## 1

## EE5609 Assignment 2

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Abstract—This assignment involves finding the matrix X by solving the equation.

The python code solution can be downloaded from

https://github.com/Vaibhav11002/EE5609/blob/master/Assignment\_2/Codes/assignment\_2.py

1 Problem

Find **X** if  $\mathbf{Y} = \begin{pmatrix} 3 & 2 \\ 1 & 4 \end{pmatrix}$  and  $2\mathbf{X} + \mathbf{Y} = \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix}$ . Express  $2\mathbf{X} + \mathbf{Y} = \mathbf{AB}$ , where B is a block matrix comprising of **X** and **Y** and find the matrix **A**.

## 2 Solution

We have,

$$2\mathbf{X} + \mathbf{Y} = \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix}$$

$$\Rightarrow 2\mathbf{X} = \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix} - \mathbf{Y}$$

$$2\mathbf{X} = \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix} - \begin{pmatrix} 3 & 2 \\ 1 & 4 \end{pmatrix}$$

$$= \begin{pmatrix} -2 & -2 \\ -4 & -2 \end{pmatrix}$$

$$(2.0.1)$$

Now,

$$\mathbf{X} = \frac{1}{2} \begin{pmatrix} -2 & -2 \\ -4 & -2 \end{pmatrix}$$
 (2.0.4)  
=  $\begin{pmatrix} -2/2 & -2/2 \\ -4/2 & -2/2 \end{pmatrix}$   
=  $\begin{pmatrix} -1 & -1 \\ -2 & -1 \end{pmatrix}$  (2.0.5)

Thus from (2.0.5) we get,

$$\mathbf{X} = \begin{pmatrix} -1 & -1 \\ -2 & -1 \end{pmatrix}$$

From (2.0.1),

$$2X + Y = AB \tag{2.0.6}$$

$$= \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix} \tag{2.0.7}$$

Where B is a block matrix comprising X and Y. So,

$$\mathbf{B} = \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix} \tag{2.0.8}$$

Now,

$$\mathbf{AB} = \mathbf{A} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix}$$
$$= \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix} \tag{2.0.9}$$

Since **B** is a 4x2 matrix, **A** should be 2x4 so that the product **AB** is a 2x2 matrix.

Let A be a block matrix comprising of  $A_1$  and  $A_2$ .

$$\mathbf{A} = \begin{pmatrix} \mathbf{A_1} & \mathbf{A_2} \end{pmatrix} \tag{2.0.10}$$

Now,

$$\mathbf{AB} = \begin{pmatrix} \mathbf{A}_1 & \mathbf{A}_2 \end{pmatrix} \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \end{pmatrix}$$
$$= \mathbf{A}_1 \mathbf{X} + \mathbf{A}_2 \mathbf{Y} \qquad (2.0.11)$$

From (2.0.6) we get,

$$2X + Y = (2I)X + IY$$
$$= A_1X + A_2Y$$
(2.0.12)

Thus,  $A_1 = 2I$  and  $A_2 = I$ Hence we get the matrix,

$$\mathbf{A} = \begin{pmatrix} 2 & 0 & 1 & 0 \\ 0 & 2 & 0 & 1 \end{pmatrix}$$

So from (2.0.1) and (2.0.6),

$$\Rightarrow 2X + Y = AB$$

$$= \begin{pmatrix} 2 & 0 & 1 & 0 \\ 0 & 2 & 0 & 1 \end{pmatrix} \begin{pmatrix} -1 & -1 \\ -2 & -1 \\ 3 & 2 \\ 1 & 4 \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 \\ -3 & 2 \end{pmatrix} \qquad (2.0.13)$$