

Assignment 15

Matish Singh Tanwar

Abstract—This document solves a problem of Linear Algebra.

Download all latex-tikz codes from

https://github.com/Matish007/Matrix-Theory-EE5609-/tree/master/Assignment_15

1 PROBLEM

The row space of a 20×50 matrix \mathbf{A} has dimension 13. What is the dimension of the space of solution $\mathbf{Ax} = 0$?

- 1) 7
- 2) 13
- 3) 33
- 4) 37

2 SOLUTION

Options	Explanation
<p>7</p> <p>Given</p> <p>Rank Nullity Theorem</p>	<p>$A: \mathbf{R}^{50} \rightarrow \mathbf{R}^{20}$ is a linear transformation</p> <p>$\dim(\text{row space}(A)) = \text{rank}(A) = 13$</p> <p>$A: \mathbf{R}^{50} \rightarrow \mathbf{R}^{20}$ is a linear transformation then,</p> <p>$\text{rank}(A) + \text{nullity}(A) = 50$</p> <p>$13 + \text{nullity}(A) = 50$</p> <p>$\text{nullity}(A) = 37$</p> <p>$\dim(\text{space of solution}(A\mathbf{x} = 0)) = \text{nullity}(A) = 37$</p> <p>Hence, incorrect</p>
13	From above, it is obvious that it is incorrect
33	It is also incorrect.
37	From above it is correct

TABLE 1: Finding Correct Option