   if(a == intervals.begin()) return false;
   if(a->fi.fi > x or a->fi.se < x) return false;</pre>
    return true;
 ii get_interval_of(int x) {
   if(!find(x)) return {-INF, INF};
    return prev(intervals.upper_bound({{x, INF}, INF}))->fi;
 ii get_interval_of(int l, int r) {
   if(!find(l)) return {-INF, INF};
   ii i = get_interval_of(l);
   if(i.fi <= r and r <= i.se) return i;</pre>
    return {-INF, INF};
  // x will be on the left side
 void cut at(int x) {
   if(!find(x)) return;
    auto a = prev(intervals.upper_bound({{x, INF}, INF}));
```

```
Color c = a -> se;
    int l1 = a->fi.fi, r1 = x;
    int 12 = x + 1, r2 = a->fi.se;
    intervals.erase(a);
    if(l1 <= r1) intervals.insert({{l1, r1}, c});</pre>
    if(12 <= r2) intervals.insert({{12, r2}, c});</pre>
  void remove_interval(int 1, int r) {
    cut_at(1 - 1);
    cut_at(r);
    auto a = prev(intervals.upper_bound({{l, INF}, INF}));
    auto b = prev(intervals.upper_bound({{r, INF}, INF}));
    intervals.erase(a, next(b));
  void remove_at(int x) {
    remove interval(x, x);
  void p_interval(iic i) {
    cout << "elements from " << i.fi.fi << " to " << i.fi.se;</pre>
    cout << " have color " << i.se.x << endl;</pre>
  void printall() {
    cout << "\n\n\nColor Of The Elements:\n";</pre>
    for(auto it : intervals)
      p_interval(it);
    cout << endl << endl;</pre>
};
int32_t main() {
  ios_base::sync_with_stdio(false);
  cin.tie(nullptr);
  ColorUpdate C(1, 100);
  for(int i = 3; i <= 50; i += 10)
    C.cut_at(i);
  C.remove_interval(16, 57);
  C.remove_at (100);
  C.remove_at(1);
  C.remove at (2);
  C.remove_at(3);
  C.cut_at(20);
  C.printall();
  return 0;
```

2.6 DSU With Partial Persistence

```
int n, pai[MAX], sz[MAX], his[MAX], tempo;
void init()
  tempo = 0;
  for(int i = 0; i < n; i++)</pre>
    pai[i] = i, sz[i] = 1, his[i] = 0;
int find(int x, int t)
  if(pai[x] == x) return x;
  if(his[x] > t) return x;
  return find(pai[x], t);
void join(int u, int v)
  tempo++;
 u = find(u, tempo);
  v = find(v, tempo);
  if(sz[u] > sz[v]) swap(u, v);
  pai[u] = v;
  his[u] = tempo;
  sz[v] += sz[u];
```

2.7 Dynamic Segment Tree With Lazy Propagation

```
#include <bits/stdc++.h>
using namespace std;

struct Node
{
   int l, r, value;
};

vector<Node> tree;
vector<int> lazy;

int init()
{
   tree.clear();
   lazy.clear();
   tree.emplace_back();
   lazy.push_back(0);
}

void createL(int node)
{
   tree[node].l = tree.size();
   tree.emplace_back();
   lazy.push_back(0);
}
```

```
void createR(int node)
  tree[node].r = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void calc(int node)
  tree[node].value = 0;
  if(tree[node].l) tree[node].value += tree[tree[node].l].value;
  if(tree[node].r) tree[node].value += tree[tree[node].r].value;
void push(int node, int start, int end)
  // +=
  tree[node].value = lazy[node] * (end - start + 1);
  if(start != end)
    if(tree[node].l == 0) createL(node);
    if(tree[node].r == 0) createR(node);
    lazy[tree[node].l] = lazy[node]; // +=
   lazy[tree[node].r] = lazy[node]; // +=
  lazy[node] = 0;
void update (int node, int start, int end, int l, int r, int value)
  if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return;
  if(1 <= start and end <= r)</pre>
    tree[node].value = value * (end - start + 1); // +=
    if(start != end)
      if(tree[node].l == 0) createL(node);
      if(tree[node].r == 0) createR(node);
      lazy[tree[node].1] = value; // +=
      lazy[tree[node].r] = value; // +=
  else
    int mid = (start + end) / 2;
    if(tree[node].l == 0) createL(node);
    update(tree[node].l, start, mid, l, r, value);
    if(tree[node].r == 0) createR(node);
    update(tree[node].r, mid + 1, end, 1, r, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
```

```
push (node, start, end);
  if(start > r or l > end) return 0;
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
int main()
  int n, q;
  cin >> n >> q;
  init();
  for(int i = 0; i < n; i++)</pre>
    int x;
    cin >> x;
    update(0, 0, n - 1, i, i, x);
  while (q--)
    int o, l, r, x;
    cin >> o >> l >> r;
    if(0 == 1)
      cin >> x;
      update(0, 0, n - 1, l - 1, r - 1, x);
    else
      cout << query (0, 0, n - 1, 1 - 1, r - 1) <math><< ' \ '';
  return 0;
```

2.8 Dynamic Segment Tree With Vector

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

struct Node
{
   int 1, r, value;
};

vector<Node> tree;

int init()
{
   tree.emplace_back();
}

void calc(int node)
{
```

```
tree[node].value = 0;
  if(tree[node].1) tree[node].value += tree[tree[node].1].value;
  if(tree[node].r) tree[node].value += tree[tree[node].r].value;
void update(int node, int start, int end, int idx, int value)
  if(start == end)
    tree[node].value = value;
  else
    int mid = (start + end) / 2;
    if(start <= idx and idx <= mid)</pre>
      if(tree[node].1 == 0)
       tree[node].l = tree.size();
        tree.emplace_back();
      update(tree[node].l, start, mid, idx, value);
    else
      if(tree[node].r == 0)
        tree[node].r = tree.size();
        tree.emplace back();
      update(tree[node].r, mid + 1, end, idx, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(l > end or r < start) return 0;</pre>
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
int main()
 int n, q;
  cin >> n >> q;
  init();
  while (q--)
    int o, 1, r;
    cin >> o >> l >> r;
   if(o == 1) update(0, 0, n - 1, 1 - 1, r);
    else cout << query(0, 0, n - 1, 1 - 1, r - 1) << '\n';
  return 0:
```

2.9 Heavy Light Decomposition Path And Subtree Queries

```
/*
no intervalo [ in[v], out[v] ) do array A
temos a subarvore de v. Para fazer consultas
basta usar a segtree.
no intervalo [ in[nxt[v]], in[v] ] temos os vertices no
caminho de nxt[v] ate v, Em que nxt[v] esta no inicio da
cadeia da HLD. e o caminho de nxt[v] ate v faz parte da
cadeia que comeca em nxt[v].
Assim, podemos processar queries rapidamente em caminhos
e subarvores usando a mesma segment tree.
Bonus: para uma query de mudanca de raiz: se a raiz atual
for v e a consulta for na subarvore de u, entao, se u for
ancestral de v a resposta eh a consulta da arvore
total menos a consulta da subarvore enraizada pelo filho
de u que eh ancestral de v, caso contrario a consulta eh
normal como se a raiz da arvore nunca tivesse mudado.
obs: Para encontrar o filho de u que eh ancestral de v
podemos usar binary lifting, da mesma forma que usamos
para calcular lca.
*/
#include <bits/stdc++.h>
using namespace std:
const int MAX = 5 * 1e5;
int n;
vector<int> Adj[MAX], G[MAX], A;
int in[MAX], out[MAX], rin[MAX], sz[MAX], nxt[MAX], arr[MAX], t = 0;
int st[MAX], lazy[MAX], val_vertex[MAX], depth[MAX], father[MAX];
void mount (int v = 0, int p = -1)
  for(int &u : Adj[v])
   if(u != p)
      G[v].push_back(u);
      mount(u, v);
void dfs_sz(int v = 0, int p = 0, int d = 0)
    sz[v] = 1;
   depth[v] = d;
    father[v] = p;
    for(int &u: G[v])
    if(u == p) continue;
       dfs_sz(u, v, d + 1);
       sz[v] += sz[u];
       if(sz[u] > sz[G[v][0]])
            swap(u, G[v][0]);
```

```
void dfs_hld(int v = 0, int p = -1)
    in[v] = t++;
  rin[in[v]] = v;
    A.push_back(val_vertex[v]);
    for(int u: G[v])
      if(u == p) continue;
        nxt[u] = (u == G[v][0] ? nxt[v] : u);
        dfs_hld(u, v);
                                                                                 return 0:
    out[v] = t;
void build(int node, int start, int end)
  if(start == end)
    st[node] = A[start];
    int mid = (start + end) / 2;
    build(2 * node, start, mid);
   build(2 * node + 1, mid + 1, end);
    st[node] = st[2 * node] + st[2 * node + 1];
                                                                                 else
void update (int node, int start, int end, int l, int r, int value)
  if(lazy[node])
    st[node] += (end - start + 1) * lazy[node];
                                                                               while(true)
    if(start != end)
      lazy[2 * node] += lazy[node];
      lazy[2 * node + 1] += lazy[node];
    lazy[node] = 0;
  if(l > end or start > r)
    return:
  if(l <= start and end <= r)</pre>
    st[node] += value * (end - start + 1);
    if(start != end)
      lazy[2 * node] += value;
      lazy[2 * node + 1] += value;
    return;
  int mid = (start + end) / 2;
  update(2 * node, start, mid, 1, r, value);
  update(2 * node + 1, mid + 1, end, 1, r, value);
  st[node] = st[2 * node] + st[2 * node + 1];
                                                                               int ans = 0;
                                                                               while(true)
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
                                                                                   ans += query(1, 0, n - 1, in[1], in[u]);
```

```
st[node] += (end - start + 1) * lazy[node];
    if(start != end)
      lazy[2 * node] += lazy[node];
     lazy[2 * node + 1] += lazy[node];
    lazy[node] = 0;
  if(l > end or start > r)
  if(l <= start and end <= r)</pre>
    return st[node];
  int mid = (start + end) / 2;
  int q1 = query(2 * node, start, mid, l, r);
  int q2 = query(2 * node + 1, mid + 1, end, 1, r);
  return q1 + q2;
int lca(int u, int v)
  while(nxt[u] != nxt[v])
    if(depth[nxt[u]] < depth[nxt[v]])</pre>
     v = father[nxt[v]];
      u = father[nxt[u]];
  return depth[u] < depth[v] ? u : v;
void update_up(int u, int l, int value)
    if(nxt[u] == nxt[l])
      update(1, 0, n - 1, in[1], in[u], value);
    update(1, 0, n - 1, in[nxt[u]], in[u], value);
    u = father[nxt[u]];
// atualiza o valor de cada vertice no caminho de
void updatePath(int u, int v, int value)//u para v.
  int l = lca(u, v);
  update up(u, l, value);
  update_up(v, l, value);
  update(1, 0, n - 1, in[1], in[1], -value);
int query_up(int u, int 1)
    if(nxt[u] == nxt[l])
```

```
break;
   ans += query(1, 0, n - 1, in[nxt[u]], in[u]);
   u = father[nxt[u]];
 return ans;
//consulta a soma do valor de cada vertice no caminho
int queryPath(int u, int v)// de u para v.
 int l = lca(u, v), ans = 0;
 ans += query_up(u, 1);
 ans += query_up(v, 1);
 ans -= query(1, 0, n - 1, in[1], in[1]);
 return ans;
int main()
 int q;
 scanf(" %d %d", &n, &q);
  for(int i = 1; i < n; i++)</pre>
  {// ler a arvore em qualquer ordem
   int u, v;
   scanf(" %d %d", &u, &v); u--; v--;
   Adj[u].push_back(v);
   Adj[v].push_back(u);
 mount();// montar a arvore direcionada
 dfs sz();
 dfs_hld();
 // realizar consultas
 return 0;
```

2.10 Heavy Light Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

// Heavy-Light Decomposition
vector<int> adj[MAX];
int par[MAX], h[MAX];

int chainno, chain[MAX], head[MAX], chainpos[MAX],;
int chainsz[MAX], pos[MAX], arrsz;
int sc[MAX], sz[MAX];

void dfs(int u)
{
    sz[u] = 1, sc[u] = 0; // nodes 1-indexed (0-ind: sc[u]=-1)
    for(int v : adj[u])
        if(v != par[u])
        {
        par[v] = u, h[v] = h[u]+1, dfs(v);
    }
}
```

```
sz[u] += sz[v];
            if(sz[sc[u]] < sz[v]) sc[u] = v; // 1-indexed (0-ind: sc[u])
                1<0 or ...)
void hld(int u)
    if(!head[chainno]) head[chainno] = u; // 1-indexed
    chain[u] = chainno;
    chainpos[u] = chainsz[chainno];
    chainsz[chainno]++;
    pos[u] = ++arrsz;
    if(sc[u]) hld(sc[u]);
    for(int v : adj[u]) if(v != par[u] and v != sc[u]) chainno++, hld(
int lca(int u, int v)
    while(chain[u] != chain[v])
        if(h[head[chain[u]]] < h[head[chain[v]]]) swap(u, v);</pre>
        u = par[head[chain[u]]];
    if(h[u] > h[v]) swap(u, v);
    return u;
/*int query_up(int u, int v)
    if(u == v) return 0;
    int ans = -1;
    while(true)
        if(chain[u] == chain[v])
            if (u == v) break;
            ans = max(ans, query(1, 1, n, chainpos[v]+1, chainpos[u]))
            break;
        ans = max(ans, query(1, 1, n, chainpos[head[chain[u]]],
            chainpos[u]));
        u = par[head[chain[u]]];
    return ans;
int query(int u, int v)
    int l = lca(u, v);
    return max(query_up(u, 1), query_up(v, 1));
int main()
    int n:
    cin >> n:
    for(int i = 1; i < n; i++)</pre>
```

```
int u, v;
        cin >> u >> v;
        adj[u].push_back(v);
                                                                            int lca(int u, int v)
        adj[v].push_back(u);
                                                                                while(chain[u] != chain[v])
   dfs(1);
   hld(1);
                                                                                    if (h[head[chain[u]]] < h[head[chain[v]]]) swap(u, v);</pre>
    for(int i = 1; i <= n; i++)</pre>
                                                                                    u = par[head[chain[u]]];
        cout << chain[i] << ' ';
    puts("");
                                                                                if(h[u] > h[v]) swap(u, v);
    for(int i = 1; i <= n; i++)</pre>
                                                                                return u;
        cout << chainpos[i] << ' ':</pre>
   puts("");
                                                                            void build(int node, int start, int end)
   return 0;
                                                                                if(start == end)
                                                                                    st[node] = A[start];
else
//Heavy Light Decomposition para encontrar a major aresta no
// caminho de u para v em uma arvore
                                                                                    int mid = (start + end) / 2;
                                                                                    build(2 * node, start, mid);
#include <bits/stdc++.h>
                                                                                    build(2 * node + 1, mid + 1, end);
using namespace std;
                                                                                    st[node] = max(st[2 * node], st[2 * node + 1]);
const int MAX = 1e5;
// Heavy-Light Decomposition
vector<int> adj[MAX], W[MAX];
                                                                            int query(int node, int start, int end, int 1, int r)
int par[MAX], h[MAX];
map<pair<int, int>, int> number edge;
                                                                                if(l > end or start > r)
int chainno, chain[MAX], head[MAX], A[MAX], pos[MAX];
                                                                                    return -1;
int sc[MAX], sz[MAX], weight[MAX], st[MAX], edge_counted, n;
                                                                                if(l <= start and end <= r)</pre>
                                                                                    return st[nodel:
void dfs(int u)
                                                                                int mid = (start + end) / 2;
                                                                                int q1 = query(2 * node, start, mid, l, r);
   sz[u] = 1, sc[u] = 0; // nodes 1-indexed (0-ind: sc[u]=-1)
                                                                                int q2 = query(2 * node + 1, mid + 1, end, 1, r);
    for(int i = 0; i < adj[u].size(); i++)</pre>
                                                                                return max(q1, q2);
        int v = adj[u][i], w = W[u][i];
        if(v != par[u])
                                                                            void update(int node, int start, int end, int idx, int value)
            weight[v] = w, par[v] = u, h[v] = h[u] + 1, dfs(v);
                                                                                if(start == end)
                                                                                    st[node] = A[idx] = value;
            sz[u]+=sz[v];
            if(sz[sc[u]] < sz[v]) sc[u] = v; // 1-indexed (0-ind: sc[u])
                                                                                else
                ]<0 or ...)
                                                                                    int mid = (start + end) / 2;
                                                                                    if(start <= idx and idx <= mid)</pre>
                                                                                        update(2 * node, start, mid, idx, value);
                                                                                    else
void hld(int u)
                                                                                        update (2 * node + 1, mid + 1, end, idx, value);
                                                                                    st[node] = max(st[2 * node], st[2 * node + 1]);
   if(!head[chainno]) head[chainno] = u; // 1-indexed
   chain[u] = chainno;
   pos[u] = edge_counted;
   A[edge counted++] = weight[u];
                                                                            int query_up(int u, int v)
   if(sc[u]) hld(sc[u]);
    for(int v : adj[u])
                                                                                if(u == v) return 0;
        if(v != par[u] and v != sc[u])
                                                                                int ans = -1;
                                                                                while(true)
            number_edge[{u, v}] = edge_counted;
            chainno++, hld(v);
                                                                                    if(chain[u] == chain[v])
```

```
if(u == v) break;
            ans = \max(ans, query(1, 0, n-1, pos[v] + 1, pos[u]));
            break;
        ans = max(ans, query(1, 0, n-1, pos[head[chain[u]]], pos[u]));
        u = par[head[chain[u]]];
    return ans;
int queryMaxEdge(int u, int v)
    int l = lca(u, v);
    return max(query_up(u, 1), query_up(v, 1));
void updateEdge(int u, int v, int value)
    if(number_edge.find({u, v}) != number_edge.end())
        idx = number_edge[{u, v}];
    else
        idx = number_edge[{v, u}];
    update(1, 0, n-1, idx, value);
int main()
    cin >> n;
    for(int i = 1; i < n; i++)</pre>
        int u, v, w;
        cin >> u >> v >> w;
        adj[u].push_back(v);
        adj[v].push_back(u);
        W[u].push_back(w);
        W[v].push_back(w);
    weight[1] = -1;
    dfs(1);
    hld(1);
    build(1, 0, n-1);
   int x, y, o;
    while(cin >> o >> x >> y)
        if(0 == 1)
            cout << queryMaxEdge(x, y) << '\n';</pre>
        else
            int w; cin >> w;
            updateEdge(x, y, w);
    return 0;
```

2.11 Implicit Treap

```
#include<bits/stdc++.h>
using namespace std;
```

```
struct Node
  int valor, priority, size, sum;
  Node *1, *r;
  Node(int _valor) : rev(false), sum(_valor), valor(_valor),
    priority((rand() << 16) ^ rand()), size(1), l(nullptr), r(nullptr)</pre>
  "Node() { delete 1; delete r; }
  void recalc()
    size = 1;
    sum = valor;
    if(1) size += 1->size, sum += 1->sum;
    if(r) size += r->size, sum += r->sum;
};
struct Treap
  int size(Node* t) { return t ? t->size : 0; }
  int size() const { return root ? root->size : 0; }
  Node* propagate (Node* t)
    if(t == nullptr) return t;
    if(t->rev)
      swap(t->1, t->r);
      if(t->l != nullptr) t->l->rev ^= 1;
      if(t->r != nullptr) t->r->rev ^= 1;
      t->rev = 0;
    t->recalc():
    return t;
  int position(Node *t, int n)
    //nao esta na treap, botar valor que noa esta no array...
    if(t == nullptr) return -1;
    propagate(t);
    if(n == size(t->1) + 1) return t->valor;
    else if(n <= size(t->1)) return position(t->1, n);
    else return position(t->r, n - size(t->l) - 1);
  int at(int n)
    return position(root, n);
  Node* merge(Node *1, Node *r)
    l = propagate(1);
    r = propagate(r);
    if(!l or !r) return 1 ? 1 : r;
    if(l->priority < r->priority)
```

```
1->r = merge(1->r, r);
    1->recalc();
    return 1;
  else
    r->1 = merge(1, r->1);
    r->recalc();
    return r;
void split (Node *v, int valor, Node *&l, Node *&r)
 v = propagate(v);
 l = r = nullptr;
 if(!v) return;
 if(size(v->1) < valor)</pre>
    split(v->r, valor - size(v->l) - 1, v->r, r);
    1 = v;
  }else
    split (v->1, valor, 1, v->1);
    r = v;
 v->recalc();
Node * root;
Treap() : root(nullptr) {}
~Treap() { delete root; }
void insert(int valor, int pos)
 Node * 1, * r;
 split(root, pos - 1, 1, r);
 root = merge(merge(l, new Node(valor)), r);
void erase(int valor)
 Node * 1, * m, * r;
 split(root, valor - 1, 1, m);
 split(m, 1, m, r);
 delete m;
 root = merge(1, r);
void reverse(int 1, int r)
 1--; r--;
 if(1 > r) swap(1, r);
 Node *a, *b, *c, *d;
 split(root, l, a, d);
  split(d, r - l + 1, b, c);
 if(b) b->rev ^= 1;
 root = merge(a, merge(b, c));
```

```
int query(int 1, int r)
    Node *a, *b, *c, *d;
    split(root, l - 1, a, b);
    split(b, r - l + 1, c, d);
    int ans = c->sum;
    root = merge(a, merge(c, d));
    return ans;
  /*void emOrdem(Node *node)
    if(node == nullptr) return;
    emOrdem(node->1);
   printf("%d ", node->valor);
    emOrdem(node->r);
  } */
}treap;
int main()
  srand(time(0));
  for(int i = 1; i <= 6; i++)
    int x; cin >> x;
    cout << x << ' ';
    treap.insert(x, i);
  return 0;
```

2.12 LiChao Tree

```
#include <bits/stdc++.h>
using namespace std;
#define x real
#define y imag
typedef int ftype;
typedef complex<ftype> point;
const int 00 = 0x3f3f3f3f3f;
const int maxn = 2e5;
point line[4 * maxn];
void init()
    for(int i = 0; i < 4 * maxn; i++)
        line[i] = point(0, 00);
ftype dot(point a, point b)
    return (conj(a) * b).x();
ftype f(point a, ftype x)
    return dot(a, {x, 1});
```

```
void add_line(point nw, int v = 1, int l = 0, int r = maxn)
    int m = (1 + r) / 2;
    bool lef = f(nw, 1) < f(line[v], 1);
    bool mid = f(nw, m) < f(line[v], m);</pre>
        swap(line[v], nw);
    if(r - 1 == 1)
        return;
    else if(lef != mid)
        add_line(nw, 2 * v, l, m);
    else
        add_line(nw, 2 * v + 1, m, r);
int get(int x, int v = 1, int l = 0, int r = maxn)
    int m = (1 + r) / 2;
    if(r - 1 == 1)
        return f(line[v], x);
    else if (x < m)
        return min(f(line[v], x), get(x, 2 * v, 1, m));
    else
        return min(f(line[v], x), get(x, 2 * v + 1, m, r));
int main()
    init();
    point a(2, 4);
    point b(1, 3);
    add_line(a);
    add_line(b);
    cout << get(2) << '\n';
    return 0;
```

2.13 Max Queue

```
#include <bits/stdc++.h>
using namespace std;

struct MaxQueue
{
  int plus = 0;
  deque<pair<int, int>> dq;

  bool empty()
  {
    return (int)dq.size() == 0;
  }

  void clear()
  {
```

```
plus = 0;
    dq.clear();
  void add(int x)
  { // somar x em cada elemento da fila
   plus += x;
  int max()
    return dq.begin()->first + plus;
  void push (int x)
    x -= plus;
    int amt = 0;
    while (dq.size() and dq.back().first <= x)</pre>
      amt += dq.back().second + 1, dq.pop_back();
    dq.push_back({ x, amt });
  void pop()
    if (dq.empty()) return;
    if (!dq.front().second) dq.pop_front();
    else dq.front().second--;
};
int main()
 int n, aux;
 MaxQueue Q;
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
    int aux;
    cin >> aux;
    Q.push(aux);
   cout << "max " << Q.max() << '\n';
  return 0;
```

2.14 Merge Sort Tree Iterative

```
#include <bits/stdc++.h>
using namespace std;
#define 00 0x3f3f3f3f

struct MergeSortTree
{
   int n;
   vector<vector<int>> tree;

   MergeSortTree(vector<int> &a)
   {
      n = a.size();
      tree.resize(n << 1);</pre>
```

```
for(int i = 0; i < n; i++)</pre>
    tree[i + n] = vector<int>{a[i]};
 build();
void build()
 for(int i = n - 1; i > 0; --i)
    int L = i << 1;</pre>
    int R = (i << 1) | 1;
    int l = 0, r = 0, sz = tree[L].size() + tree[R].size();
    tree[i].resize(sz);
    tree[L].push_back(00);
    tree[R].push_back(00);
    for (int i = 0; i < sz; i++)
      if(tree[L][l] < tree[R][r])
       tree[i][j] = tree[L][l++];
       tree[i][j] = tree[R][r++];
    tree[L].pop_back();
    tree[R].pop_back();
int queryMax(int 1, int r, int x)
 if(1 >= r) return 0;
 int res = 0;
 for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
   if(1 & 1)
      auto it = upper_bound(tree[1].begin(), tree[1].end(), x);
      int p = it - tree[l].begin();
      if(it != tree[l].end())
       int p = it - tree[l].begin();
       res += (int)tree[1].size() - p;
      1++;
    if(r & 1)
      auto it = upper_bound(tree[r].begin(), tree[r].end(), x);
      if(it != tree[r].end())
       int p = it - tree[r].begin();
       res += (int)tree[r].size() - p;
 return res;
int queryMin(int 1, int r, int x)
```

```
if(1 >= r) return 0:
    int res = 0;
    for(1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
      if(1 & 1)
        auto it = lower_bound(tree[1].begin(), tree[1].end(), x);
        if(it == tree[l].end()) res += tree[l].size();
        else res += it - tree[l].begin();
       1++;
      if(r & 1)
        auto it = lower_bound(tree[r].begin(), tree[r].end(), x);
       if(it == tree[r].end()) res += tree[r].size();
        else res += it - tree[r].begin();
    return res;
};
int32_t main()
  int n;
  scanf(" %d", &n);
  vector<int> v(n);
  for(int &w : v) cin >> w;
 MergeSortTree T(v);
  // query(1, r, x)
                        [1, r)
  return 0;
```

2.15 Merge Sort Tree Range Order Statistics Queries

```
int query(int node, int start, int end, int 1, int r, int k)
    if(start == end)
        return arr[start].first;
    int M = upper_bound(tree[2 * node].begin(), tree[2 * node].end(),
       - lower_bound(tree[2 * node].begin(), tree[2 * node].end(), 1);
    int mid = (start + end) / 2;
    if(M >= k)
        return query (2 * node, start, mid, 1, r, k);
    else
        return query (2 * node + 1, mid + 1, end, 1, r, k - M);
int main()
    cin >> n;
    int aux;
    for(int i = 0; i < n; i++)</pre>
        cin >> aux;
        arr.push_back({aux, i});
    sort(arr.begin(), arr.end());
    build(1, 0, n-1);
    int 1, r, k;
    while(cin >> 1 >> r >> k)
        cout << query(1, 0, n-1, 1-1, r-1, k) << '\n';
    return 0;
```

2.16 Merge Sort Tree With Set

```
encontra o menor numero na range [L, R] que eh maior
ou iqual a K. build eh O(NloqNloqN) e query eh O(loqNloqN)
e o erasee eh O(logNlogN).
#define ii pair<int, int>
#define value first
#define index second
const int MAX = 1e6;
int n, m;
vector<array<int, 3>> B, A;
set<ii> tree[MAX];
void build(int node, int start, int end)
    if(start == end)
        tree[node] = set<ii>{ii(A[start][1], start)};
    else
        int mid = (start + end) / 2;
        build(2*node, start, mid);
```

```
build(2*node + 1, mid + 1, end);
      for(auto &it : tree[2 * node])
        tree[node].insert(it);
      for(auto &it : tree[2 * node + 1])
        tree[node].insert(it);
ii query(int node, int start, int end, int l, int r, int k)
    if(start > r or end < 1)</pre>
        return ii(-1, -1);
    if(l <= start and end <= r)</pre>
      auto it = tree[node].upper_bound({k, n + 1});
      ii q = \{-1, -1\};
        if(it != tree[node].begin()) q = *--it;
        return q;
    int mid = (start + end) / 2;
    ii p1 = query(2 * node, start, mid, l, r, k);
    ii p2 = query(2 * node + 1, mid + 1, end, 1, r, k);
  return p1.value <= p2.value ? p2 : p1;</pre>
void erasee(int node, int start, int end, ii p)
  if(tree[node].count(p) == 0) return;
  if(start == end)
    tree[node].erase(p);
    return;
  int mid = (start + end) / 2;
  erasee(2 * node, start, mid, p);
  erasee (2 * node + 1, mid + 1, end, p);
  tree[node].erase(p);
```

2.17 Merge Sort Tree

```
int mid = (start + end) / 2;
        build(2*node, start, mid);
        build(2*node + 1, mid + 1, end);
        merge(tree[2*node].begin(), tree[2*node].end(),
            tree [2*node + 1].begin(), tree [2*node + 1].end()
            , back_inserter(tree[node]));
int query(int node, int start, int end, int 1, int r, int k)
   if(start > r or end < 1)</pre>
        return 0;
   if(l <= start and end <= r)</pre>
        return upper_bound(tree[node].begin(), tree[node].end(), k)
                - tree[node].begin();
   int mid = (start + end) / 2;
   int p1 = query(2*node, start, mid, 1, r, k);
   int p2 = query(2*node + 1, mid + 1, end, 1, r, k);
   return p1 + p2;
int main()
   int n, aux;
   cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> aux;
        a[i].push_back(aux);
   build(1, 0, n-1);
   int 1, r, k;
   cin >> 1 >> r >> k;
//quantidade de elementos menores ou iquais a k na range [1 - r].
   cout << query(1, 0, n-1, 1-1, r-1, k) << '\n';
   return 0;
```

2.18 Ordered Set With BIT

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5+10;

int bit[MAX], arr[MAX];

int bitSearch(int v)
{
  int sum = 0, pos = 0, LOGN = log2(MAX - 2);
  for(int i = LOGN; i >= 0; i--)
    if(pos + (1 << i) < MAX and sum + bit[pos + (1 << i)] < v)
  {
    sum += bit[pos + (1 << i)];
    pos += (1 << i);
  }
  return pos + 1;</pre>
```

```
// pos + 1, pq pos eh a maior posicao cuja soma do prefixo ate
  // ela eh menor que V
// essa funcao retorna o indice J no array em que a soma do
// prefixo [1, J] eh o lower_bound para V
// inserir os elemento na BIT com add(i, arr[i]), para todo i em [1, n
int query(int idx)// soma de um prefixo
  int sum = 0;
  for(; idx > 0; idx -= idx&-idx) sum += bit[idx];
  return sum;
void add(int idx, int k)
  for(int i = idx; i < MAX; i += i&-i) bit[i] += k;</pre>
int smallerCount(int v)
  return query(v);
int count(int v)
  return query(v) - query(v - 1);
int greaterCount(int v)
  return query (MAX - 3) - query (v - 1);
int orderOfKey(int v)
  return smallerCount(v);
int kth(int k)
  return bitSearch(k);
int main()
  int n;
  cin >> n;
  for(int i = 1; i <= n; i++)</pre>
   cin >> arr[i];
   add(arr[i], 1);
  cout << smallerCount(3) << '\n';</pre>
 cout << count(3) << '\n';
  cout << greaterCount(3) << '\n';</pre>
  cout << kth(2) << '\n';
  cout << orderOfKey(4) << '\n';</pre>
```

```
return 0;
```

2.19 PBDS

```
#include <bits/stdc++.h>
// Common file
#include <ext/pb_ds/assoc_container.hpp>
// Including tree_order_statistics_node_update
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __qnu_pbds;
typedef tree<int, null_type, less<int>,
    rb_tree_tag, tree_order_statistics_node_update> ordered_set;
int main()
    ordered_set X;
    X.insert(2);
    X.insert(13);
    X.insert(5);
    X.insert(2):
    cout << *X.find_by_order(0) << '\n';</pre>
    cout << X.order_of_key(1) << '\n';
    return 0;
#include <bits/stdc++.h>
// Common file
#include <ext/pb_ds/assoc_container.hpp>
// Including tree_order_statistics_node_update
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
#define vi vector<int>
#define var pair<int,int>
#define ordered_multiset tree<var, null_type, less<var>
  , rb_tree_tag, tree_order_statistics_node_update>
int id = 0; map<int, vi> ids;
void insere(ordered_multiset &s, int x)
    s.insert({x, ++id});
    ids[x].push_back(id);
void apaga(ordered_multiset &s, int x)
  if(ids[x].empty()) return;
    s.erase({x, ids[x].back()});
    ids[x].pop_back();
```

```
int kth(ordered_multiset &s, int x)
{
    return s.find_by_order(x)->first;
}
int smallerCount(ordered_multiset &s, int x)
{
    return s.order_of_key({x, 0});
}
int count(ordered_multiset &s, int x)
{
    return smallerCount(s, x + 1) - smallerCount(s, x);
}
ordered_multiset::iterator find(ordered_multiset &s, int x)
{
    if(ids[x].empty())
        return s.end();
        return s.find({x, ids[x].back()});
}
int main()
{
    ordered_multiset X;
    // usar funcces ...
    return 0;
}
```

2.20 Persistent Segment Tree

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

struct Node
{
   int 1, r, value;
};

vector<Node> tree;
vector<int> root;

void init()
{
   tree.emplace_back();
   root.push_back(0);
}

void calc(int node)
{
   tree[node].value = 0;
   if(tree[node].l) tree[node].value += tree[tree[node].r].value;
   if(tree[node].r) tree[node].value += tree[tree[node].r].value;
}
```

```
void update (int prev, int node, int start, int end, int idx, int value
 if(start == end)
   tree[node].value = value;
  else
   int mid = (start + end) / 2;
   if(start <= idx and idx <= mid)</pre>
      tree[node].r = tree[prev].r;
      if(tree[node].1 == 0)
       tree[node].l = tree.size();
        tree.emplace_back();
      update(tree[prev].l, tree[node].l, start, mid, idx, value);
    else
      tree[node].l = tree[prev].l;
      if(tree[node].r == 0)
       tree[node].r = tree.size();
       tree.emplace_back();
      update(tree[prev].r, tree[node].r, mid + 1, end, idx, value);
    calc(node);
int query(int node, int start, int end, int 1, int r)
 if(l > end or r < start) return 0;</pre>
 if(l <= start and end <= r) return tree[node].value;</pre>
 int mid = (start + end) / 2, q1 = 0, q2 = 0;
 if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
 if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
 return q1 + q2;
int main()
 int n, q;
 cin >> n >> q;
 init();
  while (q--)
   int o, 1, r;
   cin >> o >> l >> r;
   if(0 == 1)
      int prev = root.back();
      root.push_back(tree.size());
      tree.emplace_back();
      update(prev, root.back(), 0, n - 1, 1 - 1, r);
   else
```

```
int version;
    scanf(" %d", &version);
    cout << query(root[version], 0, n - 1, l - 1, r - 1) << '\n';
    }
}
return 0;
}</pre>
```

2.21 Segment Tree Iterative

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
int tree[MAX << 1], n;</pre>
void build()
  for(int i = n - 1; i > 0; --i) tree[i] = tree[i << 1] + tree[i << 1</pre>
      | 11;
void update(int p, int value)
  for(tree[p += n] = value; p > 1; p >>= 1) tree[p >> 1] = tree[p] +
      tree[p ^ 1];
int query(int 1, int r)
  int res = 0:
  for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
    if(l & 1) res += tree[l++];
   if(r & 1) res += tree[--r];
  return res;
int main()
  cin >> n;
  for(int i = 0; i < n; i++)
   cin >> tree[i + n];
  build();
  int q, l, r, o;
  cin >> q;
  while (q--)
    cin >> o >> l >> r;
    if(0 == 1)
      cout << query(l - 1, r) << '\n'; // soma de [l, r)
      update(l - 1, r); // atualiza a posicoo l pra r
  return 0;
```

2.22 Segment Tree Tree 2D

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e3;
int n, leaf;
int arr[MAX][MAX];
int ST[4*MAX][4*MAX];
void buildLeaf(int k, int node, int l, int r)
 if(1 == r)
   ST[k][node] = arr[leaf][l];
    int mid = (1 + r) / 2;
    buildLeaf(k, 2*node, 1, mid);
   buildLeaf(k, 2*node + 1, mid + 1, r);
    ST[k][node] = ST[k][2*node] + ST[k][2*node+1];
void build(int node, int 1, int r)
  if(1 == r)
   buildLeaf(node, 1, 0, n-1), leaf++;
    int mid = (1 + r) / 2;
    build(2*node, 1, mid);
    build(2*node + 1, mid + 1, r);
    for(int i = 1; i < 4*n; i++)</pre>
      ST[node][i] = ST[2*node][i] + ST[2*node+1][i];
int queryNode(int k, int node, int 1, int r, int cx, int cy)
 if(1 > cv or r < cx)
    return 0;
  if(cx <= 1 and r <= cy)
    return ST[k][node];
  int mid = (1 + r) / 2;
  int ans = gueryNode(k, 2*node, 1, mid, cx, cy);
  ans += queryNode(k, 2*node + 1, mid + 1, r, cx, cy);
  return ans;
int query (int node, int 1, int r, int 1x, int 1y, int cx, int cy)
 if(1 > ly or r < lx)
    return 0;
  if(lx \le l and r \le ly)
   return queryNode (node, 1, 0, n-1, cx, cy);
  int mid = (1 + r) / 2;
  int ans = query(2*node, 1, mid, 1x, 1y, cx, cy);
  ans += query (2*node + 1, mid + 1, r, lx, ly, cx, cy);
  return ans;
```

```
void updateNode(int k, int node, int l, int r, int x, int y, int value
  if(1 == r)
    ST[k][node] = arr[x][v] = value;
    int mid = (1 + r) / 2;
    if(1 <= y and y <= mid)</pre>
      updateNode(k, 2*node, 1, mid, x, y, value);
      updateNode(k, 2*node + 1, mid + 1, r, x, y, value);
    ST[k][node] = ST[k][2*node] + ST[k][2*node + 1];
void update(int node, int 1, int r, int x, int y, int value)
  if(1 == r)
    updateNode(node, 1, 0, n-1, x, y, value);
    int mid = (1 + r) / 2;
    if(1 \le x and x \le mid)
      update(2*node, 1, mid, x, y, value);
      update (2*node + 1, mid + 1, r, x, y, value);
    for(int i = 1; i < 4*n; i++)
      ST[node][i] = ST[2*node][i] + ST[2*node+1][i];
int main()
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
   for (int j = 0; j < n; j++)
      cin >> arr[i][j];
  build(1, 0, n-1);
  int o, a, b, c, d;
  while(cin >> o)
    cin >> a >> b >> c;
    if(0 == 1)
      update(1, 0, n-1, a-1, b-1, c);
    else
      cout << query(1, 0, n-1, a-1, b-1, c-1, d-1) << '\n';
  return 0;
```

2.23 Segment Tree With Lazy Propagation

```
#include <bits/stdc++.h>
using namespace std;
```

```
#define int long long
#define esq node << 1LL
#define dir (node << 1) | 1LL
struct SegmentTree {
 vector<int> tree, lazy;
  int size;
  void build(int node, int start, int end, vector<int> &a) {
   if(start == end) {
     tree[node] = a[start];
      return;
   int mid = (start + end) >> 1;
   build(esq, start, mid, a);
   build(dir, mid + 1, end, a);
   tree[node] = tree[esg] + tree[dir];
  SegmentTree() {}
  SegmentTree(int n) {
   size = n;
   tree.resize(size << 2);
   lazv.resize(size << 2);
  void init(vector<int> &a) {
   build(1, 0, size -1, a);
 // += add in the interval
 void push(int node, int start, int end) {
   tree[node] += lazy[node] * (end - start + 1);
   if(start != end) {
     lazy[esq] += lazy[node];
     lazy[dir] += lazy[node];
   lazy[node] = 0;
  int query(int node, int start, int end, int 1, int r) {
   if(lazy[node]) push(node, start, end);
   if(l > end or start > r or l > r) return 0;
   if(l <= start and end <= r) return tree[node];</pre>
   int mid = (start + end) >> 1;
   int g1 = guery(esg, start, mid, l, r);
   int q2 = query(dir, mid + 1, end, 1, r);
   return q1 + q2;
  int query(int 1, int r) {
   return query (1, 0, size - 1, 1, r);
 void update(int node, int start, int end, int 1, int r, int v) {
   if(lazy[node]) push(node, start, end);
   if(l > end or start > r or l > r) return;
   if(1 <= start and end <= r)</pre>
```

```
lazy[node] += v;
      push (node, start, end);
    int mid = (start + end) >> 1;
    update(esq, start, mid, l, r, v);
    update(dir, mid + 1, end, l, r, v);
    tree[node] = tree[esq] + tree[dir];
  void update(int 1, int r, int v) {
    update(1, 0, size - 1, 1, r, v);
} ;
int32_t main() {
  ios base::svnc with stdio(false);
  cin.tie(nullptr);
  int n;
  cin >> n;
  SegmentTree T(n);
  return 0;
```

2.24 Sparse Table RMQ

```
#include <bits/stdc++.h>
#define maxn 100000
#define maxnlog 20
using namespace std;
const double EPS = 1e-6;
int n, q, Sparse_Table[maxnlog][maxn];
void build()
  for (int i = 1; (1 << i) <= n; i++)
    for (int j = 0; j + (1 << i) <= n; <math>j++)
      Sparse Table[i][j] = max(Sparse Table[i-1][j],
        Sparse_Table[i-1][j+(1 << (i-1))]);
int range_query(int i, int j)
  int sz = log2(j-i+1);
 return max(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
int main()
  scanf("%d %d", &n, &q);
  for(int i = 0; i < n; i++)
    scanf("%d", &Sparse_Table[0][i]);
  build();
```

```
for(int i = 0; i < q; i++)
{
   int a, b;
   scanf("%d %d", &a, &b);
   cout << range_query(a,b) << endl;
}
return 0;
}</pre>
```

2.25 Treap

```
#include <bits/stdc++.h>
using namespace std;
struct Node
  int valor, priority, size, maior;
 Node *1, *r;
  Node(int _valor) : valor(_valor), priority((rand() << 16)</pre>
  ^ rand()), size(1), l(nullptr), r(nullptr), maior(_valor) {}
  ~Node() { delete l; delete r; }
 void recalc()
   size = 1:
   maior = valor;
   if (1) size += 1->size, maior = max(maior, 1->maior);
   if (r) size += r->size, maior = max(maior, r->maior);
};
struct Treap
 Node* merge(Node *1, Node *r)
   if(!l or !r) return 1 ? 1 : r;
   // Se a prioridade esquerda eh menor.
   if(l->priority < r->priority)
     1->r = merge(1->r, r);
     l->recalc();
     return 1;
     // Se a prioridade direita eh maior ou igual.
    else
     r->1 = merge(1, r->1);
     r->recalc();
      return r:
// Valores maiores ou iquais a "valor" ficarao no r, e os demais no 1.
 void split(Node *v, int valor, Node *&l, Node *&r)
   l = r = nullptr;
```

```
if(!v) return;
  // Se o valor for maior, ir para direita
  if(v->valor < valor)</pre>
    split(v->r, valor, v->r, r);
    // Se o valor for menor ou iqual ir para esquerda.
  }else
    split (v->1, valor, l, v->1);
    r = v;
  v->recalc();
bool find (Node *v, int valor)
 if(!v) return false;
 if( v->valor == valor ) return true;
 if( v->valor < valor ) return find(v->r, valor);
 if( v->valor > valor ) return find(v->1, valor);
int smallestCount(Node *v, int valor)
 if(!v) return 0;
  // Se for menor ou iqual adicionar + 1.
 if(v->valor == valor) return (v->l ? v->l->size : 0);
  if(v->valor < valor) return 1 + (v->1 ? v->1->size : 0)
    + smallestCount(v->r, valor);
  if(v->valor > valor) return smallestCount(v->1, valor);
Node* kth(Node *v, int posicao)
 if(!v) return nullptr;
  int esquerda = (v->1? v->1->size: 0);
  if(posicao-esquerda == 1) return v;
  if(posicao-esquerda > 1) return kth(v->r, posicao-esquerda-1);
  if (posicao-esquerda < 1) return kth(v->1, posicao);
// Sendo i e j os indices no array ordenado
// Talvez deh problemas de i e j estiverem fora do range.
int query(int i, int j)
 Node *1, *q, *r;
  split(root, kth(root, i+1)->valor, l, q);
  split(q, kth(q, j+1-i) -> valor+1, q, r);
 int x = q->maior;
 root = merge(1, merge(q, r));
  return x;
Node * root;
Treap() : root(nullptr) {}
~Treap() { delete root; }
// Se existe um elemento com o valor
bool find(int valor)
```

```
return find(root, valor);
// Quantidade de elementos menores que o valor
int smallestCount(int valor)
 return smallestCount(root, valor);
// Retorna o k-th menor elemento
Node * kth(int posicao) {
 return kth(root, posicao);
// Insere o valor mesmo se ja exista outro com valor iqual
void insert(int valor)
 Node * 1, * r;
 split(root, valor, l, r);
 root = merge(merge(l, new Node(valor)), r);
// Apaga todos os elementos que possuem o valor.
void erase(int valor)
 Node * 1, * m, * r;
 split (root, valor, 1, m);
 split(m, valor + 1, m, r);
 delete m;
 root = merge(1, r);
// Quantos valores existem menor que "valor"
int menoresQue(int valor)
 Node * 1, * r;
 split(root, valor, l, r);
 int res = (1? 1->size: 0);
 root = merge(l,r);
 return res;
// splitSmallest eh uma funcao que esta na implicit treap
// Retorna a consulta dos primeiros "quantidade" valor
int top(int quantidade)
 Node *1, *r;
 splitSmallest(root, quantidade, 1, r);
 int valor = (1 ? 1->maior : 0);
 root = merge(l,r);
 return valor;
// Remover os d menores
void removeSmallest(int d)
 Node *1, *r;
 splitSmallest(root, d, l, r);
 root = r;
 if(1) delete 1;
// Remover todos menos os d menores
void limit (int d)
```

```
Node * 1, * r;
    splitSmallest(root, d, l, r);
    root = 1;
    if(r) delete r;
  int size() const { return root ? root->size : 0; }
int n, a;
char op;
int main()
    srand(time(0));
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
    cin >> op >> a;
    if(op == 'I')
      if(!treap.find(a))
        treap.insert(a);
    else if(op == 'D' )
      treap.erase(a);
    else if(op == 'C' )
      cout << treap.smallestCount(a) << '\n';</pre>
    else if(op == 'K' )
      Node *v = treap.kth(a);
      if(v == nullptr) cout << "invalid" << '\n';</pre>
      else cout << v->valor << '\n';</pre>
  return 0:
```

2.26 TreeIsomorfismWithMap

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;

int n, ID, degree[MAX];
map<map<int, int>, int> formato;
bool vis[MAX];

void init()
{
   formato.clear();
   ID = 1;
}

int dfs(int v, int p, vector<vector<int>> &G)
{
   if((int)G[v].size() == 1)
       return 1;
   map<int, int> ids;
```

```
for(int &u : G[v])
        if(u == p) continue;
        int x = dfs(u, v, G);
        ids[x]++;
    if(formato.count(ids) <= 0)</pre>
        formato[ids] = ++ID;
    return formato[ids];
inline void findCenterAndComputeID(vector<vector<int>> &G, vector<int>
    memset(vis, 0, sizeof(vis));
    queue<int> fila[2];
    for(int i = 0; i < n; i++)</pre>
        if(degree[i] == 1)
            fila[0].push(i);
    int cnt = 0, turn = 0;
    while (cnt + 2 < n)
        while(!fila[turn].empty())
            int u = fila[turn].front(); fila[turn].pop();
            vis[u] = true;
            cnt++;
            for(int i = 0; i < G[u].size(); i++)</pre>
                 if(!vis[G[u][i]])
                     degree[G[u][i]]--;
                     if (degree[G[u][i]] == 1) fila[1-turn].push(G[u][i
                         ]);
        turn ^= 1;
    for(int i = 0; i < n; i++)</pre>
        if(vis[i]) continue;
        val.push_back(dfs(i, -1, G));
int32_t main()
    while(cin >> n)
        init();
        vector<int> val[2];
        for (int j = 0; j < 2; j++)
            memset(degree, 0, sizeof(degree));
            vector<vector<int>> G(n + 1);
            for(int i = 1; i < n; i++)</pre>
                 int u, v;
                scanf(" %d %d", &u, &v); u--; v--;
                G[u].push_back(v);
                G[v].push_back(u);
                degree[v]++;
```

2.27 TreeIsomorfismWithPolynomialHashing

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long
const int MAX = 1e5 + 10;
const 11 A = 911382323;
const 11 B = 972663749;
int n, ID, degree[MAX];
map<11, 11> formato;
bool vis[MAX];
inline ll norm(ll a)
    return a > B ? a = a % B : a;
inline ll add(ll a, ll b)
    a = norm(a); b = norm(b);
    return norm(a + b);
inline ll prod(ll a, ll b)
    a = norm(a); b = norm(b);
    return norm(a * b);
inline ll pol_hash(vector<ll> &v)
    11 p = 1, ans = 0;
    for(ll &w : v)
    ans = add(ans, prod(p, w));
    p = prod(p, A);
  return norm(ans);
11 dfs(int v, int p, vector<vector<int>> &G)
    if((int)G[v].size() == 1)
        return 1;
```

```
vector<ll> ids;
    for(int &u : G[v])
        if(u == p) continue;
        11 x = dfs(u, v, G);
        ids.push back(x);
    sort(ids.begin(), ids.end());
  11 ph = pol hash(ids);
  if(formato.count(ph) <= 0) formato[ph] = ++ID;</pre>
    return formato[ph];
inline void findCenterAndComputeID(vector<vector<int>> &G, vector<ll>
    (fav3
    memset(vis, 0, sizeof(vis));
    queue<int> fila[2];
    for(int i = 0; i < n; i++)
        if(degree[i] == 1)
            fila[0].push(i);
    int cnt = 0, turn = 0;
    while (cnt + 2 < n)
        while(!fila[turn].empty())
            int u = fila[turn].front(); fila[turn].pop();
            vis[u] = true;
            cnt++;
            for(int i = 0; i < G[u].size(); i++)</pre>
                if(!vis[G[u][i]])
                     degree[G[u][i]]--;
                     if (degree[G[u][i]] == 1) fila[1-turn].push(G[u][i
                         ]);
        turn ^= 1;
    for(int i = 0; i < n; i++)</pre>
        if(vis[i]) continue;
        val.push_back(dfs(i, -1, G));
int32 t main()
    while(cin >> n)
    formato.clear();
    ID = 1;
        vector<ll> val[2];
        for (int j = 0; j < 2; j++)
            memset(degree, 0, sizeof(degree));
            vector<vector<int>> G(n + 1);
            for(int i = 1; i < n; i++)</pre>
                int u, v;
                scanf(" %d %d", &u, &v); u--; v--;
```

```
G[u].push_back(v);
    G[v].push_back(u);
    degree[v]++;
    degree[u]++;
}
    findCenterAndComputeID(G, val[j]);
}
bool fl = false;
for(ll &v0 : val[0])
    for(ll &v1 : val[1])
        if(v0 == v1)
            fl = true;
    puts(fl ? "S" : "N");
}
return 0;
}
```

2.28 Two Stacks Trick

```
const int 00 = 0x3f3f3f3f3f;
struct Stack {
    vector<int> s, smax = \{-00\}, smin = \{00\};
    void push(int x) {
        s.push back(x);
        smax.push_back(max(smax.back(), x));
        smin.push_back(min(smin.back(), x));
    int pop() {
        int x = s.back();
        s.pop_back();
        smax.pop_back();
        smin.pop_back();
        return x;
    int min () {
        return smin.back();
    int max () {
        return smax.back();
    bool empty() {
        return s.empty();
};
Stack s1, s2;
void push(int x) {
    s2.push(x);
void pop() {
    if(s1.empty()) {
        while(!s2.empty())
            s1.push(s2.pop());
    s1.pop();
```

```
int min_() {
    return min(s1.min_(), s2.min_());
}
int max_() {
    return max(s1.max_(), s2.max_());
}
```

2.29 Wavelet Tree

```
#include <bits/stdc++.h>
using namespace std;
const int N = 100100;
const int MAX = 30 * N;
// MAX = N * log(maxX - minX)
// Queries in O(log(maxX - minX))
struct WaveletTree
  int arr[N], aux[N];
  int lo[MAX], hi[MAX];
  vector<int> freq[MAX];
  int lef[MAX], rig[MAX];
  int nextNode;
  WaveletTree(vector<int> a, int minX, int maxX)
    int sz = a.size();
    for(int i = 0; i < sz; i++)
      arr[i] = a[i]:
    nextNode = 1;
    build(0, 0, sz, minX, maxX);
  int stable_partition(int s, int e, int mid)
    int pivot = 0;
    for(int i = s; i < e; i++)</pre>
      aux[i] = arr[i], pivot += (arr[i] <= mid);
    int l = s, r = s + pivot;
    for(int i = s; i < e; i++)</pre>
      if(aux[i] <= mid)</pre>
        arr[l++] = aux[i];
        arr[r++] = aux[i];
    return 1;
  void build(int node, int s, int e, int minX, int maxX)
    lo[node] = minX, hi[node] = maxX;
    if(lo[node] == hi[node] or s >= e) return;
    int mid = (minX + maxX - 1) / 2;
    freq[node].resize(e - s + 1);
    freq[node][0] = 0;
    for(int i = s; i < e; i++)
```

```
freq[node][i - s + 1] = freq[node][i - s] + (arr[i] <= mid);
  int pivot = stable_partition(s, e, mid);
  lef[node] = nextNode++, rig[node] = nextNode++;
 build(lef[node], s, pivot, minX, mid);
 build(rig[node], pivot, e, mid + 1, maxX);
int went_right(int node, int i)
  return i - freq[node][i];
// less than ou equal to x in range [1, r]
int lte(int l, int r, int x, int node = 0)
 if(l > r or x < lo[node]) return 0;</pre>
 if(hi[node] <= x) return r - l + 1;</pre>
  int 11 = freq[node][1 - 1] + 1, r1 = freq[node][r];
 int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
 return lte(l1, r1, x, lef[node]) + lte(l2, r2, x, rig[node]);
// greater than ou equal to x in range [l, r]
int gte(int 1, int r, int x, int node = 0)
 if(l > r or x > hi[node]) return 0;
 if(lo[node] >= x) return r - l + 1;
 int l1 = freq[node][l - 1] + 1, r1 = freq[node][r];
  int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
 return gte(11, r1, x, lef[node]) + gte(12, r2, x, rig[node]);
// counting numbers equal to x in range [l, r]
int count(int 1, int r, int x, int node = 0)
 if(l > r or lo[node] > x or hi[node] < x) return 0;</pre>
 if(lo[node] == hi[node] and lo[node] == x) return r - l + 1;
  int 11 = freq[node][1 - 1] + 1, r1 = freq[node][r];
 int 12 = went_right(node, 1 - 1) + 1, r2 = went_right(node, r);
  return count(11, r1, x, lef[node]) + count(12, r2, x, rig[node]);
// find kth number in range [1, r]
int kth(int 1, int r, int k, int node = 0)
 if(1 > r) return 0;
 if(lo[node] == hi[node]) return lo[node];
 int inLeft = freq[node][r] - freq[node][l - 1];
  int l1 = freq[node][l - 1] + 1, r1 = freq[node][r];
```

```
if(k <= inLeft) return kth(l1, r1, k, lef[node]);
int l2 = went_right(node, l - 1) + 1, r2 = went_right(node, r);

return kth(l2, r2, k - inLeft, rig[node]);

};
int main()
{
  vector<int> a = {2, 5, 3, 2, 4, 2};

  WaveletTree T(a, 0, 9);

  cout << T.lte(3, 5, 3) << '\n';
  cout << T.gte(3, 5, 3) << '\n';
  cout << T.count(l, 6, 2) << '\n';
  cout << T.kth(l, 6, 5) << '\n';
  return 0;
}</pre>
```

3 Dynamic Programming

3.1 Coin Problem Topdown Dp

```
#include <bits/stdc++.h>
using namespace std;
using namespace std;
vector<int> coin:
int memo[1000000];
int solve(int troco)
  if(troco < 0)
    return (1 << 25);
  if(memo[troco] != -1)
    return memo[troco];
  if(troco == 0)
    return 0;
  int ans = (1 << 25);
  for(int i = 0; i < coin.size(); i++)</pre>
    ans = min(ans, 1 + solve(troco - coin[i]));
  return memo[troco] = ans;
void ans (int troco)
  if(troco < 0)</pre>
    return;
  if(troco == 0)
  for(int i = 0; i < coin.size(); i++)</pre>
    if(solve(troco - coin[i]) + 1 == memo[troco])
      cout << coin[i] << ' ';
      ans(troco - coin[i]);
```

```
break;
}

int main()
{
  memset (memo, -1, sizeof(memo));
  int n, troco;
  cin >> n >> troco;
  coin.resize(n);
  for(int &w : coin)
     cin >> w;
  cout << solve(troco) << '\n';
  ans(troco);
  puts("");

return 0;
}</pre>
```

3.2 Digit DP Sum Of Digits In Range

```
#include "bits/stdc++.h"
using namespace std;
int dp[20][200][2];
int digitDP(int idx, int sum, int can, vector<int> &digit)
{// idx eh o indice atual, sum a soma dos digitos ate idx,
//e can uma flag para indicar se pode colocar
//qualquer valor a partir daqui
  if(idx == (int)digit.size())
    return sum;
  if (dp[idx][sum][can] != -1)
    return dp[idx][sum][can];
  int ans = 0;
  for(int i = 0; i < 10; i++)
    if(can or i <= digit[idx])</pre>
      ans += digitDP(idx + 1, sum + i,
        can or i < digit[idx], digit);</pre>
  return dp[idx][sum][can] = ans;
int query(int x) // responde a consulta de 0 ate x
  memset (dp, -1, sizeof (dp));
    vector<int> digit;
    while (x)
        digit.push_back(x%10);
        x /= 10;
    reverse(digit.begin(), digit.end());
    return digitDP(0, 0, 0, digit);
int main()
    int q, a, b;
    cin >> q;
    while (q--)
```

```
{
  cin >> a >> b;
  cout << query(b) - query(a - 1) << '\n';
}
  return 0;
}</pre>
```

3.3 Edit Distance With DP

```
#include <bits/stdc++.h>
using namespace std;
string a, b;
int PD[2008][2008];
int solve(int i, int j)
  if(!i) return j;
  if(!j) return i;
  if(PD[i][j] != −1)
    return PD[i][j];
  // substituir um caracter se for preciso
  int ans1 = solve(i - 1, j - 1) + (a[i] != b[j]);
  //apagar o caracter da string i
  int ans2 = solve(i - 1, j) + 1;
  //apagar o caracter da string j
  int ans 3 = solve(i, j - 1) + 1;
  return PD[i][j] = min(ans1, min(ans2, ans3));
int main()
  int q;
  cin >> q;
  while (q--)
    memset (PD, -1, sizeof (PD));
   cin >> a >> b;
    a = "#" + a;
    b = "#" + b;
    cout << solve(a.size()-1, b.size()-1) << '\n';
  return 0:
```

3.4 Kadane 2D

```
#include <bits/stdc++.h>
using namespace std;

int pd[100][100], A[100][100];

int main()
{
   int n, m;
   cin >> n >> m;
   for(int i = 1; i <= n; i++)</pre>
```

```
for(int j = 1; j <= m; j++)
    cin >> A[i][j], pd[i][j] = pd[i][j - 1] + A[i][j];
int ans = 0;
for(int i = 1; i <= n; i++)
    for(int j = i + 1; j <= m; j++)
    {
       int sum = 0;
       for(int k = 1; k <= n; k++)
       {
            sum += pd[k][j] - pd[k][i - 1];
            if(sum < 0) sum = 0;
            ans = max(ans, sum);
        }
    }
    cout << ans << '\n';
    return 0;
}</pre>
```

3.5 Kadane 3D

```
#include <bits/stdc++.h>
using namespace std;
int A, B, C;
int par[22][22][22], pd[22][22][22];
int main()
  cin >> A >> B >> C;
  for(int i = 1; i <= A; i++)</pre>
    for(int j = 1; j <= B; j++)</pre>
      for(int k = 1; k <= C; k++)</pre>
        cin >> par[i][j][k];
  for(int i = 1; i <= A; i++)</pre>
    for(int j = 1; j <= B; j++)
      for(int k = 1; k <= C; k++)</pre>
        pd[i][j][k] = pd[i][j - 1][k] + pd[i][j][k - 1]
           - pd[i][j-1][k-1] + par[i][j][k];
  int ans = -(1 << 25);
  for(int h1 = 1; h1 <= C; h1++)
  for(int h2 = h1; h2 <= C; h2++)
  for(int 11 = 1; 11 <= B; 11++)
    for(int 12 = 11; 12 <= B; 12++)
      int sum = -(1 << 25);
      for(int i = 1; i <= A; i++)</pre>
        int s = pd[i][12][h2] - pd[i][11 - 1][h2]
        - pd[i][12][h1 - 1] + pd[i][11 - 1][h1 - 1];
        sum = max(sum + s, s);
        ans = max(ans, sum);
  cout << ans << '\n';
  return 0;
```

3.6 Knapsack With Copies SqrtN Memory

```
#include <bits/stdc++.h>
using namespace std:
#define bug(x) cout << #x << " >>>>>> " << x << '\n'
#define _ << " , " <<
//#define int long long
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
#define ii pair<int, int>
#define fi first
#define se second
#define UNTIL(t) while (clock() < (t) * CLOCKS PER SEC)
const int MAX = 20002; //2 * 10^5
const int MOD = 1000000007; //10^9 + 7
const int 00 = 0x3f3f3f3f; // <math>0x3f3f3f3f;
const double EPS = 1e-9; //10^-9
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
int n, S;
int B[205];
int C[205];
int V[3500];
int W[3500];
int ID[3500];
int id = 1;
int dp[MAX];
int linha[70][MAX], T[70][MAX];
int L[70];
void add(int i)
  for (int k = 0; sum + (1 << k) <= C[j]; sum += (1 << k), k++)
   V[id] = B[i] * (1 << k);
    W[id] = (1 << k);
    ID[id] = i;
    id++;
  int r = C[j] - sum;
  if(r > 0)
   V[id] = B[j] * r;
   W[id] = r;
   ID[id] = j;
    id++;
int32_t main()
  for(int i = 1; i <= n; i++) cin >> B[i];
  for(int i = 1; i <= n; i++) cin >> C[i];
  for(int i = 1; i <= n; i++) add(i);</pre>
  cin >> S;
  for (int j = 1; j \le S; j++)
    dp[j] = 00;
```

```
int cnt = 0, k = -1, sq = max(10, (int) sqrt(id * 1.));
for(int i = 1; i < id; i++)</pre>
 if(cnt % sq == 0)
    cnt = 0;
    k++;
    for(int j = 0; j <= S; j++)</pre>
     linha[k][j] = dp[j];
    L[k] = i - 1;
  for(int j = S; j >= V[i]; j--)
    dp[j] = Min(dp[j - V[i]] + W[i], dp[j]);
 cnt++;
int last_raw = id - 1, s = S;
vector<int> note(n + 1);
while(last raw >= 1)
  int first raw = last raw - 1;
 while(first_raw > L[k])
    first_raw--;
  for (int j = 0; j \le S; j++)
    T[0][i] = linha[k][i];
  for(int i = 1; i <= last_raw - first_raw; i++)</pre>
    for(int j = 0; j <= S; j++)</pre>
      if(j >= V[i + first_raw])
        T[i][j] = Min(T[i-1][j], T[i-1][j-V[i+first_raw]] +
            W[i + first_raw]);
      else
        T[i][j] = T[i - 1][j];
  for(int i = last_raw - first_raw; i > 0; i--)
    if(T[i][s] != T[i - 1][s])
     note[ID[i + first_raw]] += W[i + first_raw];
      s -= V[i + first_raw];
 last raw = first raw;
int number of notes = 0;
for(int &w : note)
 number_of_notes += w;
cout << number of notes << '\n';
for(int i = 1; i <= n; i++)</pre>
 cout << note[i] << ' ';
puts("");
return 0;
```

3.7 Knapsack Zero One Without Value

```
// Knapsack 0 - 1 sem valor em O((N*W) / word)
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[10000];
bitset<10000> T[100];
bool knapsack()
 T[0][0] = 1;
  for(int i = 1; i <= n; i++)
   T[i] = ((T[i-1] << weight[i-1]) | T[i-1]);
  return T[n][W];
void retrieve()
 vector<int> ans:
  for (int i = n; i > 0; i--)
    if(W >= weight[i - 1]  and T[i - 1][W - weight[i - 1]])
      ans.push_back(i - 1);
      W = weight[i - 1];
  for(int &w : ans) cout << weight[w] << ' '; puts("");</pre>
int main()
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
   cin >> weight[i];
  cin >> W;
  cout << knapsack() << '\n';
  retrieve();
  return 0;
```

3.8 Knapsack0-kSemValor

```
// Knapsack 0 - k sem valor em O((N*W*LogK) / word)
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[10000], K[10000];
bitset<10000> T[100];

bool knapsack()
{
    T[0][0] = 1;
    for(int i = 1; i <= n; i++)</pre>
```

```
int s = K[i - 1];
    T[i] = T[i - 1];
    for (int p = 1; p \le s; s -= p, p *= 2)
      T[i] \mid = ((T[i] << (weight[i - 1] * p)) \mid T[i]);
    if(s)
      T[i] = ((T[i] << (weight[i - 1] * s)) | T[i]);
  return T[n][W];
void retrieve()
  vector<pair<int, int>> ans;
  for (int i = n; i > 0; i--)
    int s = K[i - 1], qtd = 0;
    for (int p = 1; p <= s; p \star= 2)
    if(W \ge weight[i - 1] * p and T[i - 1][W - weight[i - 1] * p])
      W \rightarrow weight[i - 1] * p, qtd += p, s -= p;
    if(W \ge weight[i - 1] * s and T[i - 1][W - weight[i - 1] * s])
      W \rightarrow s * weight[i - 1], qtd += s;
    if(qtd) ans.push_back({qtd, i - 1});
  }//first eh q quantidade de pesos i - 1
  for(pair<int, int> &w : ans)
    cout << w.first << ' ' << weight[w.second] << '\n';</pre>
int main()
  cin >> n;
  for(int i = 0; i < n; i++)</pre>
    cin >> weight[i];
  for(int i = 0; i < n; i++)</pre>
    cin >> K[i];
  cin >> W;
  cout << (knapsack() ? "possible\n" : "impossible\n");</pre>
  retrieve();
  return 0;
```

3.9 KnapsackErrichto

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
const int 00 = 0x3f3f3f3f3f3f3f3f3f3f;

int n, w, maxi;
int value[120], weight[120];
int dp[100040];

int32_t main()
{
   cin >> n >> w;
   for(int i = 0; i < n; i++)
        cin >> weight[i] >> value[i];
   // dp[i] = maximum total value of itens with total weight exactly
   for(int item = 0; item < n; item++)
        for(int cur_wei = w - weight[item]; cur_wei >= 0; cur_wei--)
```

3.10 KnapsackWithCopies

```
// O( S * sqrt( SumKi ) )
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
int freq[50];
vector<int> value, weight;
int memo[5000][5000];
// Decompor o numero em uma soma de potencias
//de 2 de tal forma que qualquer numero entre 0 e k
// pode ser formado usando os numeros da decomposicao.
void decomp(int k, int w, int v)
  int i = 1;
  frea[1] = k:
  while(true)
    int m = (freq[i] - 1) / 2;
    if(freq[i] - m * 2 == 0) break;
    freg[i] -= 2 * m;
    freq[2 * i] += m;
    i++;
  for (int i = 0; i < 32; i++)
    while (freq[i]--)
      value.push_back(i * v);
      weight.push back(i * w);
    freq[i] = 0;
int solve(int id, int W)
  if (memo[id][W] != -1)
    return memo[id][W];
  if(id == value.size() or !W)
    return memo[id][W] = 0;
  int ans = 0;
  if(weight[id] > W)
    ans = solve(id + 1, W);
    ans = max(value[id] + solve(id + 1, W
     - weight[id]), solve(id + 1, W));
  return memo[id][W] = ans;
```

```
int main()
{
   int n, w, v, k, S;
   memset(memo, -1, sizeof(memo));
   cin >> n >> S;
   for(int i = 0; i < n; i++)
   {
      cin >> v >> w >> k;
      decomp(k, w, v);
   }
   cout << solve(0, S) << '\n';
   return 0;
}</pre>
```

3.11 KnapsackwithPDtopdown

```
#include <bits/stdc++.h>
using namespace std;
int n, W, weight[2005], value[2005];
int memo[2005][2005];
int solve(int id, int W)
  if (memo[id][W] != -1)
    return memo[id][W];
 if(id == n or !W)
    return memo[id][W] = 0;
  int ans = 0;
  if (weight[id] > W)
    ans = solve(id + 1, W);
    ans = max(value[id] + solve(id + 1,
      W - weight[id]), solve(id + 1, W));
  return memo[id][W] = ans;
void ans (int id, int W)
  if(id == n or !W)
    return;
  if(solve(id + 1, W) == memo[id][W])
    ans(id + 1, W);
  else
    cout << id << ' ';
    ans(id + 1, W - weight[id]);
int main()
 memset (memo, -1, sizeof (memo));
  cin >> n >> W;
 for(int i = 0; i < n; i++)</pre>
   cin >> weight[i] >> value[i];
  cout << solve(0, W) << '\n';
  cout << "Objetos escolhidos 0 - indexdos\n";</pre>
  ans (0, W);
```

```
puts("");
return 0;
```

3.12 Longest Common Subsequece And Edit Distance

```
#include <bits/stdc++.h>
using namespace std;
// longest common substring
int pd[1000][1000];
int LCS(string a, string b)
    for(int i = 1; i <= a.size(); i++)</pre>
        for(int j = 1; j <= b.size(); j++)</pre>
            if(a[i-1] == b[j-1])
                 pd[i][j] = pd[i-1][j-1] + 1;
            else
                 pd[i][j] = max(pd[i][j-1], pd[i-1][j]);
    return pd[a.size()][b.size()];
int main()
    string a, b;
    cin >> a >> b;
    int lcs = LCS(a, b);
    cout << lcs << '\n';
    cout << "Edit Distance: " << a.size()+b.size()-2*lcs << '\n';</pre>
    return 0;
```

3.13 Longest Increasing Subsequence

```
else
      pai[i] = pos[p - 1];
  vector<int> L;
  int aux = pos[pilha.size() - 1];
  cout << pilha.size() << '\n';</pre>
  while (aux !=-1)
    L.push_back(arr[aux]);
    aux = pai[aux];
  reverse(L.begin(), L.end());
  for(const int &w : L)
    cout << w << ' ';
  cout << '\n';
int main()
 int n;
  cin >> n;
  vector<int> arr(n);
  for(int &w : arr)
   cin >> w;
 lis(arr);
  return 0;
```

3.14 Subset Sum

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6 + 10;
int n, x, weight[1005];
bool pd[MAX];
int ans[MAX];
void printAns(int m)
  cout << ans[m] << ' ';
  if(m - ans[m] > 0)
    printAns(m - ans[m]);
int main()
  cin >> n >> x;
  int sum = 0;
 for(int i = 0; i < n; i++) cin >> weight[i], sum += weight[i];
  pd[0] = 1;
  for (int j = 0; j < n; j++)
    for(int i = sum; i >= 0; i--)
      if(pd[i] and !pd[i + weight[j]])
        ans[i + weight[j]] = weight[j];
        pd[i + weight[j]] = 1;
```

```
printAns(x);
puts("");
return 0;
```

3.15 Traveling Salesman Problem Bottom Up Dp

```
#include <bits/stdc++.h>
using namespace std;
const int 00 = 0x3f3f3f3f;
int n;
double dist[20][20];
double pd[1 << 17][20];
int tsp(int ori)
 memset (pd, 63, sizeof (pd));
  for(int i = 0; i < n; i++)
   if(i != ori)
      pd[1 << i][i] = dist[ori][i];
  for (int k = 0; k < (1 << n); k++)
  for(int i = 0; i < n; i++)</pre>
  if(k & (1 << i))
    for(int j = 0; j < n; j++)
      if((k & (1 << j)) and i != j)
      pd[k][j] = min(pd[k][j], pd[k ^ (1 << j)][i] + dist[i][j]);
  return pd[(1 << n) - 1][ori];</pre>
int main()
  // inicializar dist, dist[i][j] quarda a distancia de i para j no
  // chamar tsp
  return 0;
```

3.16 Traveling Salesman Problem Topdown Dp

```
#include <bits/stdc++.h>
using namespace std;

int dist[22][22], m;
int memo[20][1 << 20];

int solve(int id, int mask) {
   if(((1 << m) - 1) == mask)
        return dist[id][0];
   if(memo[id][mask] != -1)
        return memo[id][mask];
   int ans = INT_MAX;
   for(int i = 0; i < m; i++)
        if((mask & (1 << i)) == 0)
        ans = min(ans, dist[id][i] + solve(i, mask | (1 << i)));</pre>
```

```
return memo[id][mask] = ans;
}
int main() {
  memset(memo, -1, sizeof(memo));
  //inicializa a matriz dist com as distancias
  //de todo mundo pra todo mundo..
  cout << solve(0, 1) << '\n';
  return 0;
}</pre>
```

4 String

4.1 Aho Corasick

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
int p[MAX], f[MAX], nxt[MAX][26], ch[MAX];
int tsz = 1; // size of the trie
int cnt[MAX]; // used to know number of matches
const int S = 2e3+5;
bitset<MAX> elem[S]:
// S eh tamanho da maior das N strings que sao
// pradroes para buscar no texto
void init()
    tsz = 1;
    memset(f, 0, sizeof(f));
    memset(nxt, 0, sizeof(nxt));
    memset(cnt, 0, sizeof(cnt));
    for (int i = 0; i < MAX; i++)</pre>
      elem[i].reset();
void add(const string &s, int x)
  // the first element of the trie is the root
    int cur = 1;
    for(int i = 0; s[i]; ++i)
        int j = s[i] - 'a';
        if(!nxt[cur][j])
            tsz++;
            p[tsz] = cur;
            ch[tsz] = j;
            nxt[cur][j] = tsz;
        cur = nxt[cur][j];
    cnt[cur]++;
    elem[cur].set(x);
```

```
void build()
    queue<int> q;
    for(int i = 0; i < 26; ++i)
        nxt[0][i] = 1;
        if(nxt[1][i])
            q.push(nxt[1][i]);
    while(!q.empty())
        int v = q.front(); q.pop();
        int u = f[p[v]];
        while(u and !nxt[u][ch[v]]) u = f[u];
        f[v] = nxt[u][ch[v]];
        cnt[v] += cnt[f[v]];
        for(int i = 0; i < 26; ++i)
            if(nxt[v][i])
                q.push(nxt[v][i]);
bitset<MAX> match(const string &s)
    int ans = 0;
    // Numero de matches
    bitset<MAX> found;
    // Usado pra saber quais strings matches
    int x = 1;
    for(int i = 0; i < s.size(); ++i)</pre>
        int t = s[i] - 'a';
        while(x and !nxt[x][t])
           x = f[x];
        x = nxt[x][t];
        ans += cnt[x];
        found |= elem[x];
    return found;
int main()
    int n;
    string s;
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> s;
        add(s, i);
    build();
    cin >> s;
    bitset<MAX> ans = match(s);
    for(int i = 0; i < n; i++)</pre>
        cout << ans[i] << '\n';
        // 1 se a i-esima string lida
        // aparece no texto, 0 cc
  return 0:
```

```
#include <bits/stdc++.h>
using namespace std;
const int K = 60;
struct Vertex {
   int next[K];
  bool leaf = false;
  int p = -1;
   char c;
   int link = -1:
   int go[K];
   bitset<1005> S;
   Vertex(int _p=-1, char _c = '$') : p(_p), c(_c) {
      fill(begin(next), end(next), -1);
      fill(begin(go), end(go), -1);
} ;
vector<Vertex> t;
void init() {
   t.clear();
   t.resize(1);
void add(string &s, int i) {
   int v = 0;
   for(char ch : s) {
      int c = ch - 'A';
      if(t[v].next[c] == -1) {
         t[v].next[c] = t.size();
         t.push_back(Vertex(v, ch));
      v = t[v].next[c];
   t[v].leaf = true;
   t[v].S[i] = 1;
int go(int v, char ch);
int get_link(int v) {
   if(t[v].link == -1) {
      if(v == 0 or t[v].p == 0)
         t[v].link = 0;
         t[v].link = go(get_link(t[v].p), t[v].c);
   return t[v].link;
int go(int v, char ch) {
  int c = ch - 'A';
   if(t[v].go[c] == -1) {
      if(t[v].next[c] != -1)
```

```
t[v].go[c] = t[v].next[c];
      else
         t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
   return t[v].go[c];
int32_t main() {
  ios_base::sync_with_stdio(false);
  cin.tie(nullptr);
   int caso;
   cin >> caso;
   while (caso--)
      init();
      string s;
      int n;
      cin >> s >> n;
      bitset<1005> S:
      for(int i = 0; i < n; i++) {</pre>
         string a;
         cin >> a;
         add(a, i);
      int v = 0;
      for(char &c : s) {
         v = qo(v, c);
         S \mid = t[v].S;
      for(int i = 0; i < n; i++)</pre>
         cout << (S[i] ? 'y' : 'n') << '\n';
  return 0;
```

4.2 Dynamic Trie

```
#include <bits/stdc++.h>
using namespace std;

struct TrieNode
{
    map<int, TrieNode*> childreen;
    bool isLeaf;
    TrieNode()
    {
        isLeaf = false;
    }
};

void inserir(TrieNode *root, string s)
{
    TrieNode *node = root;
    for(int i = 0; i < s.size(); i++)
    {
        int index = s[i] - 'a';
        if(node->childreen.find(index) == node->childreen.end())
            node = node->childreen[index];
```

```
node->isLeaf = true;
bool buscar(TrieNode *root, string s)
  TrieNode *node = root;
  for(int i = 0; i < s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(node->childreen.find(index) == node->childreen.end())
      return false:
    node = node->childreen[index];
  return node->isLeaf;
bool remover(TrieNode *node, string s, int level)
  if(node != nullptr)
    if(s.size() == level)
      if (node->isLeaf)
       node->isLeaf = false;
        return !node->childreen.size();
    else
      int index = s[level] - 'a';
      if (remover(node->childreen[index], s, level+1))
        delete node->childreen[index];
        node->childreen.erase(index);
        return !node->childreen.size();
  return false;
int main()
  TrieNode *root = new TrieNode();
  inserir(root, "abc");
  inserir(root, "abd");
  inserir(root, "cfa");
  remover(root, "abc", 0);
  printf(buscar(root, "abc") ? "yes\n" : "no\n");
  printf(buscar(root, "abd") ? "yes\n" : "no\n");
  return 0;
```

4.3 KMP

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;
```

```
int n, m;
// n eh o tamanho do texto e m eh o
// tamanho do padrao
int arr[MAX];
// array que guarda o tamanho do maior
// prefixo proprio que tambem eh sufixo
string t, p; // t eh o texto e p eh o padrao
void build() // kMP Preprocess
    int i = 0, j = 1;
    while(j < m)</pre>
        if(p[i] == p[j])
           arr[j] = ++i;
        else
            i = 0;
            if(p[i] == p[j])
                arr[j] = ++i;
        j++;
int matching() // KMP search
    int i = 0, j = 0;
    while (j < n)
        if(p[i] == t[j]) i++, j++;
        else if(i) i = arr[i - 1];
        else j++;
        if(i == m)
            return j - m;
    // a substring P inicia na posicao j - m em T
    return -1; // P nao eh substring de T
int main()
    cin >> t >> p;
    n = (int)t.size();
    m = (int)p.size();
    build();
    cout << matching() << '\n';</pre>
    return 0;
```

4.4 LIS LDS

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
int n;
int LI[MAX], LD[MAX];
```

```
vector<int> arr;
int LIS() {
    for(int i = 0; i < n; i++)</pre>
        LI[i] = 1;
    for(int i = n - 1; i >= 0; i--)
        for (int j = 0; j < i; j++)
            if(arr[j] < arr[i])
                LI[j] = max(LI[j], LI[i] + 1);
int LDS() {
    reverse(arr.begin(), arr.end());
    for(int i = 0; i < n; i++)</pre>
        LD[i] = 1;
    vector<int> pilha;
    for(int i = 0; i < n; i++) {</pre>
        int p = (int) (lower_bound(pilha.begin(),
          pilha.end(), arr[i]) - pilha.begin());
        if(p == pilha.size())
            pilha.push_back(arr[i]);
            pilha[p] = arr[i];
        LD[i] = p + 1;
int main() {
    cin >> n; arr.resize(n);
    for(int i = 0; i < n; i++) cin >> arr[i];
    LIS();
    LDS();
    for(int i = 0; i < n; i++)</pre>
      cout << LI[i] << ' '; puts("");
    for(int i = 0; i < n; i++)</pre>
      cout << LD[n - i - 1] << ' '; puts("");
  return 0;
```

4.5 Longest Common Substring

```
#include <stdio.h>
#include <string.h>

int pd[10000][10000];

int max(int a, int b)
{
   return a > b ? a : b;
}

int solve(char *a, char *b)
{
   int i, j, ans = 0;
   int t1 = strlen(a), t2 = strlen(b);
   for(i = 1; i < t1; i++)</pre>
```

```
for (j = 1; j < t2; j++)
    if(a[i-1] == b[j-1])
        pd[i][j] = pd[i-1][j-1] + 1,
            ans = max(ans, pd[i][j]);
    else
        pd[i][j] = 0;
    return ans;
}
int main()
{
    char s1[55], s2[55];
    while(fgets(s1, 54, stdin) != NULL)
        printf("%d\n", solve(s1, s2));
    return 0;
}</pre>
```

4.6 Manacher

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 100;
int lps[2*MAX+5];
char s[MAX];
int manacher()
    int n = strlen(s);
    string p(2*n+3, '#');
    p[0] = '^{'};
    for(int i = 0; i < n; i++)</pre>
        p[2*(i+1)] = s[i];
    p[2*n+2] = '$';
    int k = 0, r = 0, m = 0;
    int l = p.length();
    for(int i = 1; i < 1; i++)</pre>
        int o = 2*k - i;
        lps[i] = (r > i) ? min(r-i, lps[o]) : 0;
        while (p[i + 1 + lps[i]] == p[i - 1 - lps[i]])
            lps[i]++;
        if(i + lps[i] > r) k = i, r = i + lps[i];
        m = max(m, lps[i]);
    /*for(int i = 1; i \le 2 * n + 1; i++)
        cout << lps[i] << ' ';
    puts(""); */
    return m;
int main()
    cin >> s;
    cout << manacher() << '\n';</pre>
  return 0;
```

4.7 SA

```
* Code frin Competitive Programming 3
#include <algorithm>
#include <cstdio>
#include <cstring>
using namespace std;
typedef pair<int, int> ii;
#define MAX_N 100010
                                             // second approach: O(n
    log n)
char T[MAX N];
                                 // the input string, up to 100K
    characters
                                              // the length of input
int n;
    string
                                     // rank array and temporary rank
int RA[MAX_N], tempRA[MAX_N];
int SA[MAX_N], tempSA[MAX_N];
                                 // suffix array and temporary suffix
    array
                                                 // for counting/radix
int c[MAX_N];
     sort
char P[MAX_N];
                                // the pattern string (for string
    matching)
                                            // the length of pattern
int m:
    string
int Phi[MAX_N];
                                     // for computing longest common
    prefix
int PLCP[MAX_N];
int LCP[MAX_N]; // LCP[i] stores the LCP between previous suffix T+SA
                                              // and current suffix T+
                                                   SA[i]
bool cmp(int a, int b) { return strcmp(T + a, T + b) < 0; }</pre>
    compare
void constructSA slow() {
                                       // cannot go beyond 1000
    characters
  for (int i = 0; i < n; i++) SA[i] = i; // initial SA: {0, 1, 2, ...,
  sort(SA, SA + n, cmp); // sort: O(n log n) * compare: O(n) = O(n^2)
      log n)
                                                                     11
void countingSort(int k) {
  int i, sum, maxi = max(300, n); // up to 255 ASCII chars or length
       of n
  memset(c, 0, sizeof c);
                                                   // clear frequency
      table
  for (i = 0; i < n; i++)
                              // count the frequency of each integer
   c[i + k < n ? RA[i + k] : 0]++;
  for (i = sum = 0; i < maxi; i++) {</pre>
```

```
int t = c[i]; c[i] = sum; sum += t;
 for (i = 0; i < n; i++) // shuffle the suffix array if
   necessary
  tempSA[c[SA[i]+k < n ? RA[SA[i]+k] : 0]++] = SA[i];
 for (i = 0; i < n; i++)
                        // update the suffix
   arrav SA
  SA[i] = tempSA[i];
characters
 int i, k, r;
 rankings
 for (i = 0; i < n; i++) SA[i] = i;  // initial SA: {0, 1, 2, ...,</pre>
     n-1
 for (k = 1; k < n; k <<= 1) { // repeat sorting process log n
   countingSort(k); // actually radix sort: sort based on the second
   countingSort(0); // then (stable) sort based on the first
    item
   tempRA[SA[0]] = r = 0; // re-ranking; start from rank
    r = 0
   for (i = 1; i < n; i++)
                                   // compare adjacent
     suffixes
    tempRA[SA[i]] = // if same pair => same rank r; otherwise,
    (RA[SA[i]] == RA[SA[i-1]] \&\& RA[SA[i]+k] == RA[SA[i-1]+k]) ? r :
   for (i = 0; i < n; i++)
                         // update the rank
    array RA
    RA[i] = tempRA[i];
  if (RA[SA[n-1]] == n-1) break; // nice optimization
     trick
} }
void computeLCP_slow() {
 LCP[0] = 0;
                                             // default
   value
 definition
   int L = 0;
                                        // always reset L
    to 0
   while (T[SA[i] + L] == T[SA[i-1] + L]) L++; // same L-th char
   , L++
  LCP[i] = L;
void computeLCP() {
 int i, L;
                                        // default
 Phi[SA[0]] = -1;
 for (i = 1; i < n; i++)
                                       // compute Phi in
  Phi[SA[i]] = SA[i-1]; // remember which suffix is behind this
     suffix
 for (i = L = 0; i < n; i++) { // compute Permuted LCP in
   if (Phi[i] == -1) { PLCP[i] = 0; continue; } // special
```

```
while (T[i + L] == T[Phi[i] + L]) L++; // L increased max n
   times
   PLCP[i] = L;
 L = \max(L-1, 0);
                                     // L decreased max n
     times
 for (i = 0; i < n; i++)
                                         // compute LCP in
    0(n)
   LCP[i] = PLCP[SA[i]]; // put the permuted LCP to the correct
    position
                     // string matching in O(m
ii stringMatching() {
   log n)
 int lo = 0, hi = n-1, mid = lo;
                                   // valid matching =
     [0..n-1]
 while (lo < hi) {</pre>
                                           // find lower
   bound
                            // this is round
   mid = (lo + hi) / 2;
   int res = strncmp(T + SA[mid], P, m); // try to find P in suffix
   if (res >= 0) hi = mid;  // prune upper half (notice the >=
    sign)
   else
            lo = mid + 1;  // prune lower half
    including mid
                               // observe '=' in "res >= 0"
    above
 if (strncmp(T + SA[lo], P, m) != 0) return ii(-1, -1);  // if not
 ii ans; ans.first = lo;
 lo = 0; hi = n - 1; mid = lo;
 bound
   mid = (lo + hi) / 2;
   int res = strncmp(T + SA[mid], P, m);
   if (res > 0) hi = mid;
                                           // prune upper
    half
   including mid
                      // (notice the selected branch when res
    == 0)
 if (strncmp(T + SA[hi], P, m) != 0) hi--; // special
     case
ans.second = hi;
 return ans;
} // return lower/upperbound as first/second item of the pair,
  respectively
ii LRS() { // returns a pair (the LRS length and its
   index)
 int i, idx = 0, maxLCP = -1;
                                     // O(n), start from
 for (i = 1; i < n; i++)
   i = 1
 if (LCP[i] > maxLCP)
   maxLCP = LCP[i], idx = i;
 return ii(maxLCP, idx);
int owner(int idx) { return (idx < n-m-1) ? 1 : 2; }</pre>
```

```
ii LCS() {
                           // returns a pair (the LCS length and its
    index)
  int i, idx = 0, maxLCP = -1;
  for (i = 1; i < n; i++)
                                                   // O(n), start from
      i = 1
   if (owner(SA[i]) != owner(SA[i-1]) && LCP[i] > maxLCP)
     maxLCP = LCP[i], idx = i;
 return ii(maxLCP, idx);
int main() {
  //printf("Enter a string T below, we will compute its Suffix Array:\
 strcpy(T, "GATAGACA");
 n = (int)strlen(T);
 T[n++] = ' $';
 // if '\n' is read, uncomment the next line
 //T[n-1] = '$'; T[n] = 0;
  constructSA_slow();
                                                             // O(n^2
      log n)
  printf("The Suffix Array of string T = '%s' is
   shown below (O(n^2 \log n) \text{ version}): n", T);
  printf("i\tSA[i]\tSuffix\n");
  for (int i = 0; i < n; i++) printf("%2d\t%2d\t%s\n", i, SA[i], T +</pre>
      SA[i]);
  constructSA();
                                                               // O(n
      log n)
 printf("\nThe Suffix Array of string T = '%s' is
     shown below (O(n log n) version):\n", T);
 printf("i\tSA[i]\tSuffix\n");
  for (int i = 0; i < n; i++) printf("%2d\t%2d\t%s\n", i, SA[i], T +
      SA[i]);
  computeLCP();
       0(n)
  // LRS demo
  ii ans = LRS();
                                  // find the LRS of the first input
      string
  char lrsans[MAX_N];
  strncpy(lrsans, T + SA[ans.second], ans.first);
 printf("\nThe LRS is '%s' with length = %d\n\n", lrsans, ans.first);
  // stringMatching demo
  //printf("\nNow, enter a string P below, we will try to find P in T
      :\n");
  strcpy(P, "A");
 m = (int)strlen(P);
  // if '\n' is read, uncomment the next line
  //P[m-1] = 0; m--;
  ii pos = stringMatching();
  if (pos.first != -1 && pos.second != -1) {
   printf("%s is found SA[%d..%d] of %s\n", P, pos.first, pos.second,
         T);
    printf("They are:\n");
    for (int i = pos.first; i <= pos.second; i++)</pre>
      printf(" s\n, T + SA[i]);
  } else printf("%s is not found in %s\n", P, T);
```

```
// LCS demo
//printf("\nRemember, T = ' s' \setminus NNow, enter another string P: \setminus n", T);
// T already has '$' at the back
strcpy(P, "CATA");
m = (int)strlen(P);
// if '\n' is read, uncomment the next line
//P[m-1] = 0; m--;
strcat(T, P);
                                                                //
    append P
strcat(T, "#");
                                                     // add '$' at the
     back
n = (int)strlen(T);
    update n
// reconstruct SA of the combined strings
constructSA();
                                                              // O(n
    log n)
                                                                    11
computeLCP();
     0(n)
printf("\nThe LCP information of 'T+P' = '%s':\n", T);
printf("i\tSA[i]\tLCP[i]\tOwner\tSuffix\n");
for (int i = 0; i < n; i++)
  printf("%2d\t%2d\t%2d\t%2d\t%s\n", i, SA[i], LCP[i], owner(SA[i]),
       T + SA[i]);
ans = LCS();
                     // find the longest common substring between T
    and P
char lcsans[MAX N];
strncpy(lcsans, T + SA[ans.second], ans.first);
printf("\nThe LCS is '%s' with length = %d\n", lcsans, ans.first);
return 0;
```

4.8 Suffix Array And Applications

```
#include <bits/stdc++.h>
using namespace std;
string s;
vector<int> sa, c, lcp;
// O(n)
void countSort()
  int n = sa.size();
  vector<int> buc(n), new_sa(n);
  for(int &w : sa)
   buc[c[w]]++;
  for(int i = 1; i < n; i++)</pre>
    buc[i] += buc[i - 1];
  for(int i = n - 1; i >= 0; i--)
    new_sa[--buc[c[sa[i]]]] = sa[i];
  sa = new_sa;
// O(|s| * log|s|)
void buildSuffixArray()
```

```
int n = s.size();
                                                                                  if(!r)
  sa.resize(n);
                                                                                    e = mid - 1, ans = mid;
  c.resize(n);
                                                                                  else if (r == -1)
  for (int i = 0; i < n; i++)
                                                                                    e = mid - 1;
   sa[i] = i, c[i] = s[i];
                                                                                  else
  sort(sa.begin(), sa.end(), [&](int a, int b)
                                                                                    b = mid + 1;
      return c[a] < c[b];</pre>
                                                                                if(s.substr(sa[ans], p.size()) != p)
    });
                                                                                  return -1;
  c[sa[0]] = 0;
                                                                                return ans;
  for(int i = 1; i < n; i++)</pre>
    if(s[sa[i - 1]] == s[sa[i]])
      c[sa[i]] = c[sa[i - 1]];
                                                                              // posicao no suffix array do sufixo mais
    else
                                                                              // a direita que contem p como prefixo
      c[sa[i]] = c[sa[i - 1]] + 1;
                                                                              // O(|p| * log|s|)
  int k = 0:
                                                                              int upper_bound(string &p)
  while ((1 << k) < n)
                                                                                int b = 0, e = (int)sa.size() - 1, ans = 0;
    for(int i = 0; i < n; i++)
                                                                                while(b <= e)</pre>
      sa[i] = (sa[i] - (1 << k) + n) % n;
    countSort();
                                                                                  int mid = (b + e) / 2;
    vector<int> new_c(n);
                                                                                  int r = cmp(sa[mid], p);
                                                                                  if(!r)
    new_c[sa[0]] = 0;
    for(int i = 1; i < n; i++)
                                                                                    b = mid + 1, ans = mid;
                                                                                  else if (r == -1)
      pair<int, int> prev = \{c[sa[i-1]], c[(sa[i-1] + (1 << k)) \}
                                                                                    e = mid - 1;
                                                                                  else
      pair<int, int> cur = {c[sa[i]], c[(sa[i] + (1 << k)) % n]};
                                                                                    b = mid + 1;
      if(prev == cur) new_c[sa[i]] = new_c[sa[i - 1]];
      else new_c[sa[i]] = new_c[sa[i-1]] + 1;
                                                                                if(s.substr(sa[ans], p.size()) != p)
                                                                                  return -1;
                                                                                return ans;
    c = new_c;
   k++;
                                                                              // numero de ocorrencias da string p
                                                                              // como substring de s
// 0: padrao esta no sufixo
                                                                              // O(|p| * log|s|)
// 1: o padrao eh lexicograficamente maior que o sufixo k
                                                                              int count(string &p)
//-1: o padrao en lexicograficamente menor que o sufixo k
((al))0 //
                                                                                int l = lower_bound(p);
int cmp(int k, string &p)
                                                                                int u = upper_bound(p);
                                                                                if (1 == -1 \text{ or } u == -1)
  for(int i = 0; i < p.size(); i++)</pre>
                                                                                  return 0:
                                                                                return u - 1 + 1;
    if(i + k >= s.size()) return 1;
   if(s[i + k] < p[i]) return 1;
   if(s[i + k] > p[i]) return -1;
                                                                              // construcao do array lcp
                                                                              // lcp[i] eh o maior prefixo comum
  return 0;
                                                                              // aos sufixos i e i - 1 do suffix array
                                                                              // O(n)
                                                                              void buildLcp()
// posicao no suffix array do sufixo mais
// a esquerda que contem p como prefixo
                                                                                int n = s.size();
// O(|p| * log|s|)
                                                                                lcp.resize(n);
int lower_bound(string &p)
                                                                                int k = 0;
                                                                                for (int i = 0; i < n - 1; i++)
  int b = 0, e = (int) sa.size() - 1, ans = 0;
  while (b \leq e)
                                                                                // pi eh a posicao no suffix array do
                                                                                // sufixo que comeca na posicao i da strig
   int mid = (b + e) / 2;
                                                                                  int pi = c[i];
    int r = cmp(sa[mid], p);
                                                                                  int j = sa[pi - 1];
```

```
while (s[i + k] == s[j + k]) k++;
    lcp[pi] = k;
    k = \max(k - 1, 0);
// conta a quantidade de substrings
// diferentes na string s
// O(IsI)
long long numberOfDifSubStr()
  long long n = s.size();
  long long ans = n * (n - 1) / 2;
  for(int i = 0; i < n; i++)</pre>
    ans -= lcp[i];
  return ans;
// encontra a maior substring comum a s e p
// O(|s + p|) depois de construir suffix array
void longestCommonSubstring(string p)
  int n = s.size();
  int m = p.size();
  int ans = -1, j = 1;
  s = s + "$" + p + "#";
 buildSuffixArray();
  buildLcp();
  for(int i = 1; i < sa.size(); i++)</pre>
    int p = sa[i - 1] < n ? 1 : -1;
   int q = sa[i] < n ? 1 : -1;</pre>
   if(p * q < 0 and ans < lcp[i])
      ans = lcp[i], j = i;
  int a = sa[j];
  int b = sa[j - 1];
  string lcs;
  while(a < s.size() and b < s.size() and s[a] == s[b])</pre>
    lcs.push_back(s[a]);
    a++, b++;
  cout << ans << '\n';
  cout << lcs << '\n';
int32_t main()
  string p;
  cin >> s >> p;
   // o tamanho do maior prefixo comum entre dois
  // sufixos que estao nas posicoes a e b do
  // suffix array eh igual ao menor valor no
  // intervalo [a+1, b] do array lcp
```

```
// descomentar as linhas abaixo para todas as
// funcoes, exceto para longestCommonSubstring

// s.push_back('$');
// buildSuffixArray();
// buildLcp();

longestCommonSubstring(p);

return 0;
}
```

4.9 Suffix Array

#include <bits/stdc++.h>

```
using namespace std;
string txt; // texto
string pat; // padrao
int n; // tamanho do texto
int chave[100]; // chave para comparacao dos sufixos
int vs[100]; // vetor de sufixos
int ord[100]; // ordem de um sufixo (qual classe ele pertence)
int lcp[100]; // maior prefixo comum
bool comp(int a, int b)
    return chave[a] < chave[b];</pre>
void constroi() // O(N*Log(N) *Log(N))
    for(int i = 0; i < n; i++)</pre>
        vs[i] = i;
        chave[i] = txt[i] - 'a' + 1;
    sort (vs, vs+n, comp);
    for(int i = 0; i++)
        int classes = 0;
        for (int j = 0; j < n; j++)
            ord[vs[j]] = j > 0 and chave[vs[j]]
              == chave[vs[j-1]] ? ord[vs[j-1]] : ++classes;
        if(classes == n) break;
        for (int j = 0; j < n; j++)
            chave[j] = ord[j] * (classes+1);
            chave[j] += j+(1<<i) < n ? ord[j+(1<<i)] : 0;
        sort(vs, vs+n, comp);
int strcompara(int pos)
{// retorna 0 se o padrao esta no sufixo, maior que zero se o padrao
//lexicograficamente maior que o sufixo, e menor que 0 se o padrao
//eh lexicograficamente menor que o sufixo
```

```
for(int i = 0; i < pat.size(); i++)</pre>
        if(i+pos >= n)
            return 1;
        else if(pat[i] != txt[i+pos])
            return pat[i] - txt[i+pos];
    return 0;
bool search() // O(Size(Pat)*Log(N))
    int b = 0, e = n - 1, m, aux;
    while(b <= e)</pre>
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            return true;
        else if(aux > 0)
            b = m + 1;
        else
            e = m - 1;
    return false;
// numero de vezes que o padrao aparece no texto. O(Size(Pat)*Log(N))
int numberOfOcur()
    int b = 0, e = n - 1, m, aux, l = INT_MAX, r = INT_MIN;
    while(b <= e)</pre>
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            l = min(l, m);
            e = m - 1:
        else if(aux > 0)
            b = m + 1;
        else
            e = m - 1;
    b = 0, e = n - 1;
    while(b <= e)
        m = (b + e) / 2;
        aux = strcompara(vs[m]);
        if(aux == 0)
            r = max(r, m);
            b = m + 1;
        else if(aux > 0)
            b = m + 1;
        else
            e = m - 1;
    return abs(r-l+1);
```

```
// kasai em O(NlogN) pra construir o LCP (longest common prefix)
void kasai()
    vector<int> invSuff(n, 0);
    for(int i = 0; i < n; i++)</pre>
        invSuff[vs[i]] = i;
    int k = 0;
    for(int i = 0; i < n; i++)
        if(invSuff[i] == n-1)
            k = 0;
            continue;
        int j = vs[invSuff[i]+1];
        while (i + k < n \text{ and } j + k < n \text{ and } txt[i + k] == txt[j + k])
            k++;
        lcp[invSuff[i]] = k;
        if(k > 0)
            k--;
void printAll()
    cout << "Vetor de sufixos:\n";</pre>
    for(int i = 0; i < n; i++)</pre>
        cout << vs[i] << ' ';
    cout << '\n';
    cout << "Sufixos em ordem:\n";</pre>
    for(int i = 0; i < n; i++)</pre>
        cout << txt.substr(vs[i]) << '\n';</pre>
  Dado um array LCP onde LCP[i] armazena o tamanho do maior prefixo
   em comum entre os sufixos i e i + 1 da suffix arrav
  , entao para achar o maior prefixo em comum entre dois sufixos que
   estao nas posicoes a e b da suffix array, corresponde a achar
   o menor valor no intervalo [a, b-1] no LCP array.
  Outra aplicacao eh dada uma string, para contar quantas substrings
   diferentes ela tem basta contar quantas tem no total ( ((n + 1) * n)
    possiveis substrings) e remover todos os valores de LCP do total.
int main()
    cin >> txt;
    n = txt.size();
    constroi();
    printAll();
    cout << '\n';
    cin >> pat;
    cout << (search() ? "found " : "not found ") << numberOfOcur()</pre>
        << " vez(es)\n\n";
    kasai();
```

```
cout << "LCP\n";
for(int i = 0; i < n; i++)
  cout << lcp[i] << ' ';
  cout << '\n';
return 0;
}</pre>
```

4.10 Trie Static

```
#include <bits/stdc++.h>
using namespace std;
// as posicoes de 0 ate 25 representam as letras
// de a ate z do alfabeto.
// a posicao 26 armazena quantas strings terminam
// nesse vertice.
// a posicao 27 armazena quantas strings passam
// nesse vertice.
int trie[8000000][30], CUR = 1;
// fl eh zero se for uma operacao de inserir
// fl eh um se for uma operacao de buscar
int add(string &s, int fl)
  int root = 0;
  for (char &c : s)
    if(trie[root][c - 'a'] == 0)
      if(f1) return 0;
      trie[root][c - 'a'] = CUR++;
    if(!fl) trie[root][27]++;
    root = trie[root][c - 'a'];
  if(fl) return trie[root][26];
  trie[root][26]++;
  return 1;
void sub(string &s)
  int root = 0;
  for (char &c : s)
    if(trie[root][c - 'a'] and trie[root][27])
      trie[root][27]--;
      root = trie[root][c - 'a'];
  trie[root][26]--;
int main()
  int q;
  cin >> q;
```

```
while(q--)
{
   int o;
   string s;
   cin >> o >> s;
   if(o == 1) add(s, 0);
   else if(o == 2) puts(add(s, 1) ? "existe" : "nao existe");
   else sub(s);
}
return 0;
}
```

4.11 Trie With Vector

#include <bits/stdc++.h>

```
using namespace std;
struct TrieNode
  int child[26], size, cnt;
  TrieNode()
   memset(child, 0, sizeof(child));
    size = cnt = 0;
};
vector<TrieNode> trie;
void init()
  trie.clear();
  trie.push_back(TrieNode());
void add(string s)
  int root = 0;
  for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(trie[root].child[index] == 0)
      trie[root].child[index] = trie.size();
      trie.push_back(TrieNode());
    root = trie[root].child[index];
    trie[root].size++;
  trie[root].cnt++;
void sub(string s)
  int root = 0;
  for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    root = trie[root].child[index];
```

```
trie[root].size--;
  trie[root].cnt--;
int query(string s)
  int root = 0;
  for(int i = 0; i < (int)s.size(); i++)</pre>
    int index = s[i] - 'a';
    if(!trie[trie[root].child[index]].size)
      return false;
   root = trie[root].child[index];
  return trie[root].cnt;
int main()
  string s;
  int o;
  init();
  while(cin >> o >> s)
   if(o == 1) add(s);
    else if (o == 2) sub(s);
    else cout << query(s) << '\n';</pre>
  return 0;
```

4.12 Trie

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;
int trie[MAX][26], cnt[MAX], tsz = 1;
bool leaf[MAX];
void insert (string s)
    int cur = 1;
    cnt[cur]++;
    for(int i = 0; i < s.size(); i++)</pre>
        int a = s[i] - 'a';
        if(!trie[cur][a]) trie[cur][a] = ++tsz;
        cur = trie[cur][a];
        cnt[cur]++;
    leaf[cur] = true;
bool find(string s)
    int cur = 1;
    for(int i = 0; i < s.size(); i++)</pre>
```

```
int a = s[i] - 'a';
        if(!trie[cur][a] or !cnt[cur])
            return false;
        cur = trie[cur][a];
    return leaf[cur] and cnt[cur];
int remove(string s)
    int cur = 1;
    for(int i = 0; i < s.size(); i++)</pre>
        int a = s[i] - 'a';
        cnt[cur]--;
        cur = trie[cur][a];
    leaf[cur] = false;
    cnt[cur]--;
int main()
    string s;
    int n, o;
    while(cin >> o >> s)
        if(0 == 1)
            cout << (find(s) ? "found\n" : "not found\n");</pre>
        else if (\circ == 2)
            insert(s);
        else
            remove(s);
  return 0;
```

4.13 Z Function

```
#include "bits/stdc++.h"
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
using namespace std;
const int MAX = 1e5;

vector<int> Z(string &s)
{
   int n = s.size(), x = 0, y = 0;
   vector<int> z(n);
   for(int i = 1; i < n; i++)
   {
      z[i] = Max(0, Min(z[i - x], y - i + 1));
      while(i + z[i] < n and s[z[i]] == s[i + z[i]])
      x = i, y = i + z[i], z[i]++;
   }
   return z;
}</pre>
```

```
int main()
{
    string txt, pattern;

    cin >> txt >> pattern;
    string s = pattern + "#" + txt;
    vector<int> z = Z(s);
    for(int &w : z)
        cout << w << ' ';
    cout << '\n';
    return 0;
}</pre>
```

5 Math

5.1 Baby Step Giant Step

// a ^ kcongb mod m

```
int value[1000008];
int cor[1000008], tempo = 1;
// com vetor o modulo deve ser <= 10^7 fica O(sgrt(m))
inline int discreteLogarithm(int a, int b, int m) {
    tempo++;
  a %= m; b %= m;
    int n = (int) sqrt(m + .0) + 1, an = 1;
  for(int i = 1; i <= n; i++) an = (an * 1LL * a) % m;</pre>
    for(int i = 1, cur = an; i <= n; i++) {</pre>
      if(cor[cur] < tempo) value[cur] = i, cor[cur] = tempo;</pre>
        cur = (cur * 1LL * an) % m;
    for (int j = 0, cur = b; j \le n; j++) {
        if(cor[cur] == tempo) {
            int ans = value[cur] * n - j;
            if(ans < m)</pre>
                return ans;
    cur = (cur * 1LL * a) % m;
  return -1;
// com mapa o modulo pode ser ateh <= 10^12 fica O(sqrt(m) * log(m))
int discreteLogarithm(int a, int b, int m)
  a %= m; b %= m;
    int n = (int) sqrt(m + .0) + 1, an = 1;
  for(int i = 1; i <= n; i++) an = (an * a) % m;</pre>
    unordered map<int, int> value;
    for(int i = 1, cur = an; i <= n; i++) {</pre>
      if(!value.count(cur)) value[cur] = i;
        cur = (cur * an) % m;
    for (int j = 0, cur = b; j \le n; j++) {
        if(value[cur]) {
            int ans = value[cur] * n - j;
```

5.2 Catalan Numbers

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
const long long MOD = 1000000000;
int catalan[MAX];
void init()
    catalan[0] = catalan[1] = 1;
    for(int i = 2; i <= 1000; i++)
        for (int j = 0; j < i; j++)
            catalan[i] += (catalan[j] * catalan[i-j-1]) % MOD;
            if(catalan[i] >= MOD)
                catalan[i] -= MOD;
int main()
  init();
  int n;
  while(cin >> n)
    printf("%d\n", catalan[n]);
  return 0;
```

5.3 Chinese Remainder Theorem

```
//codar em Python para evitar problemas de overflow
// O(Tlog(lcm(n1*n2*..)))
//https://codeforces.com/blog/entry/61290

#include<bits/stdc++.h>
using namespace std;
const int MAX = 20;
#define ll long long

ll GCD(ll a, ll b) { return (b == 0) ? a : GCD(b, a % b); }

inline ll LCM(ll a, ll b) { return a / GCD(a, b) * b; }

inline ll normalize(ll x, ll mod) { x %= mod; if (x < 0) x += mod; return x; }</pre>
```

```
struct GCD_type { ll x, y, d; };
GCD_type ex_GCD(ll a, ll b)
    if (b == 0) return {1, 0, a};
    GCD_type pom = ex_GCD(b, a % b);
    return {pom.y, pom.x - a / b * pom.y, pom.d};
int t;
ll a[MAX], n[MAX], ans, lcm;
int main()
    cin >> t;
    for(int i = 1; i <= t; i++)</pre>
        cin >> a[i] >> n[i], normalize(a[i], n[i]);
    ans = a[1]:
    lcm = n[1];
    for(int i = 2; i <= t; i++)</pre>
        auto pom = ex_GCD(lcm, n[i]);
        11 \times 1 = pom.x;
        11 d = pom.d;
        if((a[i] - ans) % d != 0) return cerr << "No solutions" <<</pre>
        ans = normalize(ans + x1 * (a[i] - ans) / d % (n[i] / d) * lcm
      lcm * n[i] / d);
        lcm = LCM(lcm, n[i]);
        // you can save time by replacing above lcm * n[i] /d
        // by lcm = lcm * n[i] / d
    cout << ans << " " << lcm << endl;
    return 0;
```

5.4 Conversion Base

```
#include <bits/stdc++.h>
using namespace std;

int a,b; char sa[10000]; char sb[10000];

void rev(char s[])
{
   int l = strlen(s);
   for(int i = 0; i < l - l - i; i++)
      swap(s[i], s[l - l - i]);
}

void multi(char s[], int k)
{
   int i, c = 0, d;
   for(i=0;s[i];i++)
   {
      d = (s[i] - '0') * k + c;
      c = d / b; d %= b;</pre>
```

```
while (c)
   s[i] = '0' + (c % b); i++;
   c /= b;
  s[i] = ' \setminus 0';
void add(char s[], int k)
  int i, c = k, d;
  for(i = 0; s[i]; i++)
   d = (s[i] - '0') + c;
   c = d / b; d %= b;
   s[i] = '0' + d;
  while (c)
   s[i] = '0' + (c % b); i++;
   c /= b;
  s[i]='\0';
void trans(char s[])
  for(int i = 0; s[i]; i++)
    char\& c = s[i];
   if(c >= 'A' \&\& c <= 'Z') c = '0' + 10 + (c - 'A');
    if(c >= 'a' \&\& c <= 'z') c = '0' + 36 + (c - 'a');
void itrans(char s[])
  for(int i = 0; s[i]; i++)
    char& c = s[i]; int d = c - '0';
   if(d >= 10 \&\& d <= 35) c = 'A' + (d - 10);
    if(d >= 36) c = 'a' + (d - 36);
int main()
//digitos \{0-9, A-Z, a-z\}
  int q; cin>>q;
  int i, j;
  while (q)
    q--;
    cin >> a >> b >> sa; sb[0] = '0'; sb[1] = '\0';
    // a e b sao dados na base 10
    // sa eh dado na base a
    // converter sa da base a pra base b
    cout << a << " " << sa << '\n';
```

s[i] = '0' + d;

```
trans(sa);
for(i = 0; sa[i]; i++)
{
    multi(sb, a);
    add(sb, sa[i] - '0');
}
rev(sb);
itrans(sb);
// sb eh a na base b
cout << b << " " << sb << '\n';
puts("");
}
return 0;</pre>
```

5.5 Counting Number Of Times That A Digit Appears Until N

```
11 digits(int n, int d)
{
    11 res = 0, pot = 1, rem = 0;
    while (n)
    {
        int x = n%10;
        n /= 10;
        if (x > d) res += (n+1)*pot;
        else res += n*pot;
        if (x == d) res += rem+1;
        if (d == 0) res -= pot;
        rem += pot * x;
        pot *= 10;
    }
    return res;
}
```

5.6 Fast Fourier Transform

```
#include <bits/stdc++.h>
using namespace std;

typedef complex<double> ftype;
const double pi = acos(-1);
const int maxn = 1 << 22;
ftype w[maxn];

void init()
{
   for(int i = 0; i < maxn; i++)
        w[i] = polar(1., 2 * pi / maxn * i);
}

template<typename T>
void fft(T *in, ftype *out, int n, int k = 1)
{
   if(n == 1)
    }
}
```

```
*out = *in;
        return;
    int t = maxn / n;
    n >>= 1:
    fft(in, out, n, 2 * k);
    fft(in + k, out + n, n, 2 * k);
    for(int i = 0, j = 0; i < n; i++, j += t)
        ftype t = w[j] * out[i + n];
        out[i + n] = out[i] - t;
        out[i] += t;
vector<ftype> evaluate(vector<int> p)
    while (__builtin_popcount (p.size()) != 1)
        p.push back(0);
    vector<ftype> res(p.size());
    fft(p.data(), res.data(), p.size());
    return res;
vector<int> interpolate(vector<ftype> p)
    int n = p.size();
    vector<ftype> inv(n);
    fft(p.data(), inv.data(), n);
    vector<int> res(n);
    for(int i = 0; i < n; i++)
        res[i] = round(real(inv[i]) / n);
    reverse(begin(res) + 1, end(res));
    return res;
void align(vector<int> &a, vector<int> &b)
    int n = a.size() + b.size() - 1;
    while(a.size() < n)</pre>
        a.push_back(0);
    while(b.size() < n)</pre>
        b.push_back(0);
vector<int> poly_multiply(vector<int> a, vector<int> b)
    align(a, b);
    auto A = evaluate(a);
    auto B = evaluate(b);
    for(int i = 0; i < A.size(); i++)</pre>
        A[i] \star = B[i];
    return interpolate (A);
const int base = 10:
vector<int> normalize(vector<int> c)
    int carry = 0;
    for(auto &it: c)
```

```
it += carry;
                                                                               cin >> s1 >> s2;// le os dois numeros como strings
                                                                               if(s1 == "0" or s2 == "0")
        carry = it / base;
       it %= base;
                                                                                 puts("0");
   while(carry)
                                                                                 continue;
                                                                               vector<int> A = faz(s1), B = faz(s2);
        c.push_back(carry % base);
        carry /= base;
                                                                               A = normalize(A);
                                                                               B = normalize(B);
                                                                               reverse(A.begin(), A.end());
   return c;
                                                                               reverse(B.begin(), B.end());
vector<int> multiply(vector<int> a, vector<int> b)
                                                                               auto C = multiply(A, B);
   return normalize(poly_multiply(a, b));
                                                                               while(C.back() == 0)
                                                                                     C.pop_back();
                                                                               reverse(C.begin(), C.end());
vector<int> faz(string s)
                                                                               for(int &c: C)
                                                                                 cout << c:
 vector<int> ans;
                                                                               puts("");
  for (char &c : s)
   ans.push back (c-'0');
                                                                             /*
  return ans;
                                                                                 vector<int> a = \{3, 4\}, b = \{2, 3\};
string multAB(string s1, string s2)
                                                                               auto C = poly_multiply(a, b);
                                                                               int k = int(a.size() + b.size()) - 1;
  if(s1 == "0" or s2 == "0")
                                                                               for(int i = 0; i < k; i++)
   return "0";
                                                                                   cout << C[i] << "X^" << k-i-1 << (i < k-1 ? " + " : "\n");
 bool sinall;
  if(s1[0] == '-' and s2[0] == '-' or s1[0] != '-' and s2[0] != '-')
    sinall = true:
                                                                               return 0:
  else
   sinall = false:
  if(s1[0] == '-') s1[0] = '0';
  if(s2[0] == '-') s2[0] = '0';
  vector < int > A = faz(s1), B = faz(s2);
                                                                           A = normalize(A);
  B = normalize(B);
  reverse(A.begin(), A.end());
  reverse(B.begin(), B.end());
                                                                           #include <bits/stdc++.h>
  auto C = multiply(A, B);
  while(C.back() == 0)
                                                                           using namespace std;
     C.pop_back();
                                                                           typedef long double ld;
  reverse(C.begin(), C.end());
                                                                           const double PI = acos(-1);
  string ans;
  ans += (!sinall ? "-" : "");
                                                                           struct T
  for(int &c: C)
   ans += char(c + '0');
  return ans;
                                                                             ld x, y;
                                                                             T() : x(0), y(0) \{ \}
                                                                             T(1d a, 1d b=0) : x(a), y(b) {}
int main()
                                                                             T operator/=(ld k) { x/=k; y/=k; return (*this); }
                                                                             T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
  int t;
                                                                             T operator+(T a) const { return T(x+a.x, y+a.y); }
   init();
                                                                             T operator-(T a) const { return T(x-a.x, y-a.y); }
   cin >> t:
                                                                           a[1 << 23], b[1 << 23];
   while (t--)
                                                                           void fft(T* a, int n, int s)
   string s1, s2;
```

```
for (int i=0, j=0; i<n; i++)</pre>
    if (i>j) swap(a[i], a[j]);
    for (int l=n/2; (j^=1) < 1; l>>=1);
  for (int i = 1; (1<<i) <= n; i++)
    int M = 1 << i;</pre>
    int K = M >> 1;
    T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
    for (int j = 0; j < n; j += M)
      T w = T(1, 0);
      for (int 1 = j; 1 < K + j; ++1)
        T t = w * a[1 + K];
        a[1 + K] = a[1]-t;
        a[1] = a[1] + t;
        w = wn * w;
void multiply(T* a, T* b, int n)
  fft(a,n,1);
  fft(b,n,1);
  for (int i = 0; i < n; i++)</pre>
   a[i] = a[i] * b[i];
  fft(a, n, -1);
  for (int i = 0; i < n; i++)</pre>
    a[i] /= n;
int main()
  int n, na, nb, c;
  cin >> na >> nb;
  n = na + nb;
  while (n&(n-1))
  for (int i = n - na; i < n; i++)
    cin >> c;
    a[i] = T(c);
  for (int i = n - nb; i < n; i++)
    cin >> c;
    b[i] = T(c);
  multiply(a, b, n);
  for (int i = 0; i < n - 1; i++)
    cout << int(a[i].x + 0.5) << "X^"
     << n - 2 - i << (i < n - 2 ? " + " : "");
  puts("");
  /*
   3 2
    1 0 0
```

```
0X^{6} + 0X^{5} + 0X^{4} + 2X^{3} + 3X^{2} + 0X^{1} + 0X^{0}
 return 0;
//contar quantos subarrays de soma diferentes existem usando FFT
#include <bits/stdc++.h>
using namespace std;
typedef long double ld;
const long double PI = acos(-1);
struct T
  ld x, y;
 T() : x(0), y(0) \{ \}
 T(1d a, 1d b=0) : x(a), y(b) {}
 T operator/=(ld k) { x/=k; y/=k; return (*this); }
 T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
  T operator+(T a) const { return T(x+a.x, y+a.y); }
  T operator-(T a) const { return T(x-a.x, y-a.y); }
} a[16777219], b[16777219];
int pd[16777219];
void fft(T* a, int n, int s)
  for(int i=0, j=0; i<n; i++)</pre>
   if (i>j) swap(a[i], a[j]);
   for (int l=n/2; (j^=1) < 1; l>>=1);
  for(int i = 1; (1<<i) <= n; i++)</pre>
   int M = 1 << i;</pre>
   int K = M >> 1;
   T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
    for(int j = 0; j < n; j += M)
     T w = T(1, 0);
     for (int 1 = j; 1 < K + j; ++1)
       T t = w*a[1 + K];
       a[1 + K] = a[1]-t;
       a[1] = a[1] + t;
       w = wn * w;
void multiply(T* a, T* b, int n)
  fft(a,n,1);
```

```
fft(b,n,1);
  for (int i = 0; i < n; i++)</pre>
                                                                            using namespace std;
   a[i] = a[i] * b[i];
 fft(a,n,-1);
                                                                            typedef long double ld;
 for (int i = 0; i < n; i++)</pre>
                                                                            const double PI = acos(-1);
   a[i] /= n;
                                                                            struct T
int main()
                                                                              ld x, y;
                                                                              T() : x(0), y(0) \{ \}
 int k;
                                                                              T(1d a, 1d b=0) : x(a), y(b) {}
 cin >> k:
  for(int i = 1; i <= k; i++)</pre>
                                                                              T operator/=(ld k) { x/=k; y/=k; return (*this); }
                                                                              T operator*(T a) const { return T(x*a.x - y*a.y, x*a.y + y*a.x); }
                                                                              T operator+(T a) const { return T(x+a.x, y+a.y); }
   int aux;
   cin >> aux;
                                                                              T operator-(T a) const { return T(x-a.x, y-a.y); }
   pd[i] = pd[i - 1] + aux;
                                                                            a[1 << 20], b[1 << 20];
  if(k >= 10000)
                                                                            void fft(T* a, int n, int s)
   for(int i = 0; i <= k; i++)</pre>
                                                                              for (int i=0, j=0; i<n; i++)</pre>
     a[pd[i] + pd[k]].x = 1;
                                                                                if (i>j) swap(a[i], a[j]);
     b[pd[k] - pd[i]].x = 1;
                                                                                for (int l=n/2; (\dot{1}=1) < 1; l>>=1);
   int n = pd[k] + pd[k];
                                                                              for(int i = 1; (1<<i) <= n; i++)</pre>
   n = 2 * n;
   while (n \& (n - 1))
                                                                                int M = 1 << i;</pre>
     n++;
                                                                                int K = M >> 1;
   multiply(a, b, n);
                                                                                T wn = T(\cos(s*2*PI/M), \sin(s*2*PI/M));
   int ans = 0;
                                                                                for (int j = 0; j < n; j += M)
   for(int i = 0; i <= n; i++)</pre>
     if (int (a[i].x + 0.5) > 0 and (i - 2 * pd[k]) > 0)
                                                                                  T w = T(1, 0);
        ans++;
                                                                                  for (int 1 = j; 1 < K + j; ++1)
   cout << ans << '\n';
                                                                                    T t = w * a[1 + K];
 else
                                                                                    a[1 + K] = a[1]-t;
                                                                                    a[1] = a[1] + t;
   int cnt = 0;
                                                                                    w = wn *w;
   unordered_set<int> ans1;
   for(int i = 1; i <= k; i++)</pre>
     for(int j = i; j <= k; j++)</pre>
        if (ans1.find(pd[j] - pd[i - 1]) == ans1.end())
                                                                            void multiply(T* a, T* b, int n)
         ans1.insert(pd[j] - pd[i - 1]);
         cnt++;
                                                                              fft(a,n,1);
   cout << cnt << '\n';
                                                                              fft(b,n,1);
                                                                              for (int i = 0; i < n; i++)
                                                                                a[i] = a[i] * b[i];
  // quantidade de subarrays com soma diferente
                                                                              fft(a,n,-1);
 return 0;
                                                                              for (int i = 0; i < n; i++)</pre>
                                                                                a[i] /= n;
                                                                            const int base = 10:
    int carry = 0;
                                                                                for(auto &it: c)
#include <bits/stdc++.h>
```

```
it += carry;
        carry = it / base;
        it %= base;
    while (carry)
        c.push_back(carry % base);
        carry /= base;
    return c;
vector<int> faz(string s)
  vector<int> ans:
  for (char &c : s)
    ans.push_back(c-'0');
  return ans;
string mul(string s1, string s2)
  vector<int> A = normalize(faz(s1));
  vector<int> B = normalize(faz(s2));
  int na = A.size(), nb = B.size();
  int n = na + nb;
  while (n&(n-1))
   n++;
  reverse(A.begin(), A.end());
  reverse(B.begin(), B.end());
  while(A.size() < n) A.push_back(0);</pre>
  while(B.size() < n) B.push_back(0);</pre>
  reverse(A.begin(), A.end());
  reverse(B.begin(), B.end());
  for(int i = 0; i < n; i++)</pre>
    a[i] = T(A[i]);
  for(int i = 0; i < n; i++)</pre>
    b[i] = T(B[i]);
  multiply(a, b, n);
  vector<int> r;
  for (int i = 0; i < n - 1; i++)
    r.push_back(a[i].x + 0.5);
  reverse(r.begin(), r.end());
  r = normalize(r);
  while(r.back() == 0)
          r.pop_back();
  reverse(r.begin(), r.end());
  string ans;
```

```
for(int &c: r)
    ans.push_back(c + '0');

return ans;
}
int main()
{
    return 0;
}
```

5.7 Gaussian Elimination For Max Subset Xor

```
#include <bits/stdc++.h>
using namespace std;
#define ull unsigned long long
int MSB(ull n)
    int cnt = 0;
    while(n)
        cnt++;
        n >>= 1;
    return cnt;
int main()
    int n;
    cin >> n;
    ull a[n];
    for(int i = 0; i < n; i++)</pre>
        cin >> a[i];
    int lengths[n];
    for(int i = 0; i < n; i++)</pre>
        lengths[i] = MSB(a[i]);
    //eh um array que armazena os coeficientes
    //das equacoes
    vector<ull> buckets[65];
    //para a Gaussian Elimination, semelhante
    //a linha da matriz em algebra linear
    for(int i = 0; i < n; i++)</pre>
        buckets[lengths[i]].push_back(a[i]);
    ull modified_array[100], m_index = 0;
    // Gaussian Elimination
    for(int i = 64; i > 0; i--)
        if(buckets[i].size())
            modified_array[m_index++] = buckets[i][0];
            for(int j = 1; j < buckets[i].size(); j++)</pre>
                ull temp = buckets[i][0] ^ buckets[i][j];
                int len = MSB(temp);
```

```
buckets[len].push_back(temp);
}
ull ans = 0;
for(int i = 0; i < m_index; i++)
    if(ans < (ans ^ modified_array[i]))
        ans = (ans ^ modified_array[i]);
cout << ans << '\n';
return 0;
}</pre>
```

5.8 Karatsuba

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<long long> vll;
vll karatsubaMultiply(const vll &a, const vll &b) {
  int n = a.size();
  vll res(n + n);
  if (n <= 32)
      for (int i = 0; i < n; i++)</pre>
      for (int j = 0; j < n; j++)
          res[i + j] += a[i] * b[j];
      return res;
  int k = n \gg 1;
  vll a1(a.begin(), a.begin() + k);
  vll a2(a.begin() + k, a.end());
  vll b1(b.begin(), b.begin() + k);
  vll b2(b.begin() + k, b.end());
  vll alb1 = karatsubaMultiply(a1, b1);
  vll a2b2 = karatsubaMultiply(a2, b2);
  for(int i = 0; i < k; i++)</pre>
      a2[i] += a1[i];
  for(int i = 0; i < k; i++)</pre>
      b2[i] += b1[i];
  vll r = karatsubaMultiply(a2, b2);
  for(int i = 0; i < (int) alb1.size(); i++)</pre>
      r[i] = a1b1[i];
  for(int i = 0; i < (int) a2b2.size(); i++)</pre>
      r[i] -= a2b2[i];
  for(int i = 0; i < (int) r.size(); i++)</pre>
      res[i + k] += r[i];
  for(int i = 0; i < (int) alb1.size(); i++)</pre>
      res[i] += a1b1[i];
  for(int i = 0; i < (int) a2b2.size(); i++)</pre>
      res[i + n] += a2b2[i];
  return res;
int main()
```

```
vll a = {8, 7, 5};
vll b = {12};

vll c = karatsubaMultiply(a, b);

for(auto it : c) cout << it << ' '; puts("");

return 0;
}</pre>
```

5.9 Matrix Exponentiation

```
#include <bits/stdc++.h>
using namespace std;
#define matrix vector<vector<int>>
matrix init(int n, int m, int value = 0)
    return vector<vector<int>>(n, vector<int>(m, value));
void printtt(const matrix &M)
    for(int i = 0; i < M.size(); i++)</pre>
        for(int j = 0; j < M[0].size(); j++)</pre>
            cout << M[i][j] << ' ';
        puts("");
matrix multiply (const matrix &A, const matrix &B)
    matrix C = init(A.size(), B[0].size());
    for(int i = 0; i < A.size(); i++)</pre>
        for(int j = 0; j < B[i].size(); j++)</pre>
            for(int k = 0; k < B.size(); k++)
                C[i][j] += A[i][k] * B[k][j];
    return C;
matrix exp(matrix M, int k)
    matrix I = init(M.size(), M[0].size());
    for(int i = 0; i < M.size(); i++) I[i][i] = 1;</pre>
    while(k)
        if (k \& 1) I = multiply (I, M), k--;
        else M = multiply(M, M), k \neq 2;
    return I:
int determinantOfMatrix(matrix mat)
  int n = mat.size();
    int num1, num2, det = 1, index, total = 1;
    int temp[n + 1];
    for(int i = 0; i < n; i++)</pre>
```

```
index = i;
        while (mat[index][i] == 0 and index < n)</pre>
            index++;
        if(index == n)
            continue;
    if(index != i)
            for (int j = 0; j < n; j++)
                 swap(mat[index][j], mat[i][j]);
            det = det*pow(-1, index-i);
    for (int j = 0; j < n; j++)
      temp[j] = mat[i][j];
    for (int j = i+1; j < n; j++)
      num1 = temp[i];
      num2 = mat[j][i];
      for (int k = 0; k < n; k++)
        mat[j][k] = (num1 * mat[j][k]) - (num2 * temp[k]);
      total = total * num1;
    for(int i = 0; i < n; i++)</pre>
        det = det * mat[i][i];
    return (det/total);
int32_t main()
    int n, m;
    cin >> n >> m;
    matrix A = init(n, m);
    for(int i = 0; i < n; i++)</pre>
        for(int j = 0; j < m; j++)
            cin >> A[i][j];
    matrix C = \exp(A, 7);
    printtt(C);
    return 0;
```

5.10 Miller Rabin

```
#include <bits/stdc++.h>
using namespace std;
#define ll long long

ll add(ll a, ll b, ll c)
{
    ll ans = (a + b) % c;
        if(ans < 0) ans += c;
        return ans;
}

ll mulmod(ll a, ll b, ll c)
{
    ll ans = 0;
    while(b)</pre>
```

```
if(b & 1) ans = add(ans, a, c);
    a = add(a, a, c);
    b /= 2;
  return ans;
ll fexp(ll a, ll b, ll c)
  ll ans = 1;
  while (b)
    if(b \& 1) ans = mulmod(ans, a, c);
    a = mulmod(a, a, c);
    b /= 2;
  return ans;
bool miller(ll a, ll n)
    if (a >= n) return true;
    11 s = 0, d = n - 1;
    while (d%2 == 0 \text{ and } d) d >>= 1, s++;
    11 x = fexp(a, d, n);
    if(x == 1 or x == n - 1) return true;
    for (int r = 0; r < s; r++, x = mulmod(x, x, n))
        if (x == 1) return false;
        if (x == n-1) return true;
    return false:
bool isprime(ll n)
    int base[] = {2, 3, 5, 7, 11,
       13, 17, 19, 23, 29, 31, 37};
    for(int i = 0; i < 12; i++)
        if(!miller(base[i], n))
             return false:
    return true;
int32 t main()
    ll n;
    cin >> n;
    cout << (isprime(n) ? "PRIME\n"</pre>
       : "NOT PRIME\n");
    return 0;
```

5.11 Mobius

```
/* - mi(n) = 0 se n tem como divisor um outro numero natural ao quadrado
```

```
-mi(n) = 1 se n nao tem como divisor um outro
numero natural ao quadrado
e eh decomposto em uma quantidade par de
numeros primos
- mi(n) = -1 se n nao tem como divisor um outro
numero natural ao quadrado
e eh decomposto em uma quantidade impar de
numeros primos
#include "bits/stdc++.h"
using namespace std;
const int MAX = 1e6;
bool np[MAX];
int mob[MAX];
void mobius()
  for(int i = 1; i < MAX; i++)</pre>
    mob[i] = 1;
  for(int i = 2; i < MAX; i++)</pre>
    if(np[i]) continue;
    for(int j = i; j < MAX; j += i)
      np[j] = true;
      mob[j] *= -1;
      if((j / i) % i == 0)
       mob[j] = 0;
int main()
 mobius();
    for(int i = 2; i <= 10; i++)</pre>
      cout << i << ' ' << mob[i] << '\n';
  puts("");
  return 0;
```

5.12 Mod Gaussian Elimination

```
#include<bits/stdc++.h>
using namespace std;
//#define int long long
#define pb push_back
#define inf 0x3f3f3f3f

int MOD = 1000000007LL;

inline int prod(int a, int b)
{
   return ((((a % MOD) * 1LL * (b % MOD)) % MOD) + MOD) % MOD;
}
```

```
inline int sub(int a, int b)
  return ((((a % MOD) - (b % MOD)) % MOD) + MOD) % MOD;
inline int expMod(int x, int e)
  int ans = 1;
  while (e > 0)
   if(e & 1LL) ans = prod(ans, x), e--;
   else x = prod(x, x), e \neq 2;
  return ans;
inline int inv(int x)
  return expMod(x, MOD - 2);
inline int gauss (vector<vector<int>> a, int mod)
 MOD = mod;
    int n = (int) a.size();
    int m = (int) a[0].size();
    vector<int> where (m, -1);
    for (int col = 0, row = 0; col < m and row < n; ++col)
        int sel = row;
        for(int i = row; i < n; ++i)
            if(abs(a[i][col]) > abs(a[sel][col]))
                sel = i;
        if(a[sel][col] == 0)
            continue:
        for(int i = col; i < m; ++i)</pre>
            swap(a[sel][i], a[row][i]);
        where [col] = row;
        for(int i = row + 1; i < n; ++i)</pre>
            int c = prod(a[i][col], inv(a[row][col]));
            for(int j = col; j < m; ++j)</pre>
            a[i][j] = sub(a[i][j], prod(a[row][j], c));
        ++row;
  int ans = 0;
    for(int i = 0; i < m; ++i)</pre>
        if(where[i] != -1)
            ans++;
    return n - ans;
int32_t main()
  int n, m, a, k, t, caso = 1;
  cin >> t:
  while (t--)
```

```
{
    scanf(" %d %d %d", &n, &m, &k);
    vector<vector<int>> A(n, vector<int>(n));
    while(m--)
    {
        int u, v;
        scanf(" %d %d", &u, &v), u--; v--;
        A[u][v] = A[v][u] = 1;
        if(u != v) A[u][v] = A[v][u] = k - 1;
    }
    for(int i = 0; i < n; i++) A[i][i] = 1;
    int ans = gauss(A, k);
    MOD = 1000000007LL;
    printf("Case %d: %d\n", caso++, expMod(k, ans));
}
return 0;</pre>
```

5.13 Modular Arithmetic

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
const int MOD = 1000000007LL;
int normalize(int x)
 x = x % MOD;
 if(x < 0) x += MOD;
 return x;
int add(int a, int b)
  return normalize(normalize(a) + normalize(b));
int prod(int a, int b)
  return normalize(normalize(a) * normalize(b));
int sub(int a, int b)
  return normalize(normalize(a) - normalize(b));
int expMod(int x, int e)
 int ans = 1:
  while(e > 0)
   if(e & 1LL) ans = prod(ans, x), e--;
    else x = prod(x, x), e \neq 2;
  return normalize(ans);
int inv(int x)
```

```
{
    return expMod(x, MOD - 2);
}

int extended_euclidean(int a, int b, int& x, int& y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    }
    int x1, y1;
    int d = extended_euclidean(b, a % b, x1, y1);
    x = y1;
    y = x1 - y1 * (a / b);
    return d;
}

int inv(int a, int m) {
    int x, y;
    int g = extended_euclidean(a, m, x, y);
    if (g != 1) return -1; // nao tem inverso
    return ((x % m) + m) % m;
}
```

5.14 Mulmod Trick

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;

ll mulmod(ll a, ll b, ll m)
{
    ll q = ll((long double)a*b/m);
    ll r = a * b - m * q;
    while(r < 0) r += m;
    while(r >= m) r -= m;
    return r;
}

int main()
{
    ll a, b, c;
    cin >> a >> b >> c;
    cout << mulmod(a, b, c) << '\n';
    return 0;
}</pre>
```

5.15 Pollard Rho

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long

11 llrand()
```

```
11 \text{ tmp} = \text{rand();}
  return (tmp << 31) | rand();
ll add(ll a, ll b, ll c)
 ll ans = (a + b) % c;
    if(ans < 0) ans += c;
    return ans;
ll mulmod(ll a, ll b, ll c)
  11 \text{ ans} = 0;
  while (b)
    if(b & 1) ans = add(ans, a, c);
    a = add(a, a, c);
    b /= 2;
  return ans;
ll rho(ll n)
    if(n % 2 == 0) return 2;
    11 d = n;
    while(d == n)
        ll c = llrand() % n, x = llrand() % n, y = x;
            x = add(mulmod(x, x, n), c, n);
            y = add(mulmod(y, y, n), c, n);
            y = add(mulmod(y, y, n), c, n);
            d = \underline{gcd(abs(x - y), n)};
        }while(d == 1);
    return d;
// Miller-Rabin AOUI
vector<ll> fac;
void factors(ll n) // encontrar os fatores primos de N
{// Usar Miller-Rabin para testar se N eh primo
    if(n == 1) return;
    if(isprime(n)) { fac.push back(n); return; }
    11 d = rho(n);
    factors(d);
    factors(n / d);
int32_t main()
    srand(time(NULL));
    11 n;
    cin >> n;
    cout << rho(n) << '\n';
```

```
return 0;
```

6 Geometry

6.1 Andrew Algorithm Convex Hull

```
#include <bits/stdc++.h>
using namespace std;
#define X first
#define Y second
typedef pair<int, int> ii;
int cross(ii O, ii A, ii B)
    return (((A.X - O.X) * (B.Y - O.Y)) - ((A.Y - O.Y) * (B.X - O.X)))
vector<ii> ConvexHull(vector<ii> P)
  if(P.size() <= 1) return P;</pre>
   vector<ii>> H(2*P.size());
    int k = 0;
    sort(P.begin(), P.end());
    //lower hull
    for(int i = 0; i < P.size(); i++)</pre>
        while (k \ge 2 \text{ and } cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    //upper hull
    for(int i = P.size()-2, l = k + 1; i >= 0; i--)
        while (k \ge 1 \text{ and } cross(H[k-2], H[k-1], P[i]) < 0) k--;
        H[k++] = P[i];
    H.resize(k-1);
    return H;
int main()
    int n, x, y;
    vector<ii>> P;
    cin >> n:
    while (n--)
        cin >> x >> y;
        P.push_back(\{x, y\});
    vector<ii> H = ConvexHull(P);
    for(int i = 0; i < H.size(); i++)</pre>
        cout << H[i].X << ' ' << H[i].Y << '\n';
```

```
return 0;
```

6.2 Build Two Lines That Go Through All Points Of A Set

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6 + 10;
typedef long long 11;
struct Point
    11 x, y;
    Point(ll _x, ll _y) : x(_x), y(_y) {}
    Point() {}
    Point operator-(const Point& p)
        return Point(x - p.x, y - p.y);
    11 operator*(const Point& p)
        return (x * p.y) - (y * p.x);
};
int n;
int visit[MAX];
Point point [MAX];
bool inLine(int a, int b, int c)
    return ((point[a] - point[c]) * (point[b] - point[c])) == 0LL;
bool check(int a, int b) // traca a reta AB e verifica se todos os
//pontos que nao estao em AB estao contidos em uma mesma reta
    memset(visit, 0, sizeof(visit));
    visit[a] = visit[b] = 1;
    for(int i = 0; i < n; i++)</pre>
        if(!visit[i] and inLine(a, b, i))
            visit[i] = 1;// marco todos os pontos que estao na reta AB
    vector<int> c;
    for(int i = 0; i < n and c.size() < 2; i++)</pre>
        if(!visit[i])
            c.push_back(i);// procuro dois pontos que nao estao na
                reta AB
    if(c.size() < 2) return true;</pre>
    visit[c[0]] = visit[c[1]] = 1;
    for(int i = 0; i < n; i++)</pre>
        if(!visit[i])
        { // checo se o ponto que nao esta na reta AB esta na reta
            if(inLine(c[0], c[1], i))
                visit[i] = 1;
            else
                return false;
    return true;
```

```
int main()
{
    cin >> n;
    for(int i = 0; i < n; i++)
        cin >> point[i].x >> point[i].y;
    if(n <= 2) return cout << "YES\n", 0;
    int k = 2;
    while(k < n and inLine(0, 1, k)) k++;
    if(k == n) return cout << "YES\n", 0;
    cout << ((check(0, 1) or check(0, k)
        or check(1, k)) ? "YES\n" : "NO\n");
    return 0;
}</pre>
```

6.3 Check If A Point Is Inside A Convex Polygon

```
#include <bits/stdc++.h>
using namespace std;
#define int long long
#define ii pair<int, int>
#define fi first
#define se second
int n:
vector<ii>> P;
ii operator-(ii a, ii b)
    return {a.fi - b.fi, a.se - b.se};
int operator*(ii a, ii b)
    return a.fi * b.se - a.se * b.fi;
void setFirstPoint()
    int pos = 0;
    for(int i = 0; i < n; i++)
        if(P[i].fi < P[pos].fi or P[i].fi == P[pos].fi and P[i].se < P</pre>
            [pos].se)
            pos = i;
    rotate(P.begin(), P.begin() + pos, P.end());
bool pointInTriangle(ii a, ii b, ii c, ii p)
    int s1 = abs((a - c) * (b - c));
    int s2 = abs((a - p) * (b - p)) + abs((b - p) * (c - p)) +
       abs((c - p) * (a - p));
    return s1 == s2; //mesma area
int dist(ii a, ii b)
```

```
return (a.fi - b.fi) * (a.fi - b.fi) + (a.se - b.se) * (a.se - b.
        se);
// O(logN) per query
bool pointInConvexPolygon(ii p)
    //adicionar = desconsidera pontos na borda
    if((P[1] - P[0]) * (p - P[0]) < 0)
        return false:
    //adicionar = desconsidera pontos na borda
    if((p - P[0]) * (P[n - 1] - P[0]) < 0)
        return false:
    //o ponto esta em cima do segento P[0], P[n-1]
    if((p - P[0]) * (P[n - 1] - P[0]) == 0)
        return dist(P[0], p) <= dist(P[0], P[n-1]) and dist(P[n-1])
            1], p) \leq dist(P[0], P[n - 1]);
    //o ponto esta em cima do segento P[0], P[1]
    if((P[1] - P[0]) * (p - P[0]) == 0)
        return dist(P[0], p) <= dist(P[0], P[1]) and dist(P[1], p) <=
             dist(P[0], P[1]);
    // se o ponto esta entre os segmentos P[0], P[n]
    int 1 = 0, e = n - 1, ans = 0;
    while(1 <= e)
        int m = 1 + (e - 1) / 2;
        if((P[m] - P[0]) * (p - P[0]) >= 0) 1 = m + 1, ans = m;
        else e = m - 1;
    return pointInTriangle(P[ans], P[ans + 1], P[0], p);
int32_t main()
    int q, x, y;
    cin >> n >> q;
    for(int i = 0; i < n; i++)</pre>
    {//poligono no sentido anti-horario
        cin >> x >> y;
        P.push_back(\{x, y\});
    setFirstPoint():
    while (q--)
        cin >> x >> v;
        cout << (pointInConvexPolygon({x, y}) ? "Dentro" : "Fora") <<</pre>
            '\n';
    return 0;
```

6.4 Convex Hull Trick

```
#include <bits/stdc++.h>
using namespace std;
#define type int
const int MAX = 1e5;
const int 00 = 0x3f3f3f3f3f;
```

```
struct line
  type m, b;
  line(type _m, type _b) { m = _m, b = _b; }
int pointer; // Keeps track of the best line from previous query
vector<line> hull;//store hull
//Returns true if line 13 is always better than line 12
bool bad(int 11, int 12, int 13)
    intersection (11,12) has x-coordinate (b1-b2)/(m2-m1)
  intersection(11.13) has x-coordinate (b1-b3)/(m3-m1)
  set the former greater than the latter, and cross-multiply to
    eliminate division
  line L1 = hull[11], L2 = hull[12], L3 = hull[13];
  return (L3.b-L1.b) * (L1.m-L2.m) < (L2.b-L1.b) * (L1.m-L3.m);
//Adds a new line
void add(type m, type b)
    if(hull.size() > 0 and hull.back().m == m) return;
    //First, let's add it to the end
    hull.emplace_back(m, b);
    //If the penultimate is now made irrelevant between the
        antepenultimate
    //and the ultimate, remove it. Repeat as many times as necessary
    while (hull.size()>=3 and bad(hull.size()-3,hull.size()-2,hull.size
        ()-1))
        hull.erase(hull.end()-2);
//Returns v value of a function i
type eval(int i, type x)
  return hull[i].m * x + hull[i].b;
//Returns the minimum y-coordinate of any intersection
//between a given vertical line and the lower envelope
//O(N) for all queries (queries are in ascending order of x)
type query(type x)
    if(pointer >= hull.size())
        pointer = hull.size() - 1;
    while(pointer < hull.size()-1 and eval(pointer+1, x) < eval(</pre>
        pointer, x))
    pointer++;
    return eval(pointer, x);
//Returns the minimum y-coordinate of any intersection
//between a given vertical line and the lower envelope
//O(LogN) time (queries are in any order of x)
type binarySearch(type x)
 int b = 0, e = hull.size() - 1;
```

```
while (b < e)
   int mid = (b + e) / 2;
   if(eval(mid+1, x) < eval(mid, x)) b = mid + 1;
   else e = mid;
 return eval(b, x);
   Maximum Y coordenate query, we have two options:
   1) Maximum Y-coordenate query: multiply m and b by -1 and
   make minimum Y-corrdenate query...
   2) Order lines by increasing m if m is not equal, otherwise by
        decreasing b
       in the function query and binary Search change < to >
            eval(pointer+1, x) < eval(pointer, x)
            eval(pointer+1, x) > eval(pointer, x)
int main()
 int n;
   //Order lines by decreasing m if m is not equal, otherwise by
        increasing b
    for(int i = 0; i < n; i++)
        int m, b;
        cin >> m >> b;
        add(m, b);
   int q;
   cin >> q;
   vector<int> queries(q);//queries are in ascending order of x - run
         in O(N)
   for(int &w : queries)
   cin >> w:
  //processing queries in ascending order of x
  for(int &w : queries)
   cout << query(w) << '\n';
  int x;
  while (cin >> x) //queries are in any order of x - run in O(log N)
   cout << binarySearch(x) << '\n';</pre>
   return 0;
```

6.5 Distance Between Nearest Pair Of Points

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
const double EPS = 1e7;
typedef pair<double, double> ii;
vector<ii> v;
```

```
set<ii>> sy, sx;
int n;
int main()
    double x, v;
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> x >> y;
        v.push_back({x, y});
    sort(v.begin(), v.end());
    double d = 0x3f3f3f3f;
    for(int i = 0; i < n; i++)</pre>
        x = v[i].first, y = v[i].second;
        while(!sx.empty())
            ii p = *(sx.begin());
            if(p.first + d < x)
                 sy.erase({p.second, p.first});
                 sx.erase(p);
            else
                break;
        auto it = sy.lower_bound({int(floor(y-d))-1, 0});
        while(it != sy.end() and it->first < y + d + 1)</pre>
            d = min(d, hypot(x - it->second, y - it->first));
        sy.insert({y, x});
        sx.insert({x, y});
    cout << d << '\n';
    return 0:
```

6.6 Dynamic Convex Hull Trick

```
#include <bits/stdc++.h>
using namespace std;
#define type __int128
#define int __int128
#define gc getchar
#define pc putchar
#define Min(a, b) (a > b ? b : a)

inline void scanint(int &k)
{
  bool sinal = true;
    register char c;
    k = 0;
    for(c = gc(); sinal and (c < '0' or c > '9'); c = gc())
        if(c == '-')
        sinal = false;
```

```
for(; c \ge '0' and c \le '9'; c = gc())
                                                                                    int mid = (b + e) / 2;
        k = (k \ll 3) + (k \ll 1) + c - '0';
                                                                                    if(eval(mid+1, x, hull) < eval(mid, x, hull)) b = mid + 1;</pre>
  if(!sinal) k = -k;
                                                                                    else e = mid;
                                                                                  return eval(b, x, hull);
inline void printint (int n)
                                                                               //########DAOUI PRA BAIXO EH O SUCESSO##################
  if (n < 0) pc('-');
 n = abs(n);
  int rev = n, cnt = 0;
                                                                               vector<line> merge(vector<line> a, vector<line> b)
  if(!n)
                                                                                    if(a.size() < b.size()) swap(a, b);</pre>
    pc('0');
                                                                                    for(int i = 0; i < b.size(); i++)</pre>
   pc('\n');
                                                                                        a.push_back(b[i]);
   return;
                                                                                    sort(a.begin(), a.end(), [](line c, line d)
                                                                                     { return c.m == d.m ? c.b < d.b : c.m > d.m; });
  while(!(rev % 10))
                                                                                    b.clear();
                                                                                    for(int i = 0; i < a.size(); i++)</pre>
    cnt++, rev /= 10;
  rev = 0:
                                                                                        add(a[i].m, a[i].b, b);
  while (n)
                                                                                    return b;
    rev = (rev << 3) + (rev << 1) + n % 10, n /= 10;
  while (rev)
    pc(rev % 10 + '0'), rev /= 10;
                                                                               vector<vector<line>> groups;
  while (cnt--)
   pc('0');
                                                                               void add(line 1)
 pc('\n');
                                                                                    vector<line> q = {1};
                                                                                    while(!groups.empty() and groups.back().size() <= g.size())</pre>
struct line
                                                                                        g = merge(g, groups.back());
                                                                                        groups.pop_back();
  type m, b;
  line(type _m, type _b) { m = _m, b = _b; }
                                                                                    groups.push_back(g);
    line() { m = 0, b = 0; }
};
                                                                               type query (int x)
bool bad(int 11, int 12, int 13, vector<line> &hull)
                                                                                    int ans = 0;
 line L1 = hull[11], L2 = hull[12], L3 = hull[13];
                                                                                    for(int i = 0; i < groups.size(); i++)</pre>
 return (L3.b-L1.b) * (L1.m-L2.m) < (L2.b-L1.b) * (L1.m-L3.m);
                                                                                        ans = Min(ans, binarySearch(x, groups[i]));
                                                                                    return -ans;
void add(type m, type b, vector<line> &hull)
                                                                                int32_t main()
    if(hull.size() > 0 and hull.back().m == m) return;
    hull.emplace_back(m, b);
                                                                                  int n, q;
    while (hull.size() >= 3 and bad(hull.size() - 3, hull.size() - 2, hull.size
                                                                                  scanint(n);
        ()-1, hull))
                                                                                  scanint (q);
        hull.erase(hull.end()-2);
                                                                                    vector<line> cyc(n + 1);
type eval(int i, type x, vector<line> &hull)
                                                                                    while (q--)
  return hull[i].m * x + hull[i].b;
                                                                                        int t, T;
                                                                                        scanint(t);
                                                                                        scanint(T);
type binarySearch(type x, vector<line> &hull)
                                                                                        if(t % 2 == 1)
  int b = 0, e = hull.size() - 1;
                                                                                            int N, C;
  while(b < e)</pre>
                                                                                            scanint(C);
                                                                                            scanint(N);
```

```
int b = - N * T + cyc[C].m * T + cyc[C].b;
    //cout << N << ' ' << b << '\n';
    add(line(-N, -b));
    cyc[C] = line(N, b);
}
else
    printint(query(T));
}
return 0;</pre>
```

6.7 Enclosing Circle R2

```
#include <cstdio>
#include <cmath>
int n;
double x[1005], y[1005], X, Y, d, e;
double dist(double a, double b) {
  return a*a + b*b:
int main() {
  scanf("%d", &n);
  for (int i = 0; i < n; i++) {</pre>
   scanf("%lf%lf", &x[i], &y[i]);
   X += x[i]; Y += y[i];
 X /= n; Y /= n;
  double P = 0.1;
  for (int i = 0; i < 30000; i++) {
   int f = 0;
    d = dist(X - x[0], Y - y[0]);
    for (int j = 1; j < n; j++) {
      e = dist(X - x[i], Y - v[i]);
      if (d < e) { d = e; f = j; }
    X += (x[f] - X) *P;
    Y += (y[f] - Y) *P;
    P *= 0.999;
  printf("%.31f %.31f\n%.31f", X, Y, sqrt(d));
```

6.8 Enclosing Circle R3

```
#include <cstdio>
#include <cmath>
int n;
double x[105], y[105], z[105], X, Y, Z, d, e;
double dist(double a, double b, double c) {
  return a*a + b*b + c*c;
}
int main() {
  scanf("%d", &n);
  for (int i = 0; i < n; i++) {
    scanf("%lf%lf%lf", &x[i], &y[i], &z[i]);
    X += x[i];
    Y += y[i];</pre>
```

```
Z += z[i];
X /= n; Y /= n; Z /= n;
double P = 0.1;
for (int i = 0; i < 70000; i++) {</pre>
  int f = 0;
  d = dist(X - x[0], Y - y[0], Z - z[0]);
  for (int j = 1; j < n; j++) {
    e = dist(X - x[j], Y - y[j], Z - z[j]);
    if (d < e) {
      d = e;
      f = \dot{j};
  X += (x[f] - X) *P;
  Y += (v[f] - Y) *P;
  Z += (z[f] - Z) *P;
  P *= 0.998;
printf("%.10lf %.10lf %.10lf", X, Y, Z);
```

6.9 Geometry Stan

```
struct PT {
  double x, y;
  PT() {}
  PT(double x, double y) : x(x), y(y) {}
 PT(const PT &p) : x(p.x), y(p.y) {}
  PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
  PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
  PT operator * (double c) const { return PT(x*c, y*c); }
  PT operator / (double c) const { return PT(x/c, y/c); }
 bool operator == (PT p) const {
    return (fabs(x-p.x) < EPS && (fabs(y-p.y) < EPS)); };
  bool operator < (PT p) const {</pre>
    if(fabs(x-p.x) > EPS) return x<p.x; return y<p.y; };</pre>
};
// dot(p,q) = length(p) *length(q) *cos(angle between p and q)
double dot(PT p, PT q) { return p.x*q.x+p.v*q.v; }
double dist2(PT p, PT q) { return dot(p-q,p-q); }
double dist(PT p, PT q) { return sqrt(dist2(p,q)); }
double mdist(PT p, PT q) { return fabs(p.x-q.x)+fabs(p.y-q.y); }
double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
ostream & operator << (ostream &os, const PT &p) {return os << "("<<p.x<<",
    "<<p.v<<")";}
// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x); }
PT RotateCW90(PT p) { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
  return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// returns angle aob in rad
double angle (PT a, PT o, PT b) {
  return acos(dot(a-o,b-o)/sqrt(dot(a-o,a-o)*dot(b-o,b-o)));
// returns true if point r is on the left side of line pg
bool ccw(PT p, PT q, PT r) {
  return cross(p,q)+cross(q,r)+cross(r,p) > 0;
```

```
// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
 return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
  double r = dot(b-a,b-a);
  if (fabs(r) < EPS) return a;</pre>
  r = dot(c-a, b-a)/r;
 if (r < 0) return a;</pre>
  if (r > 1) return b;
  return a + (b-a) *r;
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
 return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,v,z) and plane ax+bv+cz=d
double DistancePointPlane (double x, double y, double z,
double a, double b, double c, double d) {
  return fabs(a*x+b*v+c*z-d)/sgrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
 return fabs(cross(b-a, c-d)) < EPS;</pre>
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
    && fabs(cross(a-b, a-c)) < EPS
    && fabs(cross(c-d, c-a)) < EPS;
// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
 if (LinesCollinear(a, b, c, d)) {
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
    if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
      return false:
    return true;
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true;
// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
 b=b-a; d=c-d; c=c-a;
 assert (dot (b, b) > EPS && dot (d, d) > EPS);
  return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
 b = (a+b)/2;
  c = (a+c)/2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90
      (a-c));
```

```
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT g) {
  bool c = 0;
 for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1)%p.size();
   if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
     p[j].y \le q.y \&\& q.y < p[i].y) \&\&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y)
          il.v))
       c = !c;
  return c;
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT g) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) <</pre>
      return true;
  return false;
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
 vector<PT> ret:
 b = b-a;
 a = a-c;
 double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push back(c+a+b*(-B+sgrt(D+EPS))/A);
 if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret:
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
 vector<PT> ret;
  double d = sgrt(dist2(a, b));
  if (d > r+R \mid | d+min(r, R) < max(r, R)) return ret;
  double x = (d*d-R*R+r*r)/(2*d);
  double y = sqrt(r*r-x*x);
 PT v = (b-a)/d;
 ret.push back(a+v*x + RotateCCW90(v)*v);
 if ( \lor > 0 )
   ret.push_back(a+v*x - RotateCCW90(v)*y);
  return ret;
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
```

```
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
   int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
// gravity center
PT ComputeCentroid(const vector<PT> &p) {
 PT c(0,0):
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
   int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  return c / scale;
// tests whether or not a given polygon (in CW or CCW order) is simple
// segments do not intersect
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++) {</pre>
    for (int k = i+1; k < p.size(); k++) {</pre>
      int j = (i+1) % p.size();
      int 1 = (k+1) % p.size();
      if (i == l \mid | j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false:
  return true;
// compute two center's of circle given two points a and b
// and a radius r
pair<PT, PT> CumputeTwoCircleCenter(PT a, PT b, double R)
  if(dist(a, b) < EPS)</pre>
    return {a, b};
 PT middle = (a + b) / 2;
 PT v = RotateCCW90 (middle - a);
 v = v / sqrt(dot(v, v));
  double l = 0, r = 100, escalar;
  for (int i = 0; i < 100; i++)
    double mid = (1 + r) / 2;
    PT u = v * mid + middle;
    if(dist(a, u) \le R + EPS)
     l = mid, escalar = mid;
    else
      r = mid;
  PT c1 = v * escalar + middle;
  PT c2 = v * (-escalar) + middle;
```

```
return {c1, c2};
```

6.10 Graham Scan

```
#include <bits/stdc++.h>
using namespace std;
#define ii pair<int, int>
#define fi first
#define se second
vector<ii>> P;
ii operator-(ii a, ii b)
    return ii(a.fi - b.fi, a.se - b.se);
ii operator+(ii a, ii b)
    return ii(a.fi + b.fi, a.se + b.se);
int operator*(ii a, ii b)
    return a.fi * b.se - a.se * b.fi;
int dist(ii a, ii b)
    return (a.fi - b.fi) * (a.fi - b.fi) + (a.se - b.se) * (a.se - b
        .se);
bool cmp(ii a, ii b)
    int cross = (a - P[0]) * (b - P[0]);
    if(!cross) return dist(P[0], a) > dist(P[0], b);
    return cross > 0;
void setFirstPoint()
    for(int i = 1; i < P.size(); i++)</pre>
        if(P[i].fi < P[0].fi or P[i].fi == P[0].fi and P[i].se < P[0].</pre>
            swap(P[0], P[i]);
vector<ii> GrahamScan()
    setFirstPoint():
    sort(P.begin() + 1, P.end(),cmp);
    vector<ii>> H(P.size() * 2);
    int k = 0;
    for(int i = 0; i < P.size(); i++)</pre>
    { //crsso <= 0 para remover os pontos colineares
        while (k > 2 \text{ and } (H[k-1] - H[k-2]) * (P[i] - H[k-1]) < 0)
             k--;
```

```
H[k++] = P[i];
}
H.resize(k);
return H;
}

int main()
{
    int n;
    cin >> n;
    for(int i = 0; i < n; i++)
    {
        ii p;
        cin >> p.fi >> p.se;
        P.push_back(p);
    }
    vector<ii>> H = GrahamScan();
    for(int i = 0; i < H.size(); i++)
        cout << H[i].fi << ' ' << H[i].se << '\n';
    return 0;
}</pre>
```

6.11 Maximum Dot Product

```
#include <bits/stdc++.h>
using namespace std:
#define int long long
#define X first
#define Y second
const int 00 = 0x3f3f3f3f3f3f3f3f3f;
typedef pair<int, int> ii;
int cross(ii O, ii A, ii B)
    return (((A.X - O.X) * (B.Y - O.Y)) - ((A.Y - O.Y) * (B.X - O.X)))
int dot(ii a, ii b)
    return a.X * b.X + a.Y * b.Y;
vector<ii> ConvexHull(vector<ii> P)
    if(P.size() <= 1) return P;</pre>
    vector<ii>> H(2*P.size());
    int k = 0;
    sort(P.begin(), P.end());
    for(int i = 0; i < P.size(); i++)</pre>
        while (k \ge 2 \text{ and } cross(H[k-2], H[k-1], P[i]) \le 0) k--;
        H[k++] = P[i]:
    for(int i = P.size()-2, l = k + 1; i >= 0; i--)
        while (k \ge 1 \text{ and } cross(H[k-2], H[k-1], P[i]) \le 0) k--;
        H[k++] = P[i];
    H.resize(k-1);
```

```
return H;
vector<ii> merge(vector<ii> H1, vector<ii> H2)
    for(auto &it : H2) H1.push back(it);
    return ConvexHull(H1);
int maxConcavityUp(int b, int e, vector<ii> &H, ii p)
    if(b > e) return -00;
    return max(dot(H[b], p), dot(H[e], p));
int maxConcavityDown(int b, int e, vector<ii> &H, ii p)
    if(b > e) return -00;
    b--:
    while (e - b > 1)
      int m = b + (e - b) / 2;
      if(dot(H[m], p) > dot(H[m + 1], p))
      else
          b = m;
    return dot(H[e], p);
int maximumDot(vector<ii> &H, ii p)
    bool growing = dot(H[0], p) \le dot(H[1], p);
    if(arowina)
      int b = 0, e = H.size() - 1, w = -1;
      while (b \leq e)
          int m = (b + e) / 2;
          if(dot(H[0], p) <= dot(H[m], p))
              b = m + 1, w = m;
              e = m - 1;
      return max(maxConcavityUp(w, H.size() - 1, H, p),
         maxConcavityDown(0, w, H, p));
      //cout << "caso #1\n0 " << w << " concavidade para baixo\n"
             << w + 1 << ' ' << H.size() - 1 << " concavidade para
          cima\n";
    else
      int b = 0, e = H.size() - 1, w = -1;
      while(b <= e)
          int m = (b + e) / 2;
          if(dot(H[0], p) >= dot(H[m], p))
              b = m + 1, w = m;
          else
              e = m - 1;
```

```
//cout << "caso #2\n0 " << w << " concavidade para cima\n"
      // << w + 1 << ' ' << H.size() - 1 << " cocavidade para
          baixo\n";
      return max(maxConcavityUp(0, w, H, p),
        maxConcavityDown(w, H.size() - 1, H, p));
vector<vector<ii>>> st;
void add(ii p)
    vector<ii> q = {p};
    while(!st.empty() and st.back().size() <= g.size())</pre>
        g = merge(g, st.back());
        st.pop_back();
    st.push_back(g);
int query(ii p)
    int ans = -00;
    for(int i = 0; i < st.size(); i++)</pre>
        ans = max(ans, maximumDot(st[i], p));
    return ans;
int32_t main()
   int n, q;
    scanf(" %lld", &n);
    for(int i = 0; i < n; i++)</pre>
        int x, y;
        scanf(" %lld %lld", &x, &y);
        add(\{x, y\});
   scanf(" %lld", &q);
    while (q--)
        char s[10];
        int x, y;
        scanf(" %s %lld %lld", s, &x, &y);
        if(s[0] == 'a') add({x, y});
        else printf("%lld\n", query({x, y}));
    return 0;
```

6.12 Radial Sort

```
#include <bits/stdc++.h>
using namespace std;
#define type int
#define point pair<type, type>
#define X first
#define Y second
```

```
point operator-(point a, point b)
    return {a.X - b.X, a.Y - b.Y};
type operator* (point a, point b)
    return a.X * b.Y - a.Y * b.X;
int n:
vector<point> P;
point R;
int dist(point a, point b)
    return (a.X - b.X) * (a.X - b.X) + (a.Y - b.Y) * (a.Y - b.Y);
bool cmp (point a, point b)
    if((a - R).Y * (b - R).Y <= 0) return a.Y > R.Y;
    int c = (a - R) * (b - R);
    if(c == 0) return dist(R, a) <= dist(R, b);</pre>
    return c > 0;
int main()
    cin >> n >> R.X >> R.Y;
    for (int i = 0; i < n; i++)
        type x, y;
        cin >> x >> y;
        P.push_back({x, y});
    sort(P.begin(), P.end(), cmp);
    for(point p : P) cout << p.X << ' ' << p.Y << '\n';</pre>
    return 0;
```

6.13 Segment Intersection

7 Miscellaneous

7.1 Big Num Product

```
string mul(string a, string b)
 while (a.size() > b.size()) b = "0" + b;
 while(a.size() < b.size()) a = "0" + a;</pre>
 a = "00" + a;
 b = "00" + b;
 int ans = 0, n = a.size(), carry = 0;
 vector<int> num(2 * n, 0);
  for (int i = n - 1; i >= 0; i--)
   for (int j = n - 1; j >= 0; j--)
      int di = a[i] - '0';
      int dj = b[j] - '0';
      num[i + j + 1] += (di * dj) + carry;
      carry = (num[i + j + 1] / 10);
     num[i + j + 1] %= 10;
  string r:
  for (int i = 0, fl = 0; i < 2 * n; i++)
   if(num[i]) fl = 1;
   if(fl) r.push_back(num[i] + '0');
  return r;
```

7.2 Count Divisors

```
#include <bits/stdc++.h>
using namespace std;
long long add (long long a, long long b, long long c)
  long long ans = (a + b) % c;
    if(ans < 0) ans += c;
    return ans;
long long mulmod(long long a, long long b, long long c)
 long long ans = 0;
  while(b)
   if(b & 1) ans = add(ans, a, c);
    a = add(a, a, c);
    b /= 2;
  return ans;
long long fexp(long long a, long long b, long long c)
  long long ans = 1;
  while (b)
```

```
if(b & 1) ans = mulmod(ans, a, c);
    a = mulmod(a, a, c);
    b /= 2;
  return ans;
bool miller (long long a, long long n)
    if (a >= n) return true;
    long long s = 0, d = n - 1;
    while (d%2 == 0 \text{ and } d) d >>= 1, s++;
    long long x = fexp(a, d, n);
    if (x == 1 \text{ or } x == n - 1) return true;
    for (int r = 0; r < s; r++, x = mulmod(x, x, n))
        if (x == 1) return false;
        if (x == n-1) return true;
    return false;
bool isprime (long long n)
  if(n < 2) return false;</pre>
    int base[] = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
    for(int i = 0; i < 12; i++)
        if(!miller(base[i], n))
             return false;
    return true;
vector<int> prime;
bitset<10000000> composite;
void sieve()
  for(int i = 2; i < 10000000; i++)</pre>
    if(!composite[i])
      prime.push_back(i);
      for (int j = 2; i * j < 10000000; j++)
        composite[i * j] = 1;
long long countDivisors(long long n)
  int idx = 1;
  long long ans = 1, p = prime[0];
  while (p * p * p \le n)
    int cnt = 1;
    while (n % p == 0)
      n \neq p, cnt++;
    ans *= cnt;
    p = prime[idx++];
  if(n == 1) return ans;
  if(isprime(n)) ans \star = 2;
```

```
else
{
    long long sq = sqrt(n);
    if(sq * sq == n)
        ans *= 3;
    else if(n != 1)
        ans *= 4;
    }
    return ans;
}
int main()
{
    long long n;
    cin >> n;
    sieve();
    cout << countDivisors(n) << '\n';
    return 0;
}</pre>
```

7.3 Count Sort

```
#include <bits/stdc++.h>
using namespace std;
int n, m;
int arr[100];
int cnt[10000];
int aux[100];
void count_sort()
    for(int i = 0; i < n; i++)</pre>
        cnt[arr[i]]++;
    for(int i = 1; i <= m; i++)</pre>
        cnt[i] += cnt[i-1];
    for(int i = 0; i < n; i++)</pre>
        aux[--cnt[arr[i]]] = arr[i];
    memcpy(arr, aux, n*sizeof(int));
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> arr[i], m = max(arr[i], m);
    count_sort();
    for (int i = 0; i < n; i++)
      cout << arr[i] << ' '; cout << '\n';
    return 0;
```

7.4 Counting Different Elements In A Path With Mo

```
//COT - Count on a tree (SPOJ)
//Em cada vertice existe um valor
//A resposta para uma query eh quantos valores
//distintos existem no caminho de u a v
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e6;
typedef long long 11;
struct Query
    int x, y, l, r, lc, res;
};
int n, q, max_log, tempo, blk, ans;
vector<int> G[MAX];
int value[MAX], pos[MAX], anc[MAX][25], depth[MAX];
int tl[MAX], ST[MAX], EN[MAX], freq[MAX], node[MAX];
Query Q[MAX];
11 arr[MAX];
void dfs(int v, int p, int d)
    anc[v][0] = p;
    depth[v] = d;
    tl[tempo] = v;
    ST[v] = tempo++;
    if(d) max_log = max(max_log, (int)log2(d));
    for(const int &u : G[v])
        if(u != p)
            dfs(u, v, d + 1);
    tl[tempo] = v;
    EN[v] = tempo++;
int walk(int v, int k)
    while (k) v = anc[v][(int)log2(k&-k)], k -= k&-k;
    return v:
int lca(int u, int v)
    if(depth[u] > depth[v]) u = walk(u, depth[u] - depth[v]);
    if(depth[u] < depth[v]) v = walk(v, depth[v] - depth[u]);</pre>
    if(u == v) return u;
    for(int i = max_log; i >= 0; i--)
        if(anc[u][i] != anc[v][i])
            u = anc[u][i];
            v = anc[v][i];
    return anc[u][0];
void build()
    memset(anc, -1, sizeof(anc));
    dfs(0, -1, 0);
    for(int j = 1; j <= max_log; j++)</pre>
```

```
for(int i = 0; i < n; i++)</pre>
            if(anc[i][j-1] != -1)
                anc[i][j] = anc[anc[i][j-1]][j-1];
inline void mo(int i)
    int u = tl[i];
    if(node[u] and --freq[value[u]] == 0) ans--;
    else if(!node[u] and ++freq[value[u]] == 1) ans++;
    node[u] ^= 1;
bool compare(int a, int b)
    if(Q[a].1/blk != Q[b].1/blk)
        return Q[a].1 < Q[b].1;
    return Q[a].r > Q[b].r;
int main()
    scanf("%d %d", &n, &q);
    for (int i = 0; i < n; i++) //values
        scanf("%d", &arr[i]), pos[i] = i;
    sort(pos, pos + n, [](ll a, ll b){return arr[a] < arr[b];});</pre>
    for (int i = 0, j = 1; i < n; i++)
        if(!i)
            value[pos[i]] = j++;
        else if(arr[pos[i]] != arr[pos[i-1]])
            value[pos[i]] = j++;
        else value[pos[i]] = value[pos[i-1]];
    for(int i = 0; i < n-1; i++)
        int u, v;
        scanf("%d %d", &u, &v); u--; v--;
        G[u].push_back(v);
        G[v].push_back(u);
    build();
    for(int i = 0; i < q; i++)
        int u, v;
        scanf("%d %d", &u, &v); u--; v--;
        if(ST[u] > ST[v]) swap(u, v);
        O[i].lc = lca(u, v);
        Q[i].x = u, Q[i].y = v;
        if(u == O[i].lc)
            Q[i].l = ST[u], Q[i].r = ST[v];
            O[i].l = EN[u], O[i].r = ST[v];
        pos[i] = i;
    blk = sqrt(tempo);
    sort (pos, pos + q, compare);
    int curL = 0, curR = 0;
```

```
for(int i = 0; i < q; i++)
    int L = Q[pos[i]].l, R = Q[pos[i]].r;
    while(curL < L)</pre>
        mo(curL++):
    while(curL > L)
        mo(--curL);
    while (curR < R + 1)
        mo(curR++);
    while(curR > R + 1)
        mo(--curR);
    if(Q[pos[i]].x != Q[pos[i]].lc)
        mo(ST[Q[pos[i]].lc]);
    Q[pos[i]].res = ans;
    if(Q[pos[i]].x != Q[pos[i]].lc)
        mo(ST[Q[pos[i]].lc]);
for(int i = 0; i < a; i++)
   printf("%d\n", Q[i].res);
return 0;
```

7.5 Custom Hash Function Unordered Map Or Set

```
#include <bits/stdc++.h>
using namespace std;
struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
       x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    size_t operator()(uint64_t x) const {
        static const uint64 t FIXED RANDOM = chrono::steady clock::now
             ().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
};
const int N = 2e5;
void insert_numbers(long long x)
    clock_t begin = clock();
    unordered_map<long long, int, custom_hash> numbers;
    for (int i = 1; i <= N; i++)</pre>
        numbers[i * x] = i;
    long long sum = 0;
    for (auto &entry : numbers)
        sum += (entry.first / x) * entry.second;
```

7.6 Divide Conquer Optimization

```
#include <bits/stdc++.h>
using namespace std;
#define maxn 20005
#define maxnlog 22
const long long 00 = 0x3f3f3f3f3f3f3f3f;
struct SparseTableDS
 int Sparse_Table[maxnlog][maxn];
 bool maxi;
 int n;
 void build()
   for(int i = 1; (1 << i) <= n; i++)
      for (int j = 0; j + (1 << i) <= n; <math>j++)
        if (maxi)
          Sparse_Table[i][j] = max(Sparse_Table[i-1][j],
            Sparse_Table[i-1][j+(1 << (i-1))]);
        else
          Sparse_Table[i][j] = min(Sparse_Table[i-1][j],
              Sparse_Table[i-1][j+(1 << (i-1))]);
  int query(int i, int j)
   int sz = log2(j-i+1);
      return max(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
   return min(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
  void init(bool fl, vector<int> &arr)
   maxi = fl;
   if(!maxi) memset(Sparse_Table, 63, sizeof(Sparse_Table));
   n = arr.size();
    for(int i = 0; i < n; i++)</pre>
      Sparse_Table[0][i] = arr[i];
   build();
```

```
};
int n, k;
SparseTableDS maxi, mini;
long long dp_before[maxn];
long long dp_cur[maxn];
int get(int 1, int r)
  int a = maxi.query(l, r);
  int b = mini.query(l, r);
  return abs(a - b);
void compute(int 1, int r, int opt1, int optr)
  if(l > r) return;
  int mid = (1 + r) >> 1;
  int best = 0;
  int opt = optl;
  for(int k = optl; k < min(mid, optr + 1); k++)</pre>
    if(best < dp_before[k] + get(k + 1, mid))</pre>
      best = dp_before[k] + get(k + 1, mid);
      opt = k;
  dp_cur[mid] = best;
    compute(1, mid - 1, optl, opt);
    compute (mid + 1, r, opt, optr);
int32_t main()
  cin >> n >> k;
  vector<int> arr(n);
  for(int &w : arr) scanf(" %d", &w);
  maxi.init(true, arr);
  mini.init(false, arr);
  for(int i = 0; i < n; i++)</pre>
    dp_cur[i] = get(0, i);
  for(int i = 2; i <= k; i++)</pre>
    for (int j = 0; j < n; j++)
      dp_before[j] = dp_cur[j];
      dp_cur[j] = 0;
    compute (i - 2, n - 1, i - 2, n - 1);
  cout << dp_cur[n - 1] << endl;</pre>
  return 0;
```

7.7 FastIO

```
#include <bits/stdc++.h>
using namespace std;
#define gc getchar_unlocked
#define pc putchar_unlocked
inline void scanint (int &k)
 bool sinal = true;
    register char c;
    k = 0;
    for(c = gc(); sinal and (c < '0' or c > '9'); c = gc())
      if(c == '-')
        sinal = false;
    for(; c \ge '0' and c \le '9'; c = gc())
       k = (k \ll 3) + (k \ll 1) + c - '0';
  if(!sinal) k = -k;
inline void printint(int n)
  if (n < 0) pc ('-');
  n = abs(n);
  int rev = n, cnt = 0;
  if(!n)
    pc('0');
    pc('\n');
    return;
  while(!(rev % 10))
    cnt++, rev \neq 10;
  rev = 0;
  while (n)
    rev = (rev << 3) + (rev << 1) + n % 10, n /= 10;
    pc(rev % 10 + '0'), rev /= 10;
  while (cnt--)
    pc('0');
 pc('\n');
inline void scanstr(string &k)
    register char c;
  k = "";
    for(c = qc(); c < 'a' or c > 'z'; c = qc());
    for (; c \ge 'a') and c \le 'z'; c = gc() k.push_back(c);
inline void printstr(string &k)
  for(char &c : k) putchar(c);
 putchar('\n');
```

```
int main()
{
  int k;
  scanint(k);
  printint(k);
  return 0;
}
```

7.8 Fence Problem With Max Flow

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4;
const int 00 = 0x3f3f3f3f3f;
int SOURCE, SINK;
struct edge
    int v, f, c;
    edge(){}
    edge(int _v, int _f, int _c)
        v = _v, f = _f, c = _c;
};
vector<edge> edges:
vector<int> G[MAX];
int dist[MAX], work[MAX];
void add_edge(int u, int v, int cp, int rc) {
  edges.push_back(edge(v, 0, cp));
  G[u].push_back(edges.size()-1);
  edges.push_back(edge(u, 0, rc));
  G[v].push_back(edges.size()-1);
bool bfs(int s, int t)
    memset(dist, -1, sizeof(dist));
    dist[s] = 0;
    queue<int> q;
    q.push(s);
    while(!q.empty())
        int u = q.front();
        q.pop();
        for(int e : G[u])
            if(dist[edges[e].v] == -1 and edges[e].c-edges[e].f > 0)
                q.push(edges[e].v);
                dist[edges[e].v] = dist[u] + 1;
    return dist[t] != -1;
int dfs(int s, int t, int f)
```

```
if(s == t) return f;
    for(int &i = work[s]; i < G[s].size(); i++)</pre>
      int e = G[s][i];
        if(dist[edges[e].v] == dist[s] + 1 and edges[e].c-edges[e].f >
            if(int a = dfs(edges[e].v, t, min(f, edges[e].c-edges[e].f
                )))
                edges[e].f += a;
                edges[e^1].f -= a;
                return a:
    return 0;
int MaxFlow(int s, int t)
    int mf = 0;
    while(bfs(s, t))
      memset (work, 0, sizeof (work));
        while(int a = dfs(s, t, 00))
            mf += a;
    return mf;
int n, m, a, b;
int dx[] = \{1, 0, -1, 0\};
int dy[] = \{0, -1, 0, 1\};
char ANS[60][60];
bool cor[MAX];
bool check(int x, int y)
  return x >= 0 and x < n and y >= 0 and y < m;
int vertexIn(int i, int j)
  return i * m + j;
int vertexOut(int i, int j)
  return i * m + j + n * m + 1;
void mountANS(int v)
  cor[v] = true;
  for(int &e : G[v])
    if(cor[edges[e].v]) continue;
    if(edges[e].c - edges[e].f > 0)
      mountANS (edges [e].v);
```

```
int main()
 memset(ANS, '.', sizeof(ANS));
 cin >> n >> m >> a >> b; a--; b--;
 SOURCE = 2 * n * m + 2;
  SINK = 2 * n * m + 3;
  for(int i = 0; i < n; i++)</pre>
    for (int j = 0; j < m; j++)
      int cost;
      cin >> cost;
      if(a == i and b == j) cost = 00;
      add_edge(vertexIn(i, j), vertexOut(i, j), cost, 0);
      if(cost == 00) add_edge(vertexOut(i, j), SINK, 00, 0);
      for(int k = 0; k < 4; k++)
        int x = i + dx[k], y = j + dy[k];
       if(check(x, y))
          add_edge(vertexOut(i, j),
            vertexIn(x, y), 00, 0);
      if(!i or !j or i == n - 1 or j == m - 1)
        add_edge(SOURCE, vertexIn(i, j), 00, 0);
 cout << MaxFlow(SOURCE, SINK) << '\n';</pre>
 mountANS (SOURCE);
 for(int i = 0; i < n * m; i++)
    for(int &e : G[i])
      if(!(e & 1) and cor[i] and !cor[edges[e].v])
        ANS[i / m][i % m] = 'X';
  for(int i = 0; i < n; i++)</pre>
    for (int j = 0; j < m; j++)
      cout << ANS[i][j];
   puts("");
    return 0;
```

7.9 Gen Random Tree

```
#include <bits/stdc++.h>
using namespace std;
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());

int rand(int a, int b) {
    return a + rng() % (b - a + 1);
}

int main() {
    int n = rand(4, 20);
    cout << n << endl;
    vector<pair<int,int>> edges;
    for(int i = 2; i <= n; i++)
        edges.emplace_back(rand(1, i - 1), i);

// re-naming vertices
vector<int> perm(n + 1); // re-naming vertices
for(int i = 1; i <= n; ++i)
        perm[i] = i;</pre>
```

```
// random order of labels
shuffle(perm.begin() + 1, perm.end(), rng);
  // random order of edges
shuffle(edges.begin(), edges.end(), rng);

for(auto [u, v] : edges) {
  // random order of two vertices
   if(rng() % 2) swap(u, v);
   cout << perm[u] << ' ' << perm[v] << endl;
}

return 0;</pre>
```

7.10 Histogram

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
int n, vet[1000000];
11 histogram()
  stack<ll> s;
  11 \text{ ans} = 0, tp, cur;
  int i = 0;
  while(i < n or !s.empty())</pre>
    if(i < n and (s.empty() or vet[s.top()] <= vet[i]))</pre>
      s.push(i++);
    else
      tp = s.top();
      s.pop();
      cur = vet[tp] * (s.empty() ? i : i - s.top() - 1);
      if(ans < cur)</pre>
        ans = cur;
  return ans;
int main()
  while(cin >> n and n)
    for(int i = 0; i < n; i++)</pre>
      cin >> vet[i];
    cout << histogram() << '\n';</pre>
    return 0;
```

7.11 Inclusion Exclusion

```
contar a quantidade de numeros na range [1, b]
  que sao multiplos de pelo menos um numero na range [1, a]
#include <bits/stdc++.h>
using namespace std;
#define bug(x) cout << #x << " >>>>>> " << x << '\n'
#define _ << " , " <<
#define int long long
#define Max(a, b) (a > b ? a : b)
#define Min(a, b) (a < b ? a : b)
#define ii pair<int, int>
#define fi first
#define se second
#define SZ(v) (int)v.size()
#define UNTIL(t) while (clock() < (t) * CLOCKS_PER_SEC)</pre>
const long long MAX = (long long) le15; //2 * 10^5
const int MOD = 1000000007; //10^9 + 7
const int 00 = 0x3f3f3f3f; //3f3f3f3f;
const double EPS = 1e-9; //10^-9
mt19937 rnq(chrono::steady_clock::now().time_since_epoch().count());
vector<int> prime = {3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43,
    47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, 101, 103, 107, 109,
    113, 127};
vector<vector<ii>>> lista;
void add(int id)
  vector<ii> aux;
  for (int k = 0; k < id; k++)
    int i = SZ(lista[k]) - 1;
    while(i >= 0 and MAX / lista[k][i].fi / prime[id] == 0) i--;
    for(int j = 0; j <= i; j++)</pre>
      aux.push_back({lista[k][j].fi * prime[id], !lista[k][j].se});
  aux.push_back({prime[id], 1});
  sort(aux.begin(), aux.end());
  lista.push_back(aux);
int32_t main()
  for(int i = 0; i < SZ(prime); i++)
    add(i);
  int t;
  scanf(" %lld", &t);
  while (t--)
    int a, b;
    scanf(" %lld %lld", &a, &b);
    int ans = b / 2;
    int cnt_p = 0;
    for(int &w : prime) cnt_p += (w <= a);</pre>
```

```
for(int i = 0; i < cnt_p; i++)
{
    for(int j = 0; j < SZ(lista[i]); j++)
    {
        if(lista[i][j].fi > b) break;
        if(lista[i][j].se) ans += (b / lista[i][j].fi + 1) / 2;
        else ans -= (b / lista[i][j].fi + 1) / 2;
    }
}
printf("%lld\n", ans);
}
return 0;
}
```

7.12 Index Compression

```
#include <bits/stdc++.h>
const int MAX = 1e6 + 10:
using namespace std;
int n, arr[MAX], pos[MAX], newArr[MAX], realValue[MAX];
int main()
    cin >> n;
    for(int i = 0; i < n; i++)</pre>
        cin >> arr[i], pos[i] = i;
    sort(pos, pos + n, [](int i, int j) { return arr[i] < arr[j]; });</pre>
    for(int i = 0; i < n; i++)</pre>
    if(!i) newArr[pos[i]] = id, realValue[id] = arr[pos[i]];
    else if(arr[pos[i-1]] == arr[pos[i]]) newArr[pos[i]] = newArr[pos[
        i-1]];
    else newArr[pos[i]] = ++id, realValue[id] = arr[pos[i]];
    for(int i = 0; i < n; i++)</pre>
        cout << arr[i] << ' ' << newArr[i] <<
           ' ' << realValue[newArr[i]] << '\n';
    return 0;
```

7.13 Karp Rabin

```
using namespace std;
const int MAX = 1e5;
typedef long long 11;
11 A = 911382323, B = 972663749;
11 h1[MAX], h2[MAX], p[MAX];
int arr[MAX];
string s;
11 buildH(ll *H, int k)
    if(k == 0)
        return H[0] = s[0];
    return H[k] = (buildH(H, k - 1) *A + s[k]) % B;
11 buildP(int k)
    if(k == 0)
        return p[0] = 1;
    return p[k] = (buildP(k - 1)*A) % B;
ll vhash(ll *H, int a, int b)
    if(a == 0)
        return H[b];
    ll ans = (H[b] - H[a - 1] * p[b - a + 1]) % B;
    if(ans < 0)
        ans += B;
    return ans;
bool slidingWindow(int k)
    if(k < 0 or k > s.size()) return false;
    for(int i = 0; i + k - 1 < s.size(); i++)</pre>
        if(vhash(h1, i, i + k - 1) == vhash(h2, s.size())
           -(i+k-1)-1, s.size() -(i+k-1)-2+k))
            return true; // A substring [i, i + k - 1] eh palindromo
    return false:
int buscab()
    int tam = 0;
    for(int i = 0; i < s.size(); i++)</pre>
        arr[i] = 2*i + 1, tam++;
    int b = 0, e = tam, m, ans = 0;
    while(b <= e)</pre>
        m = (b + e) / 2;
        slidingWindow(arr[m]) ? b = m + 1, ans = arr[m] : e = m - 1;
    tam = 0:
    for(int i = 0; i < s.size(); i++)</pre>
       arr[i] = 2*i, tam++;
    b = 0, e = tam;
    while(b <= e)</pre>
```

7.14 Knapsack With Backtraking

```
#include <bits/stdc++.h>
using namespace std;
#define pii pair<int, int>
#define fi first
#define se second
#define pb push_back
int n,c;
vector<pii> v;
int res,aux;
double c2, aux2;
void bt(int i){
  if(i == n) return;
  aux2 = 0; c2 = c;
  for(int j=i; j<n && c2; j++) {</pre>
    if(v[j].fi <= c2){
      c2 -= v[j].fi; aux2 += v[j].se;
    } else {
      aux2 += (v[j].se*c2)/v[j].fi;
      c2 = 0;
  if(aux2 + aux <= res) return;</pre>
  if(v[i].fi <= c){
    c -= v[i].fi;
    aux += v[i].se;
    if(aux > res) res = aux;
    bt(i+1):
    aux -= v[i].se;
    c += v[i].fi;
 bt(i+1);
int32_t main(){
```

```
ios::sync_with_stdio(false);cin.tie(0);
cin>>n>>c;
for(int i = 0; i < n; i++)
{
   int wei,value; cin>>wei>>value;
   v.pb({wei,value});
}
sort(v.begin(), v.end(), [](pii a, pii b) {
   return (a.se+0.0)/a.fi > (b.se+0.0)/b.fi;
});
bt(0);
cout<<res<<endl;
return 0;</pre>
```

7.15 Knuth Optimization

```
#include <bits/stdc++.h>
using namespace std;
// Knuth Optimization
int pf[6000], n;
int dp[6000][6000];
int sum(int 1, int r)
  return pf[r] - pf[l - 1];
int solve(int 1, int r)
  if(1 > r) return 0;
  if (dp[l][r] != -1) return dp[l][r];
  int ans = (1 << 30);
  for(int i = 1; i <= r; i++)
    ans = min(ans, sum(1, r) + solve(1, i - 1) + solve(i + 1, r));
  return dp[l][r] = ans;
#define ii pair<int, int>
#define fi first
#define se second
ii DP[6000][6000];
//Point(1, r - 1) \le Point(1, r) \le Point(1 + 1, r)
ii knuth(int l, int r)
  if(1 == r) return {sum(1, r), 1};
  if (DP[1][r] != ii(-1, -1)) return DP[1][r];
  int lef = knuth(l, r - 1).se;
  int rig = knuth(l + 1, r).se;
  int point = 1, ans = (1 << 30);</pre>
```

```
for(int i = lef; i <= rig; i++)
{
    int cur = sum(l, r);
    if(i - 1 >= l) cur += knuth(l, i - 1).fi;
    if(i + 1 <= r) cur += knuth(i + 1, r).fi;
    if(cur < ans) ans = cur, point = i;
}
return DP[l][r] = {ans, point};
}
int main()
{
    memset(dp, -1, sizeof(dp));
    cin >> n;
    //for(int i = 1; i <= n; i++)
        //cin >> pf[i], pf[i] += pf[i - 1];
    //cout << solve(l, n) << endl;

memset(DP, -1, sizeof(DP));
    cout << knuth(l, n).fi << endl;

return 0;
}</pre>
```

7.16 Lontest Substring That Is A Correct Bracket Sequence

```
#include <bits/stdc++.h>
using namespace std;
#define 00 0x3f3f3f3f
#define qc qetchar
#define pc putchar
#define offset 1000000
string str;
int Sparse_Table[22][1000002], n;
vector<int> forest[2000002];
int pf[1000002], cnt[1000002];
inline void build()
  for (int i = 1; (1 << i) < n; i++)
    for (int j = 0; j + (1 << i) < n; j++)
      Sparse_Table[i][j] = min(Sparse_Table[i-1][j],
        Sparse_Table[i-1][j+(1 << (i-1))]);
inline int range_query(int i, int j)
 int sz = log2(j-i+1);
  return min(Sparse_Table[sz][i],Sparse_Table[sz][j+1-(1 << sz)]);</pre>
inline int countNumberOfElementEqualToXinLR(int 1, int r, int x)
  int p1 = lower_bound(forest[x + offset].begin(), forest[x + offset].
      end(), 1) - forest[x + offset].begin();
  int p2 = upper_bound(forest[x + offset].begin(), forest[x + offset].
      end(), r) - forest[x + offset].begin() - 1;
```

```
if (p1 > p2) return -1;
  return p2 - p1 + 1;
inline int nxt(int i, int x)
  int b = i, e = n - 1, ans = -1;
  while(b <= e)</pre>
    int m = (b + e) >> 1;
    int v = range_query(i, m);
    if(v >= x) ans = m, b = m + 1;
    else e = m - 1;
  return ans;
inline int queryIndex(int 1, int r, int x)
  int b = 1, e = r, ans = -1;
  while(b <= e)</pre>
    int m = (b + e) >> 1;
    if(countNumberOfElementEqualToXinLR(m, r, x) > 0) ans = m, b = m +
    else e = m - 1;
  return ans;
inline void scanstr(string &k)
    register char c;
  k = "";
    for(c = gc(); c != '(' and c != ')'; c = gc());
    for(; c \ge '(' \text{ and } c \le ')'; c = qc()) k.push_back(c);
int main()
  scanstr(str);
  n = str.size() + 1;
  for(int i = 1; i < n; i++)</pre>
    pf[i] = pf[i - 1] + (str[i - 1] == '(' ? 1 : -1);
    Sparse_Table[0][i] = pf[i];
    forest[pf[i] + offset].push_back(i);
  build();
  int ans = 0;
  cnt[0] = 1;
  for(int i = 1; i < n; i++)</pre>
    if(str[i - 1] != '(') continue;
    int e = nxt(i, pf[i] - 1);
    if(e < i) continue;</pre>
    int p = queryIndex(i, e, pf[i] - 1);
    if(p < i) continue;</pre>
    int 1 = p - i + 1;
    cnt[1]++;
    if(1 > ans) ans = 1;
```

```
} printf("%d %d\n", ans, cnt[ans]);
return 0;
}
```

7.17 Maximum Subarray Xor

```
#include <bits/stdc++.h>
using namespace std:
const int MAX = 1e4 + 10;
const int 00 = 0x3f3f3f3f3f;
const double EPS = 1e-9;
#define bug(x) cout << #x << " = " << x << '\n'
#define FOR(i, a, n) for(int i = a; i < n; i++)
#define REP(i, n) FOR(i, 0, n)
#define fi first
#define se second
#define pb push_back
#define mt make_tuple
#define all(vetor) vetor.begin(), vetor.end()
#define X real()
#define Y imag()
//#define gc getchar_unlocked
typedef long long 11:
typedef long double ld;
typedef pair<ll, ll> ii;
typedef pair<int, ii> iii;
typedef complex<11> P11;
typedef complex<ld> Pld;
struct TrieNode
    int value;
    TrieNode *children[2];
    TrieNode()
        value = 0;
        children[0] = children[1] = nullptr;
};
void insert(TrieNode *root, int n)
    TrieNode *aux = root;
    for(int i = 31; i >= 0; i--)
        bool b = (n & (1 << i));
        if(aux->children[b] == nullptr)
            aux->children[b] = new TrieNode();
        aux = aux->children[b];
    aux->value = n;
int query(TrieNode *root, int n)
```

```
TrieNode *aux = root;
    for (int i = 31; i >= 0; i--)
        bool b = (n \& (1 << i));
        if(aux->children[1-b] != nullptr)
            aux = aux->children[1-b];
        else
            aux = aux->children[b];
    return n ^ aux->value;
void maxSubArrayXor(int *arr, int n)
    TrieNode *root = new TrieNode();
    insert(root, 0);
    int px = 0, ans = INT_MIN, r = -1;
    for(int i = 0; i < n; i++)</pre>
       px = px ^ arr[i];
       insert (root, px);
        int num = max(ans, query(root, px));
        if(num > ans)
            ans = num, r = i;
    int 1 = r, xo = 0;
    for(; 1 >= 0; 1--)
        xo ^= arr[1];
       if(xo == ans)
            break;
    cout << "O Xor maximo eh: " << ans << '\n';
    while (1 \le r)
       cout << arr[l++] << ' ';
    cout << '\n';
int main()
    int arr[MAX], n;
    cin >> n;
    REP(i, n) cin >> arr[i];
    maxSubArrayXor(arr, n);
  return 0;
```

7.18 Mo

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 3 * 1e5;
struct Query
{
   int 1, r, qt;
```

//com hash no braco

```
vector<int> el;
};
Query q[MAX];
int n, m, blk, ans;
int arr[MAX], freq[MAX], qtd[MAX], pos[MAX];
vector<vector<int>> tab;
void add(int i)
    if(freq[arr[i]])
        qtd[freq[arr[i]]]--;
    freq[arr[i]]++;
    qtd[freq[arr[i]]]++;
    if(ans <= freq[arr[i]])</pre>
        ans = freq[arr[i]];
        tab[ans].push_back(arr[i]);
void sub(int i)
    qtd[freq[arr[i]]]--;
    if(!qtd[ans])
        for(int j = 0; j < tab[ans].size(); j++)</pre>
            if(tab[ans][j] == arr[i])
                 tab[ans].erase(tab[ans].begin() + j);
                break;
        ans--;
        tab[ans].push_back(arr[i]);
    freg[arr[i]]--;
    if(freq[arr[i]])
        qtd[freq[arr[i]]]++;
bool compare(int a, int b)
    if(q[a].1/blk != q[b].1/blk)
        return q[a].1 < q[b].1;
    return q[a].r < q[b].r;</pre>
int main()
    while(cin >> n >> m and n)
        blk = sqrt(n);
        for(int i = 0; i < n; i++)
            cin >> arr[i];
            arr[i] += 100000;
        for(int i = 0; i < m; i++)</pre>
            cin >> q[i].l >> q[i].r, pos[i] = i;
        sort (pos, pos + m, compare);
```

```
ans = 0;
        int curL = 0, curR = 0;
        int L, R;
       memset(freq, 0, sizeof(freq));
        memset(qtd, 0, sizeof(qtd));
        tab.clear();
        tab.resize(MAX);
        for (int j = 0; j < m; j++)
            L = q[pos[j]].l - 1;
            R = q[pos[j]].r - 1;
            while (curL < L)
                sub(curL++);
            while (curL > L)
                add (--curL);
            while (curR < R + 1)
                add(curR++);
            while (curR > R + 1)
                sub (--curR);
            q[pos[j]].qt = ans;
            q[pos[j]].el = tab[ans];
        for (int j = 0; j < m; j++)
            for(int i = 0; i < q[j].el.size(); i++)</pre>
                cout << q[j].el[i]-100000 << '\n';
    return 0;
//com unordered_multimap
#include <bits/stdc++.h>
using namespace std;
const int MAX = 3 * 1e5;
struct Query
    int 1, r, qt, morefrequent;
};
Query q[MAX];
int n, m, blk, ans;
int arr[MAX], freq[MAX], qtd[MAX], pos[MAX];
unordered_multimap<int, int> tab;
void add(int i)
    if(freq[arr[i]])
        qtd[freq[arr[i]]]--;
    freq[arr[i]]++;
    qtd[freq[arr[i]]]++;
    if(ans <= freq[arr[i]])</pre>
        ans = freq[arr[i]];
        tab.insert({ans, arr[i]});
```

```
void sub(int i)
    qtd[freq[arr[i]]]--;
    if(!qtd[ans])
        int k = 0, sz = tab.bucket(ans);
        auto it = tab.find(ans);
        for(int j = 0; j < sz; j++)</pre>
            if(it->second == arr[i])
                 tab.erase(it);
                 j = sz;
            else it++;
        ans--;
        tab.insert({ans, arr[i]});
    freg[arr[i]]--;
    if(freg[arr[i]])
        qtd[freq[arr[i]]]++;
bool compare(int a, int b)
    if(q[a].1/blk != q[b].1/blk)
        return q[a].1 < q[b].1;
    return q[a].r < q[b].r;</pre>
int main()
    while(cin >> n >> m and n)
        blk = sqrt(n);
        for(int i = 0; i < n; i++)</pre>
            cin >> arr[i];
            arr[i] += 100000;
        for(int i = 0; i < m; i++)</pre>
            cin >> q[i].l >> q[i].r, pos[i] = i;
        sort(pos, pos + m, compare);
        ans = 0:
        int curL = 0, curR = 0;
        int L, R;
        memset(freq, 0, sizeof(freq));
        memset(qtd, 0, sizeof(qtd));
        tab.clear();
        for (int j = 0; j < m; j++)
            L = q[pos[j]].l - 1;
            R = q[pos[j]].r - 1;
            while(curL < L)</pre>
                 sub(curL++);
```

```
while (curL > L)
                add (--curL);
            while (curR < R + 1)
                add(curR++);
            while(curR > R + 1)
                sub(--curR);
            q[pos[j]].qt = ans;
            q[pos[j]].morefrequent = tab.find(ans)->second;
        for (int j = 0; j < m; j++)
                cout << q[j].morefrequent-100000 << '\n';</pre>
    return 0;
Mo em arvore parte 1
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 10;
struct Ouerv
    int 1, r, v;
};
int n, q;
int freq[MAX], inicio[MAX], fim[MAX], pos[MAX], value[MAX];
vector<int> tree_linearization, G[MAX];
Ouerv O[MAX];
int ans, blk;
void TreeLinearization(int v, int p)
    inicio[v] = tree_linearization.size();
    tree_linearization.push_back(v);
    for(const int &u : G[v])
        if(u != p)
            TreeLinearization(u, v);
    fim[v] = tree_linearization.size() - 1;
void add(int i)
    if(!freq[value[tree_linearization[i]]])
        ans++;
    freq[value[tree_linearization[i]]]++;
void sub(int i)
    freq[value[tree linearization[i]]]--;
    if(!freq[value[tree_linearization[i]]])
        ans--;
bool compare (int a, int b)
    if(Q[a].1/blk != Q[b].1/blk)
```

```
return Q[a].1/blk < Q[b].1/blk;</pre>
    return Q[a].r < Q[b].r;</pre>
int main()
    int u, v;
    cin >> n >> q;
    for(int i = 0; i < n; i++)</pre>
        cin >> value[i];
    for (int i = 0; i < n-1; i++)
        cin >> u >> v;
        u--; v--;
        G[u].push_back(v);
        G[v].push_back(u);
    TreeLinearization (0, -1);
    for(int i = 0; i < q; i++)
        cin >> u;
        u--;
        Q[i].l = inicio[u];
        O[i].r = fim[u];
        pos[i] = i;
    blk = sqrt(n);
    sort (pos, pos+q, compare);
    int curL = 0, curR = 0;
    for(int i = 0; i < q; i++)
        int L = Q[pos[i]].l, R = Q[pos[i]].r;
        while(curL < L)</pre>
            sub(curL++);
        while(curL > L)
            add(--curL);
        while (curR < R + 1)
            add(curR++);
        while (curR > R + 1)
            sub(--curR);
        Q[pos[i]].v = ans;
    for(int i = 0; i < q; i++)
        cout << Q[i].v << '\n';
    return 0;
```

7.19 Odd Rectangles Area

```
integers x1, y1, x2, and y2, each between 0 and 109, describing the
    coordinates of
a rectangle.
Output: Print, on one line, the total area covered by an odd number of
     rectangles
as an exact integer.
#include <bits/stdc++.h>
using namespace std;
struct Event
    int x1, x2, y, t;
    Event(int _x1, int _x2, int _y, int _t)
        x1 = _x1, x2 = _x2, y = _y, t = _t;
    Event(){}
};
struct Node
  int 1, r, value;
int n;
vector<Node> tree;
vector<int> lazv;
vector<Event> arr;
int init()
  tree.clear();
  lazy.clear();
 tree.emplace_back();
  lazy.push_back(0);
void createL(int node)
  tree[node].l = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void createR(int node)
  tree[node].r = tree.size();
  tree.emplace_back();
  lazy.push_back(0);
void calc(int node)
  tree[node].value = 0;
  if(tree[node].1) tree[node].value += tree[tree[node].1].value;
  if(tree[node].r) tree[node].value += tree[tree[node].r].value;
```

```
void push(int node, int start, int end)
  tree[node].value = (end - start + 1) - tree[node].value;
  if(start != end)
    if(tree[node].l == 0) createL(node);
    if(tree[node].r == 0) createR(node);
    lazy[tree[node].l] ^= 1;
    lazv[tree[node].r] ^= 1;
  lazy[node] = 0;
void update(int node, int start, int end, int 1, int r)
  if(lazy[node])
   push(node, start, end);
  if(start > r or l > end) return;
  if(l <= start and end <= r)</pre>
    push (node, start, end);
  else
    int mid = (start + end) / 2;
    if(tree[node].l == 0) createL(node);
    update(tree[node].l, start, mid, l, r);
    if(tree[node].r == 0) createR(node);
    update(tree[node].r, mid + 1, end, 1, r);
    calc(node);
int query(int node, int start, int end, int 1, int r)
  if(lazy[node])
    push (node, start, end);
  if(start > r or l > end) return 0;
  if(l <= start and end <= r) return tree[node].value;</pre>
  int mid = (start + end) / 2, q1 = 0, q2 = 0;
  if(tree[node].l) q1 = query(tree[node].l, start, mid, l, r);
  if(tree[node].r) q2 = query(tree[node].r, mid + 1, end, 1, r);
  return q1 + q2;
bool cmp (Event a, Event b)
    if(a.y != b.y) return a.y < b.y;</pre>
    return a.t < b.t;</pre>
int32_t main()
    scanf(" %d", &n);
    for(int i = 0; i < n; i++)</pre>
        int x1, y1, x2, y2;
        scanf(" %d %d %d %d", &x1, &y1, &x2, &y2);
```

```
int xmi = min(x1, x2);
    int ymi = min(y1, y2);
    int xma = max(x1, x2);
    int yma = max(y1, y2);
   xma--;
    arr.emplace_back(xmi, xma, ymi, -1);
   arr.emplace_back(xmi, xma, yma, 1);
sort(arr.begin(), arr.end(), cmp);
long long Y = 0, ans = 0;
init();
for(int i = 0; i < arr.size(); i++)</pre>
    //cout << "op " << arr[i].t << '\n';
   long long s = query(0, 0, 1000000008, 0, 1000000007);
   long long aux = s * 1LL * (arr[i].y - Y);
                         " << aux << ' ' << arr[i].y1 << ' ' <<
    //cout << "this
        Y << ' ' << s << '\n';
   update(0, 0, 1000000008, arr[i].x1, arr[i].x2);
   Y = arr[i].v:
   ans += aux;
cout << ans << '\n';
return 0;
```

7.20 Quick Sort And Select

```
#include <bits/stdc++.h>
using namespace std;
int n, arr[10000];
int quickselect(int 1, int r, int k)
    int i = 1 - 1;
    for(int i = 1; i < r; i++)</pre>
        if(arr[i] <= arr[r])
             swap(arr[++j], arr[i]);
    swap(arr[j+1], arr[r]);
    if(j+1 < k) return quickselect(j+2, r, k);</pre>
    else if(j+1 > k) return quickselect(l, j, k);
    return arr[j+1];
void quicksort(int 1, int r)
    int j = 1 - 1;
    for(int i = 1; i < r; i++)</pre>
        if(arr[i] <= arr[r])</pre>
             swap(arr[++i], arr[i]);
    swap(arr[j+1], arr[r]);
    if(1 < j)
        quicksort(1, j);
    if(j+2 < r)
        quicksort(j+2, r);
```

```
int main()
{
    int k;
    cin >> n >> k;
    for(int i = 0; i < n; i++) cin >> arr[i];
    cout << quickselect(0, n-1, k-1) << '\n';
    return 0;
}</pre>
```

7.21 Rectangles Union Area

```
#include <bits/stdc++.h>
using namespace std;
#define ii pair<int, int>
#define fi first
#define se second
struct Event
    int x1, x2, y, t;
    Event (int _x1, int _x2, int _y, int _t)
        x1 = _x1, x2 = _x2, y = _y, t = _t;
    Event(){}
ii tree[500800];
int lazy[500800];
int n;
vector<pair<ii, ii>> segments, rect;
int X1, Y1, X2, Y2, P;
ii calc(ii a, ii b)
  if(a.fi > b.fi) return b;
  else if(a.fi < b.fi) return a;</pre>
  return {a.fi, a.se + b.se};
void build(int node, int start, int end)
  if(start == end)
   tree[node] = \{0, 1\}, lazy[node] = 0;
  else
    int mid = (start + end) / 2;
   build(2 * node, start, mid);
    build(2 * node + 1, mid + 1, end);
    tree[node] = calc(tree[2 * node], tree[2 * node + 1]);
    lazy[node] = 0;
void push(int node, int start, int end)
  tree[node].fi += lazy[node];
  if(start != end)
```

```
lazy[2 * node] += lazy[node];
   lazy[2 * node + 1] += lazy[node];
  lazy[node] = 0;
void update(int node, int start, int end, int 1, int r, int v)
  if(lazy[node]) push(node, start, end);
  if(start > r or end < l) return;</pre>
  if(1 <= start and end <= r)</pre>
    lazy[node] += v;
    push (node, start, end);
    return;
  int mid = (start + end) / 2;
  update(2 * node, start, mid, 1, r, v);
  update (2 * node + 1, mid + 1, end, l, r, v);
  tree[node] = calc(tree[2 * node], tree[2 * node + 1]);
int query(int node, int start, int end)
  if(lazy[node]) push(node, start, end);
  return end - start + 1 - tree[node].se;
void mount(int r)
  rect.clear();
  for (auto &it : segments)
    int x1 = max(min(it.fi.fi, it.se.fi) - r, X1);
    int y1 = max(min(it.fi.se, it.se.se) - r, Y1);
    int x2 = min(max(it.fi.fi, it.se.fi) + r, X2);
    int y2 = min(max(it.fi.se, it.se.se) + r, Y2);
    rect.push_back({{x1, y1}, {x2, y2}});
bool cmp (Event a, Event b)
    if(a.y != b.y) return a.y < b.y;</pre>
    return a.t > b.t;
long long area(int r)
 mount(r);
 vector<Event> eve;
  for(auto &it : rect)
    eve.emplace_back(it.fi.fi, it.se.fi, it.fi.se, 1);
        eve.emplace_back(it.fi.fi, it.se.fi, it.se.se, -1);
  sort(eve.begin(), eve.end(), cmp);
  build(1, 0, 100001);
  long long Y = 0, ans = 0;
```

```
for(int i = 0; i < eve.size(); i++)</pre>
        long long s = query(1, 0, 100001);
        long long aux = s * 1LL * (eve[i].y - Y);
        update(1, 0, 100001, eve[i].x1, eve[i].x2, eve[i].t);
        Y = eve[i].v;
        ans += aux;
   return ans;
int32_t main()
  scanf(" %d", &n);
  for(int i = 0; i < n; i++)</pre>
   int x1, y1, x2, y2;
   scanf(" %d %d %d %d", &x1, &y1, &x2, &y2);
   segments.push_back(\{\{x1, y1\}, \{x2, y2\}\});
  scanf(" %d %d %d %d %d", &P, &X1, &Y1, &X2, &Y2);
 long long tot = (X2 - X1) * 1LL * (Y2 - Y1);
  int b = 0, e = 100000, ans = 0;
 while(b <= e)
   int mid = (b + e) / 2;
   long long A = area(mid);
   if(P * 1LL * tot <= 100LL * A) ans = mid, e = mid - 1;</pre>
   else b = mid + 1;
  cout << ans << '\n';
   return 0;
```

7.22 Small To Large

```
https://codeforces.com/blog/entry/44351

// Small To Large (using map)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN*logN), (we are using map)

#include <bits/stdc++.h>
using namespace std;

const int MAX = 1e4 + 10;

vector<int> g[MAX];
int sz[MAX], col[MAX];
map<int, int> *cnt[MAX];

void getsz(int v, int p)
{
    sz[v] = 1;
    for(auto u : g[v])
```

```
if(u != p) {
           getsz(u, v); sz[v] += sz[u]; }
void dfs(int v, int p)
    int mx = -1, bigChild = -1;
   for(auto u : g[v])
      if(u != p)
          dfs(u, v);
          if(sz[u] > mx)
              mx = sz[u], bigChild = u;
    if(bigChild !=-1)
       cnt[v] = cnt[bigChild];
    else
       cnt[v] = new map<int, int> ();
    (*cnt[v])[ col[v] ] ++;
   for(auto u : q[v])
      if(u != p && u != bigChild)
          for(auto x : *cnt[u])
               (*cnt[v])[x.first] += x.second;
    //now (*cnt[v])[c] is the number of vertices in
    //subtree of vertex v that has color c. You can
   //answer the queries easily.
int32_t main()
   int n, m;
   cin >> n >> m;
   for(int i = 0; i < n; i++)</pre>
       cin >> col[i];
   for(int i = 0; i < m; i++)</pre>
       int u, v;
       cin >> u >> v; u--; v--;
       q[u].push_back(v);
       q[v].push_back(u);
   getsz(0, -1);
   dfs(0, -1);
 return 0;
// dsu on tree (using vector)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
```

```
vector<int> q[MAX];
int sz[MAX], col[MAX];
vector<int> *vec[MAX];
int cnt[MAX];
void getsz(int v, int p)
    sz[v] = 1;
    for(auto u : g[v])
        if(u != p) {
            getsz(u, v); sz[v] += sz[u]; }
void dfs(int v, int p, bool keep)
    int mx = -1, bigChild = -1;
    for(auto u : q[v])
       if(u != p && sz[u] > mx)
           mx = sz[u], bigChild = u;
    for(auto u : q[v])
       if(u != p && u != bigChild)
           dfs(u, v, 0);
    if(bigChild != -1)
        dfs(bigChild, v, 1), vec[v] = vec[bigChild];
    else
        vec[v] = new vector<int> ();
    vec[v]->push_back(v);
    cnt[ col[v] ]++;
    for(auto u : q[v])
       if(u != p && u != bigChild)
           for(auto x : *vec[u]){
               cnt[ col[x] ]++;
               vec[v] -> push_back(x);
//now (*cnt[v])[c] is the number of vertices in subtree
//of vertex v that has color c. You can answer the gueries
//easily. note that in this step *vec[v] contains all of
//the subtree of vertex v.
    if(keep == 0)
        for(auto u : *vec[v])
            cnt[ col[u] ]--;
int32_t main()
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        q[u].push_back(v);
        q[v].push_back(u);
    getsz(0, -1);
    dfs(0, -1, 0);
```

```
return 0;
// Small To Large (heavy-light decomposition style)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10:
vector<int> q[MAX];
int sz[MAX], col[MAX];
bool big[MAX];
int cnt[MAX];
void getsz(int v, int p)
    sz[v] = 1;
    for(auto u : g[v])
       if(u != p){
            getsz(u, v); sz[v] += sz[u]; } }
void add(int v, int p, int x)
    cnt[col[v]] += x;
    for(auto u: g[v])
       if(u != p && !big[u])
            add(u, v, x);
void dfs(int v, int p, bool keep)
    int mx = -1, bigChild = -1;
    for(auto u : q[v])
      if(u != p && sz[u] > mx)
          mx = sz[u], bigChild = u;
    for(auto u : q[v])
       if(u != p && u != bigChild)
        // run a dfs on small childs and clear them from cnt
            dfs(u, v, 0);
    if(bigChild !=-1)
        // bigChild marked as big and not cleared from cnt
        dfs(bigChild, v, 1), big[bigChild] = 1;
    add(v, p, 1);
//now cnt[c] is the number of vertices in subtree of
//vertex v that has color c. You can answer the queries easily.
    if(bigChild !=-1)
       big[bigChild] = 0;
   if(keep == 0)
        add(v, p, -1);
}
int32_t main()
    int n, m;
   cin >> n >> m;
```

```
for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        g[u].push_back(v);
        g[v].push_back(u);
    getsz(0, -1);
    dfs(0, -1, 0);
  return 0:
// Small To Large (using nesting intervals)
// Given a tree, every vertex has color. Query is
//how many vertices in subtree of vertex v are
// colored with color c?
// O(N*logN)
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e4 + 10;
vector<int> g[MAX];
int sz[MAX], col[MAX];
int st[MAX], ft[MAX];
int cnt[MAX], ver[MAX];
int tempo = 0;
void getsz(int v, int p)
    sz[v] = 1;
    ver[tempo] = v;
    st[v] = tempo++;
    for(auto u : q[v])
        if(u != p) {
            getsz(u, v); sz[v] += sz[u]; }
    ft[v] = tempo++;
void dfs(int v, int p, bool keep)
    int mx = -1, bigChild = -1;
    for(auto u : q[v])
        if(u != p && sz[u] > mx)
          mx = sz[u], bigChild = u;
    for(auto u : g[v])
        if(u != p && u != bigChild)
            // run a dfs on small childs and
            // clear them from cnt
            dfs(u, v, 0);
    if (bigChild != -1)
        // bigChild marked as big and not cleared from cnt
        dfs(bigChild, v, 1);
    for(auto u : q[v])
  if(u != p && u != bigChild)
      for (int p = st[u]; p < ft[u]; p++)
        cnt[ col[ ver[p] ] ]++;
```

```
cnt[ col[v] ]++;
//now cnt[c] is the number of vertices in subtree of vertex
//v that has color c. You can answer the queries easily.
    if(v == 1) cout << cnt[2] << '\n';</pre>
    if(keep == 0)
        for (int p = st[v]; p < ft[v]; p++)
          cnt[ col[ ver[p] ] ]--;
int32_t main()
    int n, m;
    cin >> n >> m;
    for(int i = 0; i < n; i++)</pre>
        cin >> col[i];
    for(int i = 0; i < m; i++)</pre>
        int u, v;
        cin >> u >> v; u--; v--;
        q[u].push_back(v);
        g[v].push_back(u);
    qetsz(0, -1);
    dfs(0, -1, 0);
  return 0;
But why it is ? You know that why dsu has time
(for q queries); the code uses the same method.
Merge smaller to greater.
If you have heard heavy-light decomposition you
will see that function add will go light edges
only, because of this, code works in time.
*/
```

7.23 Square Root Decomposition

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5;

int n, blk_sz;
int arr[MAX], block[MAX];

void update(int idx, int val)
{
   int blockNumber = idx/blk_sz;
   block[blockNumber] += val - arr[idx];
   arr[idx] = val;
}

int query(int l, int r)
{
   int sum = 0;
   while(1 < r and l%blk_sz != 0 and l != 0)</pre>
```

```
sum += arr[1], 1++;
    while(l+blk_sz <= r)</pre>
        sum += block[1/blk_sz], 1 += blk_sz;
    while(1 <= r)</pre>
        sum += arr[1], 1++;
    return sum;
void build()
    int blk_idx = -1;
    blk_sz = sqrt(n);
    for(int i = 0; i < n; i++)</pre>
        if(i%blk_sz == 0)
            blk_idx++;
        block[blk_idx] += arr[i];
int main()
    cin >> n;
    for (int i = 0; i < n; i++)
        cin >> arr[i];
    build();
    int o, l, r;
    while(cin >> o >> l >> r and o)
        if(0 == 1)
            update(l-1, r);
        else
            cout << query(1-1, r-1) << '\n';
    return 0;
```

7.24 String Matching Hash Sqrtdecomp

```
#include <bits/stdc++.h>
using namespace std;
const int MAX = 1e5 + 100;

typedef long long ll;

#define ii pair<int, long long>
#define fi first
#define se second

ll A = 911382323, B = 972663749;
ll h[MAX], p[MAX];
string s;

ll buildP(int k)
{
   if(k == 0)
        return p[0] = 1;
   return p[k] = (buildP(k - 1)*A) % B;
}

int main()
```

```
ios_base::sync_with_stdio(false);
cin.tie(NULL);
 cin >> s;
buildP(s.size() + 10);
  int n = s.size();
  int sz = sqrt(n);
 unordered_set<ll> AAAA;
 vector<ii> BBBB:
string aux;
  while(cin >> aux)
      long long value = 0, j = 0;
      while(j < aux.size())</pre>
          if(j == 0) value = aux[j];
          else value = (value * A + aux[i]) % B;
          j++;
      if(aux.size() > sz)
          BBBB.push_back({aux.size(), value});
          AAAA.insert(value);
 sort(BBBB.begin(), BBBB.end());
string ans;
int j = 0, i = 0;
while(i < s.size())</pre>
    ans.push_back(s[i]);
    if(j == 0) h[j] = s[i];
    else h[j] = (h[j-1] * A + s[i]) % B;
    int leng = -1;
    long long vh;
      for (int k = j; k >= 0 and k >= j - sz - 1 and leng < 0; k--)
          if(k == 0) vh = h[j];
          else
              vh = (h[j] - h[k - 1] * p[j - k + 1]) % B;
              if(vh < 0) vh += B;
          if(AAAA.count(vh))
              leng = j - k + 1;
          //length j - k + 1
    if(leng == -1)
        for (int k = 0; k < BBBB.size(); k++)
```

8 Useful Scripts

8.1 Brute

```
#include <bits/stdc++.h>
using namespace std;

int32_t main() {
    int n, x;
    cin >> n >> x;
    vector<int> v(n);
    for(int &w : v) cin >> w;

    for(int i = 0; i < n; i++)
        for(int j = i + 1; j < n; j++)
            if(v[i] + v[j] == x)
            return cout << i + 1 << ' ' << j + 1 << endl, 0;
    return 0;
}</pre>
```

8.2 Gen

```
#include <bits/stdc++.h>
using namespace std;
```

```
#define int long long
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
int32_t main() {
   int n = rng() % 100 + 10;
   vector<int> a(n);
   for(int i = 0; i < n; i++)
      a[i] = rng() % 5000 + 1;
   int j = rnq() % n;
   int k = rnq() % n;
   while (k == j) k = rng() % n;
   int x = a[j] + a[k];
   cout << n << ' ' << x << '\n';
   for(int w : a)
      cout << w << ' ';
   cout << endl;
  return 0;
```

8.3 Sol

```
#include <bits/stdc++.h>
using namespace std;
// find two number a and b that a + b = x
int32_t main() {
   int n, x;
   cin >> n >> x;
   vector<pair<int, int>> arr(n);
   for(int i = 0; i < n; i++)</pre>
      cin >> arr[i].first, arr[i].second = i;
   sort(arr.begin(), arr.end());
   // suppose the algorithm does not work for n > 108
   if(n > 108) {
      cout << "1 5" << endl;
      return 0;
   for(int i = 0; i < n; i++) {</pre>
      int b = i + 1, e = n - 1, y = x - arr[i].first;
      while(b <= e) {
         int middle = (b + e) / 2;
         if(arr[middle].first == y) {
            cout << arr[i].second + 1 << ' ' << arr[middle].second + 1</pre>
                  << '\n';
            return 0;
         } else if(arr[middle].first > y)
            e = middle - 1;
         else
            b = middle + 1;
```

```
return 0;
}
```

```
cat out2
break;
fi
echo $i
done
```

8.4 Stress With Checker.sh

8.5 Stress.sh

```
make sol brute gen
for ((i = 1; ; i++)) do
        ./gen $i > in
        ./sol < in > out
        ./brute < in > out2
        if (! cmp -s out out2) then
                echo "--> entrada:"
                cat in
                echo "--> saida sol"
                cat out
                echo "--> saida2 brute"
                cat out2
                break;
        fi
        echo $i
done
```