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Assignment 10 - Time Series

Please complete the following questions found in your textbook.

Question 9.2 (p.382-383)

$$\widehat{SALES_t} = 25.34 + 1.842 ADV_t + 3.802 ADV_{t-1} + 2.265 ADV_{t-2}$$

- a) It is a distributed lag model with 2 lags.
 Increasing 1 million in ADV will have a sustained effect of $(1.842 + 3.802 + 2.265)$ \$7.9MM.
 Impact is greatest at the 2nd week which is \$3.802 MM.

adv is impact multiplier = 1.842

adv + advt-1 is interim multiplier for 1 period = 5.644

adv + advt-1 + advt-2 is the interim multiplier for 2 periods = 7.909

adv + advt-1 + advt-2 is total multiplier for all period = 7.909

b)

	Estimate	var	T value	5% level Tc (0.95,101)	10 % level Tc(0.9,101)
adv	1.842	1.3946	1.559785201	1.645	1.282
adv(t-1)	3.802	2.1606	2.586574112	1.645	1.282
adv(t-2)	2.265	1.4214	1.899809481	1.645	1.282

Adv is significant at 10% level but not at 5% level

Adv(t-1) is significant at both 5% & 10% level

Adv (t-2) is significant at both 5% level and 10% level

c)

95% interval for impact multiplier

tc = 1.96

se = $\sqrt{1.3946}$

beta = 1.842

Lo = $\text{beta} - (1.96 * \text{se}) = -0.472$

Hi= $\text{beta} + (1.96 * \text{se}) = 4.15$

[-0.472 , 4.15]

95% interval for one period interim multiplier

tc = 1.96

se = $\sqrt{1.3946 + 2.1606 + 2 * (-1.0406) }$

beta = 1.842 + 3.802

Lo = $\text{beta} - (1.96 * \text{se}) = 3.263$

Hi= $\text{beta} + (1.96 * \text{se}) = 8.02$

[3.262 , 8.02]

95% interval for two period interim multiplier

$$t_c = 1.96$$

$$se = \sqrt{\text{var_ADV} + \text{var_ADV } t-1 + \text{var_ADVT-2} + 2 \text{cov(ADV, ADV } t-1) + 2\text{cov(ADV } t-1, \text{ADV } t-2) + 2(\text{ADV } t-2, \text{ADV})}$$

$$se = \sqrt{1.3946 + 2.1606 + 1.414 + 2 * (-1.0406) + 2 * (-1.0367) + 2 * (0.098)}$$

$$\text{beta} = 1.842 + 3.802 + 2.265$$

$$\text{Lo} = \text{beta} - (1.96 * se) \# 5.9386$$

$$\text{Hi} = \text{beta} + (1.96 * se) \# 9.8793$$

[5.938, 9.879]

Question 9.4 (p.383) - for part 9.4(b) please refer to equation 9.17 page 349

a)

t	1	2	3	4	5	6	7	8	9	10
e	0.28	-0.31	-0.09	0.03	-0.37	-0.17	-0.39	-0.03	0.03	1.02
e^2	0.0784	0.0961	0.0081	0.0009	0.1369	0.0289	0.1521	0.0009	0.0009	1.0404
et * t-1		-0.0868	0.0279	-0.0027	-0.0111	0.0629	0.0663	0.0117	-0.0009	0.0306
et*t-2			-0.0252	-0.0093	0.0333	-0.0051	0.1443	0.0051	-0.0117	-0.0306

r1	0.063423
r2	0.065302

b)

$$Z = \frac{r_k - 0}{\sqrt{1/T}} = \sqrt{T} r_k \sim N(0, 1) \quad (9.17)$$

Test significance thru T test at 5% level

H0: r1 = 0

r1 is not equal to 0

T = 10 and Z for r1 = 0.200

Critical value for z = 1.9 (from the table)

Since 1.9 >> 0.2 so we CANNOT reject the null

Test significance thru T test at 5% level

H0: r2 = 0

R2 is not equal to 0

T = 10 and Z for r2 = 0.206

Critical value for z = 1.9 (from the table)

Since 1.9 >> 0.206 so we CANNOT reject the null

Question 9.6 (p. 384) Note: in part (b) use only the correlogram

$$\widehat{DHOMES}_t = -2.077 - 53.51DIRATE_{t-1} \quad \text{obs} = 218$$

(se) (3.498) (16.98)

(part a)

1 % change in Interest rate that happened in previous month is estimated to decrease Home sale numbers by 53,510 homes in the current month.

95% confidence interval for DIRATE

Beta +/- se*tc tc = 1.96

$$-53.51 + 16.98(1.96) = -20.22$$

$$-53.51 - 16.98(1.96) = -86.79$$

$$[-86.79, -20.22]$$

B)

Use t test to see whether there is serial correlation present or not

Ho: B0 = 0 --- there is no serial correlation present

H1 B0 is not equal to 0 --- there is serial correlation present

Critical value of t = 1.96

$$t = b3/se(b3)$$

$$T \text{ value for } B3 = (-0.3306)/0.0649$$

$$T \text{ value for } B3 = -5.093$$

Since, |t| >> |tc|, the coefficient is significantly different from zero

We reject the null hypothesis and there could be serial correlation present in the model

(c) The model with AR(1) errors was estimated as

$$\widehat{DHOMES}_t = -2.124 - 58.61DIRATE_{t-1} \quad e_t = -0.3314e_{t-1} + \hat{v}_t$$

(se) (2.497) (14.10) (0.0649)

obs = 217

95% confidence interval

Beta +/- se*tc tc = 1.96

$$-58.61 + 14.10(1.96) = -30.974$$

$$-58.61 - 14.10(1.96) = -86.246$$

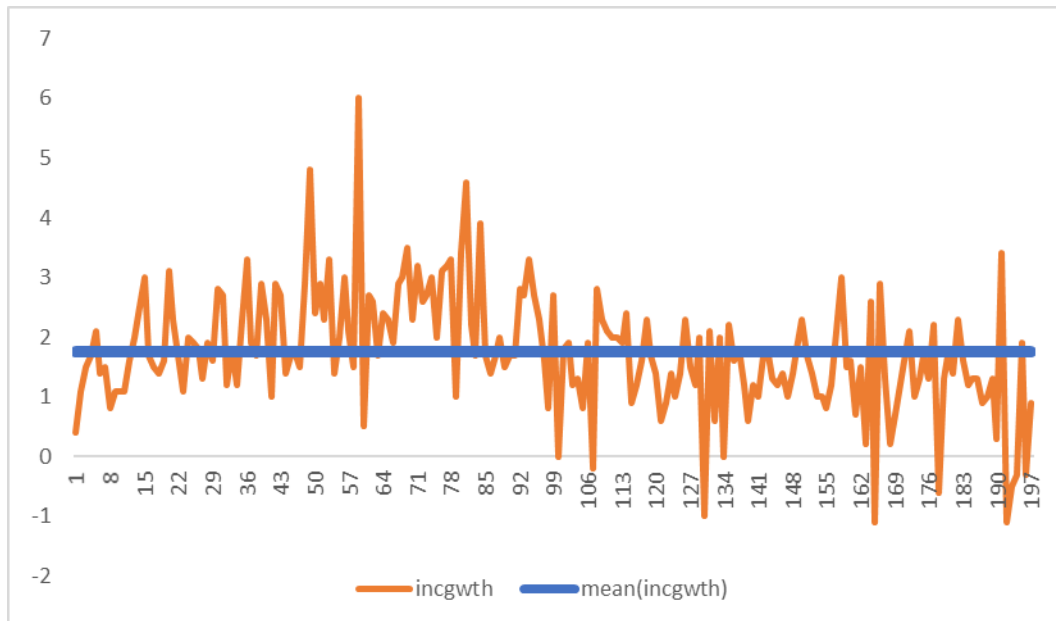
[-86.24 , -30.97]

After removing the autocorrelation error the confidence interval becomes smaller and more precise

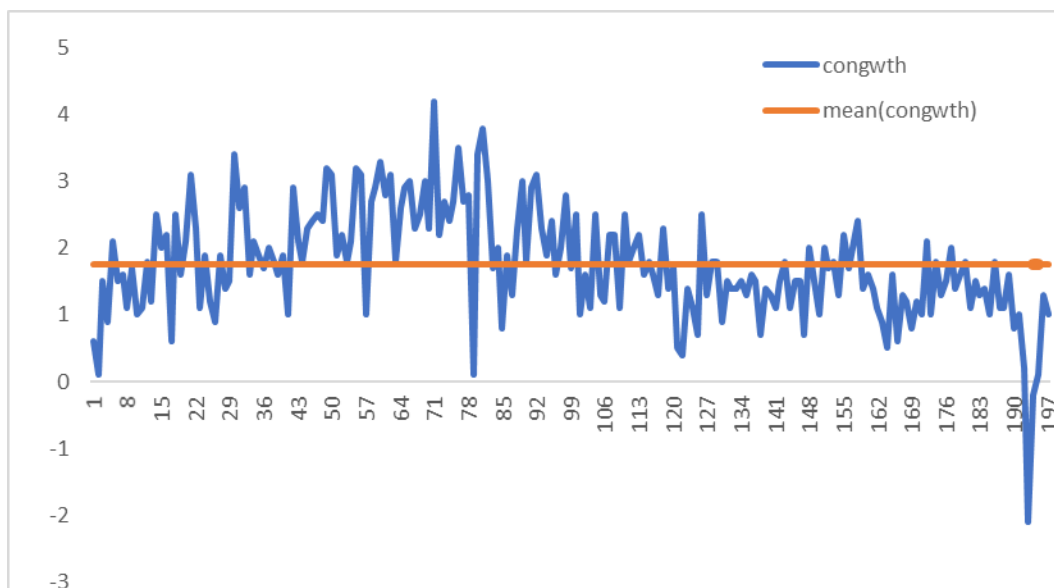
Question 9.22 (p.391-392) Note: in part (b) use only the correlogram

(part a)

INCGWTH VS Time(quarters)



CONGWTH VS Time(Quarters)



It is evident that both graphs are stationary as Mean mostly passes thru all quarters.

(part b)

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	0.97384	0.09961	9.776	<2e-16 ***
L(incgwth, 0)	0.44958	0.04967	9.052	<2e-16 ***

Estimate is significantly different from 0 for L(incgwth, 0)

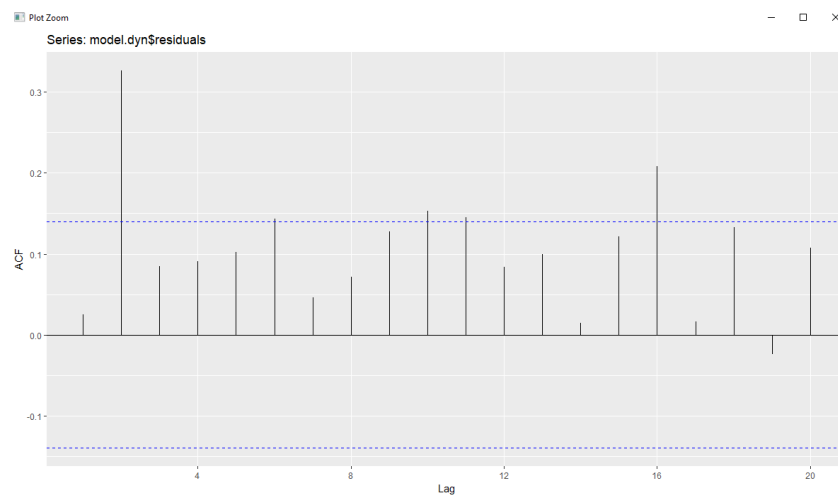
```
> AIC(model.dyn)
```

```
[1] 415.6031
```

```
> BIC(model.dyn)
```

```
[1] 425.4527
```

Increase of 1 unit in income growth is estimated to increase the consumption growth by 0.44 for the current month



At lag 2 there is significant serial correlation. There is also significant serial correlation at lag 16.

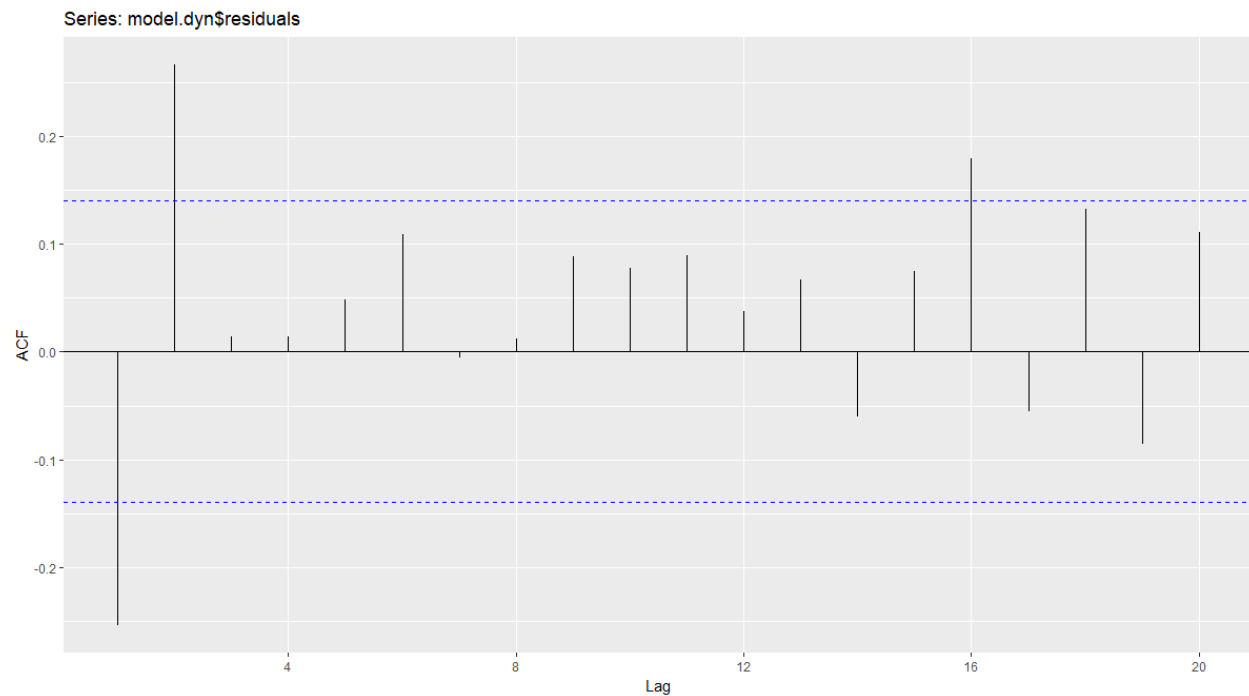
(part c)

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	0.67820	0.12083	5.613	6.84e-08 ***
L(congwth, 1)	0.26882	0.06413	4.192	4.22e-05 ***
L(incgwth, 0)	0.34953	0.05314	6.577	4.39e-10 ***

Estimate is significantly different from 0 for L(incgwth, 0) and L(congwth, 1)

```
> AIC(model.dyn)
[1] 398.7832
> BIC(model.dyn)
[1] 411.8957
```

AIC and BIC have decreased significantly indicating that this is better model



There is significant serial correlation at lag 1 and lag 2. Even though AIC and BIC have decreased but this model has significant serial correlation

(part d)

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	0.46074	0.12776	3.606	0.000397	***
L(congwth, 1)	0.14905	0.06600	2.258	0.025056	*
L(congwth, 2)	0.27521	0.06212	4.430	1.58e-05	***
L(incgwth, 0)	0.32065	0.05089	6.301	2.00e-09	***

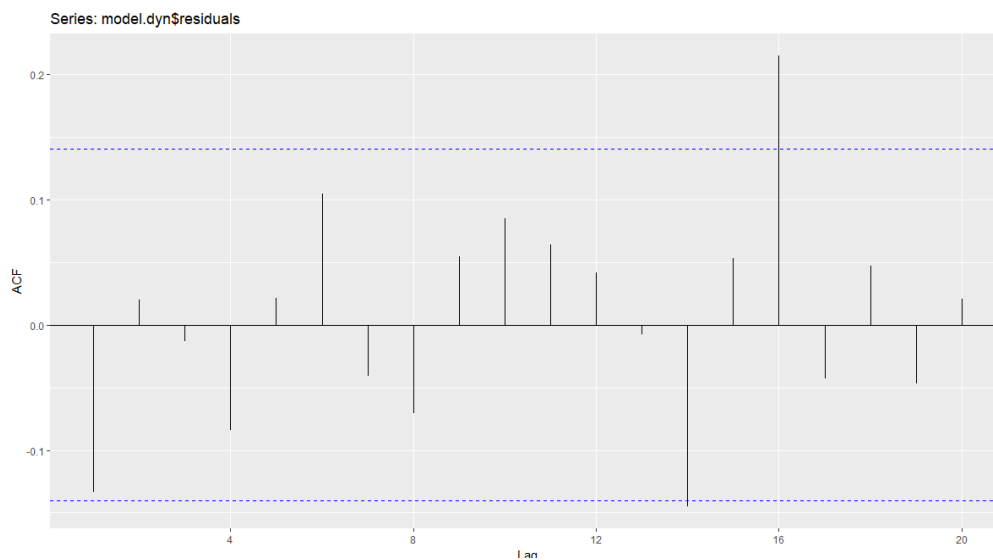
All estimates are significantly different from 0

```
> AIC(model.dyn)
```

```
[1] 377.7218
```

```
> BIC(model.dyn)
```

```
[1] 394.0868
```



There is no serial correlation in the early lags. There is SC present at lag 14 and 16 but it is irrelevant to this model.

This is a much better model because AIC and BIC values are lower and there is no serial correlation present in the lags that we are using.

(part e)

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	0.36501	0.12438	2.935	0.00375	**
L(congwth, 1)	0.01609	0.07044	0.228	0.81953	
L(congwth, 2)	0.20535	0.06169	3.329	0.00105	**
L(incgwth, 0)	0.34831	0.04916	7.085	2.64e-11	***
L(incgwth, 1)	0.23080	0.05398	4.276	3.01e-05	***

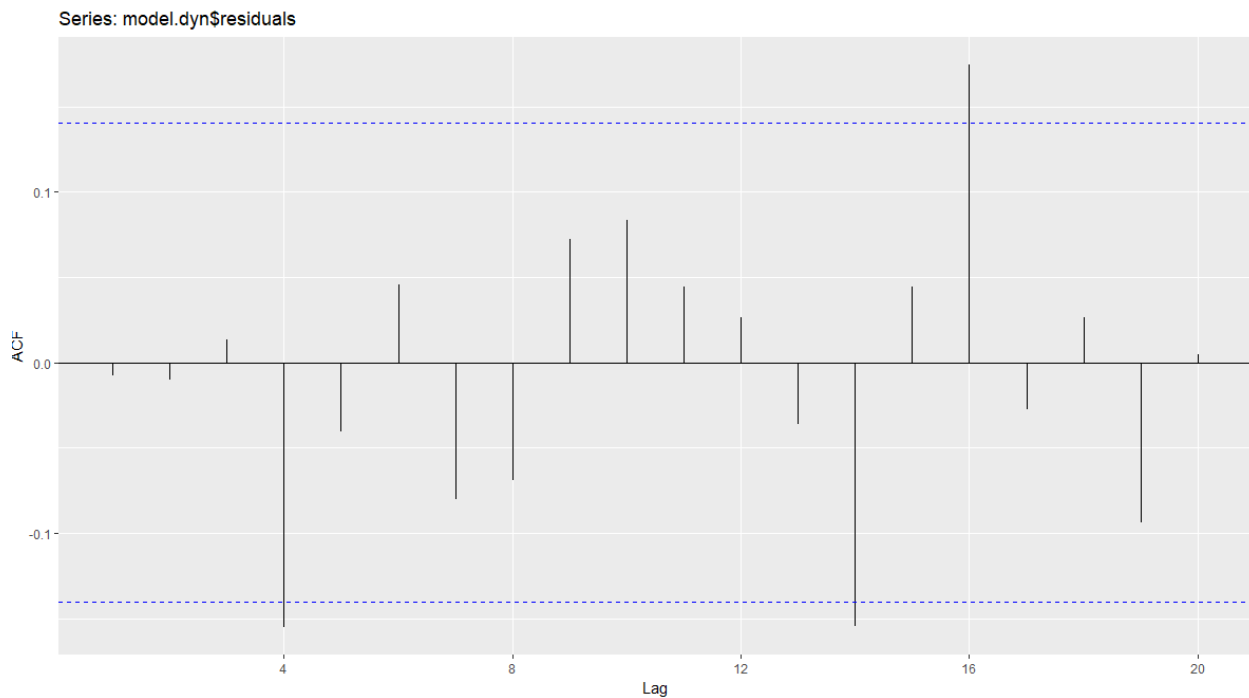
All estimates are significantly different from 0

```
> AIC(model.dyn)
```

```
[1] 361.8067
```

```
> BIC(model.dyn)
```

```
[1] 381.4447
```



No serial correlation present. This is a better model because AIC & BIC have gone further down.

More importantly serial correlation has decreased significantly in first 3 lags.

(part f)

Add $\text{congwth}(t-3)$ that is the 3rd lag

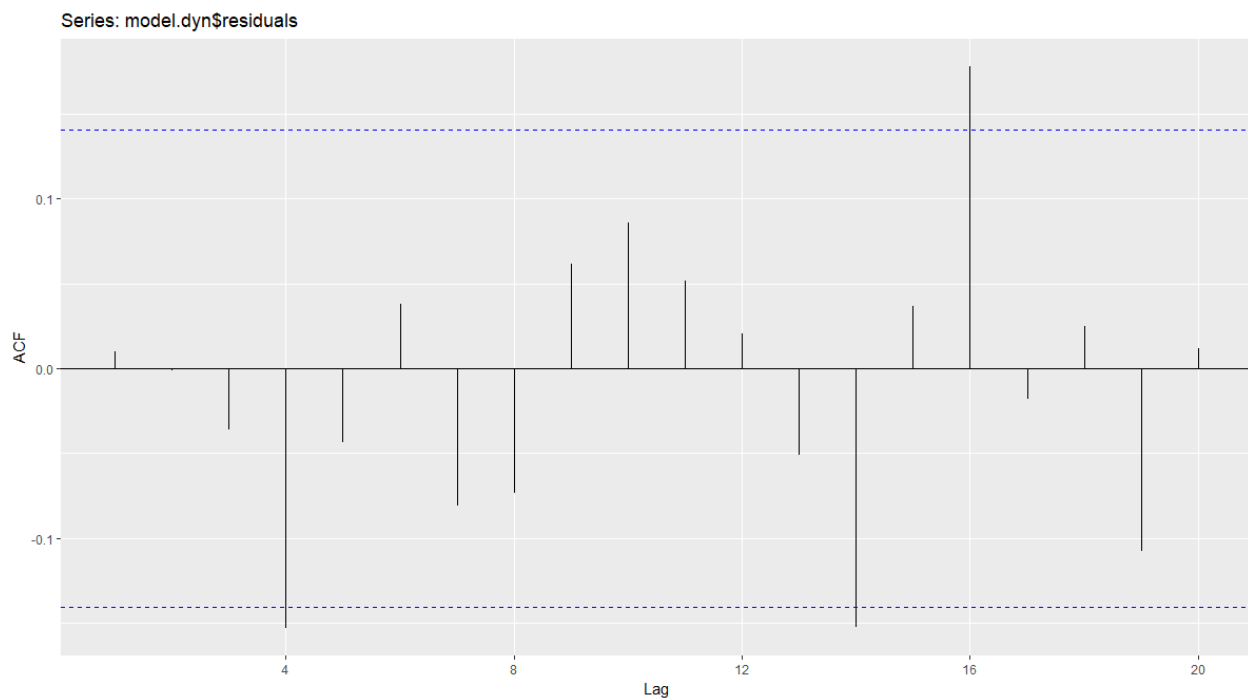
	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	0.331289	0.130596	2.537	0.01200	*
L(congwth, 1)	0.007871	0.073013	0.108	0.91426	
L(congwth, 2)	0.192861	0.064534	2.989	0.00318	**
L(congwth, 3)	0.050735	0.064904	0.782	0.43538	
L(incgwth, 0)	0.338155	0.050725	6.666	2.83e-10	***
L(incgwth, 1)	0.229157	0.054245	4.224	3.73e-05	***

```
> AIC(model.dyn)
```

```
[1] 362.2206
```

```
> BIC(model.dyn)
```

```
[1] 385.0956
```



Adding 3rd lag of congwth increases AIC and BIC. Also serial correlation has increased at lag 3 but it's still within bounds.

Based on aforementioned analysis it is better to not add $\text{congwth}(t-3)$ and leave model as in part (e)

(part g)

Coefficients:

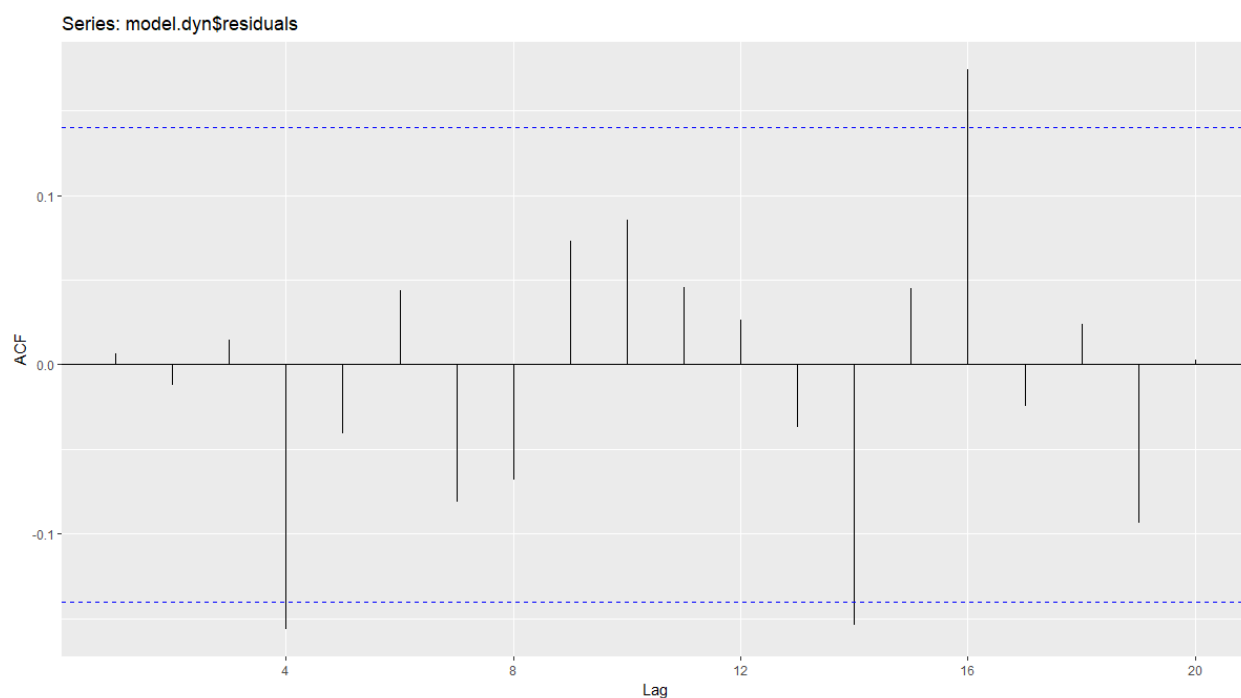
	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	0.37149	0.12080	3.075	0.002411	**
L(congwth, 2)	0.20828	0.06019	3.460	0.000666	***
L(incgwth, 0)	0.35244	0.04562	7.726	6.13e-13	***
L(incgwth, 1)	0.23624	0.04831	4.890	2.13e-06	***

```
> AIC(model.dyn)
```

```
[1] 359.8602
```

```
> BIC(model.dyn)
```

```
[1] 376.2252
```



AIC and BIC values are at their lowest. There is no sign of serial correlation in first 3 lags. However there is evidence of serial correlation at lag 4.

*****R STUDIO CODE FOR ABOVE QUESTIONS*****

QUESTION 9.2

```
rm(list=ls(all=TRUE))
```

```
library(multcomp)
```

```
library(data.table)
```

```
library(dplyr)
```

```
library(lmtest)
```

```
library(tseries)
```

```
library(dynlm)
```

```
context = fread('ex9.csv')
```

```
#table <- read.dta13("okun.dta")
```

```
#check.ts <- is.ts(table) # "is structured as time series?"
```

```
#okun.ts <- ts(table, start=c(1985,2), end=c(2009,3),frequency=4)
```

```
#okunL3.dyn <- dynlm(d(u)~L(g, 0:3), data=okun.ts) # g is explanotary variable and u is teh column we  
tryin to preict
```

```
#summary(okunL3.dyn)
```

```
table <- context
```

```
check.ts <- is.ts(table) # "is structured as time series?"
```

```
table.ts <- ts(table, start=c(2008,1),frequency=7)
```

```
check.ts <- is.ts(table.ts)
```

```
model.dyn <- dynlm(sales~L(adv, 0:2), data=table.ts) # g is explanatory variable and u is the column we
tryin to preict
```

```
summary(model.dyn)
```

```
apply(table.ts, MARGIN = 2, class)
```

```
## 95% interval for impact multiplier
```

```
# tc = 1.96
```

```
# sqrt of var(adv t) + var( adv t-1) + 2cov(advt , advt-1)
```

```
se = sqrt(1.3946)
```

```
beta = 1.842
```

```
Lo = beta-(1.96*se) # -0.472
```

```
Hi= beta+ (1.96*se) # 4.15
```

```
## 95% interval for one period interim multiplier
```

```
# tc = 1.96
```

```
se = sqrt(1.3946 + 2.1606 + 2 *(-1.0406) )
```

```
beta = 1.842 + 3.802
```

```
Lo = beta-(1.96*se) # 3.263
```

```
Hi= beta+ (1.96*se) # 8.02
```

```
## 95% interval for two period interim multiplier
```

```
# tc = 1.96
```

```
# = a2 + b2 + c2 + 2ab + 2bc + 2ca
```

```
# var. a + var b + var c + 2cov(a,b) + 2cov(b,c)+ 2 cov(c,a)
```

```
se = sqrt(1.3946 + 2.1606 + 1.414 + 2 *(-1.0406) + 2*(-1.0367) + 2*(0.098) )
```

```
beta = 1.842 + 3.802 + 2.265
```

```
Lo = beta-(1.96*se) # 5.9386
```

```
Hi= beta+ (1.96*se) # 9.8793
```

```
### QUESTION 9.22
```

```
rm(list=ls(all=TRUE))
```

```
library(multcomp)
```

```
library(data.table)
```

```
library(dplyr)
```

```
library(lmtest)
```

```
library(tseries)
```

```
library(dynlm)
```

```
library(forecast)
```

```
context = fread('consumption.csv')
```

```
# income growth
```

```
# consumption growth
```

```
context = context[ 4:200, c("incgwth","congwth")]
```

```
table <- context
```

```
check.ts <- is.ts(table) # "is structured as time series?"
```

```
table.ts <- ts(table, start=c(1960,4),frequency=4)
```

```
check.ts <- is.ts(table.ts)
```

```
model.dyn <- dynlm(congwth~L(incgwth, 0), data=table.ts)
```

```
summary(model.dyn)
plot <- ggAcf(model.dyn$residuals, lag.max = 20)
plot
AIC(model.dyn)
BIC(model.dyn)
# part c
```

```
table <- context
check.ts <- is.ts(table) # "is structured as time series?"
table.ts <- ts(table, start=c(1960,4), frequency=4)
check.ts <- is.ts(table.ts)
model.dyn <- dynlm(congwth~L(congwth, 1) + L(incgwth, 0), data=table.ts)
summary(model.dyn)
plot <- ggAcf(model.dyn$residuals, lag.max = 20)
plot
AIC(model.dyn)
BIC(model.dyn)
```

part d

```
table <- context
check.ts <- is.ts(table) # "is structured as time series?"
table.ts <- ts(table, start=c(1960,4), frequency=4)
check.ts <- is.ts(table.ts)
model.dyn <- dynlm(congwth~L(congwth, 1)+L(congwth, 2) + L(incgwth, 0), data=table.ts)
summary(model.dyn)
plot <- ggAcf(model.dyn$residuals, lag.max = 20)
plot
AIC(model.dyn)
```

```
BIC(model.dyn)
```

```
# part e
```

```
table <- context
```

```
check.ts <- is.ts(table) # "is structured as time series?"
```

```
table.ts <- ts(table, start=c(1960,4),frequency=4)
```

```
check.ts <- is.ts(table.ts)
```

```
model.dyn <- dynlm(congwth~L(congwth, 1)+L(congwth, 2) + L(incgwth, 0) + L(incgwth, 1) ,  
data=table.ts)
```

```
summary(model.dyn)
```

```
plot <- ggAcf(model.dyn$residuals,lag.max = 20)
```

```
plot
```

```
AIC(model.dyn)
```

```
BIC(model.dyn)
```

```
# part f add congwth at lag 3
```

```
table <- context
```

```
check.ts <- is.ts(table) # "is structured as time series?"
```

```
table.ts <- ts(table, start=c(1960,4),frequency=4)
```

```
check.ts <- is.ts(table.ts)
```

```
model.dyn <- dynlm(congwth~L(congwth, 1)+L(congwth, 2) + L(congwth, 3) + L(incgwth, 0) + L(incgwth,  
1) , data=table.ts)
```

```
summary(model.dyn)
```

```
plot <- ggAcf(model.dyn$residuals,lag.max = 20)
```

```
plot
```

```
AIC(model.dyn)
```

```
BIC(model.dyn)
```

part g drop congwth t-1 from part e

```
table <- context
```

```
check.ts <- is.ts(table) # "is structured as time series?"
```

```
table.ts <- ts(table, start=c(1960,4),frequency=4)
```

```
check.ts <- is.ts(table.ts)
```

```
model.dyn <- dynlm(congwth~ L(congwth, 2) + L(incgwth, 0) + L(incgwth, 1) , data=table.ts)
```

```
summary(model.dyn)
```

```
plot <- ggAcf(model.dyn$residuals,lag.max = 20)
```

```
plot
```

```
AIC(model.dyn)
```

```
BIC(model.dyn)
```