

```

Dd[x_, 0, a_] := 1
Dd[x_, k_, a_] := Dd[x, k, a] = Sum[Dd[x / (j + a), k - 1, a], {j, 0, x - a}]
Cc[x_, k_, a_] := a^(-k) Dd[x a^k, k, a + 1]
pp[x_, a_] := Sum[(-1)^(k + 1) / k Cc[x, k, a], {k, 1, 20}]

Cc[100, 2, 1]
283
pp[10, 2]
$Aborted

Expand[Integrate[(LogIntegral[100 / x] - EulerGamma - Log[Log[100 / x]]), {x, 1, 100}]]
N[101 EulerGamma - 100 ExpIntegralEi[-Log[100]] + 101 Log[Log[100]] - LogIntegral[100]]
182.601

Integrate[(LogIntegral[100 / x] - EulerGamma - Log[Log[100 / x]]), {x, 1, 100}]
101 EulerGamma - 100 ExpIntegralEi[-Log[100]] + 101 Log[Log[100]] - LogIntegral[100]
ExpIntegralEi[-Log[100.]]
-0.00182974
LogIntegral[Log[Log[100.]]]
0.190652
LogIntegral[100.]
30.1261
ExpIntegralEi[Log[100.]]
30.1261
101 EulerGamma - 100 ExpIntegralEi[-Log[100]] + 101 Log[Log[100]] - ExpIntegralEi[Log[100]]
101 EulerGamma - 100 ExpIntegralEi[-Log[100]] - ExpIntegralEi[Log[100]] + 101 Log[Log[100]]

Expand[Integrate[(LogIntegral[100 / x]), {x, 1, 100}]]
100 EulerGamma + 100 Log[Log[100]] - LogIntegral[100]
Expand[Integrate[(Log[Log[100 / x]]), {x, 1, 100}]]
-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]
Expand[Integrate[(Log[Log[100] - Log[x]]), {x, 1, 100}]]
-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]
Expand[Integrate[(Log[Log[100]]), {x, 1, 100}]]
99 Log[Log[100]]
Expand[Integrate[(Log[-Log[x]]), {x, 1, 100}]]
EulerGamma + 99 i π + 100 Log[Log[100]] - LogIntegral[100]
Expand[Integrate[(Log[Log[100] - Log[x]]), {x, 1, 100}]]
-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]

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N[-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]]
-59.4317

N[Expand[Integrate[(Log[-Log[x]]), {x, 1, 100}]] -
  Expand[Integrate[(Log[Log[100]]), {x, 1, 100}]]]
-28.0217 + 311.018 i

N[Expand[Integrate[(LogIntegral[100/x] - EulerGamma - Log[Log[100/x]]), {x, 1, 100}]]]
182.601

Expand[Integrate[(Log[Log[100] - Log[x]]), {x, 1, 100}]]
-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]

Expand[Integrate[(Log[a - Log[x]]), {x, 1, 100}]]
e^a ExpIntegralEi[-a] - e^a ExpIntegralEi[-a + Log[100]] - Log[a] + 100 Log[a - Log[100]]

Limit[e^a ExpIntegralEi[-a] - e^a ExpIntegralEi[-a + Log[100]] -
  Log[a] + 100 Log[a - Log[100]], a -> Log[100]]
-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]

N[-100 EulerGamma + 100 ExpIntegralEi[-Log[100]] - Log[Log[100]]]
-59.4317

N[-100 EulerGamma + 100 ExpIntegralEi[Log[1/100]] - Log[Log[100]]]
-59.4317

N[-100 EulerGamma + 100 LogIntegral[1/100] - Log[Log[100]]]
-59.4317

N[101 EulerGamma - 100 ExpIntegralEi[-Log[100]] + 101 Log[Log[100]] - LogIntegral[100]]
182.601

N[101 EulerGamma - 100 LogIntegral[1/100] + 101 Log[Log[100]] - LogIntegral[100]]
182.601

N[100 EulerGamma - 100 LogIntegral[1/100] +
  101 Log[Log[100]] - (LogIntegral[100] - EulerGamma)]
182.601

N[-100 (LogIntegral[1/100] - EulerGamma - Log[Log[1/100]]) -
  100 Pi I - (LogIntegral[100] - EulerGamma - Log[Log[100]])]
182.601 + 0. i

N[-100 (LogIntegral[1/100] - EulerGamma - Log[Log[100]]) -
  (LogIntegral[100] - EulerGamma - Log[Log[100]])]
182.601

N[Integrate[(LogIntegral[30/x] - EulerGamma - Log[Log[30/x]]), {x, 1, 30}]]
43.0554

N[-30 (LogIntegral[1/30] - EulerGamma - Log[Log[30]]) -
  (LogIntegral[30] - EulerGamma - Log[Log[30]])]
43.0554

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N[(30 + 1) ( EulerGamma + Log[Log[30]] ) - 30 LogIntegral[1 / 30] - LogIntegral[30]]
```

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43.0554
```

```
N[Integrate[( LogIntegral[ 130 / x ] - EulerGamma - Log[Log[130 / x]]), {x, 1, 130}]]
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246.655
```

```
N[(130 + 1) ( EulerGamma + Log[Log[130]] ) - 130 LogIntegral[1 / 130] - LogIntegral[130]]
```

```
246.655
```

```
Integrate[( LogIntegral[ 130 / x ]), {x, 1, 130}]
```

```
130 EulerGamma + 130 Log[Log[130]] - LogIntegral[130]
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