

A Simheuristic Approach to Optimize Energy Consumption in the Single-Machine Scheduling Problem with Stochastic Processing Times

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Abstract

This paper addresses a stochastic single-machine scheduling problem with energy consumption. In this problem, job processing times are random variables, and total energy consumption depends on job scheduling, as each job has its own energy use and each period follows a Time-Of-Use tariff policy. To solve the problem, we propose a simheuristic algorithm that combines the metaheuristics Simulated Annealing and Greedy Randomized Adaptive Search Procedure to explore the solution space, along with Monte Carlo Simulation to better evaluate the solutions during the search. The solutions obtained are compared with those derived from a deterministic approach, and the results show that the simheuristic outperforms the deterministic method in terms of Average, Value at Risk, and Conditional Value at Risk, emphasizing the importance of incorporating uncertainty into the solution methods.

Keywords: Green Scheduling, Time-Of-use, Stochastic Processing Time.

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1. Literature review

This document presents all the articles used in the three literature reviews conducted in the paper “Simheuristic Approach to the Single-Machine Scheduling Problem with Stochastic Processing Times and Energy-Efficient”. This section aims to establish the review protocols, which specify the objectives, the questions to be answered, the databases to be consulted, the types of studies to be analyzed, the keywords to be searched, the languages, the years of publication, and the inclusion and exclusion criteria for the studies obtained. Thus, these protocols seek to provide a clear and pre-defined framework that outlines and guides the entire review process, describing in a transparent manner all the methodological aspects for the search and selection of articles, thereby ensuring the reproducibility of the study.

Therefore, we have three objectives, one for each review. For SSMSP, we aim to identify gaps and trends regarding this model. For SMGSP, to evaluate the state of the art. And for SGSP, to analyze the current landscape of research on this topic. The questions to be answered for each objective are presented in Table 1.

Table 1: Questions to be answered for each review

| Review | Questions |
|--------|---|
| SSMSP | (1) Which methods are used to solve this type of problem; (2) What are the most addressed stochastic parameters in the literature. |
| SMGSP | (1) Classification of models according to the number of objective functions; (2) Which objective function(s) is/are considered; (3) What are the main environmental considerations; (4) What methods are used to solve this type of problem. |
| SGSP | (1) Which methods are used to solve this type of problem; (2) What are the most addressed stochastic parameters in the literature; (3) What are the main environmental considerations. |

The review was conducted exclusively using the Web of Science database as the source for the literature review. This choice was made because this database is recognized for its multidisciplinary scope and its extensive coverage of renowned international scientific journals. Additionally, the search was

limited to only one type of document, which is articles, as they represent a primary and consolidated source of academic knowledge, typically subjected to a rigorous peer-review process, which ensures the credibility and reliability of the information contained in them.

Preliminarily, a search was conducted on Google Scholar to identify keywords present in existing works in the literature. This enabled the formulation of a search string that ensured both the breadth and accuracy of the review, aiming to avoid the exclusion of relevant studies and the inclusion of irrelevant ones. Furthermore, all searches for keywords were performed only in the titles (TI) and the abstract (AB) of the works, and the asterisk (“*”) was used as a truncation operator to find all research with the same root. Thus, the search strings adopted can be observed in Table 2.

Table 2: Search string adopted for each review

| Review | Search string |
|--------|--|
| SSMSP | TI=(<i>single machine</i>) AND TI=(<i>sched*</i>) AND (TI=(<i>simheuristic</i>) OR TI=(<i>stoch*</i>) OR TI=(<i>uncert*</i>)) AND (AB=(<i>heuristi*</i>) OR TI=(<i>simheuris*</i>) OR TI=(<i>optimiz*</i>)) |
| SMGSP | TI=(<i>single machine</i>) AND TI=(<i>sched*</i>) AND (TI=(<i>green</i>) OR TI=(<i>sustainab*</i>) OR TI=(<i>energ*</i>) OR TI=(<i>carbon*</i>) OR TI=(<i>nois*</i>) OR TI=(<i>pollut*</i>) OR TI=(<i>tariff*</i>) OR TI=(<i>Time Of Use</i>) OR TI=(<i>Energy-effici*</i>) OR TI=(<i>Electricity prices*</i>)) |
| SGSP | TI=(<i>sched*</i>) AND (TI=(<i>green</i>) OR TI=(<i>sustainab*</i>) OR TI=(<i>energ*</i>) OR TI=(<i>carbon*</i>) OR TI=(<i>nois*</i>) OR TI=(<i>pollut*</i>)) AND (TI=(<i>simheuristic</i>) OR TI=(<i>stoch*</i>) OR TI=(<i>uncert*</i>)) AND (TI=(<i>single machine</i>) OR TI=(<i>parallel machines</i>) OR TI=(<i>flow shop</i>) OR TI=(<i>flow-shop</i>) OR TI=(<i>flowshop</i>) OR TI=(<i>jop shop</i>) OR TI=(<i>jop-shop</i>) OR TI=(<i>jopshop</i>) OR TI=(<i>open shop</i>) OR TI=(<i>open-shop</i>) OR TI=(<i>openshop</i>)) |

Therefore, as presented in Table 2, for the SSMSP review, the terms “simheuristic”, “stoch*”, “uncert*” were used to search for works that deal with random variables, and the terms “heuristi*”, “simheuris*”, and “optimiz*” were used to filter only approaches that use optimization methods. This search returned 19 results.

Similarly, for the SMGSP review, the terms “green”, “sustainab*”, “energ*”, “carbon*”, “nois*”, “pollut*”, “tariff*”, “Time of use”, and “Energy-

effici*” were adopted as filters to search for only works that have environmental considerations in their scope. The term “single machine*” was used to delimit the manufacturing environment, and the term “sched*” was adopted to specify the addressed problem. By using this search string, 40 works were retrieved.

For the SGSP review, where the terms “single machine”, “parallel machine”, “flow shop”, “job shop”, “open shop”, and their variants are adopted to represent all the manufacturing environments existing in the sequencing literature. This search returned 8 results. All searches and article counting for each review were conducted on 05/03/2025.

The search was conducted without any time limitations or document publication type restrictions (i.e., conferences, symposia, and journals). All works were read in full, with only those that did not address the scheduling topic or were not fully available being excluded.

The tables provide a structured summary of the key aspects analyzed in the reviewed articles, offering a comprehensive overview of the state of the art in these areas. This mapping enables the identification of emerging trends and research gaps, providing insights for the development of new approaches and contributing to advancements in the field.

Table 3: Articles used for the SSMSp review

| Ref. | Year | Objective Function | Stochastic parameter | Solution approach |
|------|------|------------------------------------|--------------------------------|----------------------------|
| [1] | 1988 | Inventory costs and setup cost | Demands | Heuristics with Simulation |
| [2] | 1988 | Inventory costs and setup cost | Demands | Heuristics with Simulation |
| [3] | 1992 | Reward | Release date | Heuristics with Simulation |
| [4] | 1994 | Inventory costs and setup cost | Demands | Heuristics with Simulation |
| [5] | 1994 | Earliness and tardiness costs | Processing times | Heuristics with Simulation |
| [6] | 1997 | Total tardiness | Processing times | Robust Programming |
| [7] | 2002 | Total tardiness | Processing times and due dates | Heuristics with Simulation |
| [8] | 2007 | Weighted total tardiness | Processing times and due dates | Heuristics with Simulation |
| [9] | 2007 | Net present value | Reward value | Branch-and-Bound |
| [10] | 2009 | Weighted total tardiness | Machine breakdown | Heuristics with Simulation |
| [11] | 2013 | Weighted total tardiness | Processing times | Heuristics with Simulation |
| [12] | 2013 | Makespan and Total completion time | Processing times | Branch-and-Bound |
| [13] | 2014 | Sum of completion times | Processing times | Robust Programming |
| [14] | 2019 | Total tardiness | Setups | Stochastic Programming |
| [15] | 2018 | Maximum tardiness | Release date | Robust Programming |
| [16] | 2020 | Maximum waiting time | Processing times | Robust Programming |
| [17] | 2020 | Makespan | Machine breakdown | Simheuristics |
| [18] | 2022 | Makespan | Processing times | Robust Programming |
| [19] | 2024 | Earliness and tardiness costs | Machine breakdown | Machine Learning |

Table 4: Articles used for the SMGSP review

| Ref. | Year | Objective Function | Environmental Characteristic | Solution approach |
|------|------|---|-------------------------------------|--------------------------------|
| [20] | 2014 | Makespan and <i>TEC</i> | TOU | Exact Method |
| [21] | 2014 | <i>TEC</i> | Machine states and TOU | Metaheuristic |
| [22] | 2015 | Maximum tardiness and <i>TEC</i> | Speed adjustment | Exact Method |
| [23] | 2016 | <i>TEC</i> | TOU and Speed adjustment | Exact Method |
| [24] | 2016 | Makespan and <i>TEC</i> | TOU | Exact Method |
| [25] | 2016 | <i>TEC</i> | TOU | Exact Method |
| [26] | 2016 | Makespan and <i>TEC</i> | TOU | Heuristic |
| [27] | 2016 | <i>TEC</i> | TOU | Heuristic |
| [28] | 2016 | Total tardiness and <i>TEC</i> | Setups | Exact Method |
| [29] | 2017 | Maximum tardiness and <i>TEC</i> | Machine states | Exact Method |
| [30] | 2017 | Total earliness and <i>TEC</i> | Machine states and TOU | Exact Method and Heuristic |
| [31] | 2017 | <i>TEC</i> | Machine reliability | Exact Method and Metaheuristic |
| [32] | 2017 | Weighted total tardiness | Speed adjustment | Metaheuristic |
| [33] | 2017 | Makespan and <i>TEC</i> | Machine states and TOU | Heuristic |
| [34] | 2018 | Total flow time and CO_2 emission | CO_2 emission | Metaheuristic |
| [35] | 2018 | Total tardiness and <i>TEC</i> | TOU | Metaheuristic |
| [36] | 2018 | Makespan and <i>TEC</i> | TOU | Exact Method and Heuristic |
| [37] | 2019 | Weighted earliness/tardiness and <i>TEC</i> | TOU | Metaheuristic |
| [38] | 2019 | Total tardiness and <i>TEC</i> | Machine reliability | Metaheuristic |
| [39] | 2019 | <i>TEC</i> | Machine states and TOU | Exact Method |
| [40] | 2019 | <i>TEC</i> | Machine states and TOU | Exact Method |
| [41] | 2019 | Total tardiness and <i>TEC</i> | Machine states | Metaheuristic |
| [42] | 2019 | <i>TEC</i> | TOU | Exact Method |
| [43] | 2019 | Makespan and <i>TEC</i> | TOU | Metaheuristic |
| [44] | 2019 | Total tardiness and <i>TEC</i> | Energy storage | Machine Learning |
| [45] | 2020 | <i>TEC</i> | Machine states and TOU | Metaheuristic |
| [46] | 2020 | Makespan and <i>TEC</i> | TOU | Metaheuristic |
| [47] | 2020 | Weighted total tardiness and <i>TEC</i> | TOU | Metaheuristic |
| [48] | 2021 | Total tardiness and <i>TEC</i> | Speed adjustment | Metaheuristic |
| [49] | 2021 | Weighted cost and <i>TEC</i> | Machine reliability | Simulated Annealing |
| [50] | 2021 | <i>TEC</i> and Production cost | TOU | Heuristic |
| [51] | 2022 | <i>TEC</i> | TOU and Speed adjustment | Metaheuristic |
| [52] | 2022 | Makespan and <i>TEC</i> | Energy storage | Metaheuristic |
| [53] | 2022 | Total tardiness and <i>TEC</i> | Setups | Metaheuristic |
| [54] | 2022 | Tardiness and Noise pollution | Noise | Metaheuristic Algorithm |
| [55] | 2022 | Total tardiness and <i>TEC</i> | Machine states | Metaheuristic |
| [56] | 2022 | Total tardiness and <i>TEC</i> | TOU | Metaheuristic |
| [57] | 2023 | Makespan and <i>TEC</i> | TOU | Metaheuristic |
| [58] | 2023 | Cost | Machine states and Speed adjustment | Exact Method and Heuristic |
| [59] | 2024 | <i>TEC</i> | TOU | Exact Method |

Table 5: Articles used for the SGSP review

| Ref. | Year | Objective Function | Stochastic parameter | Environmental Characteristic | Manuf. Env. | Solution approach |
|------|------|------------------------------|---|------------------------------|-------------|------------------------|
| [60] | 2016 | CO_2 emission and Makespan | Amplitude and magnitude of energy | Sustainable energy storage | 1 | Interval number theory |
| [61] | 2019 | Makespan and TEC | Processing time | Speed adjustment | F | Heuristic |
| [62] | 2020 | Makespan and TEC | Processing time | Speed adjustment | F | Metaheuristics |
| [63] | 2020 | Makespan and TEC | Processing time | Sustainable energy storage | F | Heuristic |
| [64] | 2021 | TEC | Arrival and cancellation of orders | TOU | F | Metaheuristics |
| [65] | 2023 | Makespan and TEC | Processing time | Speed adjustment | Pm | Heuristic |
| [66] | 2023 | Profit | Processing time | CO_2 emission | 1 | Machine learning |
| [67] | 2024 | TEC | Amplitude and magnitude of renewable energy | TOU and Renewable energy | F | Stochastic Programming |
| [68] | 2024 | Minimize total delay and TEC | Processing time | Machine states | O | Heuristic |

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