Number of vertices n = 8. Adjacencies of Graph

- 1. vertex 1 adjacent to 5 6 7 8
- 2. vertex 2 adjacent to 5 6 7 8
- 3. vertex 3 adjacent to 5 6 7 8
- 4. vertex 4 adjacent to 5 6 7 8
- 5. vertex 5 adjacent to 1 2 3 4 6 7 8
- 6. vertex 6 adjacent to 1 2 3 4 5 7 8
- 7. vertex 7 adjacent to 1 2 3 4 5 6 8
- 8. vertex 8 adjacent to 1 2 3 4 5 6 7

Size of automorphism group of the graph=576

Full group: |Aut(polytope)| = 73728

Restricted group:  $|Aut(G) \times switch| = 73728$ 

Number of orbits for the full group: 4

List of orbits of facets for the full group: Total number of orbits =4 Total number of facets =944

1. Inequality 1 with incidence 96 and stabilizer of size 768. Orbit size is 96 nature: 3-cycle inequality, C=[1, 5, 8] F=[1, 5]

(1,5): -1	(1,6):0	(1,7):0	(1,8):1	(2,5):0	(2,6):0
(2,7):0	(2,8):0	(3,5):0	(3,6):0	(3,7):0	(3,8):0
(4,5):0					
(5,8):1	(6,7):0	(6,8):0	(7,8):0		

2. Inequality 2 with incidence 96 and stabilizer of size 4608. Orbit size is 16 nature: 3-cycle inequality, C=[7, 8, 6] F=[7, 8]

(1,5):0	(1,6):0	(1,7):0	(1,8):0	(2,5):0	(2,6):0
(2,7):0	(2,8):0	(3,5):0	(3,6):0	(3,7):0	(3,8):0
(4,5):0	(4,6):0	(4,7):0	(4,8):0	(5,6):0	(5,7):0
(5,8):0	(6,7):1	(6,8):1	(7,8): -1		

3. Inequality 3 with incidence 80 and stabilizer of size 1152. Orbit size is 64 nature: Hypermetric, b=[0, -1, 0, 0, -1, 1, 1, 1]

```
(1,7):0
                                                   (2,6):1
(1,5):0
          (1,6):0
                               (1,8):0
                                         (2,5):-1
          (2,8):1
(2,7):1
                    (3,5):0
                               (3,6):0
                                         (3,7):0
                                                   (3,8):0
(4,5):0
          (4,6):0
                                         (5,6):1
                                                   (5,7):1
                    (4,7):0
                               (4,8):0
(5,8):1
         (6,7):-1
                              (7,8):-1
                    (6,8): -1
```

4. Inequality 4 with incidence 56 and stabilizer of size 96. Orbit size is 768 nature: unknown

(1,5): -1	(1,6):1	(1,7):1	(1,8):1	(2,5):1	(2,6):1
(2,7):1					
(4,5):0	(4,6):0	(4,7):0	(4,8):0	(5,6):0	(5,7):0
(5,8):0	(6,7):-1	(6,8): -1	(7,8): -1		