

A Floating-Point Standard for Balanced Ternary

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Balanced ternary is a base 3 number system, i.e. numbers in balanced ternary are written as a string of digits whose contributions to the number are scaled by powers of 3. However, rather than the usual 0, 1, and 2, the digits of balanced ternary are -1 , 0, and 1. -1 is usually written as T, as it looks like a 1 with a bar or negative sign on top. It can represent negative integers without the use of a negative sign, e.g. $T1 = (-1) \times 3 + 1 \times 1 = -2$.

In the early days of computers, this system was considered as an alternative to binary, and many balanced ternary computers were built, most notably the Setun in Russia in the early 1960s. A brief side-by-side comparison follows. First of all, since there is no real distinction between positive and negative integers, there is no need for additional circuits to handle each case. However, the same is also true for all modern binary computers thanks to the two's complement implementation of signed integers, which takes advantage of the fact that logic gates on a finite number of bits behaves like modular arithmetic. In two's complement, the larger half of what would be unsigned integers, e.g. 8 through 15 (inclusive) for 4-bit integers, are reassigned to negative numbers (-8 through -1 in this case). So in this Additionally, hardware that uses balanced ternary

Where I believe balanced ternary shines is in how it handles floating point numbers.

Float f comprised of exponent e (int) and significand s (-1.5 to 1.5)

If s starts with 1 or T, $f = 3^e \times s$ (normal)

Else if $e = e_{min}$ (all Ts), f is denormal (see formula for normal)

Else, $f = sNaN$, $qNaN$, or $\pm\infty$ (TBD when operations are implemented)

Example with 1 trit for e and 2 trits for s :

Memory	TTT	TT0	TT1	T0T	T00	T01	T1T	T10	T11
Formula	$10^T \times T.T$	$10^T \times T.0$	$10^T \times T.1$	$10^T \times 0.T$	$10^T \times 0.0$	$10^T \times 0.1$	$10^T \times 1.T$	$10^T \times 1.0$	$10^T \times 1.1$
Result	.TT	.T0	.T1	.0T	.00	.01	.1T	.10	.11
Decimal	$-4/9$	$-1/3$	$-2/9$	$-1/9$	0	$1/9$	$2/9$	$1/3$	$4/9$
Memory	0TT	0T0	0T1	00T	000	001	01T	010	011
Formula	$10^0 \times T.T$	$10^0 \times T.0$	$10^0 \times T.1$?	?	?	$10^0 \times 1.T$	$10^0 \times 1.0$	$10^0 \times 1.1$
Result	T.T	T.0	T.1	?	?	?	1.T	1.0	1.1
Decimal	$-4/3$	-1	$-2/3$?	?	?	$2/3$	1	$4/3$
Memory	1TT	1T0	1T1	10T	100	101	11T	110	111
Formula	$10^1 \times T.T$	$10^1 \times T.0$	$10^1 \times T.1$?	?	?	$10^1 \times 1.T$	$10^1 \times 1.0$	$10^1 \times 1.1$
Result	TT.	T0.	T1.	?	?	?	1T.	10.	11.
Decimal	-4	-3	-2	?	?	?	2	3	4