

Consignas de la actividad:

- 👉 Hallar la transferencia  $T = \frac{V_o}{V_i}$  en función de  $\omega_o$  y  $Q$ .
- 👉 Obtener el valor de los componentes del circuito de forma tal que  $\omega_o = 1$  y  $Q = 3$
- 👉 Ajustar el valor de  $R_1$  de forma tal que  $|T(0)| = 20$  dB.

Nodos:

$$\begin{aligned} & \bullet V_A \cdot (G_1 + sC + G_2 + G_3) - V_i \cdot G_1 - V_{o_1} (sC + G_2) - V_o \cdot G_3 = 0 \\ & \bullet V_B \cdot (G_3 + sC) - V_{o_1} \cdot G_3 - V_{o_3} \cdot (sC) = 0 \\ & \bullet V_C \cdot (Z \cdot G_4) - V_{o_3} \cdot G_4 - V_o \cdot G_4 = 0 \rightarrow \bullet V_{o_3} = -V_o \\ & \bullet V_A = V_B = V_C = 0 \\ & \bullet V_{o_1} \cdot G_3 = V_o \cdot sC \rightarrow V_{o_1} = V_o \cdot \frac{sC}{G_3} \\ & \bullet V_i \cdot G_1 = -V_o \cdot \frac{sC \cdot (sC + G_2)}{G_3} - V_o \cdot G_3 \end{aligned}$$

$$V_i \cdot G_1 = -V_o \cdot \left( \frac{s^2 C^2 + sC G_2 + G_3^2}{G_3} \right)$$

$$\frac{V_o}{V_i} = -\frac{G_1 \cdot G_3}{s^2 C^2 + sC G_2 + G_3^2}$$

$$\frac{V_o}{V_i} = - \frac{G_1 G_3}{C^2} \cdot \left( s^2 + s \frac{G_2}{C} + \frac{G_2^2}{C^2} \right)$$

$$\frac{V_o}{V_i} = - G_1 \cdot \frac{G_3}{C^2} \cdot \frac{G_3}{G_3} \cdot \frac{1}{s^2 + s \frac{G_2}{C} + \frac{G_2^2}{C^2}}$$

$\omega_o^2$

$\omega_o = G_3/C$

$$\boxed{\frac{V_o}{V_i} = - \frac{G_1}{G_3} \cdot \frac{\omega_o^2}{s^2 + s \frac{\omega_o}{Q} + \omega_o^2}}$$

- $\omega_o = \frac{G_3}{C}$
- $Q = \frac{G_2}{C} \rightarrow Q = \omega_o \cdot \frac{C}{G_2} = \frac{G_3}{G_2} \cdot \frac{C}{G_2}$
- $Q = \frac{G_3}{G_2}$

👉 Obtener el valor de los componentes del circuito de forma tal que  $\omega_o = 1$  y  $Q = 3$

$$\omega_o = 1 \Rightarrow G_3 = 1 [s] \quad C = 1 [F]$$

$$Q = 3 \Rightarrow Z = \frac{1 [s]}{G_2} \Rightarrow G_2 = \frac{1}{3} [s] \Rightarrow R_2 = 3 \Omega \quad R_3 = 1 \Omega$$

$C = 1 F$

👉 Ajustar el valor de  $R_1$  de forma tal que  $|T(0)| = 20 dB$ .

$$\left| T(s) \right|_{s=0} = - \frac{G_1}{G_3} \cdot \frac{\omega_o^2}{\omega_o^2} = G_1 = \left[ 20 dB \right]_{\text{Veces}} = 10$$

$$G_1 = 10 [s] \Rightarrow 10s[m, \Omega] = R_1$$

• +10 💎 Obtener los valores de la red normalizados en frecuencia e impedancia.

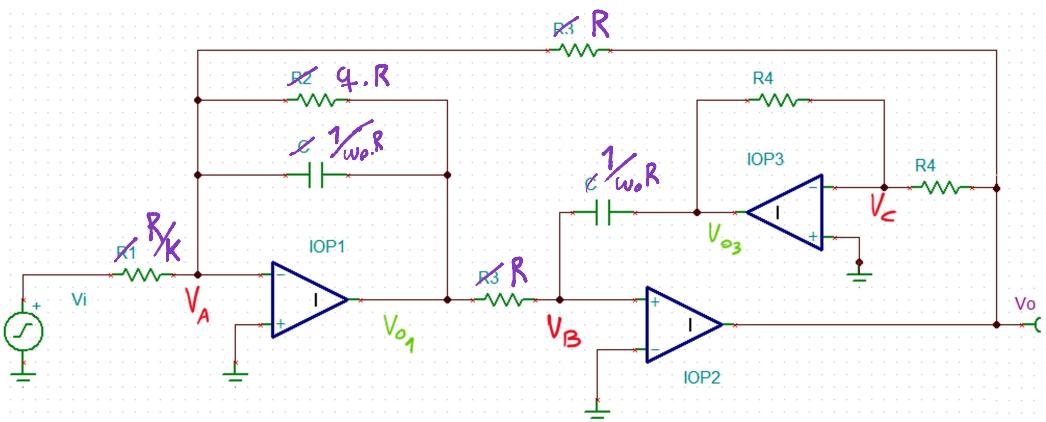
$$\boxed{\frac{V_o}{V_i} = - \frac{G_1}{G_3} \cdot \frac{\omega_o^2}{s^2 + s \frac{\omega_o}{Q} + \omega_o^2}}$$

$$\boxed{\omega_o = \frac{G_3}{C}}$$

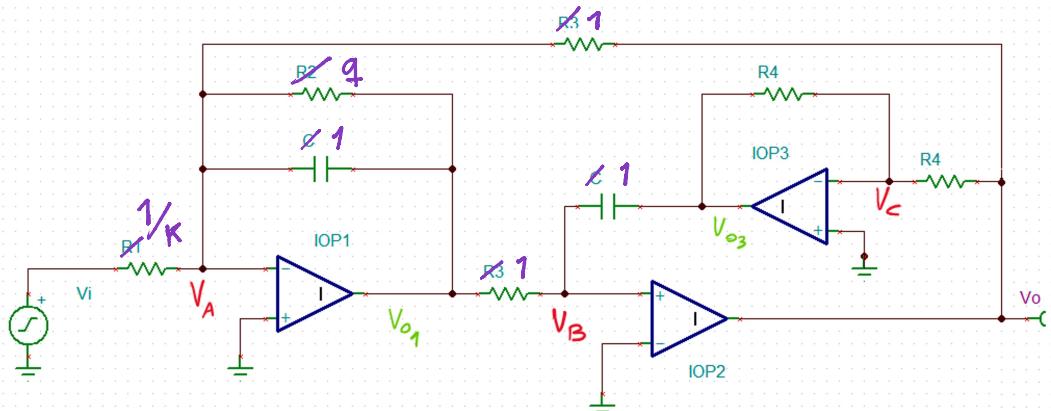
$$\boxed{Q = \frac{G_3}{G_2}}$$

Si fijamos  $G_3$  quedan componentes independientes para cada parámetro

$$\begin{aligned} R_3 &= R \\ \downarrow & R_2 = Q \cdot R \\ \downarrow & R_1 = R/K \\ \downarrow & C = 1/\omega_o \cdot R \end{aligned}$$



Normalizaciones  $\rightarrow R=1 \quad w_0=1$



- +10 Calcular las sensibilidades  $S_C^{w_0}, S_{R_2}^Q, S_{R_3}^Q$ .

$$S_C^{w_0} = \frac{C}{w_0(C)} \cdot \frac{\partial w_0(C)}{\partial C} = \frac{C}{C} \cdot \left( \checkmark_3 \left( -\frac{1}{C^2} \right) \right) = -1$$

$$S_{R_2}^Q = \frac{R_2}{Q(R_2, \dots)} \cdot \frac{\partial Q(R_2, \dots)}{\partial R_2} = \frac{\cancel{R_2}}{\frac{\cancel{R_2}}{\cancel{R_3}}} \cdot \frac{1}{\cancel{R_3}} = 1$$

$$S_{R_3}^Q = \frac{R_3}{R_2} \cdot R_2 \cdot \left( -\frac{1}{R_3} \right) = -1$$

$\rightarrow$  Todas Sensibilidades unitarias  $\rightarrow$  Lineales

$\rightarrow$  La proporción que varía a efecto es de 1  $\xrightarrow{\text{Variación}}$  Si  $R_2 = R_{2,\text{ideal}} \cdot 1,03$   
 $\Delta Q = Q_{\text{ideal}} \cdot 1,03$

- +20 🎉 Recalcular los valores de la red para que cumpla con una transferencia Butterworth.

$$T_{B_2}(s) = \frac{1}{s^2 + s \cdot \sqrt{2} + 1}$$

$\hookrightarrow \omega_0 = 1$   
 $\hookrightarrow \frac{\omega_0}{q} = \sqrt{2} \Rightarrow q = \frac{\sqrt{2}}{2}$

$$\rightarrow R_3 = 1 \rightarrow R_1 = \frac{1}{k} = 1 \Omega$$

$\hookrightarrow C = \frac{1}{\omega_0} = 1 F$   
 $\hookrightarrow R_2 = q = \frac{\sqrt{2}}{2} \Omega$

