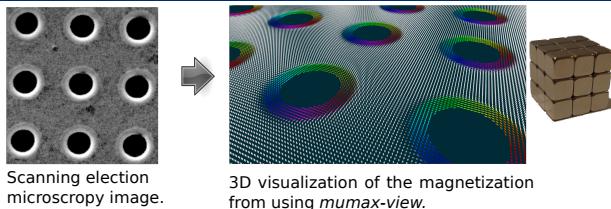


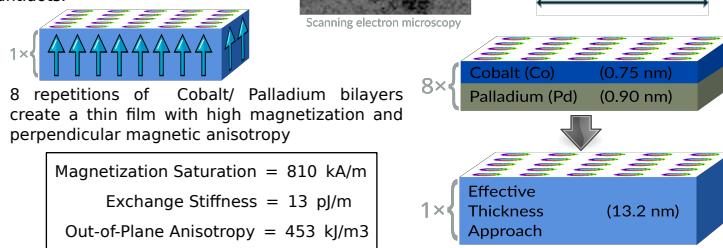
We numerically investigate spin-wave dynamics in a Co/Pd multilayer antidot lattice with reduced perpendicular magnetic anisotropy at the antidot edges. This structure forms a magnonic crystal with periodic magnetization, featuring out-of-plane magnetized bulk and in-plane magnetized rims. Our results show distinct spin-wave behaviors under varying magnetic fields, revealing complex spectra and mode hybridizations. Strong magnon-magnon coupling, driven by exchange interactions, occurs between the fundamental bulk mode and second-order radial rim modes. This study highlights the role of exchange interactions in achieving strong mode coupling through structural patterning and non-collinear magnetization.

## A multilayered thin film in Amumax

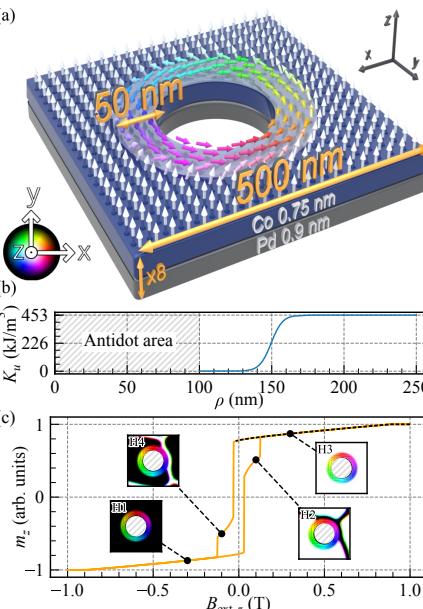
The thin film we study are based on samples studied by the group of Prof. Barman.



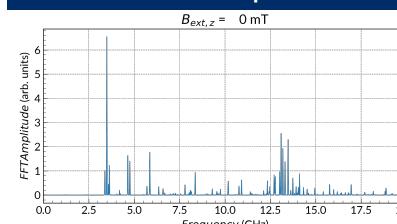
During the making of the antidots with  $\text{Ga}^+$  bombarding, a small crater is created around the antidot and gallium ions are entering the magnetic layers, changing the initial magnetic properties of the thin film in the rim around the antidots.



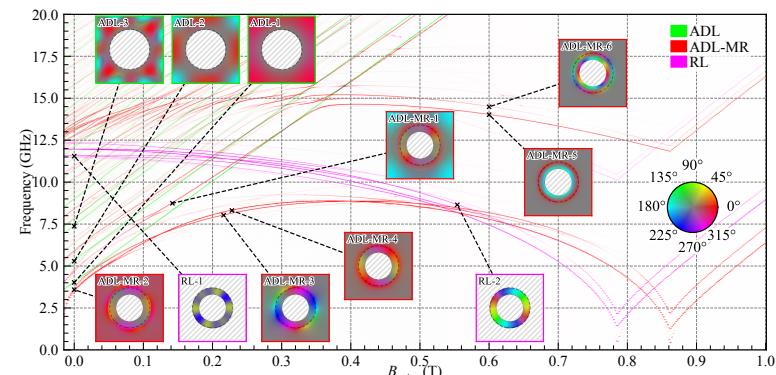
## Hysteresis



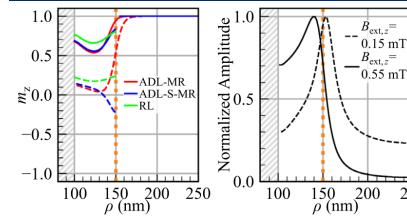
## Spin wave spectrum



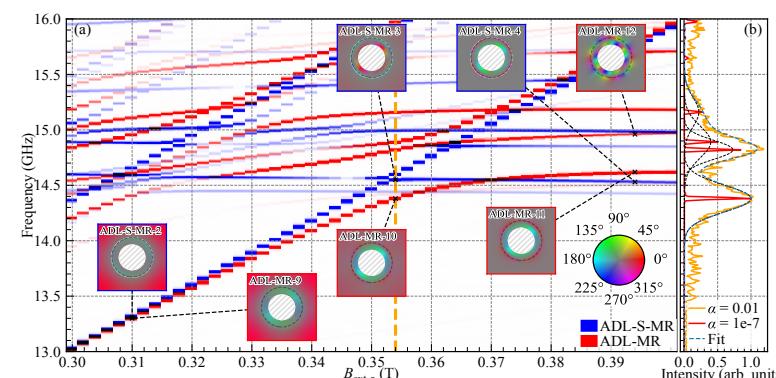
## Increasing the external field



## Cross-section



## Hybridization



## Cooperativity

$$C = \frac{g^2}{\kappa_{flow} \times \kappa_{high}} = 4.698.$$

Even though the system was not optimized for it, this value of the cooperativity indicates a strong magnon-magnon coupling in the ADL-MR between the second-order radial, first-order azimuthal rim mode and the fundamental bulk ADL mode.

In the context presented, the coupling between rim and bulk modes in the ADL-MR system based on PMA material, as demonstrated above, explores a new type of rather strong dynamic coupling between planar regions of non-collinear magnetization, which is mainly mediated by exchange interactions and turns on a higher-order azimuthal mode. The influence of the lattice type, as indicated by the hybridization selection rules, suggests a possibility for further optimization of the coupling strength, not only by changing the material but also by changing the geometry of the ADL.

## Acknowledgement

The research has received funding from the National Science Centre of Poland, Grant No. UMO-2020/37/B/ST3/03936 and 2023/49/N/ST3/03538. The simulations were partially performed at the Poznań Supercomputing and Networking Center (Grant No. 398).