EE5609 Assignment 2

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Abstract—This assignment involves finding the matrix X by solving the equation.

 $=2a^2b^2c^2(2) (2.0.2)$

$$=4a^2b^2c^2$$
 (2.0.3)

The python code solution can be downloaded from,

https://github.com/Vaibhav11002/EE5609/blob/master/Assignment_3/Codes/assignment_3.ipynb

1 Problem

Prove that,

$$\begin{vmatrix} a^{2} & bc & ac + c^{2} \\ a^{2} + ab & b^{2} & ac \\ ab & b^{2} + bc & c^{2} \end{vmatrix} = 4a^{2}b^{2}c^{2}$$

2 Solution

$$\begin{vmatrix} a^{2} & bc & ac + c^{2} \\ a^{2} + ab & b^{2} & ac \\ ab & b^{2} + bc & c^{2} \end{vmatrix}$$

$$\underset{R1 \leftarrow R1 + R2 + R3}{\overset{R1 \leftarrow R1 - R2}{2}} 2 \begin{vmatrix} a^{2} + ab & b^{2} + bc & ac + c^{2} \\ a^{2} + ab & b^{2} & ac \\ ab & b^{2} + bc & c^{2} \end{vmatrix}$$

$$\underset{C3 \leftarrow \frac{C3}{c}}{\overset{C3}{c}} 2 \begin{vmatrix} 0 & bc & c^{2} \\ a^{2} + ab & b^{2} & ac \\ ab & b^{2} + bc & c^{2} \end{vmatrix}$$

$$\underset{C3 \leftarrow \frac{C3}{c}}{\overset{C3}{c}} 2 abc \begin{vmatrix} 0 & c & c \\ a + b & b & a \\ b & b + c & c \end{vmatrix}$$

$$\underset{R3 \leftarrow R3 - R1}{\overset{R3 \leftarrow R3 - R1}{c}} 2 abc \begin{vmatrix} 0 & c & c \\ a + b & b & a \\ b & b & 0 \end{vmatrix}$$

$$\underset{R3 \leftarrow R2 - R3}{\overset{R3 \leftarrow R3 - R1}{c}} 2 abc \begin{vmatrix} 0 & c & c \\ a + b & b & a \\ b & b & 0 \end{vmatrix}$$

$$\underset{R3 \leftarrow R3 \leftarrow R3 - R1}{\overset{R3 \leftarrow R3 - R1}{c}} 2 abc \begin{vmatrix} 0 & c & c \\ a & 0 & a \\ b & b & 0 \end{vmatrix}$$