## Irrational Rhythms

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One of the most fundamental features of Western music is rhythm, the spacing between notes in time that come in multiples (or fractions) of a fixed interval. A whole note divides into two half notes, which divide into two quarter notes each, which divide into eighth notes, etc.

			wh	ole			
half			half				
quarter		quarter		quarter		quarter	
eighth	eighth	eighth	eighth	eighth	eighth	eighth	eighth

This binary system carries many interesting properties that we often take for granted. For example, it is possible to speed up or slow down a melody by a factor of 2 just by changing the notation and keeping the tempo the same, so two copies of the same music at different speeds may be placed on the same score. This allows for so-called canons in augmentation or diminution. An instant in time may be given a "strength" based on how many binary subdivisions it takes to produce it: the start of a measure is stronger than the center of one, which is in turn stronger than the beats immediately to its left and right. (In 4/4 time, theis means that beat 1 is stronger than 3, which is stronger than 2 and 4).

The binary system of subdivision is often broken on a few specific scales, namely with time signatures which are not powers of 2 and with tuplets, which can in principle subdivide a time interval into any number of equally-spaced parts. However, all of these still fall within the realm of rational numbers: any piece of music using tuplets is based on some equally-spaced (isochronic) underlying beat of which all time intervals are a multiple.

- 0: length  $1 + \sqrt{2}$  (long), 1: length 1 (short), 2: length  $\sqrt{2}$  (medium)
- $0 \to 001, 1 \to 0$ : 1,0,001,0010010,001001001001001,... (a)
- $0 \to 010, 1 \to 0$ : 1, 0, 010, 0100010, 0100010010010010010, ... (d)
- $0 \to 100, 1 \to 0$ : 1, 0, 100, 0100100, 1000100100100100, ... (g)

Reverses: (a)-(g), (b)-(i), (c)-(h), (d)-(d), (e)-(f), (j)-(k)

(g) and (k) oscillate between 2 limit words, all others converge

(j) and (k) do not have maximally even spacing (MOS-like), all others do Personal favorite: (e) - derived from palindromic (d), long beat first (swing)