

Assignment -1 in \LaTeX

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EE22BTECH11211

Problem 10.13.3.21:

Two dice are thrown together. Find the probability that the product of the numbers on the top of the dice is

- 1) 6
- 2) 12
- 3) 7

Solution:

1.

x = Outcome of the first dice

y = Outcome of the second dice

$$\begin{aligned} \Pr(\text{product} = 6) &= \Pr(x_1 \cdot x_2 = 6) = \\ \Pr(\{x_1 = 1, x_2 = 6\}, \{x_1 = 2, x_2 = 3\}, \{x_1 = 3, x_2 = 2\}, \{x_1 = 6, x_2 = 1\}) \end{aligned}$$

$$\Pr(\text{product} = 6) = \Pr(x_1 \cdot x_2 = 6) = \Pr(x_1 = 1, x_2 = 6) + \Pr(x_1 = 2, x_2 = 3) + \Pr(x_1 = 3, x_2 = 2) + \Pr(x_1 = 6, x_2 = 1)$$

$$\Pr(\text{product} = 6) = \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) = 4 \cdot \left(\frac{1}{6} \cdot \frac{1}{6}\right) = \frac{1}{9}$$

2.

x = Outcome of the first dice

y = Outcome of the second dice

$$\begin{aligned} \Pr(\text{product} = 12) &= \\ \Pr(x_1 \cdot x_2 = 12) &= \Pr(\{x_1 = 2, x_2 = 6\}, \{x_1 = 3, x_2 = 4\}, \{x_1 = 4, x_2 = 3\}, \{x_1 = 6, x_2 = 2\}) \end{aligned}$$

$$\Pr(\text{product} = 12) = \Pr(x_1 \cdot x_2 = 12) = \Pr(x_1 = 2, x_2 = 6) + \Pr(x_1 = 3, x_2 = 4) + \Pr(x_1 = 4, x_2 = 3) + \Pr(x_1 = 6, x_2 = 2)$$

$$\Pr(\text{product} = 12) = \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) + \left(\frac{1}{6} \cdot \frac{1}{6}\right) = 4 \cdot \left(\frac{1}{6} \cdot \frac{1}{6}\right) = \frac{1}{9}$$

3.

x = Outcome of the first dice

y = Outcome of the second dice

$$\Pr(\text{product} = 7) = \Pr(x_1 \cdot x_2 = 7) = 0$$