Number of vertices n = 9. Adjacencies of Graph

- 1. vertex 1 adjacent to 2 3 4 5 6 7 8 9
- 2. vertex 2 adjacent to 1 5 6 7 8 9
- 3. vertex 3 adjacent to 1 5 6 7 8 9
- 4. vertex 4 adjacent to 1 5 6 7 8 9
- 5. vertex 5 adjacent to 1 2 3 4
- 6. vertex 6 adjacent to 1 2 3 4
- 7. vertex 7 adjacent to 1 2 3 4
- 8. vertex 8 adjacent to 1 2 3 4
- 9. vertex 9 adjacent to 1 2 3 4

Size of automorphism group of the graph=720

Full group: |Aut(polytope)| = 184320

Restricted group: $|Aut(G) \times switch| = 184320$

Number of orbits for the full group: 7

List of orbits of facets for the full group: Total number of orbits = 7 Total number of facets = 71340

1. Inequality 1 with incidence 192 and stabilizer of size 3072. Orbit size is 60 nature: 3-cycle inequality, C=[1, 4, 9] F=[1, 4]

```
(1,2):0
         (1,3):0
                   (1,4):-1
                              (1,5):0
                                       (1,6):0
                                                 (1,7):0
(1,8):0
                             (2,6):0
                                                 (2,8):0
         (1,9):1
                   (2,5):0
                                       (2,7):0
(2,9):0
         (3,5):0
                   (3,6):0
                             (3,7):0
                                       (3,8):0
                                                 (3,9):0
         (4,6):0
(4,5):0
                   (4,7):0
                             (4,8):0
                                       (4,9):1
```

2. Inequality 2 with incidence 128 and stabilizer of size 768. Orbit size is 240 nature: 4-cycle inequality, C=[4, 5, 2, 9] F=[4, 5]

(1,2):0	(1,3):0	(1,4):0	(1,5):0	(1,6):0	(1,7):0
(1,8):0	(1,9):0	(2,5):1	(2,6):0	(2,7):0	(2,8):0
(2,9):1	(3,5):0	(3,6):0	(3,7):0	(3,8):0	(3,9):0
(4,5): -1	(4,6):0	(4,7):0	(4,8):0	(4,9):1	

3. Inequality 3 with incidence 80 and stabilizer of size 32. Orbit size is 5760 nature: unknown

```
(1,7):1
(1,2):0
          (1,3):1
                    (1,4):-1
                               (1,5):0
                                          (1,6):1
(1,8):0
          (1,9):0
                    (2,5):0
                               (2,6):1
                                                    (2,8):0
                                         (2,7):-1
(2,9):0
          (3,5):0
                    (3,6): -1
                               (3,7):-1
                                          (3,8):1
                                                    (3,9):0
(4,5):0
          (4,6):1
                    (4,7):1
                               (4,8):1
                                          (4,9):0
```

4. Inequality 4 with incidence 52 and stabilizer of size 12. Orbit size is 15360 nature: unknown

```
(1,3):1
                               (1,5):0
                                          (1,6):0
                                                    (1,7):0
(1,2):1
                     (1,4):1
                                                    (2,8):1
(1,8):-1
          (1,9):0
                     (2,5):0
                               (2,6):-1
                                          (2,7):0
(2,9):-1
          (3,5):1
                    (3,6):1
                               (3,7):0
                                         (3,8):1
                                                    (3,9):0
(4,5): -1
          (4,6):0
                     (4,7):0
                               (4,8):1
                                          (4,9):1
```

5. Inequality 5 with incidence 48 and stabilizer of size 8. Orbit size is 23040 nature: unknown

```
(1,2):0
          (1,3):0
                    (1,4):0
                               (1,5):0
                                         (1,6):1
                                                   (1,7):-1
(1,8):0
          (1,9):0
                    (2,5):1
                              (2,6):1
                                        (2,7):1
                                                   (2,8):0
                                        (3,8):0
(2,9):-1
          (3,5):1
                    (3,6):1
                              (3,7):1
                                                   (3,9):1
(4,5): -2
          (4,6):1
                    (4,7):1
                              (4,8):0
                                         (4,9):0
```

6. Inequality 6 with incidence 48 and stabilizer of size 16. Orbit size is 11520 nature: unknown

```
(1,7):1
(1,2):0
           (1,3):2
                     (1,4):0
                                (1,5):0
                                           (1,6):-1
(1,8): -1
          (1,9):-1
                     (2,5):0
                                (2,6):1
                                           (2,7):1
                                                     (2,8):1
(2,9):-1
           (3,5):0
                     (3,6):1
                                (3,7):-1
                                           (3,8):1
                                                     (3,9):1
(4,5):0
           (4,6):1
                     (4,7):1
                               (4,8): -1
                                           (4,9):1
```

7. Inequality 7 with incidence 40 and stabilizer of size 12. Orbit size is 15360 nature: unknown

```
(1,2):0
           (1,3):0
                     (1,4):0
                                (1,5):1
                                          (1,6):1
                                                     (1,7):0
(1,8):0
           (1,9):0
                     (2,5):1
                                (2,6): -1
                                          (2,7):0
                                                     (2,8):1
(2,9):-1
          (3,5): -1
                     (3,6):1
                                (3,7):1
                                          (3,8):1
                                                     (3,9):0
                                (4,8):0
(4,5):1
           (4,6): -1
                     (4,7):1
                                          (4,9):1
```