ECON 4360: Empirical Finance

Beta Representations

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Theory Lecture #12

What are we doing today?

• Beta Representations

Motivation: Empirical Work

- Beta Representations
 - Expected Return-Beta Representations will be seen as equivalent to a linear model for the discount factor

$$m = b'f$$

 We can derive models like the CAPM, ICAPM, and APT as factor models

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- We can derive models like the CAPM, ICAPM, and APT as factor models
 - Coming up: We will discuss what assumptions we need to express the discount factor as a linear function of factors f

Motivation: Empirical Work

- Mean-Variance Frontier
 - State-space representation provides useful framework; valid in infinite-dimensional payoff spaces
 - Many asset-pricing ideas and test statistics have interpretations in terms of the MV Frontier

Expected Return-Beta Representation

- The model:
 - Expected Return-Beta Representation of linear factor pricing models

$$E\left(R^{i}\right) = \gamma + \beta_{i,a}\lambda_{a} + \beta_{i,b}\lambda_{b} + \cdots, i = 1 \dots N$$

The general idea:

Expected Return-Beta Representation

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 - Explain the variation in average returns across assets due to each asset's exposure - as measured by the betas - to various risks, as priced by the lambdas.

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- The general idea:
 - Explain the variation in average returns across assets due to each asset's exposure - as measured by the betas - to various risks, as priced by the lambdas.
- But let's start simpler...

 Recall how our central asset pricing equation gets us to a basic pricing equation for returns

$$1=E\left[mR^{i}\right]$$

And recall how we can manipulate this expression to re-write it as

$$1 = E[mR^{i}]$$

$$1 = E(m)E(R^{i}) + cov(m, R^{i})$$

$$E(R^{i}) = R^{f} - R^{f}cov(m, R^{i})$$

$$E(R^{i}) = R^{f} + \left(\frac{cov(R^{i}, m)}{var(m)}\right)\left(-\frac{var(m)}{E(m)}\right)$$

Or, equivalently

$$E\left(R^{i}\right) = R^{f} + \beta_{i,m}\lambda_{m}$$

• Now we actually have a beta pricing model...

$$E\left(R^{i}\right) = R^{f} + \beta_{i,m}\lambda_{m}$$

• What does this equation tell us?

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- What does this equation tell us?
 - An expected return should be proportional to its beta i.e., the regression coefficient $\beta_{i,m}$ of an asset's return R^i on the discount factor m

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- Still confused?



• What can we tell from this equation?

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ullet First, recall that in the consumption-based model $m_{t+1}=etarac{u'(c_{t+1})}{u'(c_t)}$, so

$$-\frac{\textit{var}\left(m\right)}{\textit{E}\left(m\right)} \propto -\frac{\textit{u}'\left(c_{t}\right)}{\textit{u}'\left(c_{t+1}\right)}$$

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• Now - roughly - if consumption growth is high, $u'\left(c_{t+1}\right)$ is low and $u'\left(c_{t}\right)$ is high, so $-\frac{var\left(m\right)}{E\left(m\right)}$ is large and negative.

Second, from

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 - Assets that pay off well in good times (and pay off poorly in bad times) are therefore risky

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 - So with the large and negative covariance of these assets, they must have higher expected returns to compensate for the risk

Using

$$E(R^{i}) = R^{f} + \left(\frac{cov(R^{i}, m)}{var(m)}\right) \left(-\frac{var(m)}{E(m)}\right)$$

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 From the first equation, we've figured out that assets whose returns covary positively with the discount factor (consumption growth, if we are using the consumption-based model) must have higher expected returns as compensation for risk

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 - Now, we can think about/interpret λ_m as consumption growth

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 - And we can now think about the $\beta_{i,m}$'s as regression coefficients telling us whether returns for a particular asset are typically high in good times or high in bad times.

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 - And we can now think about the $\beta_{i,m}$'s as regression coefficients telling us whether returns for a particular asset are typically high in good times or high in bad times.
- What we can see now is that if we can find "proxies" for consumption growth (or, equivalently, good times/bad times), we will have a "linear factor model"!

 The first step is to use time-series data on assets to find the betas in a regression of returns on factors

$$R_t^i = a_i + \beta_{i,a} f_t^a + \beta_{i,b} f_t^b + \cdots \varepsilon_t^i, \ t = 1 \dots T$$

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- From this regression, we get estimates of the betas for each asset

From the Time-Series Regressions

• Now, from a multiple regression of returns on factors, what do we have?

$$R_t^i = \mathbf{a}_i + \mathbf{\beta}_{i,\mathbf{a}} f_t^{\mathbf{a}} + \mathbf{\beta}_{i,\mathbf{b}} f_t^{\mathbf{b}} + \cdots \mathbf{\epsilon}_t^i, \ t = 1 \dots T$$

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 - So now we have a set of $\{R_t^i\}_{t=1}^T$ and $(\beta_{i,a}, \beta_{i,b}, \ldots)$ for each $i=1\dots N$ asset

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- But what we really want to explain is how average returns vary across assets...
 - So let's use $\left\{R_t^i\right\}_{t=1}^T$ to construct $E\left(R^i\right)$ and see what we can do with that...

- Given what we have now, we can get back to
 - The model for an Expected Return-Beta Representation of linear factor pricing models

$$E\left(R^{i}\right) = \gamma + \beta_{i,a}\lambda_{a} + \beta_{i,b}\lambda_{b} + \cdots, i = 1 \dots N$$

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 - The lambdas λ (coefficients) and γ (intercept) are what are are estimating they are the same across assets

Expected Return-Beta Representation - Interpretations

From

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- For any asset i,
 - $\beta_{i,a}$ represents the amount of risk due to factor a (which depends on the asset)
 - λ_a represents the extra return per unit of (factor-specific) risk that investors demand (which is the same for all assets)
- Think about a one factor model. What should you get if you plotted expected returns vs. betas?

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 - ullet A straight line with y-intercept γ and slope λ .

Example with this Framework: CAPM

For the CAPM

$$E(R^{i}) = R^{f} + \beta_{i,m}\lambda_{m}, i = 1...N$$

$$R_{t}^{i} = a_{i} + \beta_{i,m}R_{t}^{m} + \varepsilon_{t}^{i}, t = 1...T$$

- The "factor" used in the CAPM is the return on the S&P 500, or some other market index.
- Interpretation: "For each unit of exposure $\beta_{i,m}$ to market risk, you must provide investors with an expected return premium of λ_m ."

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• Second, run a cross-section regression to see if expected returns are linearly related to the β 's:

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• Model Predictions: the pricing errors, α_i , should be small and statistically insignificant.

Special Cases: Risk-Free Rate

• If there is a risk-free rate, for

$$E\left(R^{f}\right) = \gamma + \beta_{i,a}\lambda_{a} + \beta_{i,b}\lambda_{b} + \cdots + \alpha_{i}$$

• All of its betas are zero, which implies

$$\gamma = R^f$$

- Where that gets us:
 - ullet We can estimate γ , or impose the condition that $\gamma=R^f$
 - ullet Here, γ is called the expected zero-beta rate

Special Cases: Using Excess Returns

ullet If we use excess returns, where $E\left(R^{ei}
ight)=E\left(R^{i}
ight)-E\left(R^{j}
ight)$

$$E(R^{ei}) = \beta_{i,a}\lambda_a + \beta_{i,b}\lambda_b + \cdots$$

- The intercept drops out.
- Note that if we use $E\left(R^{ei}\right) = E\left(R^{i}\right) E\left(R^{f}\right)$, we are talking about a model of equity risk premium.

Special Cases: Factors are Returns/Excess Returns

- If the factors themselves are returns, like $f = R^m$ for the CAPM, the model should apply to the factor as well.
- For example, if the factor is the market return in excess of the risk-free rate, $R_t^{em} = R_t^m R_t^f$
- Then the time-series regression is

$$\begin{array}{rcl} R_t^i & = & a_i + \beta_{i,a} f_t^a + \beta_{i,b} f_t^b + \cdots \varepsilon_t^i \\ R_t^{em} & = & \beta_{i,m} R_t^{em} + \beta_{i,b} f_t^b + \cdots \varepsilon_t^i \end{array}$$

- So $\beta_{i,m} = 1$ (the factor has a beta of one on itself) and all other betas are zero.
- And for the excess market return,

$$E(R^{em}) = (1) \lambda_m + (0) \lambda_b + \cdots$$

Special Cases: Factors are Returns/Excess Returns

ullet Now we can get that $\lambda_m=E\left(R^{em}
ight)=E\left(R^m-R^f
ight)$ and

$$E(R^{ei}) = \beta_{i,m}\lambda_m + (0)\lambda_b + \cdots$$
$$= \beta_{i,m}E(R^m - R^f)$$

Which is just the familiar CAPM

- ullet The betas eta cannot be asset-specific firm characteristics, such as firm size or book-to-market
- The betas measure the sensitivity of a firm's return to a macroeconomic factor common to all firms
 - E.g., the return on small firms minus the return on big firms (SMB)
 - E.g., the return on high book-to-market firms minus the return on low book-to-market firms (HML)
- What matters is how a firm behaves (the sensitivity to the factor)
 rather than what the firm characteristic is.

- The idea is that a market equilibrium wouldn't otherwise survive simple repacking schemes, e.g.
 - We know that returns on small firms are larger than returns on big firms. What if you could form a company that buys small firms and holds them? Your firm is large, so you pay a low return; but you earn a large return from your small constituent firms. You get to pocket the difference!
 - What is firms whose names that start with a 'Z' command a higher return than firms that start with 'A'. Can a firm increase its market value by changing its name from Zoologic to Alphalogic?
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- These schemes don't work because
 - The large company still behaves like a portfolio of small stocks
 - The firm that changed its name still behaves like the firm whose name started with a 'Z'.

- The idea is that a market equilibrium wouldn't otherwise survive simple repacking schemes, e.g.
 - We know that returns on small firms are larger than returns on big firms. What if you could form a company that buys small firms and holds them? Your firm is large, so you pay a low return; but you earn a large return from your small constituent firms. You get to pocket the difference!
 - What is firms whose names that start with a 'Z' command a higher return than firms that start with 'A'. Can a firm increase its market value by changing its name from Zoologic to Alphalogic?
- These schemes don't work because
 - The large company still behaves like a portfolio of small stocks
 - The firm that changed its name still behaves like the firm whose name started with a 'Z'.
- The idea is that betas are important, not characteristics: "Asset returns depend on how you behave, not on who you are"

End of Today's Lecture.

 That's all for today. Today's material corresponds roughly to parts of Chapter 5 in Cochrane (2005).