

Number of vertices $n = 7$.

Adjacencies of Graph

1. vertex 1 adjacent to 3 4 5 6 7
2. vertex 2 adjacent to 3 4 5 6 7
3. vertex 3 adjacent to 1 2 4 5 6 7
4. vertex 4 adjacent to 1 2 3 5 6 7
5. vertex 5 adjacent to 1 2 3 4 6 7
6. vertex 6 adjacent to 1 2 3 4 5 7
7. vertex 7 adjacent to 1 2 3 4 5 6

Size of automorphism group of the graph=240

Full group: $|Aut(polytope)| = 15360$

Restricted group: $|Aut(G) \times switch| = 15360$

Number of orbits for the full group : 17

List of orbits of facets for the full group: Total number of orbits = 17

Total number of facets = 32680

1. Inequality 1 with incidence 48 and stabilizer of size 192. Orbit size is 80

| | | | | | |
|-----------|------------|-----------|-----------|-----------|-----------|
| (1,3) : 0 | (1,4) : -1 | (1,5) : 0 | (1,6) : 0 | (1,7) : 1 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 0 | (3,5) : 0 |
| (3,6) : 0 | (3,7) : 0 | (4,5) : 0 | (4,6) : 0 | (4,7) : 1 | (5,6) : 0 |
| (5,7) : 0 | (6,7) : 0 | | | | |

2. Inequality 2 with incidence 48 and stabilizer of size 384. Orbit size is 40

| | | | | | |
|-----------|------------|-----------|-----------|-----------|-----------|
| (1,3) : 0 | (1,4) : 0 | (1,5) : 0 | (1,6) : 0 | (1,7) : 0 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 1 | (3,5) : 0 |
| (3,6) : 0 | (3,7) : -1 | (4,5) : 0 | (4,6) : 0 | (4,7) : 1 | (5,6) : 0 |
| (5,7) : 0 | (6,7) : 0 | | | | |

3. Inequality 3 with incidence 40 and stabilizer of size 96. Orbit size is 160

| | | | | | |
|-----------|------------|-----------|------------|-----------|-----------|
| (1,3) : 1 | (1,4) : -1 | (1,5) : 0 | (1,6) : -1 | (1,7) : 1 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 1 | (3,5) : 0 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : 0 | (4,6) : -1 | (4,7) : 1 | (5,6) : 0 |
| (5,7) : 0 | (6,7) : 1 | | | | |

4. Inequality 4 with incidence 40 and stabilizer of size 960. Orbit size is 16

| | | | | | |
|-----------|------------|------------|------------|-----------|------------|
| (1,3) : 0 | (1,4) : 0 | (1,5) : 0 | (1,6) : 0 | (1,7) : 0 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 1 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : -1 | (4,6) : -1 | (4,7) : 1 | (5,6) : -1 |
| (5,7) : 1 | (6,7) : 1 | | | | |

5. Inequality 5 with incidence 30 and stabilizer of size 48. Orbit size is 320

| | | | | | |
|------------|------------|-----------|------------|-----------|------------|
| (1,3) : 1 | (1,4) : -1 | (1,5) : 1 | (1,6) : -1 | (1,7) : 2 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 1 | (3,5) : -1 |
| (3,6) : 1 | (3,7) : -2 | (4,5) : 1 | (4,6) : -1 | (4,7) : 2 | (5,6) : 1 |
| (5,7) : -2 | (6,7) : 2 | | | | |

6. Inequality 6 with incidence 30 and stabilizer of size 240. Orbit size is 64

| | | | | | |
|------------|------------|-----------|------------|-----------|------------|
| (1,3) : 2 | (1,4) : -2 | (1,5) : 2 | (1,6) : -2 | (1,7) : 2 | (2,3) : 0 |
| (2,4) : 0 | (2,5) : 0 | (2,6) : 0 | (2,7) : 0 | (3,4) : 1 | (3,5) : -1 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : 1 | (4,6) : -1 | (4,7) : 1 | (5,6) : 1 |
| (5,7) : -1 | (6,7) : 1 | | | | |

7. Inequality 7 with incidence 28 and stabilizer of size 24. Orbit size is 640

| | | | | | |
|------------|-----------|-----------|-----------|------------|------------|
| (1,3) : -1 | (1,4) : 0 | (1,5) : 1 | (1,6) : 1 | (1,7) : -1 | (2,3) : -1 |
| (2,4) : 0 | (2,5) : 1 | (2,6) : 1 | (2,7) : 1 | (3,4) : 0 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : 0 | (4,5) : 0 | (4,6) : 0 | (4,7) : 0 | (5,6) : -1 |
| (5,7) : 0 | (6,7) : 0 | | | | |

8. Inequality 8 with incidence 25 and stabilizer of size 24. Orbit size is 640

| | | | | | |
|------------|------------|------------|------------|------------|------------|
| (1,3) : -1 | (1,4) : 1 | (1,5) : 1 | (1,6) : 1 | (1,7) : -2 | (2,3) : -1 |
| (2,4) : 1 | (2,5) : 1 | (2,6) : 1 | (2,7) : 0 | (3,4) : 1 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : -1 | (4,6) : -1 | (4,7) : 1 | (5,6) : -1 |
| (5,7) : 1 | (6,7) : 1 | | | | |

9. Inequality 9 with incidence 24 and stabilizer of size 8. Orbit size is 1920

| | | | | | |
|-----------|------------|------------|-----------|------------|------------|
| (1,3) : 1 | (1,4) : 1 | (1,5) : 1 | (1,6) : 1 | (1,7) : -2 | (2,3) : 1 |
| (2,4) : 1 | (2,5) : -1 | (2,6) : -1 | (2,7) : 0 | (3,4) : -1 | (3,5) : 0 |
| (3,6) : 0 | (3,7) : 1 | (4,5) : 0 | (4,6) : 0 | (4,7) : 1 | (5,6) : -1 |
| (5,7) : 1 | (6,7) : 1 | | | | |

10. Inequality 10 with incidence 22 and stabilizer of size 12. Orbit size is 1280

| | | | | | |
|------------|-----------|------------|------------|------------|------------|
| (1,3) : -2 | (1,4) : 1 | (1,5) : 1 | (1,6) : 1 | (1,7) : -1 | (2,3) : -2 |
| (2,4) : 1 | (2,5) : 1 | (2,6) : 1 | (2,7) : 1 | (3,4) : 2 | (3,5) : 2 |
| (3,6) : 2 | (3,7) : 0 | (4,5) : -1 | (4,6) : -1 | (4,7) : 0 | (5,6) : -1 |
| (5,7) : 0 | (6,7) : 0 | | | | |

11. Inequality 11 with incidence 21 and stabilizer of size 12. Orbit size is 1280

| | | | | | |
|------------|------------|------------|------------|-----------|------------|
| (1,3) : 1 | (1,4) : -1 | (1,5) : -1 | (1,6) : -1 | (1,7) : 2 | (2,3) : 2 |
| (2,4) : -1 | (2,5) : -1 | (2,6) : -1 | (2,7) : 1 | (3,4) : 2 | (3,5) : 2 |
| (3,6) : 2 | (3,7) : -3 | (4,5) : -1 | (4,6) : -1 | (4,7) : 2 | (5,6) : -1 |
| (5,7) : 2 | (6,7) : 2 | | | | |

12. Inequality 12 with incidence 21 and stabilizer of size 4. Orbit size is 3840

| | | | | | |
|-----------|------------|------------|------------|-----------|------------|
| (1,3) : 0 | (1,4) : 1 | (1,5) : -1 | (1,6) : -1 | (1,7) : 1 | (2,3) : 1 |
| (2,4) : 1 | (2,5) : -1 | (2,6) : -1 | (2,7) : 0 | (3,4) : 0 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : 1 | (4,6) : 1 | (4,7) : 0 | (5,6) : -1 |
| (5,7) : 1 | (6,7) : 1 | | | | |

13. Inequality 13 with incidence 21 and stabilizer of size 2. Orbit size is 7680

| | | | | | |
|-----------|-----------|------------|------------|-----------|-----------|
| (1,3) : 1 | (1,4) : 0 | (1,5) : -1 | (1,6) : -1 | (1,7) : 1 | (2,3) : 1 |
| (2,4) : 1 | (2,5) : 0 | (2,6) : -1 | (2,7) : -1 | (3,4) : 0 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : 0 | (4,5) : -1 | (4,6) : 1 | (4,7) : 1 | (5,6) : 0 |
| (5,7) : 1 | (6,7) : 0 | | | | |

14. Inequality 14 with incidence 21 and stabilizer of size 2. Orbit size is 7680

| | | | | | |
|-----------|------------|------------|------------|------------|------------|
| (1,3) : 1 | (1,4) : 0 | (1,5) : -1 | (1,6) : -1 | (1,7) : 1 | (2,3) : 2 |
| (2,4) : 1 | (2,5) : -1 | (2,6) : -1 | (2,7) : -1 | (3,4) : -2 | (3,5) : 2 |
| (3,6) : 2 | (3,7) : 1 | (4,5) : 1 | (4,6) : 1 | (4,7) : 1 | (5,6) : -1 |
| (5,7) : 0 | (6,7) : 0 | | | | |

15. Inequality 15 with incidence 20 and stabilizer of size 6. Orbit size is 2560

| | | | | | |
|------------|------------|------------|------------|------------|------------|
| (1,3) : -2 | (1,4) : 2 | (1,5) : 3 | (1,6) : 2 | (1,7) : -3 | (2,3) : -1 |
| (2,4) : 1 | (2,5) : 2 | (2,6) : 1 | (2,7) : 1 | (3,4) : 1 | (3,5) : 2 |
| (3,6) : 1 | (3,7) : -1 | (4,5) : -2 | (4,6) : -1 | (4,7) : 1 | (5,6) : -2 |
| (5,7) : 1 | (6,7) : 1 | | | | |

16. Inequality 16 with incidence 20 and stabilizer of size 24. Orbit size is 640

| | | | | | |
|------------|-----------|------------|------------|------------|------------|
| (1,3) : -1 | (1,4) : 1 | (1,5) : 1 | (1,6) : 1 | (1,7) : -2 | (2,3) : -2 |
| (2,4) : 2 | (2,5) : 2 | (2,6) : 2 | (2,7) : 2 | (3,4) : 1 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : 0 | (4,5) : -1 | (4,6) : -1 | (4,7) : 0 | (5,6) : -1 |
| (5,7) : 0 | (6,7) : 0 | | | | |

17. Inequality 17 with incidence 20 and stabilizer of size 4. Orbit size is 3840

| | | | | | |
|-----------|------------|------------|------------|------------|------------|
| (1,3) : 1 | (1,4) : 1 | (1,5) : 1 | (1,6) : 1 | (1,7) : -2 | (2,3) : 3 |
| (2,4) : 3 | (2,5) : -2 | (2,6) : -2 | (2,7) : -2 | (3,4) : -2 | (3,5) : 1 |
| (3,6) : 1 | (3,7) : 2 | (4,5) : 1 | (4,6) : 1 | (4,7) : 2 | (5,6) : -1 |
| (5,7) : 0 | (6,7) : 0 | | | | |