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E2a[n_, k_, a_] :=
  E2a[n, k, a] = Sum[E2a[n / j, k - 1, a], {j, 2, n}] - a Sum[E2a[n / (a j), k - 1, a], {j, 1, n / a}];
E2a[n_, 0, a_] := 1
D2a[n_, k_] := D2a[n, k] = Sum[D2a[Floor[n / j], k - 1], {j, 2, n}]; D2a[n_, 0] := 1
DD[n_, z_] := DD[n, z] = Sum[FactorialPower[z, a] / a! D2a[n, a], {a, 0, Log[2, n]}]
EE[n_, z_, b_] :=
  EE[n, z, b] = Sum[FactorialPower[z, a] / a! E2a[n, a, b], {a, 0, Log[If[b > 2, 2, b], n]}]

EE[100, 2, 2]

2

DD[100, 2]

482

DD[100, 2] - 4 DD[50, 2] + 4 DD[25, 2]

2

f1[n_] := EE[n, 2, 2] + 4 DD[n / 2, 2] - 4 DD[n / 4, 2]

f1[100]

482

f2[n_] := EE[n, 2, 2] + 4 (EE[n / 2, 2, 2] + 4 DD[n / 4, 2] - 4 DD[n / 8, 2]) -
  4 (EE[n / 4, 2, 2] + 4 DD[n / 8, 2] - 4 DD[n / 16, 2])

f2[100]

482

Expand[EE[n, 2, 2] + 4 (EE[n / 2, 2, 2] + 4 DD[n / 4, 2] - 4 DD[n / 8, 2]) -
  4 (EE[n / 4, 2, 2] + 4 DD[n / 8, 2] - 4 DD[n / 16, 2])]

16 DD[ $\frac{n}{16}, 2$ ] - 32 DD[ $\frac{n}{8}, 2$ ] + 16 DD[ $\frac{n}{4}, 2$ ] - 4 EE[ $\frac{n}{4}, 2, 2$ ] + 4 EE[ $\frac{n}{2}, 2, 2$ ] + EE[n, 2, 2]

Sum[Binomial[2 + j - 1, 2 - 1] 2^j EEa[100 / 2^j, 2, 2], {j, 0, Log[2, 100]}]

448 EEa[ $\frac{25}{16}, 2, 2$ ] + 192 EEa[ $\frac{25}{8}, 2, 2$ ] + 80 EEa[ $\frac{25}{4}, 2, 2$ ] +
  32 EEa[ $\frac{25}{2}, 2, 2$ ] + 12 EEa[25, 2, 2] + 4 EEa[50, 2, 2] + EEa[100, 2, 2]

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