

```

Dk[n_, k_, s_] := Sum[j^-s Dk[n / j, k - 1, s], {j, 1, n}]; Dk[n_, 0, s_] := UnitStep[n - 1]
Table[Dk[n, k, 0], {n, 1, 50}, {k, 1, 7}] // TableForm

```

1	1	1	1	1	1	1
2	3	4	5	6	7	8
3	5	7	9	11	13	15
4	8	13	19	26	34	43
5	10	16	23	31	40	50
6	14	25	39	56	76	99
7	16	28	43	61	82	106
8	20	38	63	96	138	190
9	23	44	73	111	159	218
10	27	53	89	136	195	267
11	29	56	93	141	201	274
12	35	74	133	216	327	470
13	37	77	137	221	333	477
14	41	86	153	246	369	526
15	45	95	169	271	405	575
16	50	110	204	341	531	785
17	52	113	208	346	537	792
18	58	131	248	421	663	988
19	60	134	252	426	669	995
20	66	152	292	501	795	1191
21	70	161	308	526	831	1240
22	74	170	324	551	867	1289
23	76	173	328	556	873	1296
24	84	203	408	731	1209	1884
25	87	209	418	746	1230	1912
26	91	218	434	771	1266	1961
27	95	228	454	806	1322	2045
28	101	246	494	881	1448	2241
29	103	249	498	886	1454	2248
30	111	276	562	1011	1670	2591
31	113	279	566	1016	1676	2598
32	119	300	622	1142	1928	3060
33	123	309	638	1167	1964	3109
34	127	318	654	1192	2000	3158
35	131	327	670	1217	2036	3207
36	140	363	770	1442	2477	3991
37	142	366	774	1447	2483	3998
38	146	375	790	1472	2519	4047
39	150	384	806	1497	2555	4096
40	158	414	886	1672	2891	4684
41	160	417	890	1677	2897	4691
42	168	444	954	1802	3113	5034
43	170	447	958	1807	3119	5041
44	176	465	998	1882	3245	5237
45	182	483	1038	1957	3371	5433
46	186	492	1054	1982	3407	5482
47	188	495	1058	1987	3413	5489
48	198	540	1198	2337	4169	6959
49	201	546	1208	2352	4190	6987
50	207	564	1248	2427	4316	7183

```

Dk[n_, k_, s_] := Dk[n, k, s] = Sum[j^(-s) Dk[Floor[n / j], k - 1, s], {j, 1, n}];
Dk[n_, 0, s_] := UnitStep[n - 1]
Grid[Table[Chop[Dk[30 000, k, s] - N[Zeta[s]^k]], {k, 1, 3}, {s, 2, 4, .5}]]

-0.0000333328  -1.28297 × 10-7  -5.55533 × 10-10      0      0
-0.00041542   -1.55614 × 10-6  -6.64545 × 10-9      0      0
-0.00284113   -0.0000103484  -4.35834 × 10-8   -1.98172 × 10-10  0

Dk1[n_, s_] := Sum[j^(-s), {j, 1, n}]
Dk2[n_, s_] := Sum[j^(-s) k^(-s), {j, 1, n}, {k, 1, n / j}]
Dk3[n_, s_] := Sum[j^(-s) k^(-s) m^(-s), {j, 1, n}, {k, 1, n / j}, {m, 1, n / (j k)}]
Dk[n_, k_, s_] := Sum[j^(-s) Dk[n / j, k - 1, s], {j, 1, n}]; Dk[n_, 0, s_] := UnitStep[n - 1]
FullSimplify[
  Table[{Dk1[n, s] - Dk[n, 1, s], Dk2[n, s] - Dk[n, 2, s], Dk3[n, s] - Dk[n, 3, s]}, {n, 1, 50}] //
  TableForm]

```


Dk[5, 2, s]

$$1 + 2^{1-2s} + 2^{-s} + 2 \times 3^{-s} + 2 \times 5^{-s} + 2^{-s} (1 + 2^{-s})$$

dk[n_, k_, s_] := Sum[dk[j, 1, s] dk[n/j, k-1, s], {j, Divisors[n]}];

dk[n_, 1, s_] := n^-s; dk[n_, 0, s_] := 0; dk[1, 0, s_] := 1

Dk[n_, k_, s_] := Sum[j^-s Dk[n/j, k-1, s], {j, 1, n}]; Dk[n_, 0, s_] := UnitStep[n-1]

FullSimplify[Grid[Table[dk[n, k, s] - (Dk[n, k, s] - Dk[n-1, k, s]), {n, 1, 50, 5}, {k, 1, 5}]]]

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

0 0 0 0 0

Dmy[n_, k_, s_, y_] := Sum[(j+y)^-s Dmy[n(j+y)^-1, k-1, s, y], {j, 1, n-y}];

Dmy[n_, 0, s_, y_] := UnitStep[n-1]

Grid[Table[Chop[Dmy[30000, k, s, y] - N[Zeta[s, y+1]^k]], {k, 1, 3}, {s, 2, 4}, {y, 1, 4}]]

{-0.0000333328, -0.0000333328,
-0.0000333328, -0.0000333328}

{-0.000348755, -0.000315423,
-0.000293201, -0.000276536}

{-0.00169487, -0.00123141,
-0.000963755, -0.000784785}

$\{-5.55537 \times 10^{-10}, -5.55537 \times 10^{-10},$
 $-5.55537 \times 10^{-10}, -5.55537 \times 10^{-10}\}$

$\{-5.53439 \times 10^{-9}, -4.97887 \times 10^{-9},$
 $-4.60854 \times 10^{-9}, -4.3308 \times 10^{-9}\}$

$\{-2.53136 \times 10^{-8}, -1.8007 \times 10^{-8},$
 $-1.38248 \times 10^{-8}, -1.1051 \times 10^{-8}\}$

{0, 0, 0, 0}

{0, 0, 0, 0}

{0, 0, 0, 0}

Dmy[1000, 1, 2, 1]

999

Limit[(n^z - n^0) z^-1, z -> 0]

Log[n]

Limit[(nz^-1 + n^0)^z, z -> Infinity]

e^n

Limit[(nz + n^0)^(z^-1), z -> 0]

e^n

dz[n_, z_] := dz[n, z] = Product[(-1)^p[[2]] Binomial[-z, p[[2]]], {p, FI[n]}];

FI[n_] := FactorInteger[n]; FI[1] := {}

Dz[n_, z_] := Dz[n, z] = Sum[dz[j, z], {j, 1, n}]

bin[z_, k_] := Product[z-j, {j, 0, k-1}] / k!

dd[n_, k_, x_] := dd[n, k, x] = x Sum[dd[n(jx)^-1, k-1, x], {j, 1, nx^-1}];

dd[n_, 0, x_] := UnitStep[n-1]

dda[n_, k_, x_] := x^k Dz[Floor[n/(x^k)], k]

bd[n_, z_, x_] := Sum[bin[z, k] dd[n, k, x], {k, 0, Log[x, n]}]

bda[n_, z_, x_] := Sum[bin[z, k] If[bin[z, k] == 0, 0, dda[n, k, x]], {k, 0, Log[x, n]}]

DiscretePlot[Expand[D[bda[n, z, 1.05], z]] /. z -> 0, {n, 2, 20}]

```
dd[1527, 4, 4.3]
```

```
6495.72
```

```
dda[1527, 4, 4.3]
```

```
6495.72
```

```
DiscretePlot[bda[n, -1, 1.1], {n, 2, 100}]
```

```
dd[1, 1, 1.00000001]
```

```
0.
```

```
bda[100, 1, 1.01]
```

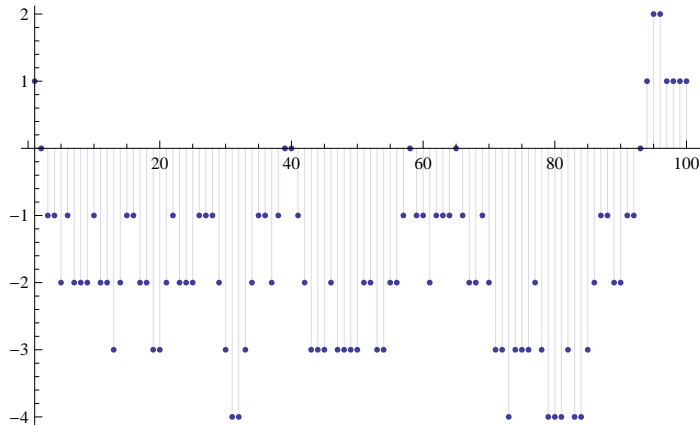
```
100.99
```

```
D2[n_, k_] := D2[n, k] = Sum[ D2[Floor[n / j], k - 1], {j, 2, n}]; D2[n_, 0] := UnitStep[n - 1]
```

```
D2a[n_, z_] := Sum[ Binomial[ z, k] D2[n, k], {k, 0, Log[2, n]}]
```

```
D2b[n_, z_] := Sum[ (-1)^k Binomial[ z, k] D2[n, k], {k, 0, Log[2, n]}]
```

```
DiscretePlot[ D2a[n, -1], {n, 1, 100}]
```



```
D2a[1, 2]
```

```
1
```

```
E2a[n_, k_, x_, s_] := E2a[n, k, x, s] = Sum[ j^(-s) E2a[n / j, k - 1, x, s], {j, 2, n}] -  
x Sum[ (j x)^(-s) E2a[n / (x j), k - 1, x, s], {j, 1, n / x}];
```

```
E2a[n_, 0, a_, s_] := UnitStep[n - 1]
```

```
E2ab[n_, k_, x_, s_] := E2ab[n, k, x, s] =
```

```
Sum[ (j + 1)^(-s) E2ab[n / (j + 1), k - 1, x, s] - x (j x)^(-s) E2ab[n / (x j), k - 1, x, s],  
{j, 1, n - 1}]; E2ab[n_, 0, a_, s_] := UnitStep[n - 1]
```

```
E1a[n_, k_, x_, s_] := E1a[n, k, x, s] = Sum[ j^(-s) E1a[n / j, k - 1, x, s], {j, 1, n}] -  
x Sum[ (j x)^(-s) E1a[n / (x j), k - 1, x, s], {j, 1, n / x}];
```

```
E1a[n_, 0, a_, s_] := UnitStep[n - 1]
```

```
E1ab[n_, k_, x_, s_] := E1ab[n, k, x, s] =
```

```
Sum[ j^(-s) E1ab[n / j, k - 1, x, s] - x (j x)^(-s) E1ab[n / (x j), k - 1, x, s], {j, 1, n}];
```

```
E1ab[n_, 0, a_, s_] := UnitStep[n - 1]
```

E1a[1, 1, 2, 0]

1

E2a[1, 1, 2, 0]

0

Series[E^ {x+1} ^2, {x, 0, 10}]

$$\left\{ e + 2ex + 3ex^2 + \frac{10ex^3}{3} + \frac{19ex^4}{6} + \frac{13ex^5}{5} + \frac{173ex^6}{90} + \frac{407ex^7}{315} + \frac{45ex^8}{56} + \frac{5281ex^9}{11340} + \frac{28787ex^{10}}{113400} + O[x]^{11} \right\}$$

D2[n_, k_] := D2[n, k] = Sum[D2[Floor[n / j], k - 1], {j, 2, n}]; D2[n_, 0] := UnitStep[n - 1]

dz[n_, z_] := dz[n, z] = Product[(-1) ^p[[2]] Binomial[-z, p[[2]]], {p, FI[n]}];

FI[n_] := FactorInteger[n]; FI[1] := {}

Dz[n_, z_] := Dz[n, z] = Sum[dz[j, z], {j, 1, n}]

F[n_, z_, t_] := Sum[z^k / k! Dz[n, k], {k, 0, t}]

F2[n_, z_] := Sum[E^z z^k / k! D2[n, k], {k, 0, Log[2, n]}]; F2[n_, 0] := UnitStep[n - 1]

F3[n_, z_] := Sum[z^k / k! D2[n, k], {k, 0, Log[2, n]}]; F3[n_, 0] := UnitStep[n - 1]

F33[n_, k_] := Sum[(-1) ^ (k - j) Binomial[k, j] F3[n, j], {j, 0, k}]

DF[n_] := Sum[(-1) ^ (k + 1) / k F33[n, k], {k, 1, Log[2, n]}]

F33[n_, 0] := UnitStep[n - 1]

N[F[100, -1, 30]]

-1.1951

N[F2[100, 1]]

825.274

N[E^2 F3[100, 2]]

9856.18

F33[100, 7]

0

F2[100, 2]

$$\frac{12005e^2}{9}$$

DF[100]

99

Limit[(nx^-1 + x^0) ^x, x → Infinity]

e^n

```

L2[n_, 1, b_] := L2[n, 1, b] = Sum[Log[j], {j, 2, n}] - b Sum[Log[j b], {j, 1, n/b}]
L2[n_, k_, b_] := Sum[L2[n/j, k-1, b], {j, 2, n}] - b Sum[L2[n/(j b), k-1, b], {j, 1, n}]
E2a[n_, k_, x_, s_] := E2a[n, k, x, s] = Sum[j^(-s) E2a[n/j, k-1, x, s], {j, 2, n}] -
  x Sum[(j x)^(-s) E2a[n/(x j), k-1, x, s], {j, 1, n/x}];
E2a[n_, 0, a_, s_] := UnitStep[n-1]

```

```

{N[L2[20, 1, 2]], N[-D[E2a[20, 1, 2, s], s] /. s -> 0]}

```

```

{-1.73615, -1.73615}

```

```

{N[L2[20, 2, 2]], N[-D[E2a[20, 2, 2, s], s] /. s -> 0] / 2}

```

```

{-1.77601, -1.77601}

```

```

{N[L2[20, 3, 2]], N[-D[E2a[20, 3, 2, s], s] /. s -> 0] / 3}

```

```

{-0.875469, -0.875469}

```

```

f[n_, k_, s_, x_] := Sum[j^(-s) (k^(-1) - f[n j^(-1), k+1, s, x]), {j, 2, n}] -
  x Sum[(j x)^(-s) (k^(-1) - f[n (j x)^(-1), k+1, s, x]), {j, 1, n/x}]

```

```

N[D[f[100, 1, s, 2], s] /. s -> 0]

```

```

-6.70877

```

```

Dly1[x_, s_, k_, y_] :=

```

```

  Dly1[x, s, k-1, y] + y Sum[(1+j y)^(-s) Dly1[x (1+j y)^(-1), s, k-1, y], {j, 1, (x-1)/y}];

```

```

Dly1[x_, s_, 0, y_] := UnitStep[x-1]

```

```

Dly[x_, s_, k_, y_] := y Sum[(1+j y)^(-s) Dly[x (1+j y)^(-1), s, k-1, y], {j, 1, (x-1)/y}];

```

```

Dly[x_, s_, 0, y_] := UnitStep[x-1]

```

```

FullSimplify[y^(z (1-s)) Sum[(j+y^(-1))^(-z s), {j, 1, Infinity}] /. {y -> 2, z -> 2, s -> 2}]

```

```

-4 +  $\frac{\pi^4}{24}$ 

```

```

Expand[(y^(1-s) Zeta[s, 1+y^(-1)])^z /. {y -> 2, z -> 2, s -> 2}]

```

```

4 -  $\pi^2$  +  $\frac{\pi^4}{16}$ 

```

```

Expand[(y^(z (1-s)) Zeta[s, 1+y^(-1)])^z /. {y -> 2, z -> 2, s -> 2}]

```

```

4 -  $\pi^2$  +  $\frac{\pi^4}{16}$ 

```

```

Expand[

```

```

  (y^(z (1-s)) (Sum[1/(j+1+y^(-1))^s, {j, 0, Infinity}])^z) /. {y -> 2, z -> 2, s -> 2}]

```

```

4 -  $\pi^2$  +  $\frac{\pi^4}{16}$ 

```

```

Expand[(y^(z (1-s)) (Sum[(j+y^(-1))^(-s), {j, 1, Infinity}])^z) /. {y -> 2, z -> 2, s -> 2}]

```

```

4 -  $\pi^2$  +  $\frac{\pi^4}{16}$ 

```

$$(j+y^{-1})^{-s} (j+y^{-1})^{-s}$$

$$\left(j + \frac{1}{y}\right)^{-2s}$$

$$\text{Expand}[(1+y^{-1})^{-s} + (2+y^{-1})^{-s} + (3+y^{-1})^{-s} + (4+y^{-1})^{-s} + (5+y^{-1})^{-s}]^2$$

$$\begin{aligned} & \left(1 + \frac{1}{y}\right)^{-2s} + \left(2 + \frac{1}{y}\right)^{-2s} + 2 \left(1 + \frac{1}{y}\right)^{-s} \left(2 + \frac{1}{y}\right)^{-s} + \left(3 + \frac{1}{y}\right)^{-2s} + 2 \left(1 + \frac{1}{y}\right)^{-s} \left(3 + \frac{1}{y}\right)^{-s} + \\ & 2 \left(2 + \frac{1}{y}\right)^{-s} \left(3 + \frac{1}{y}\right)^{-s} + \left(4 + \frac{1}{y}\right)^{-2s} + 2 \left(1 + \frac{1}{y}\right)^{-s} \left(4 + \frac{1}{y}\right)^{-s} + 2 \left(2 + \frac{1}{y}\right)^{-s} \left(4 + \frac{1}{y}\right)^{-s} + 2 \left(3 + \frac{1}{y}\right)^{-s} \left(4 + \frac{1}{y}\right)^{-s} + \\ & \left(5 + \frac{1}{y}\right)^{-2s} + 2 \left(1 + \frac{1}{y}\right)^{-s} \left(5 + \frac{1}{y}\right)^{-s} + 2 \left(2 + \frac{1}{y}\right)^{-s} \left(5 + \frac{1}{y}\right)^{-s} + 2 \left(3 + \frac{1}{y}\right)^{-s} \left(5 + \frac{1}{y}\right)^{-s} + 2 \left(4 + \frac{1}{y}\right)^{-s} \left(5 + \frac{1}{y}\right)^{-s} \end{aligned}$$

$$D[\text{Sum}[(j+y^{-1})^{-s}, \{j, 1, 10\}]^2, y]$$

$$\begin{aligned} & 2 \left(\left(1 + \frac{1}{y}\right)^{-s} + \left(2 + \frac{1}{y}\right)^{-s} + \left(3 + \frac{1}{y}\right)^{-s} + \left(4 + \frac{1}{y}\right)^{-s} + \right. \\ & \quad \left. \left(5 + \frac{1}{y}\right)^{-s} + \left(6 + \frac{1}{y}\right)^{-s} + \left(7 + \frac{1}{y}\right)^{-s} + \left(8 + \frac{1}{y}\right)^{-s} + \left(9 + \frac{1}{y}\right)^{-s} + \left(10 + \frac{1}{y}\right)^{-s} \right) \\ & \left(\frac{s \left(1 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(2 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(3 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(4 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(5 + \frac{1}{y}\right)^{-1-s}}{y^2} + \right. \\ & \quad \left. \frac{s \left(6 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(7 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(8 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(9 + \frac{1}{y}\right)^{-1-s}}{y^2} + \frac{s \left(10 + \frac{1}{y}\right)^{-1-s}}{y^2} \right) \end{aligned}$$

$$D[y^k (1-s) \text{Sum}[(j+y^{-1})^{-s}, \{j, 1, 10\}]^k, y] /. s \rightarrow 0$$

$$10^k k y^{-1+k}$$

$$D1[n_, z_, k_, s_] :=$$

$$D1[n, z, k, s] = 1 + ((z+1)/k-1) \text{Sum}[j^{-s} D1[n/j, z, k+1, s], \{j, 2, n\}]$$

$$\text{Limit}[\text{Limit}[D[D1[100, z, 1, s], z], z \rightarrow 0], s \rightarrow 0]$$

$$-\text{Limit}[D[N[\text{Limit}[D[D1[100, z, 1, s], z], z \rightarrow 0]], s], s \rightarrow 0]$$

$$\frac{428}{15}$$

$$94.0453$$

$$0$$

$$f1[n_, k_, s_] := \text{Sum}[j^{-s} (k^{-1} - f1[n/j, k+1, s]), \{j, 2, n\}]$$

$$N[\text{Limit}[D[f1[100, 1, s], s], s \rightarrow 0]]$$

$$-94.0453$$

$$s1[n_, k_, y_, s_] := s1[n, k, y, s] =$$

$$y \text{Sum}[(jy+1)^{-s} (k^{-1} - s1[n/(jy+1), k+1, y, s]), \{j, 1, (n-1)/y\}]$$


```
-N[D[s1[100, 1, .5, s], s] /. s -> 0]
```

```
95.6424
```

```
ml[n_, k_] := Sum[MoebiusMu[d] (Log[n/d])^k, {d, Divisors[n]}]
```

```
FullSimplify[ml[210, 4]]
```

```
24 Log[2] Log[3] Log[5] Log[7]
```

```
dz[n_, z_, s_] := n^-s Product[(-1)^p[[2]] Binomial[-z, p[[2]]], {p, FI[n]}];
```

```
FI[n_] := FactorInteger[n]; FI[1] := {}
```

```
D[Limit[D[dz[210, z, s], {s, 4}], s -> 0], {z}]
```

```
4 z^3 Log[210]^4
```

```
D[dz[2*3, z, 0], {z, 2}] /. z -> 0
```

```
2
```

```
dz[n_, z_, s_] :=
```

```
dz[n, z, s] = If[n < 1, 0, n^-s Product[(-1)^p[[2]] Binomial[-z, p[[2]]], {p, FI[n]}]];
```

```
FI[n_] := FactorInteger[n]; FI[1] := {}
```

```
Dz[n_, z_, s_] := Dz[n, z, s] = Sum[dz[j, z, s], {j, 1, n}]
```

```
Sum[dz[j, 1, -2] Dz[1000 j^-2, -1, -1], {j, 1, 1000^(1/2)}]
```

```
-1274
```

```
Sum[dz[j, -1, -1] Dz[Floor[(1000/j)^(1/2)], 1, -2], {j, 1, 1000}]
```

```
-1274
```

```
Sum[LiouvilleLambda[j] j^1, {j, 1, 1000}]
```

```
-1274
```

```
Sum[dz[j, 1, -1] Dz[Floor[(1000/j)^(1/2)], -1, -2], {j, 1, 1000}]
```

```
303076
```

```
Sum[MoebiusMu[j]^2 j^1, {j, 1, 1000}]
```

```
303076
```

```
FullSimplify[2^s / 3^(2s)]
```

$$\left(\frac{2}{9}\right)^s$$

```
Expand[Sum[MoebiusMu[n] (n^-s) (m^(-2s)), {n, 1, 6}, {m, 1, 6}]]
```

$$1 - 2^{-5s} - 2^{-3s} + 2^{-2s} - 2^{-s} - 3^{-3s} - 2^{-2s} 3^{-3s} + 2^{-s} 3^{-3s} + 3^{-2s} - 2^{-3s} 3^{-2s} - 2^{-s} 3^{-2s} - 3^{-s} + 2^{-5s} 3^{-s} + 2^{-3s} 3^{-s} - 2^{-2s} 3^{-s} + 4^{-2s} - 3^{-s} 4^{-2s} - 5^{-3s} + 5^{-2s} - 2^{-s} 5^{-2s} - 3^{-s} 5^{-2s} - 5^{-s} - 2^{-2s} 5^{-s} - 3^{-2s} 5^{-s} - 4^{-2s} 5^{-s} + 6^{-3s} + 6^{-2s} - 5^{-s} 6^{-2s} + 6^{-s} + 5^{-2s} 6^{-s}$$

```
Table[{n, MoebiusMu[n]}, {n, 1, 20}]
```

```
{{1, 1}, {2, -1}, {3, -1}, {4, 0}, {5, -1}, {6, 1}, {7, -1}, {8, 0}, {9, 0}, {10, 1}, {11, -1}, {12, 0}, {13, -1}, {14, 1}, {15, 1}, {16, 0}, {17, -1}, {18, 0}, {19, -1}, {20, 0}}
```

```

1 / 2 ^ (2 s) (-1 / 2 ^ s)
- 2 ^ -3 s
3 ^ (2 s) × 2 ^ s
2 ^ s 3 ^ 2 s
tt[n_] := Sum[ If[ Floor[j^(1/2)] == j^(1/2), 1, 0] MoebiusMu[n/j], {j, Divisors[n]}]
Table[ Sum[ LiouvilleLambda[j], {j, Divisors[n]}], {n, 1, 30}]
{1, 0, 0, 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0}
Table[tt[n] - LiouvilleLambda[n], {n, 1, 30}]
{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0}
Sum[ Floor[(300/j)^(1/2)] MoebiusMu[j], {j, 1, 300}]
-16
Sum[ LiouvilleLambda[j], {j, 1, 300}]
-16
Sum[ MoebiusMu[n] x^n / (1 - x^n), {n, 1, Infinity}]
x
Sum[LiouvilleLambda[n] x^n / (1 - x^n), {n, 1, Infinity}]

$$\sum_{n=1}^{\infty} \frac{x^n \text{LiouvilleLambda}[n]}{1 - x^n}$$

Table[ {n, Sum[ dz[j^2, 2, 0], {j, Divisors[n]}], dz[n, 2, 0]^2}, {n, 1, 30}]
{{1, 1, 1}, {2, 4, 4}, {3, 4, 4}, {4, 9, 9}, {5, 4, 4}, {6, 16, 16},
{7, 4, 4}, {8, 16, 16}, {9, 9, 9}, {10, 16, 16}, {11, 4, 4}, {12, 36, 36},
{13, 4, 4}, {14, 16, 16}, {15, 16, 16}, {16, 25, 25}, {17, 4, 4}, {18, 36, 36},
{19, 4, 4}, {20, 36, 36}, {21, 16, 16}, {22, 16, 16}, {23, 4, 4}, {24, 64, 64},
{25, 9, 9}, {26, 16, 16}, {27, 16, 16}, {28, 36, 36}, {29, 4, 4}, {30, 64, 64}}
Table[ {n, Sum[ MoebiusMu[n/j] dz[j, 2, 0]^2, {j, Divisors[n]}], dz[n^2, 2, 0]}, {n, 1, 30}]
{{1, 1, 1}, {2, 3, 3}, {3, 3, 3}, {4, 5, 5}, {5, 3, 3}, {6, 9, 9}, {7, 3, 3}, {8, 7, 7}, {9, 5, 5},
{10, 9, 9}, {11, 3, 3}, {12, 15, 15}, {13, 3, 3}, {14, 9, 9}, {15, 9, 9}, {16, 9, 9},
{17, 3, 3}, {18, 15, 15}, {19, 3, 3}, {20, 15, 15}, {21, 9, 9}, {22, 9, 9}, {23, 3, 3},
{24, 21, 21}, {25, 5, 5}, {26, 9, 9}, {27, 7, 7}, {28, 15, 15}, {29, 3, 3}, {30, 27, 27}}
Table[Sum[ dz[j^3, 5, 0], {j, Divisors[n]}], {n, 1, 30}]
{1, 36, 36, 246, 36, 1296, 36, 961, 246, 1296, 36, 8856, 36, 1296, 1296, 2781,
36, 8856, 36, 8856, 1296, 1296, 36, 34596, 246, 1296, 961, 8856, 36, 46656}
bin[z_, k_] := Product[z - j, {j, 0, k - 1}] / k!
d2[n_, k_] := Sum[ d2[n/j, k - 1], {j, 2, n}]; d2[n_, 0] := UnitStep[n - 1]
d2z[n_, z_] := Sum[ bin[z, k] d2[n, k], {k, 0, Log[2, n]}]
dd2z[n_, z_] := d2z[n, z] - d2z[n - 1, z]
d3[n_, k_] := Sum[ d3[n/j, k - 1], {j, 3, n}]; d3[n_, 0] := UnitStep[n - 1]
d3z[n_, z_] := Sum[ bin[z, k] d3[n, k], {k, 0, Log[3, n]}]
dd3z[n_, z_] := d3z[n, z] - d3z[n - 1, z]
da[n_, k_, a_] := Sum[ da[n/(j + a), k - 1, a], {j, 1, n}]; da[n_, 0, a_] := UnitStep[n - 1]
daz[n_, z_, a_] := Sum[ bin[z, k] da[n, k, a], {k, 0, Log[a + 1, n]}]
ddaz[n_, z_, a_] := daz[n, z, a] - daz[n - 1, z, a]

```

```
Expand[Table[{n, (ddaz[n, z, 1])}, {n, 2, 100}] // TableForm]
```

2	z
3	z
4	$z + \frac{1}{2} (-1 + z) z$
5	z
6	$z + (-1 + z) z$
7	z
8	$z + (-1 + z) z + \frac{1}{6} (-2 + z) (-1 + z) z$
9	$z + \frac{1}{2} (-1 + z) z$
10	$z + (-1 + z) z$
11	z
12	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
13	z
14	$z + (-1 + z) z$
15	$z + (-1 + z) z$
16	$z + \frac{3}{2} (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z + \frac{1}{24} (-3 + z) (-2 + z) (-1 + z) z$
17	z
18	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
19	z
20	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
21	$z + (-1 + z) z$
22	$z + (-1 + z) z$
23	z
24	$z + 3 (-1 + z) z + \frac{3}{2} (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z$
25	$z + \frac{1}{2} (-1 + z) z$
26	$z + (-1 + z) z$
27	$z + (-1 + z) z + \frac{1}{6} (-2 + z) (-1 + z) z$
28	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
29	z
30	$z + 3 (-1 + z) z + (-2 + z) (-1 + z) z$
31	z
32	$z + 2 (-1 + z) z + (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z + \frac{1}{120} (-4 + z) (-3 + z) (-2 + z)$
33	$z + (-1 + z) z$
34	$z + (-1 + z) z$
35	$z + (-1 + z) z$
36	$z + \frac{7}{2} (-1 + z) z + 2 (-2 + z) (-1 + z) z + \frac{1}{4} (-3 + z) (-2 + z) (-1 + z) z$
37	z
38	$z + (-1 + z) z$
39	$z + (-1 + z) z$
40	$z + 3 (-1 + z) z + \frac{3}{2} (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z$
41	z
42	$z + 3 (-1 + z) z + (-2 + z) (-1 + z) z$
43	z
44	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
45	$z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
46	$z + (-1 + z) z$
47	z
48	$z + 4 (-1 + z) z + 3 (-2 + z) (-1 + z) z + \frac{2}{3} (-3 + z) (-2 + z) (-1 + z) z + \frac{1}{24} (-4 + z) (-3 + z) (-2 + z)$

49 $z + \frac{1}{2} (-1 + z) z$
 50 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 51 $z + (-1 + z) z$
 52 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 53 z
 54 $z + 3 (-1 + z) z + \frac{3}{2} (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z$
 55 $z + (-1 + z) z$
 56 $z + 3 (-1 + z) z + \frac{3}{2} (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z$
 57 $z + (-1 + z) z$
 58 $z + (-1 + z) z$
 59 z
 60 $z + 5 (-1 + z) z + \frac{7}{2} (-2 + z) (-1 + z) z + \frac{1}{2} (-3 + z) (-2 + z) (-1 + z) z$
 61 z
 62 $z + (-1 + z) z$
 63 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 64 $z + \frac{5}{2} (-1 + z) z + \frac{5}{3} (-2 + z) (-1 + z) z + \frac{5}{12} (-3 + z) (-2 + z) (-1 + z) z + \frac{1}{24} (-4 + z) (-3 + z) (-2 + z)$
 65 $z + (-1 + z) z$
 66 $z + 3 (-1 + z) z + (-2 + z) (-1 + z) z$
 67 z
 68 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 69 $z + (-1 + z) z$
 70 $z + 3 (-1 + z) z + (-2 + z) (-1 + z) z$
 71 z
 72 $z + 5 (-1 + z) z + \frac{9}{2} (-2 + z) (-1 + z) z + \frac{7}{6} (-3 + z) (-2 + z) (-1 + z) z + \frac{1}{12} (-4 + z) (-3 + z) (-2 + z)$
 73 z
 74 $z + (-1 + z) z$
 75 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 76 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 77 $z + (-1 + z) z$
 78 $z + 3 (-1 + z) z + (-2 + z) (-1 + z) z$
 79 z
 80 $z + 4 (-1 + z) z + 3 (-2 + z) (-1 + z) z + \frac{2}{3} (-3 + z) (-2 + z) (-1 + z) z + \frac{1}{24} (-4 + z) (-3 + z) (-2 + z)$
 81 $z + \frac{3}{2} (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z + \frac{1}{24} (-3 + z) (-2 + z) (-1 + z) z$
 82 $z + (-1 + z) z$
 83 z
 84 $z + 5 (-1 + z) z + \frac{7}{2} (-2 + z) (-1 + z) z + \frac{1}{2} (-3 + z) (-2 + z) (-1 + z) z$
 85 $z + (-1 + z) z$
 86 $z + (-1 + z) z$
 87 $z + (-1 + z) z$
 88 $z + 3 (-1 + z) z + \frac{3}{2} (-2 + z) (-1 + z) z + \frac{1}{6} (-3 + z) (-2 + z) (-1 + z) z$
 89 z
 90 $z + 5 (-1 + z) z + \frac{7}{2} (-2 + z) (-1 + z) z + \frac{1}{2} (-3 + z) (-2 + z) (-1 + z) z$
 91 $z + (-1 + z) z$
 92 $z + 2 (-1 + z) z + \frac{1}{2} (-2 + z) (-1 + z) z$
 93 $z + (-1 + z) z$
 94 $z + (-1 + z) z$
 95 $z + (-1 + z) z$
 96 $z + 5 (-1 + z) z + 5 (-2 + z) (-1 + z) z + \frac{5}{3} (-3 + z) (-2 + z) (-1 + z) z + \frac{5}{24} (-4 + z) (-3 + z) (-2 + z)$

```

97      z
98      z + 2 (-1 + z) z +  $\frac{1}{2}$  (-2 + z) (-1 + z) z
99      z + 2 (-1 + z) z +  $\frac{1}{2}$  (-2 + z) (-1 + z) z
100     z +  $\frac{7}{2}$  (-1 + z) z + 2 (-2 + z) (-1 + z) z +  $\frac{1}{4}$  (-3 + z) (-2 + z) (-1 + z) z

bin[z_, k_] := Product[z - j, {j, 0, k - 1}] / k!
E2a[n_, k_, x_, s_] := E2a[n, k, x, s] = Sum[ j^(-s) E2a[n / j, k - 1, x, s], {j, 2, n}] -
  x Sum[ (j x)^(-s) E2a[n / (x j), k - 1, x, s], {j, 1, n / x}];
E2a[n_, 0, a_, s_] := UnitStep[n - 1]
E1[n_, z_, x_, s_] :=
  E1[n, z, x, s] = Sum[ bin[z, k] E2a[n, k, x, s], {k, 0, Log[If[x < 2, x, 2], n]}]
e1[n_, z_, x_, s_] := E1[n, z, x, s] - E1[n - 1, z, x, s]

Expand[e1[100, z, 2, 0]]


$$-\frac{3 z^2}{4} - \frac{z^3}{2} + \frac{z^4}{4}$$


Expand[e1[100, z, 1.05, 0]]

0. - 9.77707 × 10-11 z - 1.34015 z2 + 3.89813 z3 - 7.32015 z4 + 9.36244 z5 - 8.6053 z6 + 6.55789 z7 -
  4.04874 z8 + 2.12208 z9 - 0.943584 z10 + 0.35776 z11 - 0.116825 z12 + 0.0332317 z13 -
  0.00832691 z14 + 0.00185612 z15 - 0.000371057 z16 + 0.000069551 z17 - 0.0000109615 z18 +
  1.63515 × 10-6 z19 - 2.23076 × 10-7 z20 + 2.79247 × 10-8 z21 - 3.21707 × 10-9 z22 + 3.42029 × 10-10 z23 -
  3.36434 × 10-11 z24 + 3.06896 × 10-12 z25 - 2.60182 × 10-13 z26 + 2.05409 × 10-14 z27 -
  1.51286 × 10-15 z28 + 1.04118 × 10-16 z29 - 6.70546 × 10-18 z30 + 4.04648 × 10-19 z31 -
  2.29074 × 10-20 z32 + 1.21779 × 10-21 z33 - 6.08504 × 10-23 z34 + 2.86024 × 10-24 z35 -
  1.2656 × 10-25 z36 + 5.27494 × 10-27 z37 - 2.07205 × 10-28 z38 + 7.67436 × 10-30 z39 - 2.6811 × 10-31 z40 +
  8.83783 × 10-33 z41 - 2.74945 × 10-34 z42 + 8.07395 × 10-36 z43 - 2.23826 × 10-37 z44 +
  5.85776 × 10-39 z45 - 1.44721 × 10-40 z46 + 3.37492 × 10-42 z47 - 7.42757 × 10-44 z48 +
  1.5423 × 10-45 z49 - 3.02052 × 10-47 z50 + 5.57704 × 10-49 z51 - 9.70324 × 10-51 z52 +
  1.58987 × 10-52 z53 - 2.45152 × 10-54 z54 + 3.55461 × 10-56 z55 - 4.84212 × 10-58 z56 +
  6.19036 × 10-60 z57 - 7.41862 × 10-62 z58 + 8.32305 × 10-64 z59 - 8.72862 × 10-66 z60 +
  8.54243 × 10-68 z61 - 7.78695 × 10-70 z62 + 6.59739 × 10-72 z63 - 5.18256 × 10-74 z64 +
  3.76433 × 10-76 z65 - 2.52024 × 10-78 z66 + 1.54968 × 10-80 z67 - 8.71547 × 10-83 z68 +
  4.46166 × 10-85 z69 - 2.06732 × 10-87 z70 + 8.61236 × 10-90 z71 - 3.20003 × 10-92 z72 +
  1.05016 × 10-94 z73 - 3.0071 × 10-97 z74 + 7.3977 × 10-100 z75 - 1.532 × 10-102 z76 + 2.59716 × 10-105 z77 -
  3.46094 × 10-108 z78 + 3.3995 × 10-111 z79 - 2.18828 × 10-114 z80 + 6.92494 × 10-118 z81

ff[n_] := (Sign[Abs[n] - 1] + 1) / 2

fp[k_] := Sum[ Binomial[k, j] BernoulliB[k - j] / (j + 1) n^(j + 1), {j, 0, k}]

FullSimplify[fp[3]]


$$\frac{1}{4} (-1 + n)^2 n^2$$


fa[n_, a_] := N[(Sin[n] + (3 n - 3)^(1 / 2) - 1) Sum[
  BernoulliB[k] / k! D[ ((Sin[n] + (3 n - 3)^(1 / 2)) ^ z), {z, k + a - 1}] /. z → 0, {k, 0, 200}]]

fa[100, 3]

22.3553

```

```
bin[z_, k_] := Product[z - j, {j, 0, k - 1}] / k!
```

```
D2[n_, k_, s_] := D2[n, k, s] = Sum[j^(-s) D2[Floor[n / j], k - 1, s], {j, 2, n}];
```

```
D2[n_, 0, s_] := 1
```

```
Dz[n_, z_, s_] := Sum[bin[z, k] D2[n, k, s], {k, 0, Log[2, n]}]
```

```
1 + Integrate[D[Dz[100, z, 0], z], {z, 0, 1}]
```

```
100
```

```
Dz[100, 3, 0]
```

```
1471
```

```
Expand[D[Dz[100, z, 0], z]]
```

$$\frac{428}{15} + \frac{16289z}{180} + \frac{993z^2}{16} + \frac{611z^3}{36} + \frac{67z^4}{48} + \frac{7z^5}{120}$$

```
FullSimplify[D[Dz[100, z, s], z] /. z -> 0]
```

$$\begin{aligned} & \frac{1}{3} 2^{-1-6s} + 2^{-1-2s} + \frac{2^{-5s}}{5} + \frac{2^{-3s}}{3} + 2^{-s} + 3^{-1-3s} + \frac{3^{-4s}}{4} + \frac{3^{-2s}}{2} + 3^{-s} + 4^{-1-2s} + \\ & \frac{5^{-2s}}{2} + 5^{-s} + \frac{7^{-2s}}{2} + 7^{-s} + 11^{-s} + 13^{-s} + 17^{-s} + 19^{-s} + 23^{-s} + 29^{-s} + 31^{-s} + 37^{-s} + \\ & 41^{-s} + 43^{-s} + 47^{-s} + 53^{-s} + 59^{-s} + 61^{-s} + 67^{-s} + 71^{-s} + 73^{-s} + 79^{-s} + 83^{-s} + 89^{-s} + 97^{-s} \end{aligned}$$

$$\begin{aligned} 0 - \text{Integrate} \left[D \left[\frac{1}{3} 2^{-1-6s} + 2^{-1-2s} + \frac{2^{-5s}}{5} + \frac{2^{-3s}}{3} + 2^{-s} + 3^{-1-3s} + \frac{3^{-4s}}{4} + \frac{3^{-2s}}{2} + 3^{-s} + 4^{-1-2s} + \frac{5^{-2s}}{2} + \right. \right. \\ \left. \left. 5^{-s} + \frac{7^{-2s}}{2} + 7^{-s} + 11^{-s} + 13^{-s} + 17^{-s} + 19^{-s} + 23^{-s} + 29^{-s} + 31^{-s} + 37^{-s} + 41^{-s} + 43^{-s} + 47^{-s} + \right. \right. \\ \left. \left. 53^{-s} + 59^{-s} + 61^{-s} + 67^{-s} + 71^{-s} + 73^{-s} + 79^{-s} + 83^{-s} + 89^{-s} + 97^{-s}, s \right], \{s, 0, \text{Infinity}\} \right] \end{aligned}$$

```
428
```

```
15
```

```
Dz[100, 2, -1]
```

```
26879
```

```
1 - Expand[Integrate[D[Dz[10, z, s], s], {s, 0, Infinity}]]
```

```
Integrate::idiv: Integral of
```

$-2^s z \log[2] + 2^{2s} z \log[2] - 2^{3s} z \log[2] + 2^{-1+3s} z \log[2] + 2^{-1+s} 5^s z \log[2] + 6^s z \log[2] - 2^{2s} z^2 \log[2] + 2^{3s} z^2 \log[2] - 2^{-1+s} 5^s z^2 \log[2] - 6^s z^2 \log[2] - 2^{-1+3s} z^3 \log[2] - 3^s z \log[3] + 3^{2s} z \log[3] + 6^s z \log[3] - 3^{2s} z^2 \log[3] - 6^s z^2 \log[3] + 2^{-1+3s} z \log[4] - 4^s z \log[4] - 2^{-1+3s} z^2 \log[4] - 5^s z \log[5] + 2^{-1+s} 5^s z \log[5] - 2^{-1+s} 5^s z^2 \log[5] - 6^s z \log[6] - 7^s z \log[7] + 2^{-1+3s} z \log[8] - 8^s z \log[8] - 2^{-1+3s} z^2 \log[8] - 9^s z \log[9] + 2^{-1+s} 5^s z \log[10] - 10^s z \log[10] - 2^{-1+s} 5^s z^2 \log[10]$ does not converge on $\{0, \infty\}$. >>

$$\begin{aligned} 1 - \int_0^\infty \left(-2^{-1-3s} (-2+z) (-1+z) z \log[2] + \frac{1}{2} (-1+z) z \right. \\ \left(-2^{-s} (2^{-s} + 3^{-s} + 4^{-s} + 5^{-s}) \log[2] - 3^{-s} (2^{-s} + 3^{-s}) \log[3] + 3^{-s} (-2^{-s} \log[2] - 3^{-s} \log[3]) + \right. \\ \left. 2^{-s} (-2^{-s} \log[2] - 3^{-s} \log[3] - 4^{-s} \log[4] - 5^{-s} \log[5]) - 8^{-s} \log[8] - 10^{-s} \log[10]) + \right. \\ \left. z (-2^{-s} \log[2] - 3^{-s} \log[3] - 4^{-s} \log[4] - 5^{-s} \log[5] - 6^{-s} \log[6] - 7^{-s} \log[7] - \right. \\ \left. 8^{-s} \log[8] - 9^{-s} \log[9] - 10^{-s} \log[10]) \right) ds \end{aligned}$$

```
Expand[Dz[10, z, -1]]
```

$$1 + \frac{157 z}{6} + \frac{53 z^2}{2} + \frac{4 z^3}{3}$$

```
Expand[FullSimplify[1 - Expand[Integrate[D[Dz[10, z, s], s], {s, -1, Infinity}]]]]
```

$$1 + \frac{157 z}{6} + \frac{53 z^2}{2} + \frac{4 z^3}{3}$$

```
D[n^z, z]
```

```
FullSimplify[Integrate[n^z Log[n], {z, 1, 2}]]
```

$$(-1 + n) n$$

```
FullSimplify[Integrate[n^z Log[n], {z, 3, 2}]]
```

$$-(-1 + n) n^2$$

```
Integrate[D[fn[x], x], {x, 0, 100}]
```

$$-fn[0] + fn[100]$$

```
{Limit[y^(s - 1) HurwitzZeta[s, y + 1], y → Infinity], 1 / (s - 1)}
```

$$\left\{ \frac{1}{-1 + s}, \frac{1}{-1 + s} \right\}$$

```
bin[z_, k_] := Product[z - j, {j, 0, k - 1}] / k!
```

```
D2[n_, k_, s_] := D2[n, k, s] = Sum[j^(-s) D2[Floor[n / j], k - 1, s], {j, 2, n}];
```

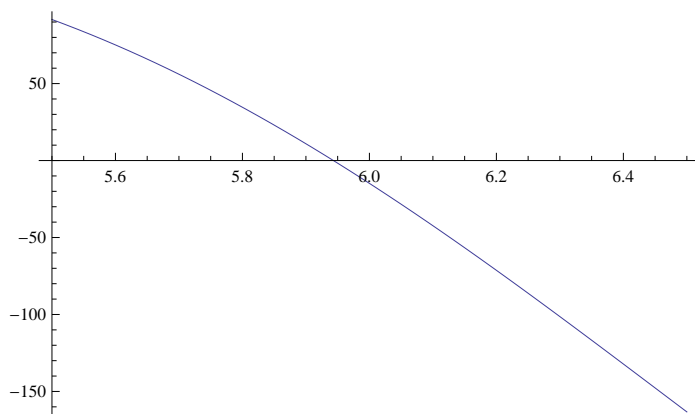
```
D2[n_, 0, s_] := 1
```

```
Dz[n_, z_, s_] := Sum[bin[z, k] D2[n, k, s], {k, 0, Log[2, n]}]
```

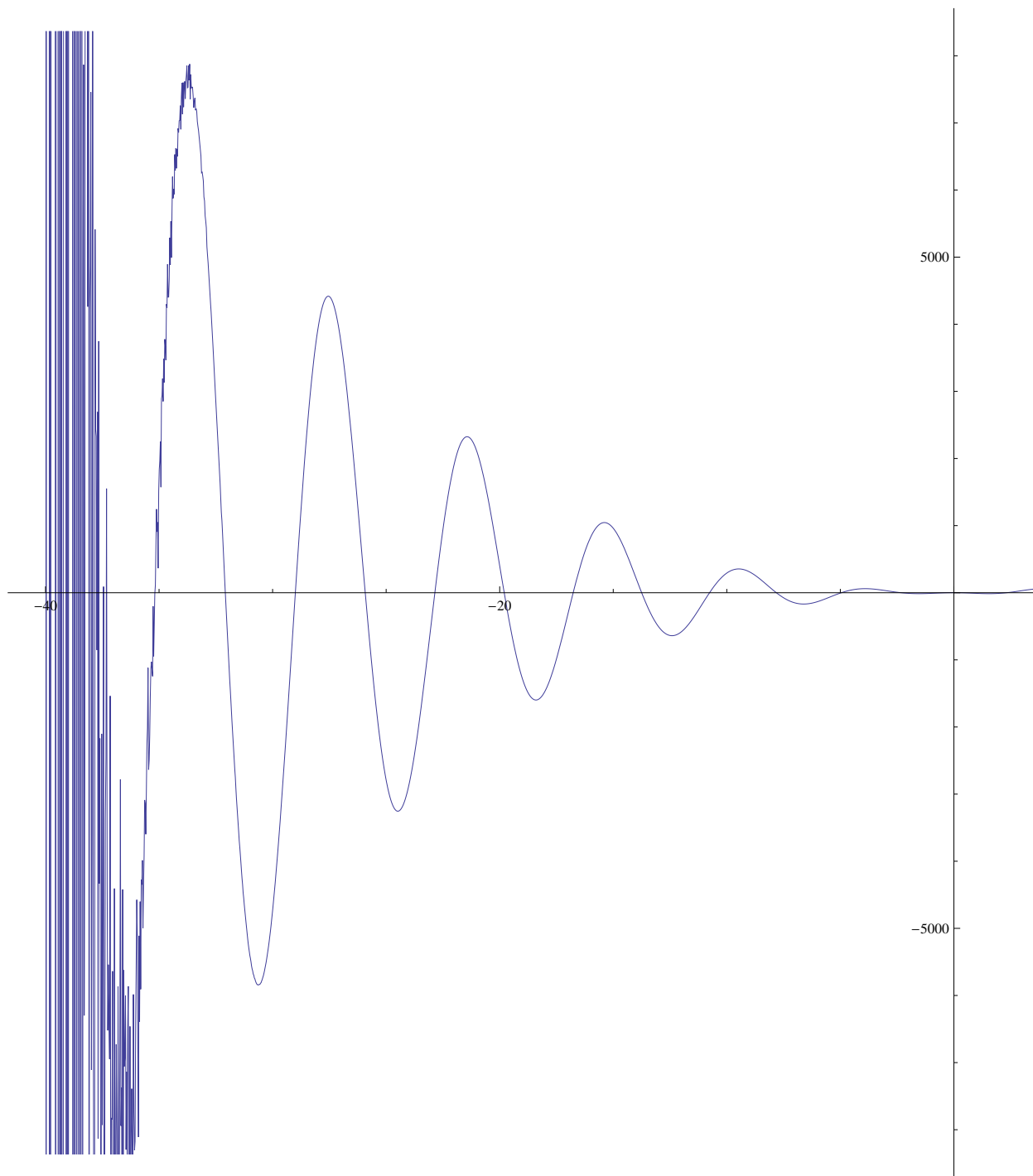
```
sind[n_, z_, s_, t_] := Sum[z^k (D[Sin[x], {x, k}] /. x → 0) / k! Dz[n, k, s], {k, 0, t}]
```

```
cosd[n_, z_, s_, t_] := Sum[z^k (D[Cos[x], {x, k}] /. x → 0) / k! Dz[n, k, s], {k, 0, t}]
```

```
Plot[N[sind[12, s, 0, 80]], {s, 5.5, 6.5}]
```



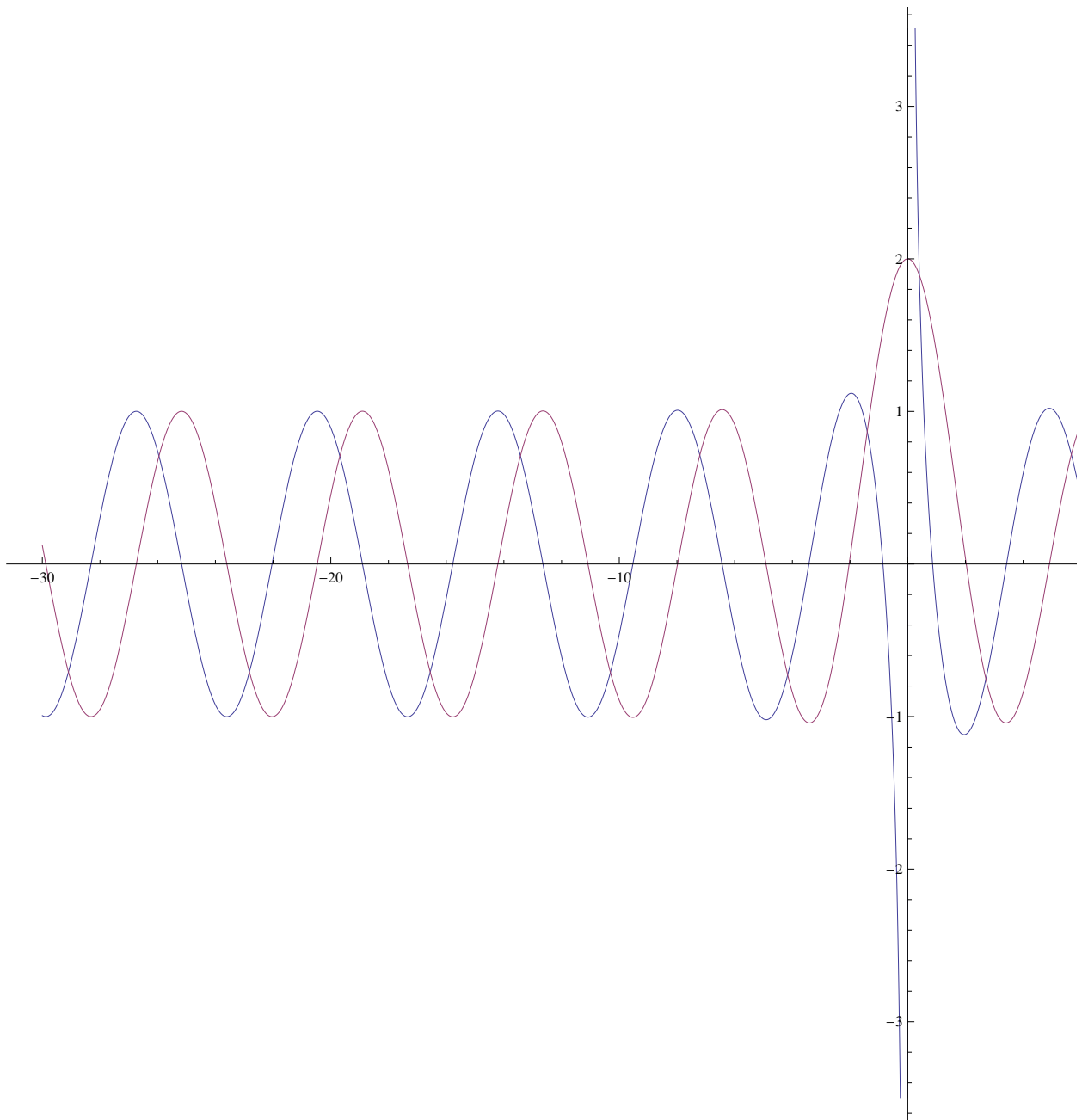
```
Plot[N[cosd[10, s, 0, 200]], {s, -40, 40}]
```



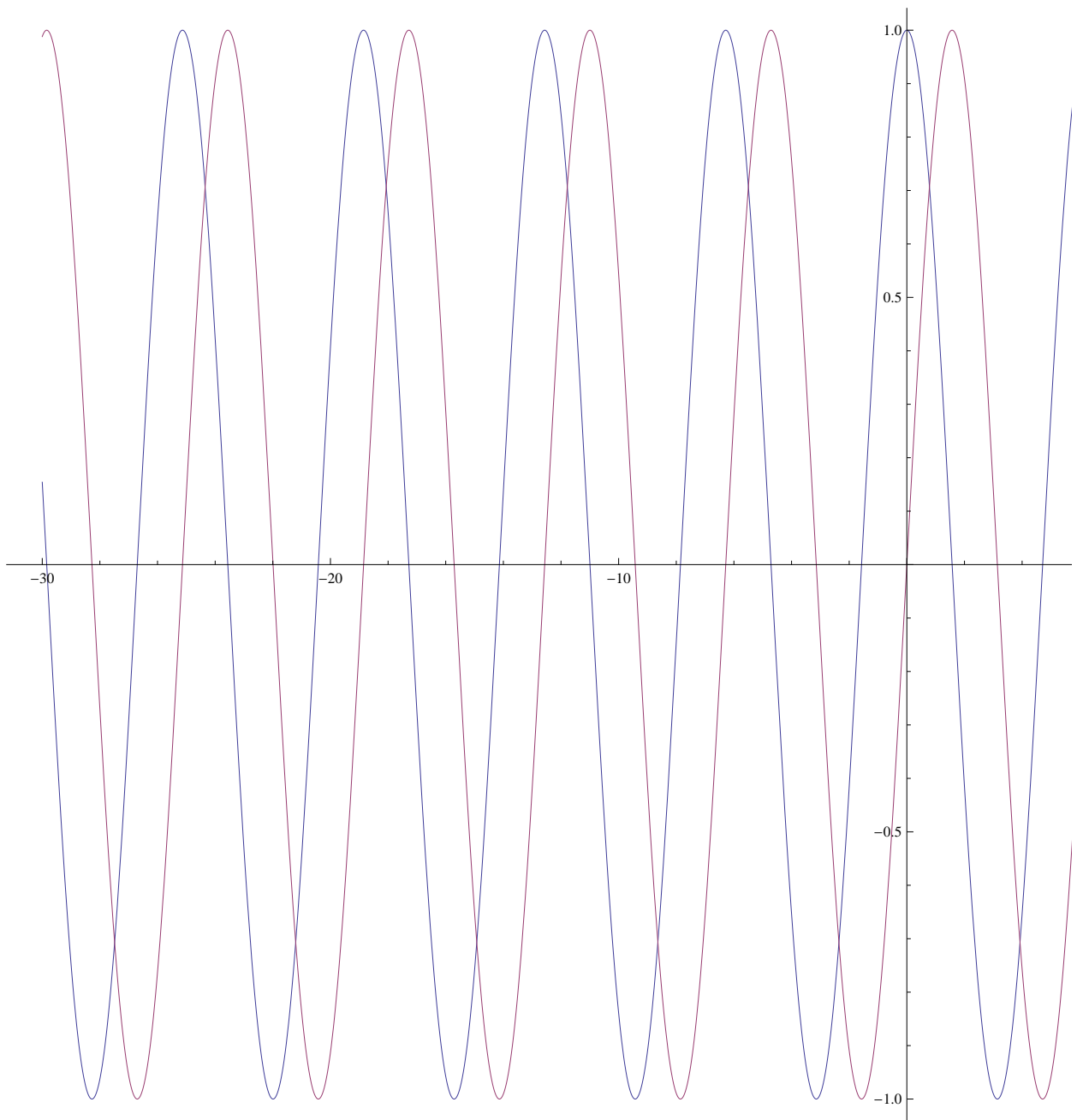
`sind[10, N[2 Pi], 0, 90]`

15.207


```
Plot[{N[cosd[E, s, 0, 200]] / s, N[sind[E, s, 0, 200]] / s}, {s, -30, 30}]
```



```
Plot[ {Cos[s], Sin[s]}, {s, -30, 30}]
```



```
Table[ {s, N[cosd[E, s, 0, 400]] / s}, {s, 4, 18, .01}] // TableForm
```

4.	0.593392
4.01	0.602193
4.02	0.610923
4.03	0.61958
4.04	0.628163
4.05	0.636673
4.06	0.645107
4.07	0.653465
4.08	0.661747
4.09	0.669951

4.1	0.678076
4.11	0.686122
4.12	0.694089
4.13	0.701974
4.14	0.709778
4.15	0.7175
4.16	0.725138
4.17	0.732693
4.18	0.740163
4.19	0.747548
4.2	0.754847
4.21	0.762059
4.22	0.769184
4.23	0.776221
4.24	0.783169
4.25	0.790028
4.26	0.796796
4.27	0.803474
4.28	0.81006
4.29	0.816555
4.3	0.822957
4.31	0.829265
4.32	0.83548
4.33	0.841601
4.34	0.847626
4.35	0.853556
4.36	0.85939
4.37	0.865127
4.38	0.870767
4.39	0.87631
4.4	0.881754
4.41	0.887099
4.42	0.892345
4.43	0.897492
4.44	0.902538
4.45	0.907484
4.46	0.912328
4.47	0.917071
4.48	0.921712
4.49	0.926251
4.5	0.930687
4.51	0.935019
4.52	0.939248
4.53	0.943374
4.54	0.947394
4.55	0.951311
4.56	0.955122
4.57	0.958828
4.58	0.962428
4.59	0.965922
4.6	0.96931
4.61	0.972591
4.62	0.975766
4.63	0.978833
4.64	0.981794
4.65	0.984646

4.66	0.987391
4.67	0.990028
4.68	0.992556
4.69	0.994976
4.7	0.997287
4.71	0.99949
4.72	1.00158
4.73	1.00357
4.74	1.00544
4.75	1.00721
4.76	1.00887
4.77	1.01041
4.78	1.01185
4.79	1.01318
4.8	1.01439
4.81	1.0155
4.82	1.0165
4.83	1.01739
4.84	1.01816
4.85	1.01883
4.86	1.01939
4.87	1.01983
4.88	1.02017
4.89	1.0204
4.9	1.02052
4.91	1.02052
4.92	1.02042
4.93	1.02021
4.94	1.01989
4.95	1.01945
4.96	1.01891
4.97	1.01826
4.98	1.0175
4.99	1.01663
5.	1.01566
5.01	1.01457
5.02	1.01337
5.03	1.01207
5.04	1.01066
5.05	1.00914
5.06	1.00751
5.07	1.00578
5.08	1.00393
5.09	1.00198
5.1	0.999928
5.11	0.997765
5.12	0.995496
5.13	0.99312
5.14	0.99064
5.15	0.988053
5.16	0.985362
5.17	0.982566
5.18	0.979666
5.19	0.976662
5.2	0.973554
5.21	0.970343

5.22	0.967029
5.23	0.963613
5.24	0.960095
5.25	0.956475
5.26	0.952753
5.27	0.948932
5.28	0.94501
5.29	0.940988
5.3	0.936866
5.31	0.932646
5.32	0.928328
5.33	0.923911
5.34	0.919398
5.35	0.914787
5.36	0.91008
5.37	0.905277
5.38	0.900379
5.39	0.895387
5.4	0.8903
5.41	0.88512
5.42	0.879847
5.43	0.874481
5.44	0.869024
5.45	0.863476
5.46	0.857837
5.47	0.852108
5.48	0.84629
5.49	0.840384
5.5	0.834389
5.51	0.828308
5.52	0.822139
5.53	0.815885
5.54	0.809546
5.55	0.803122
5.56	0.796614
5.57	0.790024
5.58	0.783351
5.59	0.776596
5.6	0.769761
5.61	0.762845
5.62	0.75585
5.63	0.748776
5.64	0.741625
5.65	0.734396
5.66	0.727092
5.67	0.719712
5.68	0.712257
5.69	0.704728
5.7	0.697126
5.71	0.689452
5.72	0.681707
5.73	0.673891
5.74	0.666006
5.75	0.658052
5.76	0.650029
5.77	0.64194

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5.79	0.625563
5.8	0.617278
5.81	0.608929
5.82	0.600517
5.83	0.592044
5.84	0.583509
5.85	0.574915
5.86	0.566262
5.87	0.55755
5.88	0.548782
5.89	0.539957
5.9	0.531076
5.91	0.522142
5.92	0.513154
5.93	0.504114
5.94	0.495022
5.95	0.485879
5.96	0.476687
5.97	0.467447
5.98	0.458159
5.99	0.448824
6.	0.439444
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6.02	0.420551
6.03	0.411039
6.04	0.401487
6.05	0.391894
6.06	0.382261
6.07	0.372589
6.08	0.36288
6.09	0.353135
6.1	0.343354
6.11	0.333539
6.12	0.32369
6.13	0.313809
6.14	0.303896
6.15	0.293954
6.16	0.283982
6.17	0.273981
6.18	0.263954
6.19	0.2539
6.2	0.243822
6.21	0.23372
6.22	0.223594
6.23	0.213447
6.24	0.203279
6.25	0.193091
6.26	0.182885
6.27	0.172661
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6.29	0.152164
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6.31	0.13161
6.32	0.121314
6.33	0.111007

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6.37	0.069689
6.38	0.0593423
6.39	0.0489909
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6.65	-0.218272
6.66	-0.228345
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6.73	-0.298094
6.74	-0.307937
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6.76	-0.327522
6.77	-0.337262
6.78	-0.346966
6.79	-0.356633
6.8	-0.366261
6.81	-0.37585
6.82	-0.385398
6.83	-0.394905
6.84	-0.40437
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7.59	-0.930981
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7.62	-0.942324
7.63	-0.94591
7.64	-0.949398
7.65	-0.952788
7.66	-0.956079
7.67	-0.959271
7.68	-0.962364
7.69	-0.965357
7.7	-0.96825
7.71	-0.971042
7.72	-0.973735
7.73	-0.976326
7.74	-0.978817
7.75	-0.981206
7.76	-0.983494
7.77	-0.98568
7.78	-0.987764
7.79	-0.989746
7.8	-0.991626
7.81	-0.993403
7.82	-0.995078
7.83	-0.99665
7.84	-0.998119
7.85	-0.999485
7.86	-1.00075
7.87	-1.00191
7.88	-1.00296
7.89	-1.00392
7.9	-1.00476
7.91	-1.00551
7.92	-1.00615
7.93	-1.00669
7.94	-1.00712
7.95	-1.00745
7.96	-1.00768
7.97	-1.0078
7.98	-1.00782
7.99	-1.00773
8.	-1.00755
8.01	-1.00725

8.02	-1.00686
8.03	-1.00636
8.04	-1.00575
8.05	-1.00504
8.06	-1.00423
8.07	-1.00332
8.08	-1.0023
8.09	-1.00118
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8.17	-0.98852
8.18	-0.986478
8.19	-0.984335
8.2	-0.982091
8.21	-0.979746
8.22	-0.9773
8.23	-0.974754
8.24	-0.972108
8.25	-0.969362
8.26	-0.966516
8.27	-0.963571
8.28	-0.960528
8.29	-0.957385
8.3	-0.954145
8.31	-0.950807
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8.51	-0.864104
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8.53	-0.853422
8.54	-0.84795
8.55	-0.842391
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8.57	-0.831016

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8.62	-0.801103
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8.64	-0.78856
8.65	-0.782167
8.66	-0.775695
8.67	-0.769144
8.68	-0.762513
8.69	-0.755806
8.7	-0.749021
8.71	-0.742159
8.72	-0.735222
8.73	-0.72821
8.74	-0.721123
8.75	-0.713963
8.76	-0.706731
8.77	-0.699426
8.78	-0.69205
8.79	-0.684603
8.8	-0.677087
8.81	-0.669502
8.82	-0.661848
8.83	-0.654127
8.84	-0.646339
8.85	-0.638486
8.86	-0.630568
8.87	-0.622585
8.88	-0.614539
8.89	-0.606431
8.9	-0.598261
8.91	-0.59003
8.92	-0.581739
8.93	-0.573389
8.94	-0.56498
8.95	-0.556515
8.96	-0.547992
8.97	-0.539414
8.98	-0.530782
8.99	-0.522095
9.	-0.513355
9.01	-0.504563
9.02	-0.49572
9.03	-0.486827
9.04	-0.477885
9.05	-0.468893
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9.07	-0.45077
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9.12	-0.404677
9.13	-0.395332

9.14	-0.385947
9.15	-0.376523
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9.32	-0.211294
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9.62	0.0920088
9.63	0.102121
9.64	0.112223
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9.67	0.142453
9.68	0.152501
9.69	0.162533

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9.71	0.182545
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9.91	0.377144
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10.14	0.581333
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10.37	0.75416
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10.39	0.767389
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10.41	0.780304
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10.51	0.84
10.52	0.845508
10.53	0.85093
10.54	0.856265
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10.56	0.866672
10.57	0.871744
10.58	0.876726
10.59	0.881619
10.6	0.886423
10.61	0.891136
10.62	0.895758
10.63	0.900289
10.64	0.904728
10.65	0.909075
10.66	0.913329
10.67	0.91749
10.68	0.921558
10.69	0.925532
10.7	0.929412
10.71	0.933197
10.72	0.936887
10.73	0.940481
10.74	0.94398
10.75	0.947383
10.76	0.950689
10.77	0.953898
10.78	0.957011
10.79	0.960026
10.8	0.962943
10.81	0.965762

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10.83	0.971105
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