
Algoritmo 27: Algoritmo de Hopcroft-Karp.

Input : um grafo bipartido não-dirigido e não-ponderado $G = (V = X \cup Y, E)$

1 $M \leftarrow \{\}$

2 **repeat**

3 $P \leftarrow$ conjunto de caminhos aumentantes alternantes p_1, p_2, \dots, p_k

4 $M \leftarrow M \oplus \bigcup_{p \in P} p$

5 **until** $P = \{\}$

6 **return** M

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Algoritmo 28: Algoritmo de Hopcroft-Karp detalhado.

Input : um grafo bipartido não-dirigido e não-ponderado $G = (V = X \cup Y, E)$

1 $D_v \leftarrow \infty \forall v \in V$

2 $mate_v \leftarrow \mathbf{null} \forall v \in V$

// tamanho do emparelhamento

3 $m \leftarrow 0$

4 **while** $BFS(G, mate, D) = \mathbf{true}$ **do**

5 **foreach** $x \in X$ **do**

6 **if** $mate_x = \mathbf{null}$ **then**

7 **if** $DFS(G, mate, x, D) = \mathbf{true}$ **then**

8 $m \leftarrow m + 1$

9 **return** $(m, mate)$

Algoritmo 28: Algoritmo de Hopcroft-Karp detalhado.

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```
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2  $mate_v \leftarrow \mathbf{null} \forall v \in V$ 

   // tamanho do emparelhamento

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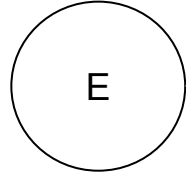
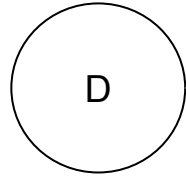
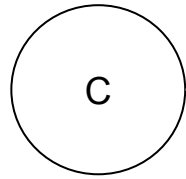
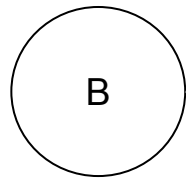
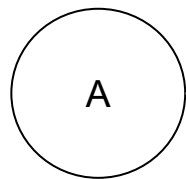
4 while  $BFS(G, mate, D) = \mathbf{true}$  do
5     foreach  $x \in X$  do
6         if  $mate_x = \mathbf{null}$  then
7             if  $DFS(G, mate, x, D) = \mathbf{true}$  then
8                  $m \leftarrow m + 1$ 

9 return  $(m, mate)$ 
```

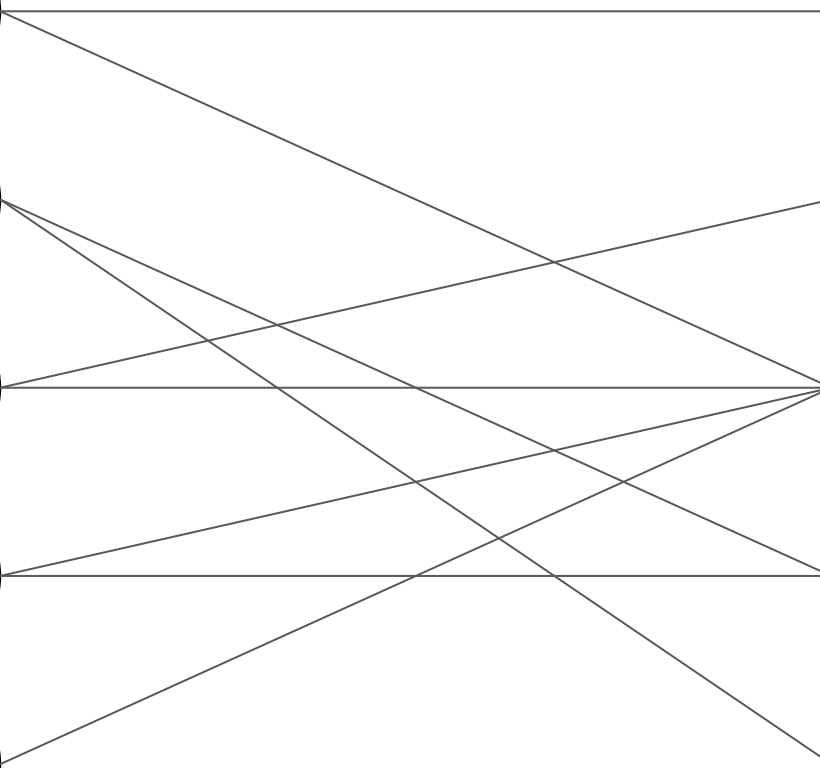
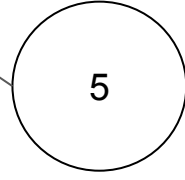
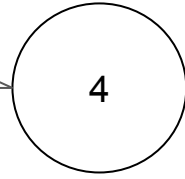
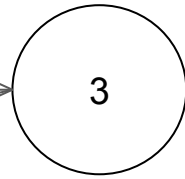
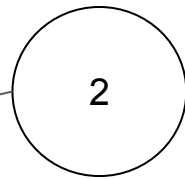
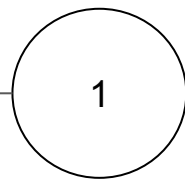
X	Y
Ana	1,3
Bruno	4,5
Carol	2,3
Diego	3,4
Eduardo	3

1	Comprar carne.
2	Comprar cerveja.
3	Arrumar o ambiente.
4	Preparar uma playlist.
5	Assar a carne.

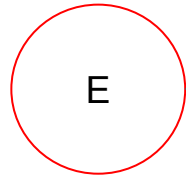
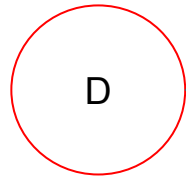
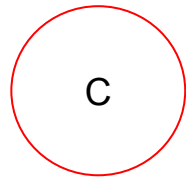
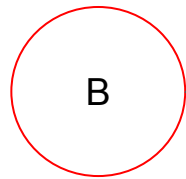
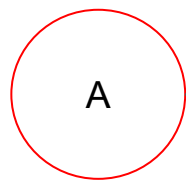
X



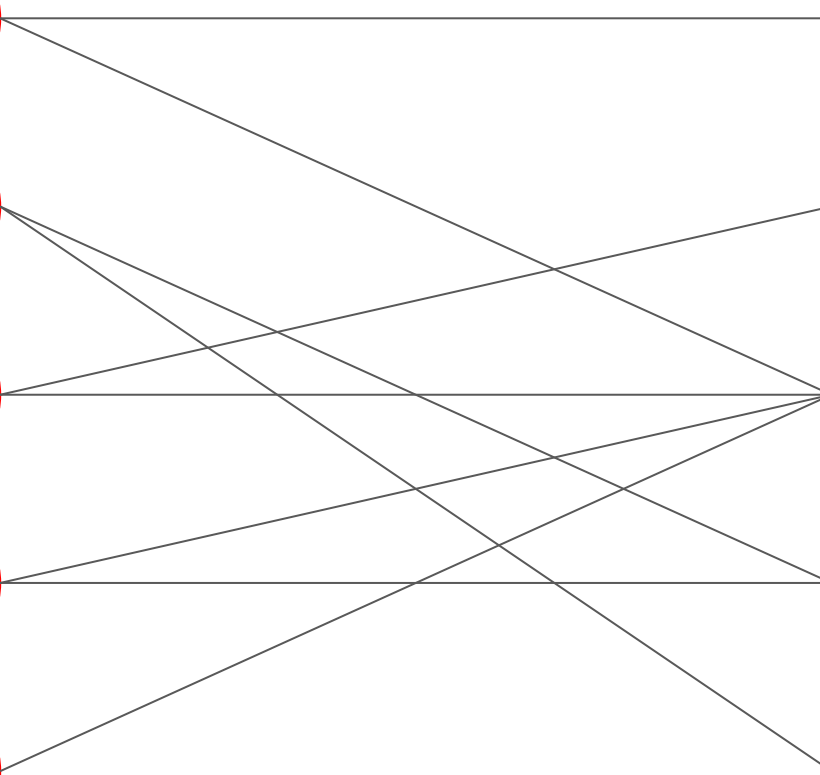
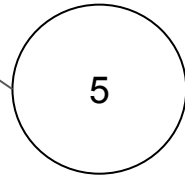
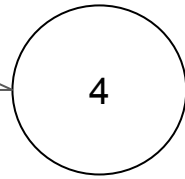
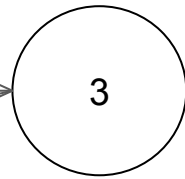
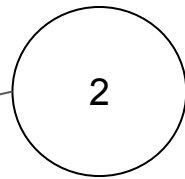
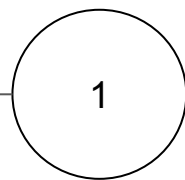
Y



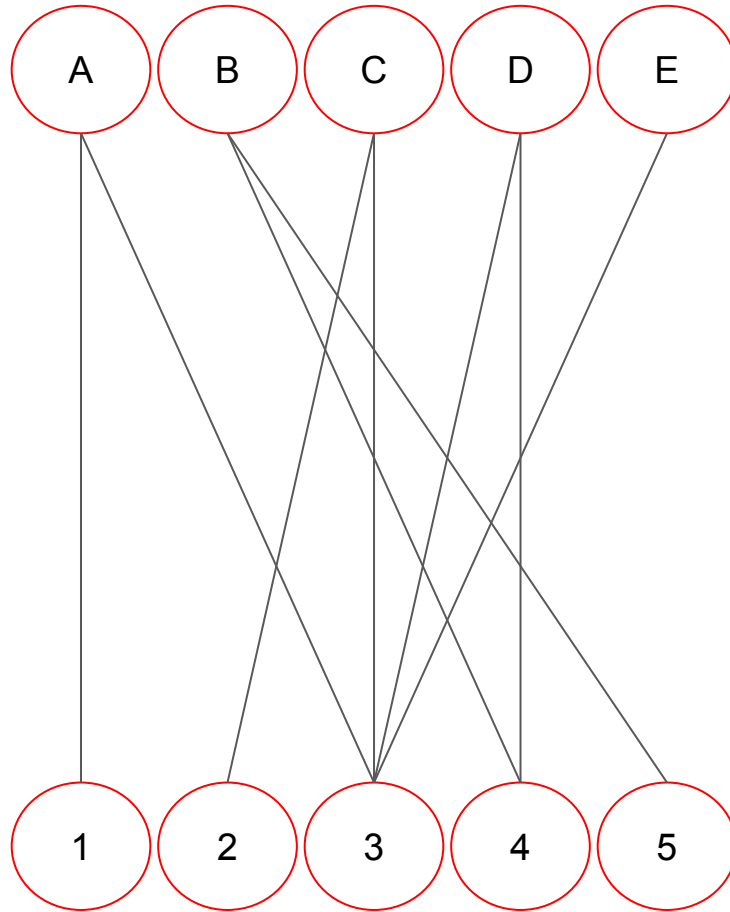
X



Y

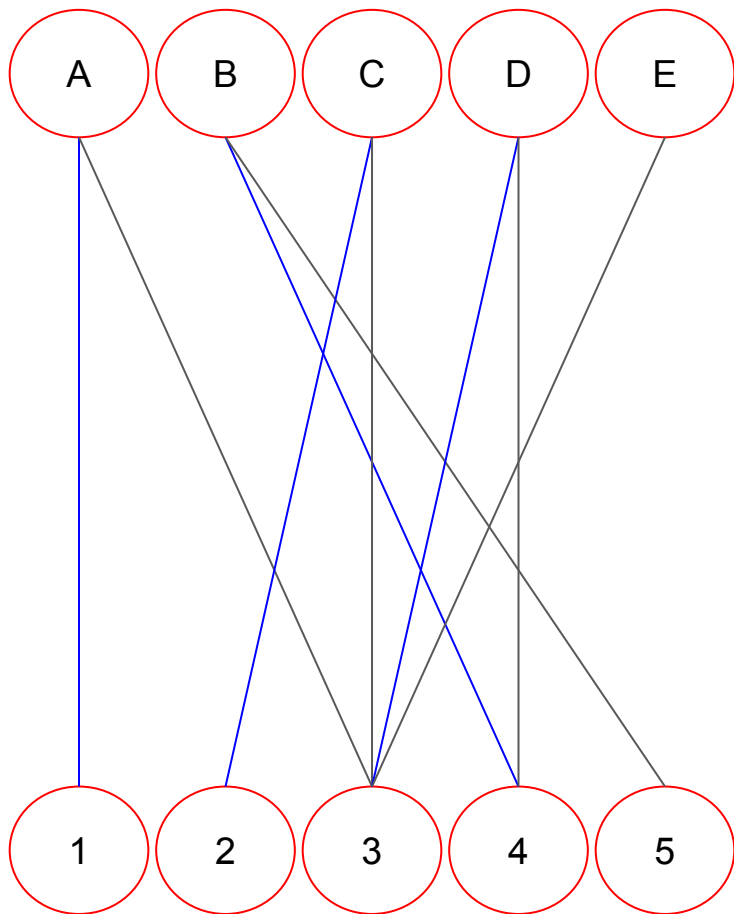


BFS



DFS

$P=\{(A,1), (B, 4), (C, 2), (D, 3)\}$



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2 **repeat**

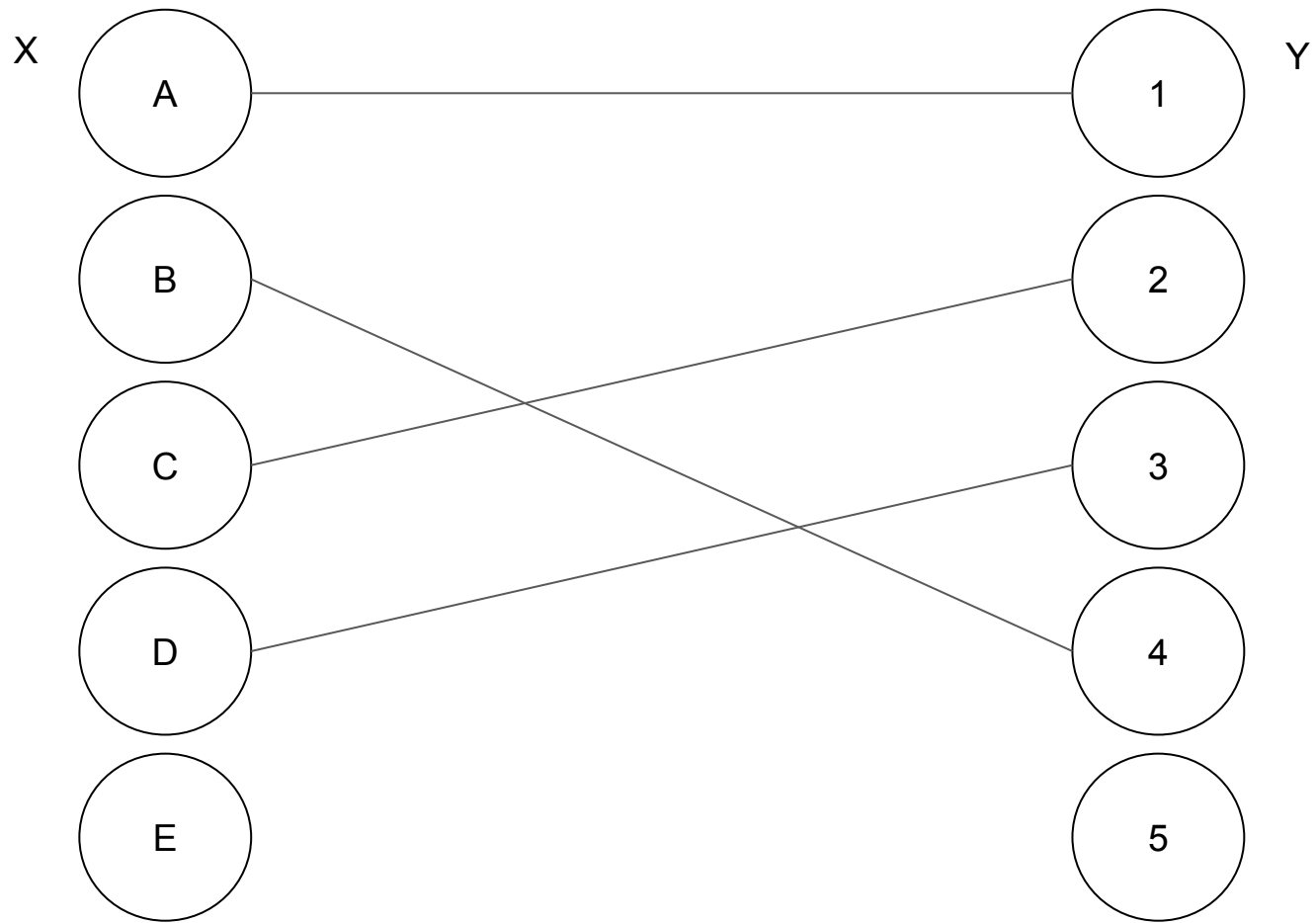
3 $P \leftarrow$ conjunto de caminhos aumentantes alternantes p_1, p_2, \dots, p_k

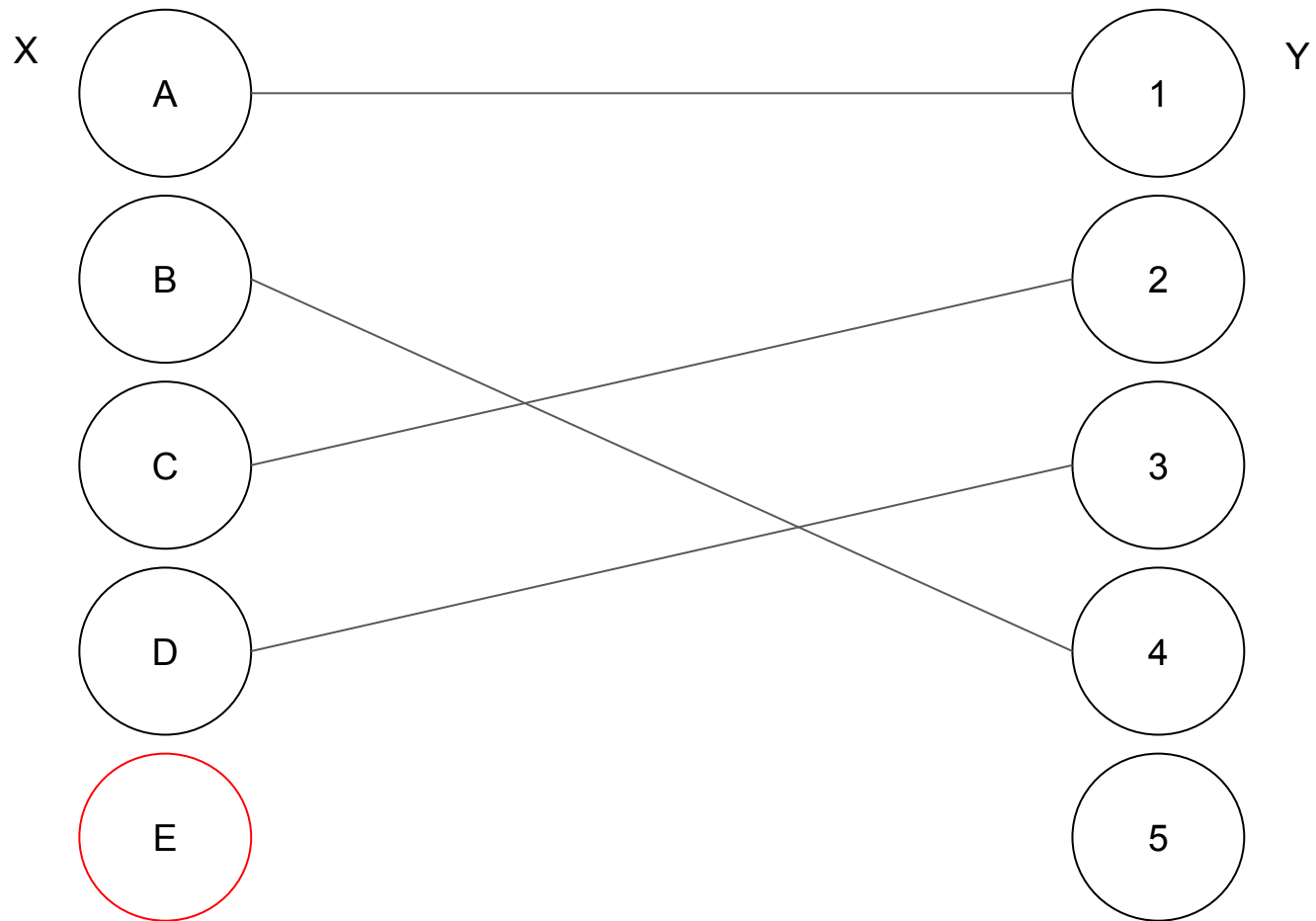
4 $M \leftarrow M \oplus \bigcup_{p \in P} p$

5 **until** $P = \{\}$

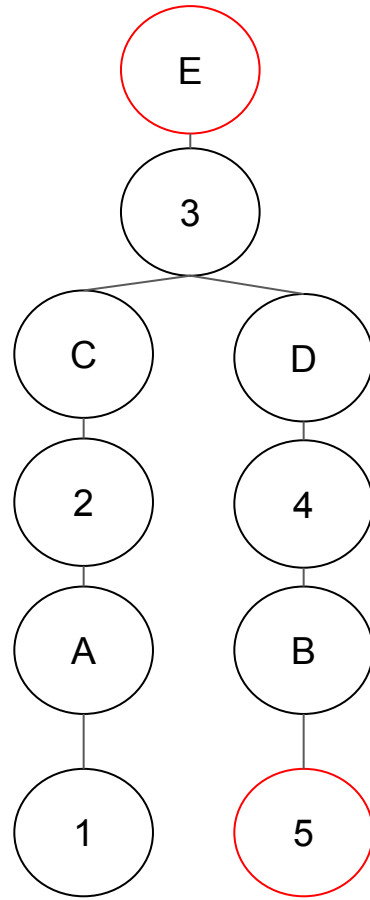
6 **return** M

$$M \leftarrow \{\} \oplus \{(A, 1), (B, 4), (C, 2), (D, 3)\}$$



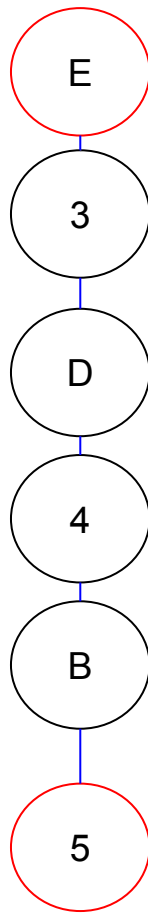


BFS



DFS

$P=\{(B,5), (D, 4), (E, 3)\}$



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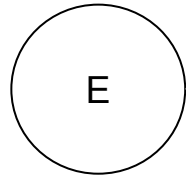
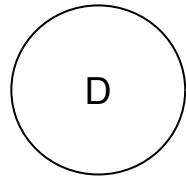
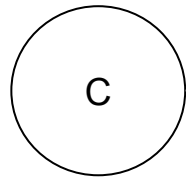
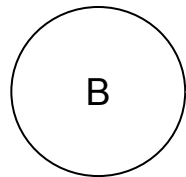
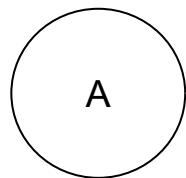
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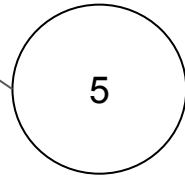
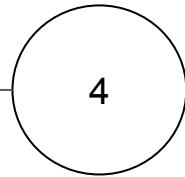
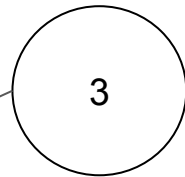
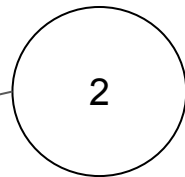
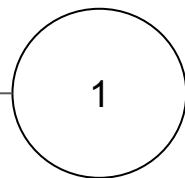
$$M \leftarrow \{(A,1), (B, 4), (C, 2), (D, 3)\} \oplus \{(B,5), (D, 4), (E, 3)\}$$

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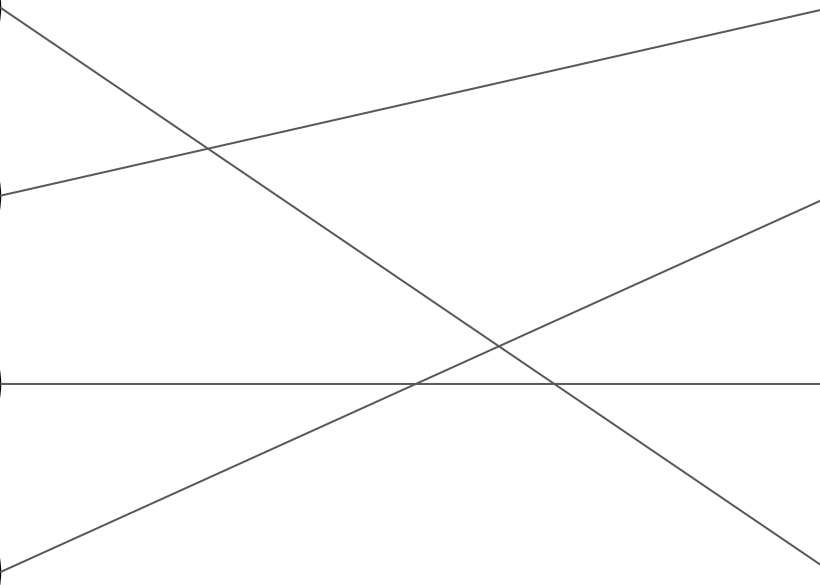
X



Y



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