

Number of vertices  $n = 8$ .

Adjacencies of Graph

1. vertex 1 adjacent to 2 6 7 8
2. vertex 2 adjacent to 1 3 7 8
3. vertex 3 adjacent to 2 4 7 8
4. vertex 4 adjacent to 3 5 7 8
5. vertex 5 adjacent to 4 6 7 8
6. vertex 6 adjacent to 1 5 7 8
7. vertex 7 adjacent to 1 2 3 4 5 6 8
8. vertex 8 adjacent to 1 2 3 4 5 6 7

Size of automorphism group of the graph=24

Full group:  $|Aut(polytope)| = 3072$

Restricted group:  $|Aut(G) \times switch| = 3072$

Number of orbits for the full group : 7

List of orbits of facets for the full group: Total number of orbits = 7 Total number of facets = 3432

1. Inequality 1 with incidence 96 and stabilizer of size 64. Orbit size is 48

|              |             |             |             |             |             |
|--------------|-------------|-------------|-------------|-------------|-------------|
| $(1,2) : -1$ | $(1,6) : 0$ | $(1,7) : 0$ | $(1,8) : 1$ | $(2,3) : 0$ | $(2,7) : 0$ |
| $(2,8) : 1$  | $(3,4) : 0$ | $(3,7) : 0$ | $(3,8) : 0$ | $(4,5) : 0$ | $(4,7) : 0$ |
| $(4,8) : 0$  | $(5,6) : 0$ | $(5,7) : 0$ | $(5,8) : 0$ | $(6,7) : 0$ | $(6,8) : 0$ |
| $(7,8) : 0$  |             |             |             |             |             |

2. Inequality 2 with incidence 96 and stabilizer of size 128. Orbit size is 24

|             |             |              |             |             |             |
|-------------|-------------|--------------|-------------|-------------|-------------|
| $(1,2) : 0$ | $(1,6) : 0$ | $(1,7) : -1$ | $(1,8) : 1$ | $(2,3) : 0$ | $(2,7) : 0$ |
| $(2,8) : 0$ | $(3,4) : 0$ | $(3,7) : 0$  | $(3,8) : 0$ | $(4,5) : 0$ | $(4,7) : 0$ |
| $(4,8) : 0$ | $(5,6) : 0$ | $(5,7) : 0$  | $(5,8) : 0$ | $(6,7) : 0$ | $(6,8) : 0$ |
| $(7,8) : 1$ |             |              |             |             |             |

3. Inequality 3 with incidence 28 and stabilizer of size 4. Orbit size is 768

|            |           |           |            |            |            |
|------------|-----------|-----------|------------|------------|------------|
| (1,2) : -1 | (1,6) : 1 | (1,7) : 1 | (1,8) : -1 | (2,3) : 1  | (2,7) : 0  |
| (2,8) : 0  | (3,4) : 1 | (3,7) : 1 | (3,8) : -1 | (4,5) : 1  | (4,7) : -1 |
| (4,8) : 1  | (5,6) : 1 | (5,7) : 1 | (5,8) : -1 | (6,7) : -1 | (6,8) : 1  |
| (7,8) : 1  |           |           |            |            |            |

4. Inequality 4 with incidence 26 and stabilizer of size 12. Orbit size is 256

|            |           |            |            |           |           |
|------------|-----------|------------|------------|-----------|-----------|
| (1,2) : -1 | (1,6) : 1 | (1,7) : 1  | (1,8) : -1 | (2,3) : 1 | (2,7) : 0 |
| (2,8) : 0  | (3,4) : 1 | (3,7) : 1  | (3,8) : -1 | (4,5) : 1 | (4,7) : 0 |
| (4,8) : 0  | (5,6) : 1 | (5,7) : -1 | (5,8) : 1  | (6,7) : 0 | (6,8) : 0 |
| (7,8) : 1  |           |            |            |           |           |

5. Inequality 5 with incidence 24 and stabilizer of size 2. Orbit size is 1536

|            |           |            |            |           |           |
|------------|-----------|------------|------------|-----------|-----------|
| (1,2) : -1 | (1,6) : 1 | (1,7) : 1  | (1,8) : -1 | (2,3) : 1 | (2,7) : 0 |
| (2,8) : 0  | (3,4) : 1 | (3,7) : 0  | (3,8) : 0  | (4,5) : 1 | (4,7) : 1 |
| (4,8) : -1 | (5,6) : 1 | (5,7) : -1 | (5,8) : 1  | (6,7) : 0 | (6,8) : 0 |
| (7,8) : 1  |           |            |            |           |           |

6. Inequality 6 with incidence 24 and stabilizer of size 96. Orbit size is 32

|            |           |           |           |           |           |
|------------|-----------|-----------|-----------|-----------|-----------|
| (1,2) : -1 | (1,6) : 1 | (1,7) : 0 | (1,8) : 0 | (2,3) : 1 | (2,7) : 0 |
| (2,8) : 0  | (3,4) : 1 | (3,7) : 0 | (3,8) : 0 | (4,5) : 1 | (4,7) : 0 |
| (4,8) : 0  | (5,6) : 1 | (5,7) : 0 | (5,8) : 0 | (6,7) : 0 | (6,8) : 0 |
| (7,8) : 0  |           |           |           |           |           |

7. Inequality 7 with incidence 22 and stabilizer of size 4. Orbit size is 768

|            |           |           |            |            |           |
|------------|-----------|-----------|------------|------------|-----------|
| (1,2) : -1 | (1,6) : 1 | (1,7) : 1 | (1,8) : -1 | (2,3) : 1  | (2,7) : 0 |
| (2,8) : 0  | (3,4) : 1 | (3,7) : 0 | (3,8) : 0  | (4,5) : 1  | (4,7) : 0 |
| (4,8) : 0  | (5,6) : 1 | (5,7) : 1 | (5,8) : -1 | (6,7) : -1 | (6,8) : 1 |
| (7,8) : 1  |           |           |            |            |           |