

# Optimization Methods in Machine Learning

## Homework Assignment 2

Code and solve the tasks from the Jupyter notebook and submit a .ipynb file. Solve Problem 2 and Problem 3 in LaTeX format and submit a PDF file before the deadlines.

Soft Deadline: +1 week after the release date: 14 Nov 2024, 23:59

Hard Deadline: +2 weeks after the release date (but with a 25% penalty in points): 21 Nov 2024, 23:59

### Problem 1

Solve the problems and run experiments from the Jupyter notebook. [8 points]

### Problem 2

Consider Lemma 12 from the lecture notes: Let  $f$  be a differentiable,  $L$ -smooth function. Then

$$f(x) \leq \underbrace{f(y) + \langle \nabla f(y), x - y \rangle + \frac{L}{2} \|x - y\|^2}_{g(x)}.$$

for all  $x, y \in \mathbb{R}^d$ . Find the optimal  $x$  that minimizes the upper bound  $g(x)$ . [2 points]

### Problem 3

Consider Theorem 21 and the corresponding proof from the lecture notes. How would the result change if, instead of  $L$ -smoothness (implies Lemma 12), the function  $f$  satisfies the inequality

$$f(x) \leq f(y) + \langle \nabla f(y), x - y \rangle + \frac{L}{2} \|x - y\|^2 + \delta$$

for all  $x, y \in \mathbb{R}^d$  and some  $\delta \geq 0$ ? (Theorem 21 is true when  $\delta = 0$ . What if  $\delta > 0$ ?) [2 points]