TSAIB tutorial

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Preface

The software package TSAIB was developed as the main deliverable for a synthesis project regarding the study-line: Earth and Space Physics and Engineering, with a specialization in Earth Observation, at the Technical University of Denmark.

Installation

The software is implemented in the open source language "R" which can be found at https://www.r-project.org/. The source code to the "R" software package TSAIB is located at GitHub at https://github.com/MathiasVendt/TSAIB

From GitHub

The easiest way to install the package is directly from Github by using the R devtools package. The R-version should be 2.10 or higher.

- 1. Open R
- 2. Install the devtools library by typing

```
install.packages('devtools')
```

3. Install the TSAIB package

```
devtools::install_github("MathiasVendt/TSAIB")
```

Or by using the remotes library like this:

- 1. Open R
- 2. Load in remotes library

library(remotes)

3. Install the TSAIB package

```
install_github("MathiasVendt/TSAIB")
```

Dependencies

The packages depends on the following R libraries which can be installed from R with the function install.packages. Hence, to install the package "ncdf4" use the following command for the R window:

```
install.packages("ncdf4")
```

- ncdf4
- ggplot2
- ggpub

forecast

A special library is also needed, and will be mentioned later in this tutorial

• TMB (Template Model Builder)

Together with a compiler tool, RTools. This can be installed by going to https://cran.r-project.org/, click on 'Download R for Windows', then 'Rtools', and select the latest version of RTools to download. After downloading has completed run the installer with default settings.

Getting started with R

The section gives a short introduction to R, which is useful to new R users.

R tutorials can be found at the r-project web side https://cran.r-project.org/manuals.html

Help pages can be accessed by typing "?" in front of a given function. If we want to access the help for the function sum we write

?sum

To start the web based help interface

help.start()

To exit R write

q()

Introduction to the package "TSAIB"

TSAIB is a R package aimed at getting statistical insight, correct for intermission bias and performing time series analysis of satellite observations consisting of sea-level anomalies measured in the arctic ocean. A variety of functions is provided in order to determine a time series model based on the analyses and insights from the analysis functions. In this introduction, examples are given to illustrate how to use the package.

To load the package simply write:

library(TSAIB)

Using "TSAIB" for analysis, visualization and manipulation of data

This section gives a step by step guide on how to utilize the package for analyzing the data, and the order in which the functions are used are recommended.

Load data

The test data set is called TSdata, and is included when the package is downloaded. When the TSAIB library is loaded, info about the data set can be found by the command:

?TSdata

In order to load the data into the R environment, the data set is assigned a name, e.g. "TSdata" like this:

TSdata=TSdata

The included data "TSdata" is a list containing 5 elements: Longitudes, latitudes, dates, measurements and a 3x3x325 construct, containing 325 measurements from a 3x3 data point grid. The data is extracted with the GridTSExtract function from the TSAIB library, and is done as:

TSdata=GridTSExtract(nco)

Where nco is the NetCDF data from which TSdata is extracted, and documentation on the data is listed in the Data appendix.

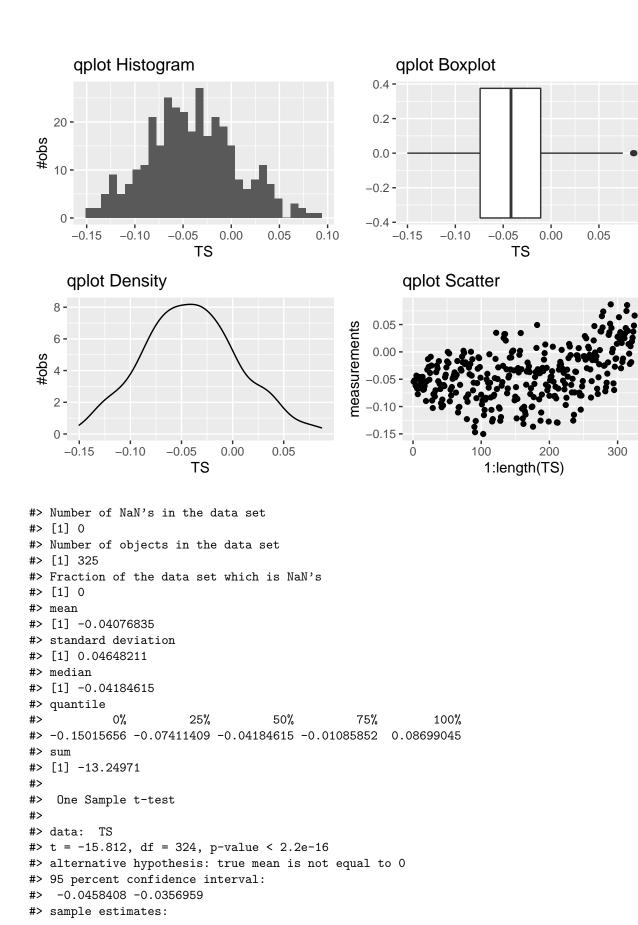
The user can also import their own data from a NetCDF file using the GridTSExtract function, and more info on how to use the function on a specific NetCDF file is shown by:

?GridTSExtract

Gather simple statistics about the data

It is now desired to get a brief overview of the data, including statistics, distributions and plotting. This can be achieved using the TSdiagnostics function. For this example, a meaned 30 point grid area (TS_area) is analyzed, which is centered around (lon,lat)=(0,73.25). To access sub elements of a construct in R, use \$ as a seperator between the parent object, and it's sub-directory. The function wont work for NaN elements, and if the extracted data contains a few of those, the nanrem option in the TSdiagnostics function is set to "TRUE", which will omit any NaN elements for the analysis.

TSdiagnostics(TS_area)



```
#> mean of x
#> -0.04076835
```

Removing NaN

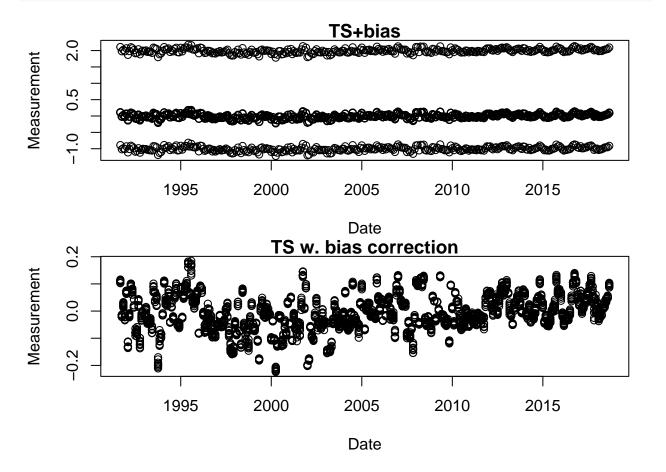
If it is decided to remove NaN objects, the function TSnanrem can be used to do this, with a variety of options of how to deal with NaN. For this example, the NaN's of TSmatrix are to be replaced with the mean of the time series:

```
TSnanrem(TSdata$TSmatrix, method = "mean")
```

Intermission bias correction

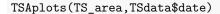
Some times, the data consists of measurements from different satellite missions, and these measurements will have different biases and need to be aligned. This calls for correction of intermission biases, and if the bias is known, it can be accounted for using the IB function. The input to this function is a time series struct TSM, a date vector, a bias vector containing up to two different biases c(bias1,bias2) and lastly, a bias index struct, with the same dimensions as TSM, containing zeros for the restrained time series, and integers 1 & 2, for bias1 and bias2 respectively. In the following example, the same 3x3x325 time series as used before, has been added a bias of c(1,-2), and is called TimeSeriesMatrixBias, with the corresponding bias index struct biasid.

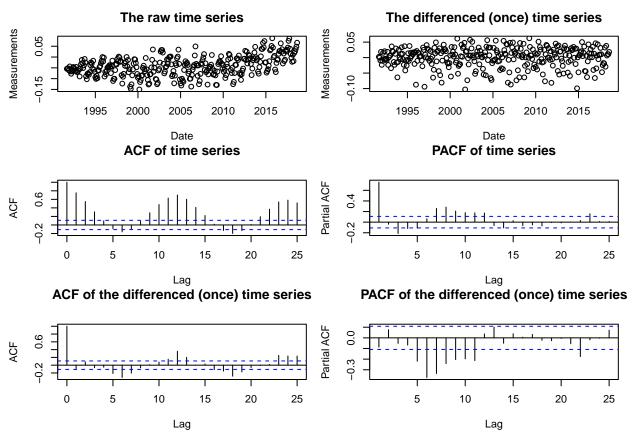
IB(TimeSeriesMatrixBias, TSdata\$date, c(1,-2), biasid)



Time series analysis plots

It is possible to get an insight of the time series with the TSAplots function. This function utilizes R's inbuilt differencing function diff, auto correlation function acf and partial auto correlation function pacf, to display a collection of plots to determine the time series characteristics. It is possible to choose a transformation of the data, being either sqrt or log transformations, and even to save the plots in a variety of formats. The default settings is used, which doesn't transform the data or save the plots:





A "tail-off" decay is observed in "ACF of time series", indicating an AR(p) part, and a cut-off is observed at lag 3 on "PACF of time series", indicating an AR(p=3) part could be reasonably assumed. The second row of plots show the ACF and PACF of the differenced time series (differenced once!), and the slow decay in the first ACF plot is clearly removed. Differencing once (d=1) is then a reasonable assumption. After differencing, a positive spike is seen at lag 12 on the "ACF of the differenced (once) time series"-plot, which could indicate a seasonality of 12 (S=12). This assumption is likely to be true, as the data used for this example is monthly observations of sea-level anomalies.

Using "TSAIB" for model estimation

To estimate a model which is describing the time series at hand, the TSAIB package containes several functions with different approches:

Iterative scanning of ARIMA(p,d,q)x(P,D,Q)s models

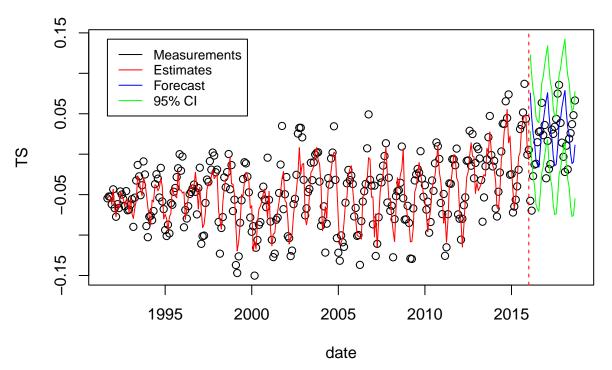
From the time series analysis functions, some indications of adequate parameter estimates for ARIMA models may be present, and if so, the ARIMAbuilder function could be useful. The inputs are the maximum number of p,q,P,Q parts in the arima model, and a fixed level of differencing: d and D. The output will display the top 5 best models, based on the Bayesian Information Criteria (BIC). BIC is chosen as it, according to (Madsen 2008), yields a consistent estimate of the model order, and is given by:

$$BIC = N\log\hat{\sigma}_{\epsilon}^2 + \log(N)(p+q+P+Q+d+D) \tag{1}$$

with N being the number of observations in the data set. By default, all parameters are set to 1, with seasonality set to 12 (i.e.: ARIMA(1,1,1)x(1,1,1)_12). For this example, however, the reasonable parameter guesses from TSAplots are used: ARIMA(p=3,d=1,q=?)x(P=?,D=?,Q=?)_S=12. Estimating ARIMA models is not an exact science, and ACF and PACF plots on real time series data is sometimes ambiguous. Hence the missing parameters are to be set to a reasonable guess of the maximum parameter value. The higher the parameter range, the more processing is needed to run ARIMAbuilder. To make the processing relatively fast, the remaining parameter estimates are set to 1: ARIMA(3,1,1,1,1)_12. Below is shown the iterations of model variations that has been evaluated, followed by a plot of the estimated best model on top of the measurements, and lastly a list of the top 5 best estimated ARIMA models:

```
ARIMAbuilder (TS_area, TSdata$date, 3, 1, 1, 1, 1, 1, 12)
#> [1] 0 1 0 0 1 0
#> [1] 0 1 0 0 1 1
#> [1] 0 1 0 1 1 0
#> [1] 0 1 0 1 1 1
#> [1] 0 1 1 0 1 0
  [1] 0 1 1 0 1 1
#> [1] 0 1 1 1 1 0
#> [1] 0 1 1 1 1 1
  [1] 1 1 0 0 1 0
  [1] 1 1 0 0 1 1
#> [1] 1 1 0 1 1 0
#> [1] 1 1 0 1 1 1
  [1] 1 1 1 0 1 0
#> [1] 1 1 1 0 1 1
#> [1] 1 1 1 1 0
#> [1] 1 1 1 1 1 1
  [1] 2 1 0 0 1 0
#> [1] 2 1 0 0 1 1
#> [1] 2 1 0 1 1 0
#> [1] 2 1 0 1 1 1
#> [1] 2 1 1 0 1 0
#> [1] 2 1 1 0 1 1
#> [1] 2 1 1 1 1 0
#> [1] 2 1 1 1 1 1
#> [1] 3 1 0 0 1 0
#> [1] 3 1 0 0 1 1
#> [1] 3 1 0 1 1 0
#> [1] 3 1 0 1 1 1
#> [1] 3 1 1 0 1 0
#> [1] 3 1 1 0 1 1
#> [1] 3 1 1 1 1 0
#> [1] 3 1 1 1 1 1
```

TS:Red, #1model:Black, Pred:Blue, 95% Conf.: Green



```
#> $'#1(p,q,P,Q)'
#> dim1 dim2 dim3 dim4
#> [1,]
        1 1
                1 1
#> $BIC1
#> [1] -2301.147
#>
#> $'#2(p,q,P,Q)'
#> dim1 dim2 dim3 dim4
#> [1,] 2 1
#>
#> $BIC2
#> [1] -2297.367
#>
#> $'#3(p,q,P,Q)'
#> dim1 dim2 dim3 dim4
#> [1,] 3 1
#>
#> $BIC3
#> [1] -2295.258
#> $'#4(p,q,P,Q)'
#> dim1 dim2 dim3 dim4
#> [1,] 1 1 0 1
#> $BIC4
```

It is seen that $ARIMA(3,1,1)x(1,1,1)_12$ is on third place, $ARIMA(2,1,1)x(1,1,1)_12$ is on second place, and the best model based on BIC is: $ARIMA(1,1,1)x(1,1,1)_12$, and that is shown in the figure above. ARIMAbuilder also takes the last 10% of the observations, and uses it as test data, on which it forecasts the remaining 10% together with a 95% CI for the forecastet predictions.

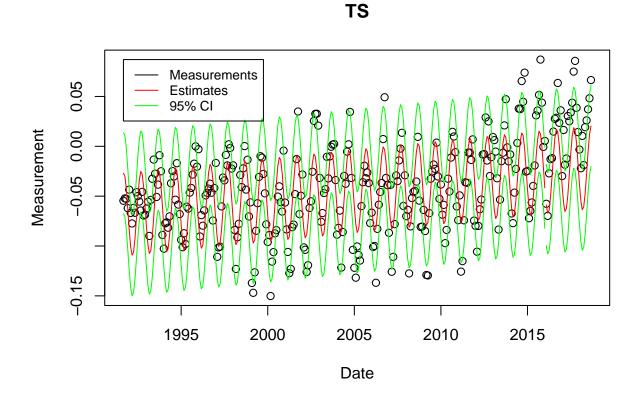
Simple time series model estimation, using OLS

The function TSSmodel estimates a simple model of the form:

$$Y_t = \alpha + \beta_t t + \beta_s \sin(\frac{2\pi}{p}t) + \beta_c \cos(\frac{2\pi}{p}t)$$
 (2)

where the alpha and the betas are the estimated parameters, and p and t is set to 12 and 1 respectively by default:

TSSmodel(TS_area,TSdata\$date)



- #> [1] "Parameter estimates:"
- #> [1] "alpha"
- #> [1] -0.06869383
- #> [1] "beta_t (trend)"
- #> [1] 0.0001462904
- #> [1] "beta_s (sinus)"
- **#>** [1] 0.02571606
- #> [1] "beta_c (cosinus)"
- #> [1] 0.03311466

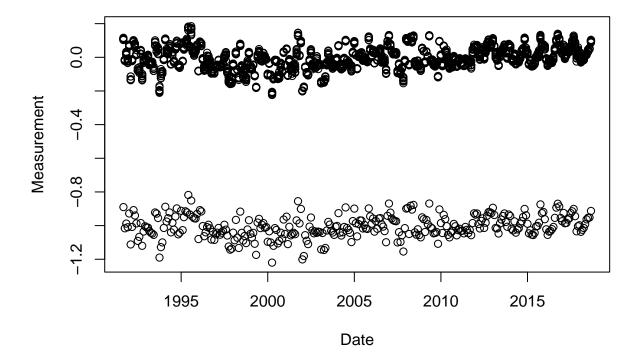
Using TMB to estimate a RW model, and account for intermission bias

TMB stands for "Template Model Builder", and is a C++ interface for automatic differentiation that implements Laplace's method to estimate a time series model. For more info on TMB and how to install the package, please visit https://github.com/kaskr/adcomp.

Selected TMB functions have been implemented into TSAIB, in order to efficiently estimate a Random Walk (RW) model, based on likelihood functions. These TMB functions are gathered in one TSAIB function, called TMBTSA. This function has three inputs: TSM (a struct with time series data), date (the usual vector containing time stamps) and biasid (a struct with the same dimensions as TSM, containing the ones where the biased data is). TMBTSA can handle one bias at a time, and doesn't need to know the exact bias value, in contrast to the IB function, as it will estimate constant bias in the process. Furthermore, TSM doesn't have to be corrected for NaN, as TMBTSA will handle those as well.

For the next example, a synthetic time series struct TimeSeriesMatrixBiasTMB is used. As with the demonstration for the IB function, this is an altered version of TSdata\$TSmatrix, with a single bias added this time. An illustration of the synthetic data is shown below:

TS with bias

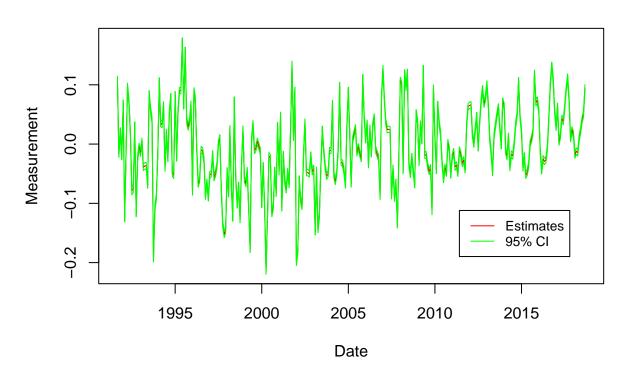


The bias index that matches TimeSeriesMatrixBiasTMB is biasidTMB. Together with the date vector TSdata\$date, TimeSeriesMatrixBiasTMB and biasidTMB are inserted into TMBTSA as so:

${\tt TMBTSA} ({\tt TimeSeriesMatrixBiasTMB}, {\tt TSdata\$date}, {\tt biasidTMB})$

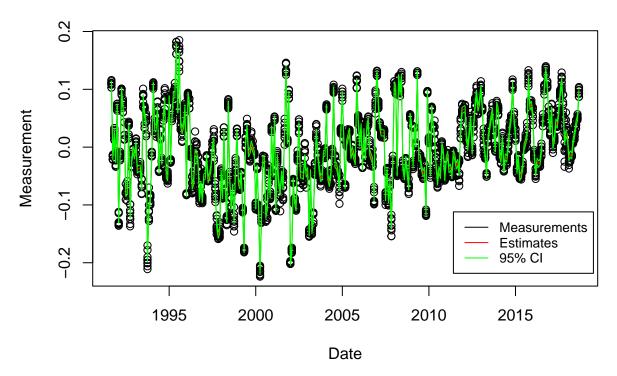
The iterative messages from the process has been left out, as it's excessive information for this tutorial. The estimated RW model is shown below:

Estimated RW



To compare the estimates with the data without bias, TSdata\$TSmatrix is plottet together with the estimates below.

TS without bias + Estimated RW



TMBTSA assumes the data to be independent and uncorrelated, and since the test data used in this example is satellite measurements of a certain area, there might be spacial correlation between the observations per time stamp. This impacts the calculation of the standard deviation, as the function interprets this as if it has more information about the data than it actually has, and it can be seen in the figures above, where the 95% CI lies extremely close to the estimates, making the estimates hard to distinguish from the CI.

Conclusion

This tutorial has presented the R package TSAIB, as well as demonstrated how to install, load, and utilize the inbuilt functions on a specific data set of satellite measurements of sea-level anomalies in the arctic ocean. GridTSExtract was used to extract the \verbnco+ object from a NetCDF file. Basic statistical insights was achieved through the TSdiagnostics function, on a meaned area of interest called TS_area. To manipulate NaN values in the data, a function was introduced to deal with this called TSnanrem. If the data contained known intermission bias, the function IB could correct the data for up to two different biases, which was demonstrated on synthetic biased data called TimeSeriesMatrixBias, with the matching bias struct biasid. The ACF and PACF of TS_area was plottet for the raw data, as well as for the differenced time series, through the TSAplots function, from which it was demonstrated how to estimate a few ARIMA parameters.

The next stage was "Model Estimation", where the ARIMAbuilder function was presented, and it was demonstrated how the parameter estimates from TSAplots could be used to restrain some of the ARIMA(p,d,q)x(P,D,Q)_S parameters, in order for the function to iteratively scan through qualitative parameter ranges, and point out the top 5 best models, and plot the best of all the possible ARIMA models based upon the BIC. Another introduced model estimation function was TSSmodel, which estimates a simple time series model using OLS, with an intercept, a trend, a sinus and a cosinus term, and was also demonstrated on the TS_area data. Lastly, the TMBTSA function was demonstrated, which utilizes

TMB, a C++ interface, to estimate a RW model, take care of NaN, and also account for one intermission bias all at once. This was done on synthetic data containing NaN and one intermission bias called TimeSeriesMatrixBiasTMB with the corresponding bias struct called biasidTMB.

Discussion

TSAIB successfully implements analysis and model estimation functions on the specific data set provided. It is not certain that the data from a NetCDF file is structured the same way, and in order to match with other data sets than what is provided in the package, the user is required to have some basic knowledge of how to manipulate the data in R in order for it to fit the functions used in TSAIB.

The functions, unless described otherwise, are sensitive to NaN values, for which an extra function is provided to take care of this before inserting the data into the functions. This could be implemented in more advanced functions, so that pre-processing of the data isn't necessary.

For the R functions that are demonstrated using the TS_area data set, only a vector of time series data can be used as input, where a more advanced function could take into account a grid of values for each time step, as it is done in the TMBTSA function.

The ARIMAbuilder function can take any range of parameters as input, and if the range is set too high, and there aren't enough restrained parameters, the processing of this function can be very time consuming, and if the user isn't careful, this process could uptake all the computer's memory. An improvement on this would be a security measure which halts the process if this limit is approaching.

TSSmodel estimates a very simple and specific model, and it was seen that the simple sinus and cosinus terms wasn't matching the data very well. This function could be further developed featuring a number of different simple linear models, from which the user could choose the most adequate.

The implementation of TMB in the TMBTSA function is very sparse compared to the enormous potential and amount of tools TMB has to offer. The function could have several different tools combined into the function, form which the user would be able to choose one of these. The wrong calculation of the standard deviation when the function is used on a grid of data per time stamp, could also be fixed, so that the function would take correlation of the data points into account. It also complicates the use of TSAIB a little by having to install TMB prior to TSAIB, but compared to the possibilities of using TMB, this is a relatively small price to pay.

All in all TSAIB provides a simple overview, and relatively simple-to-use functions for estimating time series models on satellite data of sea-level anomalies provided in this package, but the functions could be developed to be more versatile, robust and user friendly when used on other data.

Appendices

Data set used for demonstration of the TSAIB package:

TSdata

```
?TSdata

Description

An extracted list using the "GridTSExtract" function, from the data set:
Rose, S.K.; Andersen, O.B.; Passaro, M.; Ludwigsen, C.A.; Schwatke,
C. Arctic Ocean Sea Level Record from the Complete Radar
Altimetry Era: 1991-2018. Remote Sens. 2019, 11, 1672.
https://www.mdpi.com/2072-4292/11/14/1672
Usage
```

```
TSdata
Format
A large list containing 5 elements, which are:
longitude: containing longitudes from -180:180, by increments of 0.5 degrees
(length: 720)
latitude: containing latitudes from 65:81.5, by increments of 0.25 degrees (length: 67)
date: containing years from 1991:2019, by increments of 1/12 (length:325)
measurements: containing sea_level_anomaly measurements for each increments of:
longitude, latitude and date. (dimension: [67,720,325])
TSmatrix: containing a 3x3x325 grid of measurements centered around (lon,lat)=(-165,74)
```

TSdata2

```
?TSdata2
Description
 An extracted list using the "GridTSExtract" function, from the data set:
 Rose, S.K.; Andersen, O.B.; Passaro, M.; Ludwigsen, C.A.; Schwatke,
 C. Arctic Ocean Sea Level Record from the Complete Radar
 Altimetry Era: 1991-2018. Remote Sens. 2019, 11, 1672.
 https://www.mdpi.com/2072-4292/11/14/1672
 Usage
 TSdata2
Format
 A large list containing 5 elements, which are:
 longitude: Containing longitudes from -180:180, by increments of 0.5 degrees
 (length: 720)
 latitude: Containing latitudes from 65:81.5, by increments of 0.25 degrees (length: 67)
 date: Containing years from 1991:2019, by increments of 1/12 (length:325)
 measurements: Containing sea_level_anomaly measurements for each increments of:
 longitude, latitude and date. (dimension: [67,720,325])
 TSmatrix: Containing a 61x61x325 grid of measurements centered around (lon,lat)=(0,73)
```

TS area

```
Programment Progra
```

${\bf Time Series Matrix Bias}$

```
?TimeSeriesMatrixBias

Description
A time series matrix with added biases: 1 and -2, on the data: "TSdata$TSmatrix"

Usage
TimeSeriesMatrixBias

Format
A numerical struct with dimensions 3x3x325
```

biasid

```
?biasid
Description
  A bias index containing bias indicies: 1 and 2, matching the synthetic bias data
"TimeSeriesMatrixBias"
Usage
  biasid
Format
  A numerical struct with dimensions 3x3x325
```

TimeSeriesMatrixBiasTMB

```
?TimeSeriesMatrixBias

Description

A time series matrix with added biases: 1, on the data: "TSdata$TSmatrix"

Usage

TimeSeriesMatrixBiasTMB

Format

A numerical struct with dimensions 3x3x325
```

${\it biasidTMB}$

```
PbiasidTMB

Description

A bias index containing bias index: 1, matching the synthetic bias data

"TimeSeriesMatrixBiasTMB"

Usage
biasidTMB

Format

A numerical struct with dimensions 3x3x325
```

DEMOpllam

```
?DEMOpllam
Description
RW model estimates, calculated using the TMBTSA function on "TimeSeriesMatricBiasTMB"
and "biasidTMB"
Usage
DEMOpllam
Format
A numerical vector with length: 325
```

DEMOplsdlam

```
?DEMOplsdlam
Description
RW model standard deviations, calculated using the "TMBTSA" function on
"TimeSeriesMatricBiasTMB" and "biasidTMB"
Usage
DEMOplsdlam
Format
A numerical vector with length: 325
```

DEMOtval

```
?DEMOtval
Description
T-value for the 95% confidence interval for the TMBTSA function
Usage
DEMOtval
Format
A numerical value
```

Functions

GridTSExtract

```
?GridTSExtract
Description
 Extracts a time series from a NetCDF lon&lat coordinate grid
Usage
GridTSExtract(
 nco,
 lonid = "longitude",
 latid = "latitude",
 timeid = "date",
 measurementsid = "sea_level_anomaly",
 coord = c(-165, 74),
 radius = 0,
 dlon = 2,
 dlat = 4
)
 Arguments
 nco: The NetCDF object (open with "nc_open" from the "ncdf4" library)
 lonid: The variable id for longitude vector. e.g.: "longitude"
  latid: The variable id for latitude vector. e.g.: "latitude"
  timeid: The variable id for the time vector. e.g.: "date"
  measurementsid: The variable id for the measurements vector. e.g.: "sea_level_anomaly"
  coord: The center coordinate for the TS grid area. e.g.: c(lon,lat) i.e. c(-164,74)
  radius: The square radius of the TS grid. e.g: 0=1x1 grid, 1=3x3 grid, 2=5x5 grid etc.
  dlon: Number of data points for each degree longitude
  dlat:Number of data points for each degree latitude
 Value
  Time series from grid
```

TSdiagnostics

```
?TSdiagnostics
Description
   Shows basic statistics and characteristics of the time series data
Usage
   TSdiagnostics(TS, nanrem = "FALSE")
Arguments
   TS:The time series to be analyzed
   nanrem: Set NaN to be removed or not. e.g.: nanrem="TRUE"
```

```
Value
Basic statistics and characteristics
```

TSnanrem

```
?TSnanrem
Description
Removes or imputes NaN from the time series data set, with a specified method of choice
Usage
   TSnanrem(TS, method = "mean", value_nr = 0)
Arguments
TS: The time series to remove NaN from
   method: The imputation method. e.g.: "omit", "mean", "median" or "value"
   value_nr: The specific value for the "value" imputing method. e.g.: value_nr=0
Value
   Time series with NaNs removed or replaced
```

$_{\mathrm{IB}}$

```
Description
Corrects a struct of timeseries for up to two intermission biases
Usage
IB(TSM, date, biasvec = c(1, -2), biasid)
Arguments
TSM: The time series struct with the intermission bias
date: The time axis in the time series (dates, seconds, intervals)
biasvec: The vector containing up to 2 different bias. If the data only contains one7
bias, insert that value instead of the vector
biasid: A struct with the same dimensions as TSM, with integers indicating the bias:
0 for the restrained time series, 1 for the first bias and 2 for the second bias.
Value
Time series struct with bias correction
```

TSAplots

```
?TSAplots
Description
 Plots and saves the ACF and PACF for a pre-defined time series, with and without data
 transformations (log, sqrt), and differencing. Input type: Time series
 Usage
  TSAplots(TS, date, trans = "NONE", saveas = "NONE")
 Arguments
 TS: The time series for the TSAplots function
  date: The time axis in the time series (dates, seconds, intervals)
  trans: data transform parameter: trans='log' for log transform, trans='sqrt' for sqrt
  transform, and trans='NONE' for no transform
  saveas: specifies the file format to save the plots in the current working directory.
  Possible formats is: PDF, JPEG, TIFF, BMP and PNG. e.g.: "pdf" or "jpeg".
  If no format is specified, it will not save the plots
 Value
 Plots from TSAplots
```

TSSmodel

```
?TSSmodel
Description
  Estimates a simple time series model

Usage
  TSSmodel(TS, date, p = 12, t = 1, testsize = round(length(date)/10))
Arguments
  TS: The time series for the TSSmodel function
  date: The time axis in the time series (dates, seconds, intervals)
  p: The period. e.g.: p=12, for 12 months in a year
  t: The time steps. e.g.: t=1, for monthly time steps, with period 12
  testsize: The number of data points to be used for testing the model
Value
  Simple TS model
```

ARIMAbuilder

```
?ARTMAbuilder
Description
 Lists the top 5 estimated ARIMA/SARIMA models of the form: ARIMA(p,d,q)x(P,D,Q),
 based on specified parameter values and ranges
 ARIMAbuilder(TS, p = 1, d = 1, q = 1, P = 1, D = 1, Q = 1, S = 12)
  TS: The time series to build the models upon (remember to transform before
  using this function!)
  p: The maximum AR value, estimated from plot analysis
  d: The fixed differencing, often 0, 1 or 2
  q: The maximum MA value, estimated from plot analysis
  P: The maximum seasonal AR value, estimated from plot analysis
 D: The fixed seasonal differencing, often 0, 1 or 2
  Q: The maximum seasonal MA value, estimated from plot analysis
 S: The seasonality/period of the seasonal differencing
 Value
 List of top 5 ARIMA/SARIMA models
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TMBTSA

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Pescription
Utilizes TMB, which is a C++ interface for automatic differentiation that implements the Laplace method, to estimate a time series model
Usage
TMBTSA(TSM, date, biasid)
Arguments
TSM: The time series struct, with dimensions (x/lon,y/lat,timesteps)
date: The time axis in the time series (i.e., dates, seconds, intervals)
biasid: A struct with the same dimensions as TSM, with integers indicating the bias:
0 for the restrained time series and 1 for the bias. If no bias is present, biasid contains only zeros.
Value
RW model
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References

 ${\it Madsen, Henrik. 2008. "Time Series Analysis." http://www.http://henrikmadsen.org/books/time-series-analysis/.}$