

mm[n_, a_, b_] := mm[n, a, b] = If[Mod[n, a] == 0, a, 0] - If[Mod[n, b] == 0, b, 0]

Sum[N[mm[n, 2, 3] / n], {n, 1, 100 000}]

0.40547

E^0.4054701080498337`

1.50001

Sum[N[mm[n, 3, 2] / n], {n, 1, 100 000}]

-0.40547

E^-0.4054701080498337`

0.666663

Sum[N[mm[n, 9, 8] / n], {n, 1, 100 000}]

-0.117788

E^-0.11778803539805958`

0.888884

8. / 9

0.888889

```
Grid[ Table[ { N[Log[j / k]], Sum[ N[mm[n, k, j] / n], {n, 1, 10 000}]], {k, 1, 20}, {j, 1, 7}]]
```

```
{0., 0.}      {0.693147,    {1.09861,    {1.38629,    {1.60944,    {1.79176,    {1.94591,
               0.693097}    1.09861}    1.38614}    1.60924}    1.79191}    1.94601}
{-0.693147,   {0., 0.}      {0.405465,   {0.693147,   {0.916291,   {1.09861,   {1.25276,
-0.693097}    {0.405515}    0.693047}    0.916141}    1.09881}    1.25291}
{-1.09861,    {-0.405465,   {0., 0.}      {0.287682,   {0.510826,   {0.693147,   {0.847298,
-1.09861}     -0.405515}    {0.287532}    0.510626}    0.693297}    0.847398}
{-1.38629,    {-0.693147,   {-0.287682,   {0., 0.}      {0.223144,   {0.405465,   {0.559616,
-1.38614}     -0.693047}    -0.287532}    {0.223094}    0.405765}    0.559866}
{-1.60944,    {-0.916291,   {-0.510826,   {-0.223144,   {0., 0.}      {0.182322,   {0.336472,
-1.60924}     -0.916141}    -0.510626}    -0.223094}    {0.182672}    0.336772}
{-1.79176,    {-1.09861,   {-0.693147,   {-0.405465,   {-0.182322,   {0., 0.}      {0.154151,
-1.79191}     -1.09881}    -0.693297}    -0.405765}    -0.182672}    0.154101}
{-1.94591,    {-1.25276,   {-0.847298,   {-0.559616,   {-0.336472,   {-0.154151,   {0., 0.}
-1.94601}     -1.25291}    -0.847398}    -0.559866}    -0.336772}    -0.154101}
{-2.07944,    {-1.38629,   {-0.980829,   {-0.693147,   {-0.470004,   {-0.287682,   {-0.133531,
-2.07909}     -1.38599}    -0.980479}    -0.692947}    -0.469854}    -0.287182}    -0.133081}
{-2.19722,    {-1.50408,   {-1.09861,   {-0.81093,   {-0.587787,   {-0.405465,   {-0.251314,
-2.19692}     -1.50383}    -1.09831}    -0.81078}    -0.587687}    -0.405015}    -0.250914}
{-2.30259,    {-1.60944,   {-1.20397,   {-0.916291,   {-0.693147,   {-0.510826,   {-0.356675,
-2.30214}     -1.60904}    -1.20352}    -0.915991}    -0.692897}    -0.510226}    -0.356125}
{-2.3979,     {-1.70475,   {-1.29928,   {-1.0116,    {-0.788457,   {-0.606136,   {-0.451985,
-2.3975}      -1.7044}     -1.29888}    -1.01135}    -0.788257}    -0.605586}    -0.451485}
{-2.48491,    {-1.79176,   {-1.38629,   {-1.09861,   {-0.875469,   {-0.693147,   {-0.538997,
-2.48476}     -1.79166}    -1.38614}    -1.09861}    -0.875519}    -0.692847}    -0.538746}
{-2.56495,    {-1.8718,    {-1.46634,   {-1.17865,   {-0.955511,   {-0.77319,   {-0.619039,
-2.56465}     -1.87155}    -1.46604}    -1.1785}    -0.955411}    -0.77274}    -0.618639}
{-2.63906,    {-1.94591,   {-1.54045,   {-1.25276,   {-1.02962,   {-0.847298,   {-0.693147,
-2.63881}     -1.94571}    -1.5402}     -1.25266}    -1.02957}    -0.846898}    -0.692797}
{-2.70805,    {-2.0149,    {-1.60944,   {-1.32176,   {-1.09861,   {-0.916291,   {-0.76214,
-2.70835}     -2.01525}    -1.60974}    -1.32221}    -1.09911}    -0.916441}    -0.76234}
{-2.77259,    {-2.07944,   {-1.67398,   {-1.38629,   {-1.16315,   {-0.980829,   {-0.826679,
-2.77184}     -2.07874}    -1.67323}    -1.38569}    -1.1626}     -0.979929}    -0.825829}
{-2.83321,    {-2.14007,   {-1.7346,    {-1.44692,   {-1.22378,   {-1.04145,   {-0.887303,
-2.83281}     -2.13972}    -1.7342}     -1.44667}    -1.22358}    -1.0409}     -0.886803}
{-2.89037,    {-2.19722,   {-1.79176,   {-1.50408,   {-1.28093,   {-1.09861,   {-0.944462,
-2.89052}     -2.19742}    -1.79191}    -1.50438}    -1.28128}    -1.09861}    -0.944511}
{-2.94444,    {-2.25129,   {-1.84583,   {-1.55814,   {-1.335,      {-1.15268,   {-0.998529,
-2.94414}     -2.25104}    -1.84553}    -1.55799}    -1.3349}     -1.15223}    -0.998129}
{-2.99573,    {-2.30259,   {-1.89712,   {-1.60944,   {-1.38629,   {-1.20397,   {-1.04982,
-2.99478}     -2.30169}    -1.89617}    -1.60864}    -1.38554}    -1.20287}    -1.04877}
```

```
Sum[ (-1) ^ j / (2 j + 1), {j, 0, Infinity}]
```

$$\frac{\pi}{4}$$

```
N[Sum[ mm[j, 4, 1] / (2 j + 1), {j, 0, 500 000}]]
```

```
2.51935
```

```
2.51934563807327` / Pi
```

```
0.801933
```

```
N[Sum[mm[j, 1, 4] / (2 j + 1), {j, 0, 100 000}]]
```

```
-2.51935
```

```
Pi^2 / N[Sum[mm[j, 2, 9] / j^2, {j, 1, 100 000}]]
```

```
15.4286
```

```
FullSimplify[
```

```
Sum[1 / (4 j + 1)^2 + 1 / (4 j + 2)^2 + 1 / (4 j + 3)^2 - 3 / (4 j + 4)^2, {j, 0, Infinity}]]
```

```

$$\frac{\pi^2}{8}$$

```

```
N[ $\frac{\pi^2}{8}$ ]
```

```
1.2337
```

```
Pi^2 / 72.
```

```
0.137078
```

```
40 * 41
```

```
9840 / 1640
```

```
6
```

```
140 * 141
```