Number of vertices n = 9. Adjacencies of Graph

- 1. vertex 1 adjacent to 2 4 5 9
- 2. vertex 2 adjacent to 1 3 6 9
- 3. vertex 3 adjacent to 2 4 7 9
- 4. vertex 4 adjacent to 1 3 8 9
- 5. vertex 5 adjacent to 1 6 8 9
- 6. vertex 6 adjacent to 2 5 7 9
- 7. vertex 7 adjacent to 3 6 8 9
- 8. vertex 8 adjacent to 4 5 7 9
- 9. vertex 9 adjacent to 1 2 3 4 5 6 7 8

Size of automorphism group of the graph=48

Full group: |Aut(polytope)| = 12288

Restricted group:  $|Aut(G) \times switch| = 12288$ 

Number of orbits for the full group: 6

List of orbits of facets for the full group: Total number of orbits = 6 Total number of facets = 10464

1. Inequality 1 with incidence 192 and stabilizer of size 256. Orbit size is 48 nature: 3-cycle inequality, C=[1, 2, 9] F=[1, 2]

(1,2): -1	(1,4):0	(1,5):0	(1,9):1	(2,3):0	(2,6):0
(2,9):1	(3,4):0	(3,7):0	(3,9):0	(4,8):0	(4,9):0
(5,6):0	(5,8):0	(5,9):0	(6,7):0	(6,9):0	(7,8):0
(7,9):0	(8,9):0				

2. Inequality 2 with incidence 128 and stabilizer of size 256. Orbit size is 48 nature: 4-cycle inequality, C=[1, 2, 3, 4] F=[1, 2]

(1,2): -1	(1,4):1	(1,5):0	(1,9):0	(2,3):1	(2,6):0
(2,9):0	(3,4):1	(3,7):0	(3,9):0	(4,8):0	(4,9):0
(5,6):0	(5,8):0	(5,9):0	(6,7):0	(6,9):0	(7,8):0
(7,9):0					

3. Inequality 3 with incidence 52 and stabilizer of size 12. Orbit size is 1024 nature: unknown

```
(1,2): -1
          (1,4):1
                    (1,5):1
                              (1,9):-1
                                         (2,3):1
                                                    (2,6):0
                              (3,9):-1
(2,9):0
                                                    (4,9):1
          (3,4):1
                    (3,7):1
                                         (4,8):-1
(5,6):0
          (5,8):1
                    (5,9):0
                              (6,7):0
                                         (6,9):0
                                                    (7,8):1
(7,9):0
          (8,9):1
```

4. Inequality 4 with incidence 48 and stabilizer of size 96. Orbit size is 128 nature: 6-cycle inequality, C=[2, 3, 4, 8, 5, 6] F=[2, 3]

```
(1,2):0
         (1,4):0
                   (1,5):0
                             (1,9):0
                                       (2,3):-1
                                                 (2,6):1
(2,9):0
                             (3,9):0
                                       (4,8):1
                                                 (4,9):0
         (3,4):1
                   (3,7):0
(5,6):1
         (5,8):1
                   (5,9):0
                             (6,7):0
                                       (6,9):0
                                                 (7,8):0
(7,9):0
         (8,9):0
```

5. Inequality 5 with incidence 34 and stabilizer of size 4. Orbit size is 3072 nature: unknown

```
(1,2):-1
           (1,4):1
                      (1,5):1
                                (1,9):-1
                                           (2,3):1
                                                      (2,6):1
(2,9):-1
           (3,4):1
                                           (4,8):2
                                                      (4,9):0
                     (3,7):-1
                                 (3,9):1
(5,6):1
           (5,8):-1
                     (5,9):1
                                 (6,7):1
                                           (6,9):-1
                                                      (7,8):1
(7,9):1
           (8,9):0
```

6. Inequality 6 with incidence 32 and stabilizer of size 2. Orbit size is 6144 nature: unknown

```
(1,2): -1
          (1,4):1
                    (1,5):1
                              (1,9):-1
                                         (2,3):0
                                                    (2,6):1
                                                    (4,9):0
(2,9):0
          (3,4):1
                    (3,7):1
                              (3,9):0
                                         (4,8):0
                              (6,7):1
                    (5,9):1
                                         (6,9):-1
                                                   (7,8):-1
(5,6):1
          (5,8):1
(7,9):1
          (8,9):0
```