Podpora pre najdlhšie / najkratšie kružnice v grafoch

Procedúry a funkcie pre testy kružníc v grafoch

Určenie dĺžky najdlhšej kružnice v grafe:

Analýza rektilineárnych grafov z množín $\tilde{R}(k)$ pre k = 2, 3, 4

Import uvedených rektilineárnych grafov:

```
In[6]:= z2 = Import[filename <> "R_2.g6"];
  In[7]:= z3 = Import[filename <> "R_3.g6"];
  in[8]:= z4 = Import[filename <> "R_4.g6"];
  In[9]:= 12 = Length[z2]
 Out[9]= 10
 In[10]:= l3 = Length[z3]
Out[10]=
       92
 In[11]:= 14 = Length[z4]
Out[11]=
       1781
```

Kontrolné testy, či sú dané grafy navzájom neizomorfné, subkubické a majú práve 4 dvojvalentné vrcholy:

```
ln[12]:= For[i = 1, i \le l2, i++,
      For [j = i + 1, j \le l2, j++,
       If[IsomorphicGraphQ[z2[i], z2[j]], Print[i, j]]]]
In[13]:= For[i = 1, i \le 13, i++,
      For [j = i + 1, j \le l3, j++,
       If[IsomorphicGraphQ[z3[i]], z3[j]]], Print[i, j]]]]
In[14]:= For[i = 1, i \le 14, i++,
      For [j = i + 1, j \le 14, j + +,
       If[IsomorphicGraphQ[z4[i]], z4[j]]], Print[i, j]]]]
ln[15]:= For[i = 1, i \leq l2, i++, If[BadGraph[z2[i]]], Print[z2[i]]]]
\label{eq:local_local_local_local_local} $$\inf[16]:=$ For[i=1, i \leq l3, i++, If[BadGraph[z3[i]]], Print[z3[i]]]]$$
     For[i = 1, i ≤ l4, i++, If[BadGraph[z4[i]]], Print[z4[i]]]]
ln[19]:= For[i=1, i \le l3, i++, If[Not[Max[VertexDegree[z3[i]]]] == 3], Print[z3[i]]]]
```

Testy, či sú dané grafy nehamiltonovské, jednoznačne hamiltonovské resp. nehamiltonovské s jedinou najdlhšou kružnicou + export:

```
In[21]:= neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le l2, i++,
       c = Length[FindHamiltonianCycle[z2[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z2[i]];
         If[UniqueLongestCycleQ[z2[i]]], jedc += 1;
          AppendTo[jedncLst, z2[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z2[i]], inham += 1]]
      Print["Štatistika pre grafy s dvomi vrcholmi vo vnútri: ", neham,
       " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy s dvomi vrcholmi vo vnútri: 4
        nehamiltonovských, 5 jednoznačne hamiltonovských, 1 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
 In[24]:= Export[filename <> "nehamiltonovske_2.g6", nehamLst]
Out[24]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_2.g6
 In[25]:= Export[filename <> "jednoznacne_2.g6", jedhamLst]
Out[25]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_2.g6
 In[26]:= neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le l3, i++,
       c = Length[FindHamiltonianCycle[z3[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z3[i]];
         If[UniqueLongestCycleQ[z3[i]], jedc += 1;
          AppendTo[jedncLst, z3[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z3[i]], inham += 1]]
      Print["Štatistika pre grafy so 3 vrcholmi vo vnútri: ", neham,
       " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"
      Štatistika pre grafy so 3 vrcholmi vo vnútri: 41
        nehamiltonovských, 36 jednoznačne hamiltonovských, 15 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
```

```
In[29]:= Export[filename <> "nehamiltonovske 3.g6", nehamLst]
Out[29]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_3.g6
 In[30]:= Export[filename <> "jednoznacne_3.g6", jedhamLst]
Out[30]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_3.g6
 In[31]:= neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 14, i++,
       c = Length[FindHamiltonianCycle[z4[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z4[i]];
         If[UniqueLongestCycleQ[z4[i]], jedc += 1;
          AppendTo[jedncLst, z4[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z4[i]], inham += 1]]
      Print["Štatistika pre grafy so 4 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"
      Štatistika pre grafy so 4 vrcholmi vo vnútri: 432
        nehamiltonovských, 690 jednoznačne hamiltonovských, 659 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
 In[34]:= Export[filename <> "nehamiltonovske_4.g6", nehamLst]
Out[34]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_4.g6
 In[35]:= Export[filename <> "jednoznacne_4.g6", jedhamLst]
Out[35]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_4.g6
      Rozbor obvodu získaných nehamiltonovských resp. jednoznačne hamiltonovských grafov:
 In[37]:= n2 = Import[filename <> "nehamiltonovske_2.g6"];
 In[38]:= 12 = Length[n2]
Out[38]=
      4
 In[39]:= 02 = {};
      For[i = 1, i ≤ l2, i++, AppendTo[o2, ResourceFunction["Girth"][n2[i]]]];
```

```
In[43]:= res2 = Tally[02]
Out[43]=
       \{\{5, 1\}, \{4, 3\}\}
 ln[45]:= Print["Z nehamiltonovských grafov triedy \tilde{R}(2) je", res2[2, 2],
        " grafov obvodu ", res2[[2, 1]], ", ", res2[[1, 2]], " grafov obvodu ", res2[[1, 1]]]
       Z nehamiltonovských grafov triedy \tilde{\mathbb{R}}(2) je 3 grafov obvodu 4, 1 grafov obvodu 5
 In[46]:= j2 = Import[filename <> "jednoznacne_2.g6"];
 In[47]:= 12 = Length[j2]
Out[47]=
 ln[48]:= oj2 = {};
       For[i = 1, i ≤ l2, i++, AppendTo[oj2, ResourceFunction["Girth"][j2[i]]]];
 In[50]:= res2 = Tally[oj2]
Out[50]=
       \{\{4,4\},\{5,1\}\}
 ın[51]:= Print["Z jednoznačne hamiltonovských grafov triedy ℜ(2) je", res2[1, 2],
        " grafov obvodu ", res2[1, 1], ", ", res2[2, 2], " grafov obvodu ", res2[2, 1]]
       Z jednoznačne hamiltonovských grafov triedy \widetilde{\Re}\left(2\right) je
        4 grafov obvodu 4, 1 grafov obvodu 5
 In[52]:= n3 = Import[filename <> "nehamiltonovske_3.g6"];
 In[53]:= 13 = Length[n3]
Out[53]=
       41
 In[54]:= 03 = {};
       For[i = 1, i ≤ l3, i++, AppendTo[o3, ResourceFunction["Girth"][n3[i]]]];
 In[56]:= res3 = Tally[03]
Out[56]=
       \{\{4, 33\}, \{5, 8\}\}
 In[58]:= Print["Z nehamiltonovských grafov triedy R(3) je", res3[1, 2],
        " grafov obvodu ", res3[1, 1], ", ", res3[2, 2], " grafov obvodu ", res3[2, 1]]
       Z nehamiltonovských grafov triedy \widetilde{\mathbb{R}}(3) je 33 grafov obvodu 4, 8 grafov obvodu 5
 In[59]:= j3 = Import[filename <> "jednoznacne_3.g6"];
 In[60]:= l3 = Length[j3]
Out[60]=
       36
 ln[61]:= oj3 = {};
       For[i = 1, i ≤ l3, i++, AppendTo[oj3, ResourceFunction["Girth"][j3[i]]]];
```

```
In[63]:= res3 = Tally[0j3]
Out[63]=
       \{\{4,33\},\{5,3\}\}
 \ln[64]:= Print["Z jednoznačne hamiltonovských grafov triedy \tilde{R}(3) je", res3[1, 2],
        " grafov obvodu ", res3[1, 1], ", ", res3[2, 2], " grafov obvodu ", res3[2, 1]]
       Z jednoznačne hamiltonovských grafov triedy \tilde{R}(3) je
        33 grafov obvodu 4, 3 grafov obvodu 5
 In[65]:= n4 = Import[filename <> "nehamiltonovske 4.g6"];
 In[66]:= 14 = Length[n4]
       432
 In[67]:= 04 = {};
       For [i = 1, i \le 14, i++, AppendTo[04, ResourceFunction["Girth"][n4[i]]]];
 In[69]:= res4 = Tally[04]
Out[69]=
       \{\{5, 57\}, \{4, 371\}, \{6, 4\}\}
 In[70]:= Print["Z nehamiltonovských grafov triedy Ã(4) je", res4[2, 2]],
        " grafov obvodu ", res4[2, 1], ", ", res4[1, 2], " grafov obvodu ",
        res4[1, 1], ", ", res4[3, 2], " grafov obvodu ", res4[3, 1]]
       Z nehamiltonovských grafov triedy \tilde{R}(4) je 371
         grafov obvodu 4, 57 grafov obvodu 5, 4 grafov obvodu 6
 In[71]:= j4 = Import[filename <> "jednoznacne_4.g6"];
 In[72]:= 14 = Length[j4]
Out[72]=
       690
 In[73]:= oj4 = {};
       For[i = 1, i ≤ l4, i++, AppendTo[oj4, ResourceFunction["Girth"][j4[i]]]];
 In[75]:= res4 = Tally[oj4]
Out[75]=
       \{\{4,546\},\{5,133\},\{6,11\}\}
 \ln[76] = \text{Print}[\text{"Z jednoznačne hamiltonovských grafov triedy } \tilde{\mathbb{R}}(4) \text{ je ", res4[1, 2] ,}
        " grafov obvodu ", res4[1, 1], ", ", res4[2, 2], " grafov obvodu ",
        res4[2, 1], ", ", res4[3, 2], " grafov obvodu ", res4[3, 1]]
       Z jednoznačne hamiltonovských grafov triedy \tilde{R}(4) je
        546 grafov obvodu 4, 133 grafov obvodu 5, 11 grafov obvodu 6
```

Analýza veľkých kolekcií rektilineárnych grafov z množín $\tilde{R}(k)$ pre $k \ge 6$

Import vygenerovaných rektilineárnych grafov (každá kolekcia obsahuje 10000 neizomorfných grafov):

```
In[77]:= z6 = Import[filename <> "k6corr.g6"];
in[78]:= z7 = Import[filename <> "k7corr.g6"];
In[79]:= z8 = Import[filename <> "k8corr.g6"];
in[80]:= z9 = Import[filename <> "k9corr.g6"];
In[81]:= z10 = Import[filename <> "k10corr.g6"];
in[82]:= z11 = Import[filename <> "k11corr.g6"];
in[83]:= z12 = Import[filename <> "k12corr.g6"];
In[84]:= z13 = Import[filename <> "k13corr.g6"];
In[85]:= z14 = Import[filename <> "k14corr.g6"];
In[86]:= z15 = Import[filename <> "k15corr.g6"];
In[87]:= z16 = Import[filename <> "k16corr.g6"];
in[88]:= z17 = Import[filename <> "k17corr.g6"];
In[89]:= z18 = Import[filename <> "k18corr.g6"];
in[90]:= z19 = Import[filename <> "k19corr.g6"];
In[91]:= z20 = Import[filename <> "k20corr.g6"];
```

Testy, či sú dané grafy nehamiltonovské, jednoznačne hamiltonovské resp. nehamiltonovské s jedinou najdlhšou kružnicou + export:

```
In[92]:= neham = 0;
     jedham = 0;
     inham = 0;
     jedc = 0;
     nehamLst = {}; jedhamLst = {}; jedncLst = {};
     For [i = 1, i \le 10000, i++,
      c = Length[FindHamiltonianCycle[z6[i]], All]];
      If[c == 0, neham += 1; AppendTo[nehamLst, z6[i]];
       If[UniqueLongestCycleQ[z6[i]]], jedc += 1;
         AppendTo[jedncLst, z6[i]]], If[c == 1, jedham += 1;
         AppendTo[jedhamLst, z6[i]], inham += 1]]
     Print["Štatistika pre grafy so 6 vrcholmi vo vnútri: ", neham,
      " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
      " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"
     Štatistika pre grafy so 6 vrcholmi vo vnútri: 1737
       nehamiltonovských, 2682 jednoznačne hamiltonovských, 5581 iných.
     Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
```

```
In[95]:= Export[filename <> "nehamiltonovske 6.g6", nehamLst]
Out[95]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_6.g6
 In[96]:= Export[filename <> "jednoznacne_6.g6", jedhamLst]
Out[96]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_6.g6
 In[97]:= neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z7[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z7[i]];
         If[UniqueLongestCycleQ[z7[i]]], jedc += 1;
          AppendTo[jedncLst, z7[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z7[i]], inham += 1]]
      Print["Štatistika pre grafy so 7 vrcholmi vo vnútri: ", neham,
       " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 7 vrcholmi vo vnútri: 1029
        nehamiltonovských, 1715 jednoznačne hamiltonovských, 7256 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[100]:=
      Export[filename <> "nehamiltonovske 7.g6", nehamLst]
Out[100]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_7.g6
In[101]:=
      Export[filename <> "jednoznacne_7.g6", jedhamLst]
Out[101]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_7.g6
```

```
In[102]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z8[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z8[i]];
         If[UniqueLongestCycleQ[z8[i]]], jedc += 1;
          AppendTo[jedncLst, z8[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z8[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 8 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 8 vrcholmi vo vnútri: 499
        nehamiltonovských, 947 jednoznačne hamiltonovských, 8554 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[105]:=
      Export[filename <> "nehamiltonovske_8.g6", nehamLst]
Out[105]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_8.g6
In[106]:=
      Export[filename <> "jednoznacne_8.g6", jedhamLst]
Out[106]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_8.g6
```

```
In[107]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z9[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z9[i]];
         If[UniqueLongestCycleQ[z9[i]]], jedc += 1;
          AppendTo[jedncLst, z9[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z9[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 9 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 9 vrcholmi vo vnútri: 255
        nehamiltonovských, 447 jednoznačne hamiltonovských, 9298 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[110]:=
      Export[filename <> "nehamiltonovske_9.g6", nehamLst]
Out[110]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_9.g6
In[111]:=
      Export[filename <> "jednoznacne_9.g6", jedhamLst]
Out[111]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_9.g6
```

```
In[112]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z10[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z10[i]]];
         If[UniqueLongestCycleQ[z10[i]]], jedc += 1;
          AppendTo[jedncLst, z10[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z10[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 10 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 10 vrcholmi vo vnútri: 111
        nehamiltonovských, 167 jednoznačne hamiltonovských, 9722 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[115]:=
      Export[filename <> "nehamiltonovske_10.g6", nehamLst]
Out[115]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_10.g6
In[116]:=
      Export[filename <> "jednoznacne_10.g6", jedhamLst]
Out[116]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_10.g6
```

```
In[117]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z11[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z11[i]];
         If[UniqueLongestCycleQ[z11[i]]], jedc += 1;
          AppendTo[jedncLst, z11[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z11[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 11 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 11 vrcholmi vo vnútri: 50
        nehamiltonovských, 64 jednoznačne hamiltonovských, 9886 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[120]:=
      Export[filename <> "nehamiltonovske_11.g6", nehamLst]
Out[120]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_11.g6
In[121]:=
      Export[filename <> "jednoznacne_11.g6", jedhamLst]
Out[121]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_11.g6
```

```
In[122]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z12[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z12[i]]];
         If[UniqueLongestCycleQ[z12[i]]], jedc += 1;
          AppendTo[jedncLst, z12[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z12[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 12 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 12 vrcholmi vo vnútri: 19
        nehamiltonovských, 13 jednoznačne hamiltonovských, 9968 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[125]:=
      Export[filename <> "nehamiltonovske_12.g6", nehamLst]
Out[125]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_12.g6
In[126]:=
      Export[filename <> "jednoznacne_12.g6", jedhamLst]
Out[126]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_12.g6
```

```
In[127]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z13[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z13[i]];
         If[UniqueLongestCycleQ[z13[i]], jedc += 1;
          AppendTo[jedncLst, z13[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z13[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 13 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 13 vrcholmi vo vnútri: 4
        nehamiltonovských, 7 jednoznačne hamiltonovských, 9989 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[130]:=
      Export[filename <> "nehamiltonovske_13.g6", nehamLst]
Out[130]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_13.g6
In[131]:=
      Export[filename <> "jednoznacne_13.g6", jedhamLst]
Out[131]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_13.g6
```

```
In[132]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z14[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z14[i]]];
         If[UniqueLongestCycleQ[z14[i]]], jedc += 1;
          AppendTo[jedncLst, z14[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z14[i]], inham += 1]]
      ]
      Print["Štatistika pre grafy so 14 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
       " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 14 vrcholmi vo vnútri: 3
        nehamiltonovských, 1 jednoznačne hamiltonovských, 9996 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[135]:=
      Export[filename <> "nehamiltonovske_14.g6", nehamLst]
Out[135]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_14.g6
In[136]:=
      Export[filename <> "jednoznacne_14.g6", jedhamLst]
Out[136]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         jednoznacne_14.g6
```

```
In[137]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z15[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z15[i]];
         If[UniqueLongestCycleQ[z15[i]], jedc += 1;
          AppendTo[jedncLst, z15[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z15[i]], inham += 1]]
      Print["Štatistika pre grafy so 15 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 15 vrcholmi vo vnútri: 0
        nehamiltonovských, 0 jednoznačne hamiltonovských, 10000 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[140]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z16[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z16[i]];
         If[UniqueLongestCycleQ[z16[i]]], jedc += 1;
          AppendTo[jedncLst, z16[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z16[i]], inham += 1]]
      Print["Štatistika pre grafy so 16 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 16 vrcholmi vo vnútri: 0
        nehamiltonovských, 0 jednoznačne hamiltonovských, 10000 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
```

```
In[143]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z17[i]], All]];
        If[c == 0, neham += 1; AppendTo[nehamLst, z17[i]];
         If[UniqueLongestCycleQ[z17[i]], jedc += 1;
          AppendTo[jedncLst, z17[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z17[i]], inham += 1]]
      Print["Štatistika pre grafy so 17 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 17 vrcholmi vo vnútri: 1
        nehamiltonovských, 0 jednoznačne hamiltonovských, 9999 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[146]:=
      Export[filename <> "nehamiltonovske_17.g6", nehamLst]
Out[146]=
      /Users/tommymadaras/Library/CloudStorage/OneDrive-UPJŠ/Výuka/bachelor/malik/
         nehamiltonovske_17.g6
In[147]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z18[i]], All]];
        If[c == 0, neham += 1; AppendTo[nehamLst, z18[i]];
         If[UniqueLongestCycleQ[z18[i]], jedc += 1;
          AppendTo[jedncLst, z18[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z18[i]], inham += 1]]
      Print["Štatistika pre grafy so 18 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 18 vrcholmi vo vnútri: 0
        nehamiltonovských, 0 jednoznačne hamiltonovských, 10000 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
```

```
In[150]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
       c = Length[FindHamiltonianCycle[z19[i], All]];
        If[c == 0, neham += 1; AppendTo[nehamLst, z19[i]];
         If[UniqueLongestCycleQ[z19[i]], jedc += 1;
          AppendTo[jedncLst, z19[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z19[i]], inham += 1]]
      Print["Štatistika pre grafy so 19 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 19 vrcholmi vo vnútri: 0
        nehamiltonovských, 0 jednoznačne hamiltonovských, 10000 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
In[153]:=
      neham = 0;
      jedham = 0;
      inham = 0;
      jedc = 0;
      nehamLst = {}; jedhamLst = {}; jedncLst = {};
      For [i = 1, i \le 10000, i++,
        c = Length[FindHamiltonianCycle[z20[i]], All]];
       If[c == 0, neham += 1; AppendTo[nehamLst, z20[i]];
         If[UniqueLongestCycleQ[z20[i]]], jedc += 1;
          AppendTo[jedncLst, z20[i]]], If[c == 1, jedham += 1;
          AppendTo[jedhamLst, z20[i]], inham += 1]]
      Print["Štatistika pre grafy so 20 vrcholmi vo vnútri: ", neham,
        " nehamiltonovských, ", jedham, " jednoznačne hamiltonovských, ", inham,
        " iných.\n", "Z nehamiltonovských: ", jedc, " s jedinou najdlhšou kružnicou"]
      Štatistika pre grafy so 20 vrcholmi vo vnútri: 0
        nehamiltonovských, 0 jednoznačne hamiltonovských, 10000 iných.
      Z nehamiltonovských: 0 s jedinou najdlhšou kružnicou
      Rozbor obvodu získaných nehamiltonovských resp. jednoznačne hamiltonovských grafov:
In[156]:=
      n6 = Import[filename <> "nehamiltonovske 6.g6"];
In[157]:=
      l6 = Length[n6]
Out[157]=
      1737
```

```
In[158]:=
       06 = {};
       For[i = 1, i ≤ l6, i++, AppendTo[o6, ResourceFunction["Girth"][n6[i]]]];
In[160]:=
       res6 = Tally[06]
Out[160]=
       \{\{4, 1614\}, \{5, 118\}, \{6, 5\}\}\
In[161]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R}(6) je", res6[1, 2],
        " grafov obvodu ", res6[1, 1], ", ", res6[2, 2], " grafov obvodu ",
        res6[2, 1], ", ", res6[3, 2], " grafov obvodu ", res6[3, 1]]
       Z kolekcie nehamiltonovských grafov triedy \tilde{R}(6) je
        1614 grafov obvodu 4, 118 grafov obvodu 5, 5 grafov obvodu 6
In[162]:=
       j6 = Import[filename <> "jednoznacne_6.g6"];
In[163]:=
       l6 = Length[j6]
Out[163]=
       2682
In[164]:=
       oj6 = {};
       For[i = 1, i ≤ l6, i++, AppendTo[oj6, ResourceFunction["Girth"][j6[i]]]];
In[166]:=
       res6 = Tally[oj6]
Out[166]=
       \{\{4, 2446\}, \{5, 235\}, \{6, 1\}\}
In[167]:=
       Print\lceil"Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(6) je",
        res6[1, 2], " grafov obvodu ", res6[1, 1], ", ", res6[2, 2],
        " grafov obvodu ", res6[2, 1], ", ", res6[3, 2], " grafov obvodu ", res6[3, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(6) je
        2446 grafov obvodu 4, 235 grafov obvodu 5, 1 grafov obvodu 6
In[168]:=
       n7 = Import[filename <> "nehamiltonovske 7.g6"];
In[169]:=
       17 = Length[n7]
Out[169]=
       1029
In[170]:=
       07 = {};
       For[i = 1, i ≤ l7, i++, AppendTo[o7, ResourceFunction["Girth"][n7[i]]]];
In[172]:=
       res7 = Tally[o7]
Out[172]=
       \{\{4, 972\}, \{5, 55\}, \{6, 2\}\}\
```

```
In[174]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R}(7) je", res7[1, 2],
        " grafov obvodu ", res7[1, 1], ", ", res7[2, 2], " grafov obvodu ",
        res7[2, 1], ", ", res7[3, 2], " grafov obvodu ", res7[3, 1]]
       Z kolekcie nehamiltonovských grafov triedy \widetilde{\Re}(7) je
        972 grafov obvodu 4, 55 grafov obvodu 5, 2 grafov obvodu 6
In[175]:=
       j7 = Import[filename <> "jednoznacne_7.g6"];
In[176]:=
       17 = Length[j7]
Out[176]=
       1715
In[177]:=
       oj7 = {};
       For[i = 1, i ≤ l7, i++, AppendTo[oj7, ResourceFunction["Girth"][j7[i]]]];
In[179]:=
       res7 = Tally[oj7]
Out[179]=
       \{\{4, 1581\}, \{5, 131\}, \{6, 3\}\}
In[181]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy <math>\tilde{R}(7) je",
        res7[1, 2], " grafov obvodu ", res7[1, 1], ", ", res7[2, 2],
        " grafov obvodu ", res7[2, 1], ", ", res7[3, 2], " grafov obvodu ", res7[3, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\mathbb{R}}(7) je
        1581 grafov obvodu 4, 131 grafov obvodu 5, 3 grafov obvodu 6
In[182]:=
       n8 = Import[filename <> "nehamiltonovske_8.g6"];
In[183]:=
       18 = Length[n8]
Out[183]=
       499
In[184]:=
       08 = \{\};
       For[i = 1, i ≤ l8, i++, AppendTo[o8, ResourceFunction["Girth"][n8[i]]]];
In[186]:=
       res8 = Tally[08]
Out[186]=
       \{\{4, 480\}, \{5, 19\}\}
In[187]:=
       Print["Z kolekcie nehamiltonovských grafov triedy <math>\tilde{R}(8) je", res8[1, 2],
        " grafov obvodu ", res8[1, 1], ", ", res8[2, 2], " grafov obvodu ", res8[2, 1]]
       Z kolekcie nehamiltonovských grafov triedy \tilde{\Re}(8) je
        480 grafov obvodu 4, 19 grafov obvodu 5
In[188]:=
       j8 = Import[filename <> "jednoznacne_8.g6"];
```

```
In[189]:=
       l8 = Length[j8]
Out[189]=
       947
In[190]:=
       oj8 = {};
       For[i = 1, i ≤ l8, i++, AppendTo[oj8, ResourceFunction["Girth"][j8[i]]]];
In[192]:=
       res8 = Tally[oj8]
Out[192]=
       \{\{4, 886\}, \{5, 60\}, \{6, 1\}\}\
In[193]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(8) je",
         res8[1, 2]], " grafov obvodu ", res8[1, 1]], ", ", res8[2, 2]],
         " grafov obvodu ", res8[2, 1], ", ", res8[3, 2], " grafov obvodu ", res8[3, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\mathtt{R}}\left(8\right) je
        886 grafov obvodu 4, 60 grafov obvodu 5, 1 grafov obvodu 6
In[194]:=
       n9 = Import[filename <> "nehamiltonovske_9.g6"];
In[195]:=
       19 = Length[n9]
Out[195]=
       255
In[196]:=
       09 = {};
       For[i = 1, i ≤ l9, i++, AppendTo[o9, ResourceFunction["Girth"][n9[i]]]];
In[198]:=
       res9 = Tally[o9]
Out[198]=
       \{\{4, 240\}, \{5, 15\}\}
In[199]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R}(9) je", res9[1, 2],
        " grafov obvodu ", res9[1, 1], ", ", res9[2, 2], " grafov obvodu ", res9[2, 1]]
       Z kolekcie nehamiltonovských grafov triedy \widetilde{\mathbb{R}}(9) je
        240 grafov obvodu 4, 15 grafov obvodu 5
In[200]:=
       j9 = Import[filename <> "jednoznacne_9.g6"];
In[201]:=
       19 = Length[j9]
Out[201]=
       447
In[202]:=
       oj9 = {};
       For[i = 1, i ≤ l9, i++, AppendTo[oj9, ResourceFunction["Girth"][j9[i]]]];
```

```
In[204]:=
       res9 = Tally[oj9]
Out[204]=
       \{\{4, 423\}, \{5, 24\}\}
In[205]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(9) je",
         res9[1, 2], " grafov obvodu ", res9[1, 1],
         ", ", res9[2, 2], " grafov obvodu ", res9[2, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\mathbb{R}}\left(9\right) je
        423 grafov obvodu 4, 24 grafov obvodu 5
In[206]:=
       n10 = Import[filename <> "nehamiltonovske_10.g6"];
In[207]:=
       110 = Length[n10]
Out[207]=
       111
In[208]:=
       010 = {};
       For[i = 1, i ≤ l10, i++, AppendTo[o10, ResourceFunction["Girth"][n10[i]]]];
In[210]:=
       res10 = Tally[o10]
Out[210]=
       \{\{4, 110\}, \{5, 1\}\}
In[211]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R} (10) je",
         res10[1, 2], " grafov obvodu ", res10[1, 1],
         ", ", res10[2, 2], " grafov obvodu ", res10[2, 1]]
       Z kolekcie nehamiltonovských grafov triedy \widetilde{\Re}\left(10\right) je
         110 grafov obvodu 4, 1 grafov obvodu 5
In[212]:=
       j10 = Import[filename <> "jednoznacne_10.g6"];
In[213]:=
       l10 = Length[j10]
Out[213]=
       167
In[214]:=
       oj10 = {};
       For[i = 1, i ≤ l10, i++, AppendTo[oj10, ResourceFunction["Girth"][j10[i]]]];
In[216]:=
       res10 = Tally[oj10]
Out[216]=
       \{\{4, 158\}, \{5, 9\}\}
```

```
In[217]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(10) je",
         res10[1, 2], " grafov obvodu ", res10[1, 1],
        ", ", res10[2, 2], " grafov obvodu ", res10[2, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\mathbb{R}} (10) je
        158 grafov obvodu 4, 9 grafov obvodu 5
In[218]:=
       n11 = Import[filename <> "nehamiltonovske_11.g6"];
In[219]:=
       l11 = Length[n11]
Out[219]=
In[220]:=
       011 = {};
       For [i = 1, i \leq l11, i++, AppendTo [o11, ResourceFunction["Girth"] [n11[i]]]];
In[222]:=
       res11 = Tally[011]
Out[222]=
       {{4,50}}
In[223]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R}(11) je",
        res11[1, 2], " grafov obvodu ", res11[1, 1], "(t.j. všetky)"]
       Z kolekcie nehamiltonovských grafov triedy \tilde{\mathbb{R}}(11) je 50 grafov obvodu 4(t.j. všetky)
In[224]:=
       j11 = Import[filename <> "jednoznacne_11.g6"];
In[225]:=
       l11 = Length[j11]
Out[225]=
       64
In[226]:=
       oj11 = {};
       For [i = 1, i \leq l11, i++, AppendTo[oj11, ResourceFunction["Girth"][j11[i]]]];
In[228]:=
       res11 = Tally[oj11]
Out[228]=
       \{\{4, 62\}, \{5, 2\}\}
In[229]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{R}(11) je",
         res11[1, 2], " grafov obvodu ", res11[1, 1],
         ", ", res11[2, 2], " grafov obvodu ", res11[2, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\Re}\left(11\right) je
        62 grafov obvodu 4, 2 grafov obvodu 5
In[230]:=
       n12 = Import[filename <> "nehamiltonovske_12.g6"];
```

```
In[231]:=
       l12 = Length[n12]
Out[231]=
       19
In[232]:=
       012 = {};
       For[i = 1, i ≤ l12, i++, AppendTo[o12, ResourceFunction["Girth"][n12[i]]]];
In[234]:=
       res12 = Tally[o12]
Out[234]=
       \{\{4, 16\}, \{5, 3\}\}
In[235]:=
       Print["Z kolekcie nehamiltonovských grafov triedy \tilde{R} (12) je",
        res12[1, 2], " grafov obvodu ", res12[1, 1],
         ", ", res12[2, 2], " grafov obvodu ", res12[2, 1]]
       Z kolekcie nehamiltonovských grafov triedy \widetilde{\mathtt{R}}\,(12) je
        16 grafov obvodu 4, 3 grafov obvodu 5
In[237]:=
       j12 = Import[filename <> "jednoznacne_12.g6"];
In[238]:=
       l12 = Length[j12]
Out[238]=
       13
In[239]:=
       oj12 = {};
       For[i = 1, i ≤ l12, i++, AppendTo[oj12, ResourceFunction["Girth"][j12[i]]]];
In[241]:=
       res12 = Tally[oj12]
Out[241]=
       \{\{5, 1\}, \{4, 12\}\}
In[242]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy <math>\tilde{\Re}(12) je",
        res12[1, 2], " grafov obvodu ", res12[1, 1],
        ", ", res12[2, 2], " grafov obvodu ", res12[2, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \widetilde{\mathbb{R}} (12) je
        1 grafov obvodu 5, 12 grafov obvodu 4
In[243]:=
       n13 = Import[filename <> "nehamiltonovske_13.g6"];
In[244]:=
       l13 = Length[n13]
Out[244]=
In[245]:=
       013 = {};
       For[i = 1, i ≤ l13, i++, AppendTo[o13, ResourceFunction["Girth"][n13[i]]]];
```

```
In[247]:=
       res13 = Tally[o13]
Out[247]=
       { {4, 4} }
In[248]:=
       Print["Z kolekcie nehamiltonovských grafov triedy <math>\tilde{R}(13) je",
         res13[1, 2], " grafov obvodu ", res13[1, 1]]
       Z kolekcie nehamiltonovských grafov triedy \widetilde{\mathbb{R}}\,(13) je 4 grafov obvodu 4
In[249]:=
       j13 = Import[filename <> "jednoznacne_13.g6"];
In[250]:=
       l13 = Length[j13]
Out[250]=
In[251]:=
       oj13 = {};
       For [i = 1, i \leq l13, i++, AppendTo [oj13, ResourceFunction ["Girth"] [j13 [i]]]];
In[253]:=
       res13 = Tally[oj13]
Out[253]=
       { {4, 7} }
In[254]:=
       Print["Z kolekcie jednoznačne hamiltonovských grafov triedy <math>\tilde{R}(13) je",
         res13[1, 2], " grafov obvodu ", res13[1, 1]]
       Z kolekcie jednoznačne hamiltonovských grafov triedy \tilde{\mathbb{R}}(13) je 7 grafov obvodu 4
```