Number of vertices n = 7. Adjacencies of Graph

- 1. vertex 1 adjacent to 2 5 6 7
- 2. vertex 2 adjacent to 1 3 6 7
- 3. vertex 3 adjacent to 2 4 6 7
- 4. vertex 4 adjacent to 3 5 6 7
- 5. vertex 5 adjacent to 1 4 6 7
- 6. vertex 6 adjacent to 1 2 3 4 5 7
- 7. vertex 7 adjacent to 1 2 3 4 5 6

Size of automorphism group of the graph=20

Full group: |Aut(polytope)| = 1280

Restricted group: $|Aut(G) \times switch| = 1280$

Number of orbits for the full group: 6

List of orbits of facets for the full group: Total number of orbits = 6 Total number of facets = 780

1. Inequality 1 with incidence 48 and stabilizer of size 32. Orbit size is 40 nature: 3-cycle inequality, C=[2, 7, 1] F=[2, 7]

```
(1,2):1
          (1,5):0
                    (1,6):0
                              (1,7):1
                                        (2,3):0
                                                  (2,6):0
(2,7):-1
          (3,4):0
                    (3,6):0
                              (3,7):0
                                       (4,5):0
                                                  (4,6):0
(4,7):0
          (5,6):0
                    (5,7):0
                              (6,7):0
```

2. Inequality 2 with incidence 48 and stabilizer of size 64. Orbit size is 20 nature: 3-cycle inequality, C=[1, 6, 7] F=[1, 6]

```
(1,7):1
(1,2):0
         (1,5):0
                   (1,6): -1
                                        (2,3):0
                                                  (2,6):0
(2,7):0
         (3,4):0
                   (3,6):0
                              (3,7):0
                                        (4,5):0
                                                  (4,6):0
(4,7):0
         (5,6):0
                    (5,7):0
                              (6,7):1
```

3. Inequality 3 with incidence 21 and stabilizer of size 20. Orbit size is 64 nature: Hypermetric, b=[1, -1, 1, -1, -1, 1, 1]

```
(1,2):1
          (1,5):1
                    (1,6): -1
                               (1,7):-1
                                          (2,3):1
                                                     (2,6):1
(2,7):1
          (3,4):1
                    (3,6): -1
                               (3,7):-1
                                          (4,5): -1
                                                     (4,6):1
(4,7):1
          (5,6):1
                    (5,7):1
                               (6,7):-1
```

4. Inequality 4 with incidence 20 and stabilizer of size 80. Orbit size is 16 nature: 5-cycle inequality, C=[4, 5, 1, 2, 3] F=[4, 5]

```
(1,5):1
                   (1,6):0
                             (1,7):0
                                       (2,3):1
                                                  (2,6):0
(1,2):1
(2,7):0
         (3,4):1
                   (3,6):0
                             (3,7):0
                                       (4,5): -1
                                                  (4,6):0
(4,7):0
         (5,6):0
                   (5,7):0
                             (6,7):0
```

5. Inequality 5 with incidence 19 and stabilizer of size 4. Orbit size is 320 nature: unknown

```
(1,2):1
          (1,5): -1
                                (1,7):1
                                           (2,3):1
                                                     (2,6):0
                     (1,6): -1
(2,7):0
          (3,4):1
                     (3,6):1
                                (3,7):-1
                                                     (4,6): -1
                                          (4,5):1
(4,7):1
          (5,6):0
                     (5,7):0
                                (6,7):1
```

6. Inequality 6 with incidence 18 and stabilizer of size 4. Orbit size is 320 nature: unknown

```
(2,3):1
                                                    (2,6):0
(1,2):1
          (1,5): -1
                     (1,6): -1
                                (1,7):1
(2,7):0
           (3,4):1
                      (3,6):0
                                (3,7):0
                                          (4,5):1
                                                    (4,6):1
(4,7):-1
          (5,6): -1
                     (5,7):1
                                (6,7):1
```