Exercise Sheet 1

To be discussed on March 8, 2022.

In order to obtain points for the exam admission:

Please hand in your solutions to the exercises marked with a "\neq" symbol until March 7, 2022, 12:00 (by email to michael.vock@stat.unibe.ch).

Exercise 1: Oats example

In Section 1.6 of Pinheiro & Bates, the Oats data are presented, and several models with random effects at two levels are fitted.

(a) Try to reproduce the steps of the modeling process using the nlme package in R (until the top of page 50).

Notes:

• If, instead of using the groupedData object Oats, you prefer to work with an ordinary data frame (as in the examples in the lecture), you can use the following code to create it:

```
oats.df <- data.frame(Oats)
oats.df$Block <- factor(as.character(oats.df$Block))</pre>
```

- In the book, the function update is used to fit a new model (with some parts of the model specification changed) based on a model that has already been fitted. You can also call the lme function with all necessary specifications each time.
- For the fixed-effects parameters for Variety, you will probably obtain estimates that are different from those in the book, since R uses a different parametrization by default.
- (b) Represent the model fm40ats in the notation used in (P&B 2.2): Specify X_{ij} , $Z_{i,j}$, Z_{ij} , Ψ_1 , and Ψ_2 . (Please try yourself first and only consult p. 61 of Pinheiro & Bates afterwards for verifying your solution...)
- (c) Provide an equivalent model specification with only one level of random effects. $1 \triangleleft$

Exercise 2: Machines example – covariance structures

In Examples 2.4 and 2.9 in the lecture notes, three mixed-effects models for the Machines data are presented.

Let y_i be the vector of all productivity scores for worker i (as specified in Example 2.4).

- (a) What is the shape of the variance/covariance matrix $Var(\boldsymbol{y}_i)$ for the model underlying machines.lme.1? In particular: Which entries are equal?
- (b) What is the shape of $Var(y_i)$ for machines.lme.2?
- (c) What is the shape of $Var(y_i)$ for machines.lme.3?