```
colfunc = ColorData["AvocadoColors"];
poc[c_, z_] := Expand@Sum[bin[z, k], {k, 0, c}]
pocroots[n_] := If[(c = Exponent[f = poc[n, z], z]) == 0, {},
         If[c == 1, List@NRoots[f == 0, z][[2]], List@@NRoots[f == 0, z][[All, 2]]]]
pocrootsa[n_] := pocrootsa[n] = If[(c = Exponent[f = poc[n, z], z]) == 0, {},
              If[c == 1, List@Roots[f == 0, z][[2]], List@@Roots[f == 0, z][[All, 2]]]]
Clear[px, pz, t]
t[n_, a_, b_] :=
    t[n, a, b] = b (Floor[n/b] - Floor[(n-1)/b]) - a (Floor[n/a] - Floor[(n-1)/a])
px[n_{,a_{,b_{,1}}}, a_{,b_{,1}}] := t[n, a, b] / n
px[n_{a}, a_{b}, 0] := 0
pz[n_{,a_{,b_{,0}}} a_{,b_{,0}}] := 1
pz[0, a_, b_, z_] := 1
pocxrootsa[n_, a_, b_] :=
    pocxrootsa[n, a, b] = If[(c = Exponent[f = pocx[n, a, b, z], z]) == 0, {},
              If[c == 1, List@Roots[f == 0, z][[2]], List@@Roots[f == 0, z][[All, 2]]]]
pocc[c_, z_] := Expand@Sum[Pochhammer[z, k]/k!, \{k, 0, c\}]
poccrootsa[n_] := poccrootsa[n] = If[(c = Exponent[f = pocc[n, z], z]) == 0,
              {}, If[c == 1, List@Roots[f == 0, z][[2]], List@@Roots[f == 0, z][[All, 2]]]]
poc[20, z] /. z \rightarrow -3
121
N@Sum[-1/r, \{r, pocrootsa[200]\}]
0.690653 - 6.93889 \times 10^{-18} i
Log[2.]
0.693147
N@Sum[-1/r, \{r, pocrootsa[400]\}]
0.691899 + 0.i
N[pocrootsa[400]]
 -0.606245 - 2.32191 \, \dot{\mathrm{i}} \,, \, -0.606245 + 2.32191 \, \dot{\mathrm{i}} \,, \, -0.319084 - 3.35336 \, \dot{\mathrm{i}} \,, \, -0.319084 + 3.3536 \, \dot{\mathrm{i}} \,, \, -0.319084 + 3.3566 \, \dot{\mathrm{i}} \,, \, -0.319084 + 3.3566 \, \dot{\mathrm{i}} \,, \, -0.
    0.0139939 - 4.42949 \, \text{i}, 0.0139939 + 4.42949 \, \text{i}, 0.386915 - 5.5436 \, \text{i}, 0.386915 + 5.5436 \, \text{i},
    0.795861 - 6.69094 \pm ,\ 0.795861 + 6.69094 \pm ,\ 1.23818 - 7.86792 \pm ,\ 1.23818 + 7.86792 
     1.71192 - 9.0717 \text{ i}, 1.71192 + 9.0717 \text{ i}, 2.21557 - 10.3 \text{ i}, 2.21557 + 10.3 \text{ i},
    2.74793 - 11.551 \, \text{i}, 2.74793 + 11.551 \, \text{i}, 3.30801 - 12.8229 \, \text{i}, 3.30801 + 12.8229 \, \text{i},
    3.89499 - 14.1144 \, \text{i}, 3.89499 + 14.1144 \, \text{i}, 4.50817 - 15.4244 \, \text{i}, 4.50817 + 15.4244 \, \text{i},
    5.14697 - 16.7516 \, \dot{\text{i}}, 5.14697 + 16.7516 \, \dot{\text{i}}, 5.81088 - 18.0952 \, \dot{\text{i}}, 5.81088 + 18.0952 \, \dot{\text{i}},
    6\,.\,49943\,-\,19\,.\,4543\,\dot{\mathtt{i}}\,\,,\,\,6\,.\,49943\,+\,19\,.\,4543\,\dot{\mathtt{i}}\,\,,\,\,7\,.\,21223\,-\,20\,.\,828\,\dot{\mathtt{i}}\,\,,\,\,7\,.\,21223\,+\,20\,.\,828\,\dot{\mathtt{i}}\,\,,
     7.94895 - 22.2157 \, \dot{\text{i}}, 7.94895 + 22.2157 \, \dot{\text{i}}, 8.70926 - 23.6167 \, \dot{\text{i}}, 8.70926 + 23.6167 \, \dot{\text{i}},
    9.49289 - 25.0304 \, \dot{\text{i}} \, , \, 9.49289 + 25.0304 \, \dot{\text{i}} \, , \, 10.2996 - 26.4562 \, \dot{\text{i}} \, , \, 10.2996 + 26.4562 \, \dot{\text{i}} \, , \, 30.2996 + 26.4562 \, \dot{\text{i}} \, , \, 30.2996 + 26.4562 \, \dot{\text{i}} \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.2996 \, , \, 30.299
    11.1291 - 27.8935 \, \text{i}, 11.1291 + 27.8935 \, \text{i}, 11.9813 - 29.3419 \, \text{i}, 11.9813 + 29.3419 \, \text{i},
    12.856 - 30.8009 \, \text{i}, 12.856 + 30.8009 \, \text{i}, 13.7529 - 32.2701 \, \text{i}, 13.7529 + 32.2701 \, \text{i},
    14.6721 - 33.7489 i, 14.6721 + 33.7489 i, 15.6132 - 35.2371 i, 15.6132 + 35.2371 i,
     16.5762 - 36.7343 i, 16.5762 + 36.7343 i, 17.561 - 38.24 i, 17.561 + 38.24 i,
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18.5676 - 39.754 \, \text{i}, 18.5676 + 39.754 \, \text{i}, 19.5957 - 41.2758 \, \text{i}, 19.5957 + 41.2758 \, \text{i},
 20.6453 - 42.8053 \, \text{i}, 20.6453 + 42.8053 \, \text{i}, 21.7164 - 44.342 \, \text{i}, 21.7164 + 44.342 \, \text{i},
 22.8089 - 45.8857\,\,\dot{\text{i}}, 22.8089 + 45.8857\,\,\dot{\text{i}}, 23.9228 - 47.436\,\,\dot{\text{i}}, 23.9228 + 47.436\,\,\dot{\text{i}},
 25.0579 - 48.9928 \, i, 25.0579 + 48.9928 \, i, 26.2143 - 50.5557 \, i, 26.2143 + 50.5557 \, i,
 27.3919 - 52.1245 i, 27.3919 + 52.1245 i, 28.5907 - 53.6989 i, 28.5907 + 53.6989 i,
 29.8106 - 55.2786 i, 29.8106 + 55.2786 i, 31.0517 - 56.8635 i, 31.0517 + 56.8635 i,
 32.3139 - 58.4532 i, 32.3139 + 58.4532 i, 33.5973 - 60.0476 i, 33.5973 + 60.0476 i,
 34.9018 - 61.6465 \, \mathrm{i} \, , \, 34.9018 + 61.6465 \, \mathrm{i} \, , \, 36.2274 - 63.2495 \, \mathrm{i} \, , \, 36.2274 + 63.2495 \, \mathrm{i} \, , \, 36.2495 \, \mathrm{i} \, , \, 36.2495 \, \mathrm{i} \, , \, 36.2495 \, \mathrm{i} \, ,
 37.5741 - 64.8565 \; \dot{\text{i}} \; , \; 37.5741 \; + \; 64.8565 \; \dot{\text{i}} \; , \; 38.9419 \; - \; 66.4673 \; \dot{\text{i}} \; , \; 38.9419 \; + \; 66.4673 \; \dot{\text{i}} \; , \; \\
 40.3309 - 68.0816 \, \dot{\text{i}}, 40.3309 + 68.0816 \, \dot{\text{i}}, 41.7411 - 69.6993 \, \dot{\text{i}}, 41.7411 + 69.6993 \, \dot{\text{i}},
 43.1725 - 71.3201 \pm ,\ 43.1725 + 71.3201 \pm ,\ 44.6251 - 72.9438 \pm ,\ 44.6251 + 72.9438 \pm ,
 46.0989 - 74.5703 \, \text{i}, 46.0989 + 74.5703 \, \text{i}, 47.594 - 76.1993 \, \text{i}, 47.594 + 76.1993 \, \text{i},
 49.1104 - 77.8307 \pm ,\ 49.1104 + 77.8307 \pm ,\ 50.6482 - 79.4642 \pm ,\ 50.6482 + 79.4642 \pm ,
 52.2074 - 81.0996 i, 52.2074 + 81.0996 i, 53.788 - 82.7369 i, 53.788 + 82.7369 i,
 55.3901 - 84.3757 \, i, 55.3901 + 84.3757 \, i, 57.0138 - 86.0159 \, i, 57.0138 + 86.0159 \, i,
 58.6591 - 87.6572\,\dot{\text{i}}, 58.6591 + 87.6572\,\dot{\text{i}}, 60.326 - 89.2996\,\dot{\text{i}}, 60.326 + 89.2996\,\dot{\text{i}},
 62.0147 - 90.9428\,\dot{\text{i}}, 62.0147 + 90.9428\,\dot{\text{i}}, 63.7252 - 92.5867\,\dot{\text{i}}, 63.7252 + 92.5867\,\dot{\text{i}},
 65.4576 - 94.231 \, \text{i}, 65.4576 + 94.231 \, \text{i}, 67.2119 - 95.8755 \, \text{i}, 67.2119 + 95.8755 \, \text{i},
 68.9882 - 97.5202 \, \text{i} \, , \, 68.9882 + 97.5202 \, \text{i} \, , \, 70.7866 - 99.1647 \, \text{i} \, , \, 70.7866 + 99.1647 \, \text{i} \, , 
72.6072 - 100.809 \; \text{i} \; , \; 72.6072 + 100.809 \; \text{i} \; , \; 74.4501 - 102.453 \; \text{i} \; , \; 74.4501 + 102.453 \; \text{i} \; , 
76.3153 - 104.096 \pm , \ 76.3153 + 104.096 \pm , \ 78.203 - 105.738 \pm , \ 78.203 + 105.738 \pm
 80.1133 - 107.379 \, i, 80.1133 + 107.379 \, i, 82.0462 - 109.019 \, i, 82.0462 + 109.019 \, i,
 84.0019 - 110.658 \, i, 84.0019 + 110.658 \, i, 85.9805 - 112.295 \, i, 85.9805 + 112.295 \, i,
87.9821 - 113.93 \pm , \ 87.9821 + 113.93 \pm , \ 90.0067 - 115.563 \pm , \ 90.0067 + 115.563 \pm , \ 90.006
92.0546 - 117.194 \, \dot{\text{i}} \,, \, 92.0546 + 117.194 \, \dot{\text{i}} \,, \, 94.1259 - 118.823 \, \dot{\text{i}} \,, \, 94.1259 + 118.823 \, \dot{\text{i}} \,, 
 96.2206 - 120.449 \, \dot{\text{i}} \, , \, 96.2206 + 120.449 \, \dot{\text{i}} \, , \, 98.3389 - 122.072 \, \dot{\text{i}} \, , \, 98.3389 + 122.072 \, \dot{\text{i}} \, , \, 98.3
 100.481 - 123.693 \pm ,\ 100.481 + 123.693 \pm ,\ 102.647 - 125.31 \pm ,\ 102.647 + 125.31 \pm ,
 104.837 - 126.924\,\,\mathrm{i}, 104.837 + 126.924\,\,\mathrm{i}, 107.051 - 128.534\,\,\mathrm{i}, 107.051 + 128.534\,\,\mathrm{i},
109.29-130.14\,\dot{\mathtt{i}}\,,\,109.29+130.14\,\dot{\mathtt{i}}\,,\,111.553-131.742\,\dot{\mathtt{i}}\,,\,111.553+131.742\,\dot{\mathtt{i}}\,,
113.84 - 133.341 \; \dot{\text{i}} \; , \; 113.84 + 133.341 \; \dot{\text{i}} \; , \; 116.153 - 134.934 \; \dot{\text{i}} \; , \; 116.153 + 134.934 \; \dot{\text{i}} \; , \; 116.15
118.49 - 136.523 \, \text{i}, 118.49 + 136.523 \, \text{i}, 120.853 - 138.107 \, \text{i}, 120.853 + 138.107 \, \text{i},
123.241 - 139.686 \pm 1, 123.241 + 139.686 \pm 1, 125.655 - 141.26 \pm 1, 125.655 + 141.26 \pm 1, 125.65 + 141.26 \pm 1, 125.6
128.094 - 142.828 i , 128.094 + 142.828 i , 130.559 - 144.39 i , 130.559 + 144.39 i ,
133.05 - 145.946\,\,\dot{\mathrm{n}}, 133.05 + 145.946\,\,\dot{\mathrm{n}}, 135.568 - 147.496\,\,\dot{\mathrm{n}}, 135.568 + 147.496\,\,\dot{\mathrm{n}},
138.113 - 149.039 \; \text{\'i} \; , \; 138.113 \; + \; 149.039 \; \text{\'i} \; , \; 140.684 \; - \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 150.575 \; \text{\'i} \; , \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 140.684 \; + \; 14
 143.282 - 152.105 i, 143.282 + 152.105 i, 145.907 - 153.627 i, 145.907 + 153.627 i,
148.56 - 155.141 \pm ,\ 148.56 + 155.141 \pm ,\ 151.241 - 156.647 \pm ,\ 151.241 + 156.647 \pm ,
 153.949 - 158.145 \, \text{i}, 153.949 + 158.145 \, \text{i}, 156.686 - 159.635 \, \text{i}, 156.686 + 159.635 \, \text{i},
159.452 - 161.116 i, 159.452 + 161.116 i, 162.246 - 162.587 i, 162.246 + 162.587 i,
165.07 - 164.05\,\dot{\mathtt{m}}\,,\, 165.07 + 164.05\,\dot{\mathtt{m}}\,,\, 167.923 - 165.502\,\dot{\mathtt{m}}\,,\, 167.923 + 165.5024\,\dot{\mathtt{m}}\,,\, 167.923 + 165.5024\,\dot{\mathtt{m}}\,,\, 167.923 + 165.5024\,\dot{\mathtt{m}}\,,\, 167.923 + 165.5024\,\dot{\mathtt{m}}\,,\, 167.923 + 165.
170.806 - 166.945 \, \text{i}, 170.806 + 166.945 \, \text{i}, 173.718 - 168.377 \, \text{i}, 173.718 + 168.377 \, \text{i},
176.661 - 169.798 \, \text{i}, 176.661 + 169.798 \, \text{i}, 179.635 - 171.208 \, \text{i}, 179.635 + 171.208 \, \text{i},
182.64 - 172.607 \, \dot{\text{i}} \, , \, 182.64 + 172.607 \, \dot{\text{i}} \, , \, 185.677 - 173.994 \, \dot{\text{i}} \, , \, 185.677 + 173.994 \, \dot{\text{i}} \, , \, \\
 188.745 - 175.368 \, \text{i}, 188.745 + 175.368 \, \text{i}, 191.845 - 176.73 \, \text{i}, 191.845 + 176.73 \, \text{i},
194.978 - 178.08 \, \dot{\text{i}} \, , \, 194.978 + 178.08 \, \dot{\text{i}} \, , \, 198.144 - 179.415 \, \dot{\text{i}} \, , \, 198.144 + 179.415 \, \dot{\text{i}} \, , \, 198.14
 201.343 - 180.737 \,\,\dot{\text{i}} \,\,, \,\, 201.343 + 180.737 \,\,\dot{\text{i}} \,\,, \,\, 204.577 - 182.044 \,\,\dot{\text{i}} \,\,, \,\, 204.577 + 182.
 207.844 - 183.337 \, \text{i}, 207.844 + 183.337 \, \text{i}, 211.146 - 184.614 \, \text{i}, 211.146 + 184.614 \, \text{i},
 214.484 - 185.876 \; \dot{\text{i}} \; , \; 214.484 + 185.876 \; \dot{\text{i}} \; , \; 217.857 - 187.122 \; \dot{\text{i}} \; , \; 217.857 + 187.122 \; \dot{\text{i}} \; , \; 217.122 + 187.122 \; \dot{\text{i}} \; , \; 217.
 221.\, 267 - 188.\, 351 \,\, \dot{\text{i}} \,\,, \,\, 221.\, 267 \,+ 188.\, 351 \,\, \dot{\text{i}} \,\,, \,\, 224.\, 713 \,\, - \, 189.\, 562 \,\, \dot{\text{i}} \,\,, \,\, 224.\, 713 \,\, + \, 189.\, 562 \,\, \dot{\text{i}} \,\,, \,\, 360 \,\,\,, \,\, 360 \,\,\,, \,\, 3
 228.197 - 190.756\,\,\dot{\text{i}}, 228.197 + 190.756\,\,\dot{\text{i}}, 231.719 - 191.931\,\,\dot{\text{i}}, 231.719 + 191.931\,\,\dot{\text{i}},
 235.279 - 193.087 \; \text{i}\;,\; 235.279 + 193.087 \; \text{i}\;,\; 238.879 - 194.224 \; \text{i}\;,\; 238.879 + 194.224 \; \text{i}\;,\; 238.224 + 194.224 + 194.224 + 194.224 + 194.224 + 194.224 + 194.224 + 194.224 + 194.
 242.518 - 195.341 i, 242.518 + 195.341 i, 246.198 - 196.436 i, 246.198 + 196.436 i,
 249.919 - 197.51 i, 249.919 + 197.51 i, 253.681 - 198.562 i, 253.681 + 198.562 i,
 257.487 - 199.591 \, \text{i}, 257.487 + 199.591 \, \text{i}, 261.336 - 200.596 \, \text{i}, 261.336 + 200.596 \, \text{i},
 265.229 - 201.577 \pm 265.229 + 201.577 \pm 269.167 - 202.532 \pm 269.167 + 202.532 + 202.532 \pm 269.167 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.532 + 202.
 273.152 - 203.461\,\,\dot{\text{i}}, 273.152 + 203.461\,\,\dot{\text{i}}, 277.183 - 204.362\,\,\dot{\text{i}}, 277.183 + 204.362\,\,\dot{\text{i}},
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281.262 - 205.236 i, 281.262 + 205.236 i, 285.39 - 206.08 i, 285.39 + 206.08 i,
 289.567 - 206.895 i, 289.567 + 206.895 i, 293.796 - 207.678 i, 293.796 + 207.678 i,
 298.077 - 208.429 \pm, 298.077 + 208.429 \pm, 302.412 - 209.147 \pm, 302.412 + 209.147 \pm, 302.412 \pm, 302.41
 306.801 - 209.83 \pm 306.801 + 209.83 \pm 311.246 - 210.477 \pm 311.246 + 210.477 \pm 311.24
 315.749 - 211.086 i, 315.749 + 211.086 i, 320.311 - 211.657 i, 320.311 + 211.657 i,
 324.933 - 212.188\,\dot{\text{i}}, 324.933 + 212.188\,\dot{\text{i}}, 329.617 - 212.677\,\dot{\text{i}}, 329.617 + 212.677\,\dot{\text{i}},
 334.365 - 213.122 \, \text{i}, 334.365 + 213.122 \, \text{i}, 339.179 - 213.523 \, \text{i}, 339.179 + 213.523 \, \text{i},
 344.06 - 213.876 i, 344.06 + 213.876 i, 349.011 - 214.18 i, 349.011 + 214.18 i,
 354.034 - 214.433 \, i, 354.034 + 214.433 \, i, 359.131 - 214.633 \, i, 359.131 + 214.633 \, i,
 364.304 - 214.778 \pm 364.304 + 214.778 \pm 369.557 - 214.864 \pm 369.557 + 214.864 \pm 369.
374.892 - 214.889\,\,\dot{\text{i}}, 374.892 + 214.889\,\,\dot{\text{i}}, 380.312 - 214.851\,\,\dot{\text{i}}, 380.312 + 214.851\,\,\dot{\text{i}},
 385.82 - 214.747 \, \text{i}, 385.82 + 214.747 \, \text{i}, 391.42 - 214.573 \, \text{i}, 391.42 + 214.573 \, \text{i},
 397.115 - 214.325 i, 397.115 + 214.325 i, 402.909 - 214.001 i, 402.909 + 214.001 i,
408.807 - 213.596 \, \text{i}, 408.807 + 213.596 \, \text{i}, 414.812 - 213.106 \, \text{i}, 414.812 + 213.106 \, \text{i},
 420.931 - 212.525 i, 420.931 + 212.525 i, 427.169 - 211.85 i, 427.169 + 211.85 i,
 433.531 - 211.075 \pm ,\ 433.531 + 211.075 \pm ,\ 440.024 - 210.193 \pm ,\ 440.024 + 210.193 \pm ,
 446.655 - 209.198 \, \dot{\text{i}} \, , \, 446.655 + 209.198 \, \dot{\text{i}} \, , \, 453.432 - 208.084 \, \dot{\text{i}} \, , \, 453.432 + 208.084 \, \dot{\text{i}} \, , \, 463.432 + 208.084 \, \dot{\text{i}} \, , \, 463.
 460.363 - 206.841 \pm ,\ 460.363 + 206.841 \pm ,\ 467.458 - 205.462 \pm ,\ 467.458 + 205.462 \pm ,
 474.728 - 203.937 \; \text{i} \; , \; 474.728 + 203.937 \; \text{i} \; , \; 482.184 - 202.255 \; \text{i} \; , \; 482.184 + 202.255 \; \text{i} \; , 
 489.84 - 200.404\,\dot{\mathtt{n}}\,,\, 489.84 + 200.404\,\dot{\mathtt{n}}\,,\, 497.71 - 198.37\,\dot{\mathtt{n}}\,,\, 497.71 + 198.37\,\dot
505.813 - 196.138 \,\, \dot{\text{i}} \,\,, \, 505.813 \,+ 196.138 \,\, \dot{\text{i}} \,\,, \, 514.166 \,- 193.692 \,\, \dot{\text{i}} \,\,, \, 514.166 \,+ 193.692 \,\, \dot{\text{i}} \,\,, \, 514.166 \,\,, \, 193.692 \,\, \dot{\text{i}} \,\,, \, 193.692 \,\, \dot
 522.794 - 191.009 i, 522.794 + 191.009 i, 531.722 - 188.068 i, 531.722 + 188.068 i,
 540.98 - 184.842 i, 540.98 + 184.842 i, 550.606 - 181.298 i, 550.606 + 181.298 i,
560.643 - 177.397 \, \text{i}, 560.643 + 177.397 \, \text{i}, 571.145 - 173.095 \, \text{i}, 571.145 + 173.095 \, \text{i},
 582.179 - 168.334 i, 582.179 + 168.334 i, 593.827 - 163.042 i, 593.827 + 163.042 i,
 606.2 - 157.129 \, \text{i}, 606.2 + 157.129 \, \text{i}, 619.443 - 150.472 \, \text{i}, 619.443 + 150.472 \, \text{i},
 633.758 - 142.908 \, \dot{\text{i}} \, , \, 633.758 + 142.908 \, \dot{\text{i}} \, , \, 649.442 - 134.199 \, \dot{\text{i}} \, , \, 649.442 + 134.199 \, \dot{\text{i}} \, , \, \\
 666.956 - 123.985\,\dot{\text{i}}, 666.956 + 123.985\,\dot{\text{i}}, 687.102 - 111.665\,\dot{\text{i}}, 687.102 + 111.665\,\dot{\text{i}},
 711.506 - 96.086 \pm ,\ 711.506 + 96.086 \pm ,\ 744.694 - 74.3335 \pm ,\ 744.694 + 74.3335 \pm \}
```

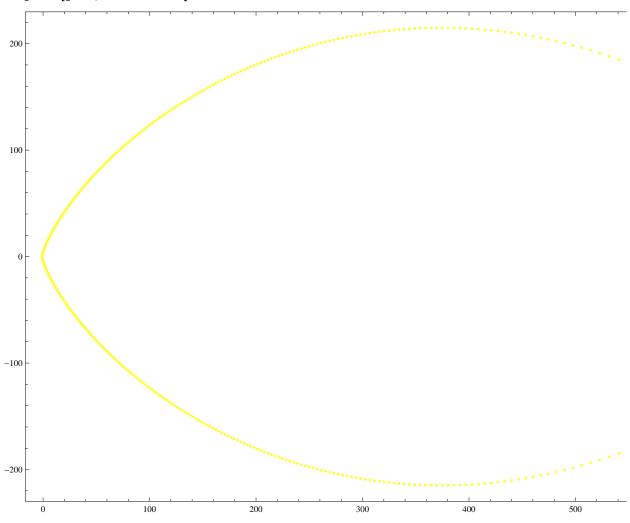
#### N@Product[1-1/r, {r, pocrootsa[400]}]

2. + 7.49717  $\times$  10<sup>-17</sup> i

#### N@2^ZetaZero[1]

-1.31714 - 0.514916 i

colfunc = ColorData["AvocadoColors"];  ${\tt pts1 = Table[\{colfunc[100], Point[\{Re[\#], Im[\#]\}]\} \& /@N@pocrootsa[400], \{n, 1, 1\}];}$  $Graphics[pts1, Frame \rightarrow True]$ 



Sum[Binomial[-ZetaZero[1], k], {k, 0, Infinity}]

Sum::div : Sum does not converge.  $\gg$ 

$$\sum_{k=0}^{\infty} \texttt{Binomial}[\,-\,\texttt{ZetaZero}\,[\,1\,]\,\,,\,\,k\,]$$

Sum::div : Sum does not converge.  $\gg$ 

$$\sum_{k=0}^{\infty} \texttt{Binomial}\left[\,\text{--}\,0.5\,+\,14\,.\,\,\dot{\mathbb{1}}\,,\,\,k\,\right]$$

## 1/2^ZetaZero[1]

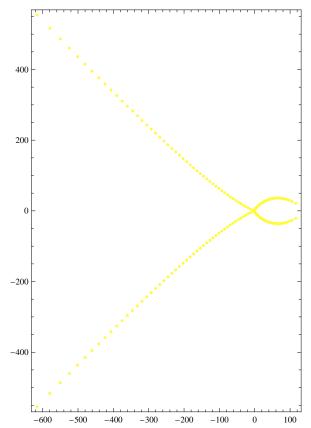
2-ZetaZero[1]

```
Clear[px, pz, t]
t[n_, a_, b_] :=
           t[n, a, b] = b (Floor[n/b] - Floor[(n-1)/b]) - a (Floor[n/a] - Floor[(n-1)/a])
px[n_{,a_{,b_{,1}}} = t[n, a, b] / n
px[n_{,a_{,b_{,0}}} a_{,b_{,0}}] := 0
pz[n_{, a_{, b_{, 0}}} = 1]
pz[0, a_, b_, z_] := 1
N@pocxrootsa[200, 3, 1]
    \{-1204.08, -1135.59, -1080.62, -1032.89, -989.963, -950.57, -913.949, -879.593, -847.143, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.963, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989.965, -989
           -816.333, -786.96, -758.862, -731.91, -705.997, -681.034, -656.945, -633.666, -611.141,
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           -435.881, -418.941, -402.433, -386.338, -370.644, -355.337, -340.404, -325.833, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.338, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386.388, -386
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           -0.780608 - 1.08241 \, i, -0.780608 + 1.08241 \, i, -0.37672 - 2.13676 \, i, -0.37672 + 2.13676 \, i,
            0.116421 - 3.22249 \pm, \ 0.116421 + 3.22249 \pm, \ 0.685648 - 4.33882 \pm, \ 0.685648 + 4.33882 \pm, \ 0.68
            1.32446 - 5.48178 \, \dot{\text{i}}, 1.32446 + 5.48178 \, \dot{\text{i}}, 2.02732 - 6.64776 \, \dot{\text{i}}, 2.02732 + 6.64776 \, \dot{\text{i}},
           2.78964 - 7.83337 \, \dot{\text{i}} \; , \; 2.78964 + 7.83337 \, \dot{\text{i}} \; , \; 3.6079 - 9.03544 \, \dot{\text{i}} \; , \; 3.6079 + 9.03544 \, \dot{\text{i}} \; 
            4.47946 - 10.2512 i, 4.47946 + 10.2512 i, 5.40234 - 11.4784 i, 5.40234 + 11.4784 i,
           6.37498 - 12.7148 \, \text{i}, 6.37498 + 12.7148 \, \text{i}, 7.39615 - 13.9588 \, \text{i}, 7.39615 + 13.9588 \, \text{i},
            8.46486 - 15.2087 \; \text{i} \; , \; 8.46486 + 15.2087 \; \text{i} \; , \; 9.58035 - 16.4631 \; \text{i} \; , \; 9.58035 + 16.4631 \; \text{i} \; , \; \\
            10.742 - 17.7206 \, \text{i}, 10.742 + 17.7206 \, \text{i}, 11.9493 - 18.9799 \, \text{i}, 11.9493 + 18.9799 \, \text{i},
           13.2021 - 20.2398 \, \dot{\text{i}} \, , \, 13.2021 + 20.2398 \, \dot{\text{i}} \, , \, 14.4999 - 21.4993 \, \dot{\text{i}} \, , \, 14.4999 + 21.4999 \, \dot{\text{i}} \, , \, 14.4
           15.8428 - 22.7572 \pm , \ 15.8428 + 22.7572 \pm , \ 17.2308 - 24.0123 \pm , \ 17.2308 + 24.0123 \pm , \ 24
           18.6638 - 25.2636 \; \dot{\text{i}} \; , \; 18.6638 + 25.2636 \; \dot{\text{i}} \; , \; 20.142 - 26.5102 \; \dot{\text{i}} \; , \; 20.142 + 26.5102 \; \dot{\text{i}} \; 
            21.6658 - 27.7508 i, 21.6658 + 27.7508 i, 23.2353 - 28.9844 i, 23.2353 + 28.9844 i,
            24.851 - 30.2099 i, 24.851 + 30.2099 i, 26.5135 - 31.4263 i, 26.5135 + 31.4263 i,
            28.2232 - 32.6323 \, \text{i}, 28.2232 + 32.6323 \, \text{i}, 29.9808 - 33.8269 \, \text{i}, 29.9808 + 33.8269 \, \text{i},
           31.787 - 35.0087 \, \text{i}, 31.787 + 35.0087 \, \text{i}, 33.6428 - 36.1765 \, \text{i}, 33.6428 + 36.1765 \, \text{i},
            35.5489 - 37.329 \, \text{i}, 35.5489 + 37.329 \, \text{i}, 37.5065 - 38.4647 \, \text{i}, 37.5065 + 38.4647 \, \text{i},
            39.5168 - 39.5822 i, 39.5168 + 39.5822 i, 41.5809 - 40.6798 i, 41.5809 + 40.6798 i,
            43.7004 - 41.756 \pm ,\ 43.7004 + 41.756 \pm ,\ 45.8767 - 42.8089 \pm ,\ 45.8767 + 42.8089 \pm ,\ 45.8087 + 42.8089 \pm ,\
            48.1116 - 43.8366\,\,\dot{\text{i}}, 48.1116 + 43.8366\,\,\dot{\text{i}}, 50.4071 - 44.837\,\,\dot{\text{i}}, 50.4071 + 44.837\,\,\dot{\text{i}},
            52.7651 - 45.8078 i, 52.7651 + 45.8078 i, 55.1881 - 46.7466 i, 55.1881 + 46.7466 i,
           57.6786 - 47.6507 \, \text{i}, 57.6786 + 47.6507 \, \text{i}, 60.2396 - 48.5173 \, \text{i}, 60.2396 + 48.5173 \, \text{i},
           62.8741 - 49.343\,\dot{\mathrm{i}}, 62.8741 + 49.343\,\dot{\mathrm{i}}, 65.5858 - 50.1244\,\dot{\mathrm{i}}, 65.5858 + 50.1244\,\dot{\mathrm{i}},
            68.3787 - 50.8575 i, 68.3787 + 50.8575 i, 71.2574 - 51.5379 i, 71.2574 + 51.5379 i,
           74.227 - 52.1608 \, \text{i}, 74.227 + 52.1608 \, \text{i}, 77.2933 - 52.7205 \, \text{i}, 77.2933 + 52.7205 \, \text{i},
           80.463 - 53.2108\,\dot{\text{i}}, 80.463 + 53.2108\,\dot{\text{i}}, 83.7438 - 53.6246\,\dot{\text{i}}, 83.7438 + 53.6246\,\dot{\text{i}},
           87.1447 - 53.9536\,\,\dot{\text{i}} , 87.1447 + 53.9536\,\,\dot{\text{i}} , 90.676 - 54.1883\,\,\dot{\text{i}} , 90.676 + 54.1883\,\,\dot{\text{i}} ,
            94.3501 - 54.3176\,\,\dot{\text{i}}, 94.3501 + 54.3176\,\,\dot{\text{i}}, 98.1817 - 54.3283\,\,\dot{\text{i}}, 98.1817 + 54.3283\,\,\dot{\text{i}},
           102.188 - 54.2048 \; \text{i} \; , \; 102.188 + 54.2048 \; \text{i} \; , \; 106.392 - 53.9281 \; \text{i} \; , \; 106.392 + 53.9281 \; \text{i} \; , \; 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 106.392 + 
           110.82 - 53.4748 i, 110.82 + 53.4748 i, 115.506 - 52.8156 i, 115.506 + 52.8156 i,
           120.496 - 51.9131 \, i, 120.496 + 51.9131 \, i, 125.848 - 50.7177 \, i, 125.848 + 50.7177 \, i,
           131.647 - 49.162 \pm , \ 131.647 + 49.162 \pm , \ 138.014 - 47.1493 \pm , \ 138.014 + 47.1493 \pm , \ 138.01
           145.141 - 44.5327 \, \text{i}, 145.141 + 44.5327 \, \text{i}, 153.358 - 41.0673 \, \text{i}, 153.358 + 41.0673 \, \text{i},
```

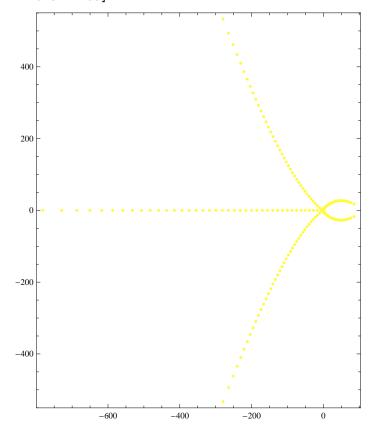
 $163.339 - 36.2828 \pm 1, 163.339 + 36.2828 \pm 1, 176.961 - 28.9948 \pm 1, 176.961 + 28.9948 \pm 1, -2., -1.$ 

```
Graphics[
  Table[\{colfunc[100], Point[\{Re[\#], Im[\#]\}]\} \& /@N@pocxrootsa[200, 3, 1], \{n, 1, 1\}], \} 
 Frame → True]
50
-50
     -1200
                                -1000
                                                            -800
Graphics[
 Frame → True]
 100
 50
 0
-50
-100
              100
N@Sum[-1/r, \{r, pocxrootsa[200, 3, 1]\}]
1.1036 + 0. i
Chop@N@Product[1 -1/r, {r, pocxrootsa[200, 3, 1]}]
N@Sum[-1/r, {r, pocxrootsa[200, 4, 1]}]
1.37883 + 0. i
Chop@N@Product[1 -1/r, {r, pocxrootsa[200, 4, 1]}]
4.
Log[4.]
1.38629
```

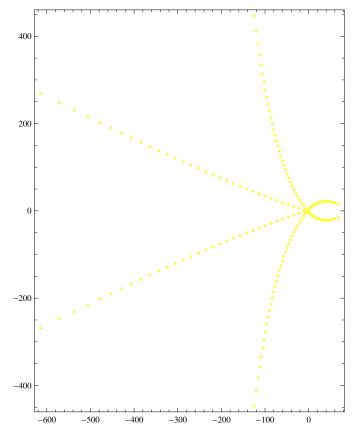
Graphics[ Frame → True]



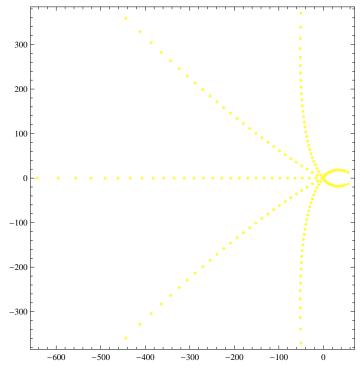
Graphics[ Frame → True]



Graphics[  $Table[\{colfunc[100], Point[\{Re[\#], Im[\#]\}]\} \& /@N@pocxrootsa[200, 6, 1], \{n, 1, 1\}], And And Andrews Andrews$ Frame → True]



## Graphics[ $\label{localization} Table[\{colfunc[100], Point[\{Re[\#], Im[\#]\}]\} \& /@N@pocxrootsa[200, 7, 1], \{n, 1, 1\}], \\$ $Frame \rightarrow True]$

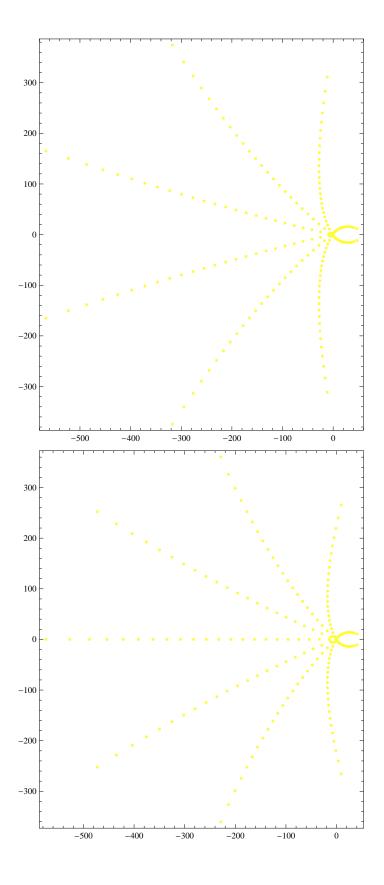


## Graphics[

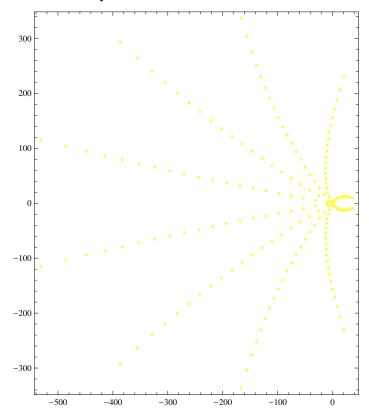
 $\label{lem:colfunc [100], Point[{Re[\#], Im[\#]}]} & @ N@pocxrootsa[200, 8, 1], {n, 1, 1}], \\ \end{aligned}$ Frame → True]

## Graphics[

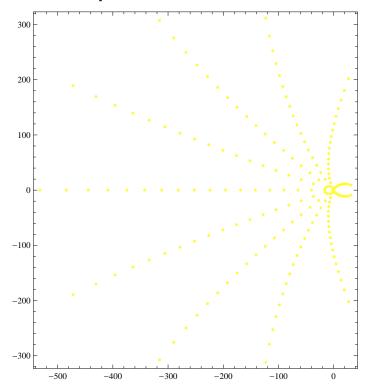
 $\label{lem:colfunc [100], Point[{Re[\#], Im[\#]}]} & @ N@pocxrootsa[200, 9, 1], {n, 1, 1}], \\ \end{aligned}$ Frame → True]



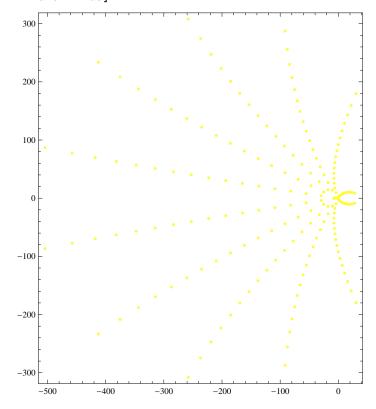
Graphics[  $Frame \rightarrow True]$ 



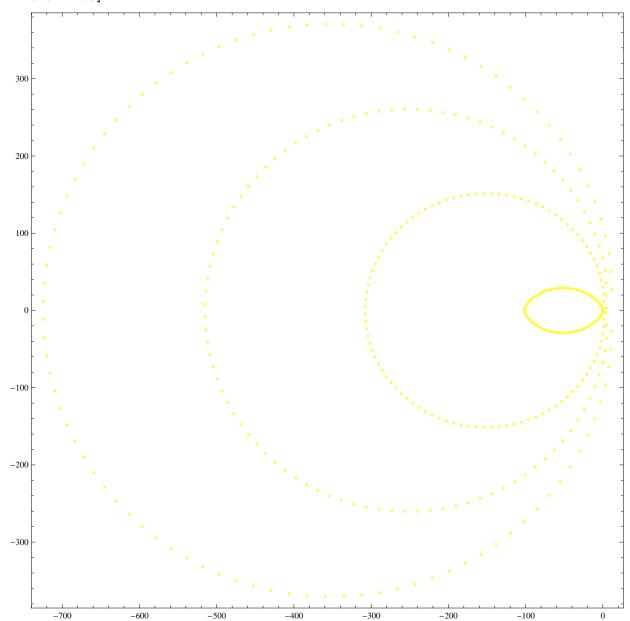
Graphics[  $Frame \rightarrow True]$ 



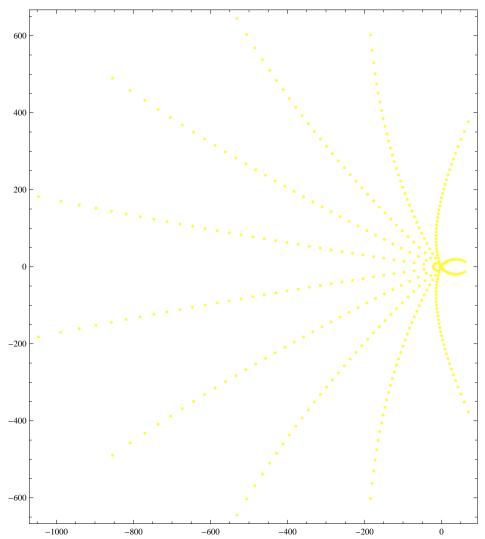
Graphics[  $Frame \rightarrow True]$ 



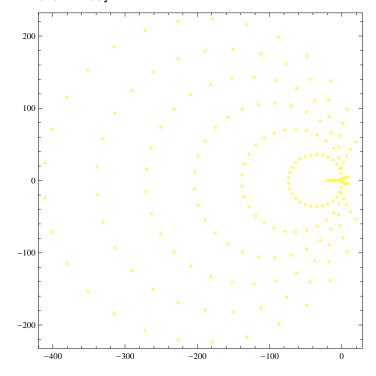
Graphics[  $Table[\{colfunc[100], Point[\{Re[\#], Im[\#]\}]\} \& /@N@pocxrootsa[400, 100, 1], \{n, 1, 1\}], And And Andrews Andre$ Frame → True]



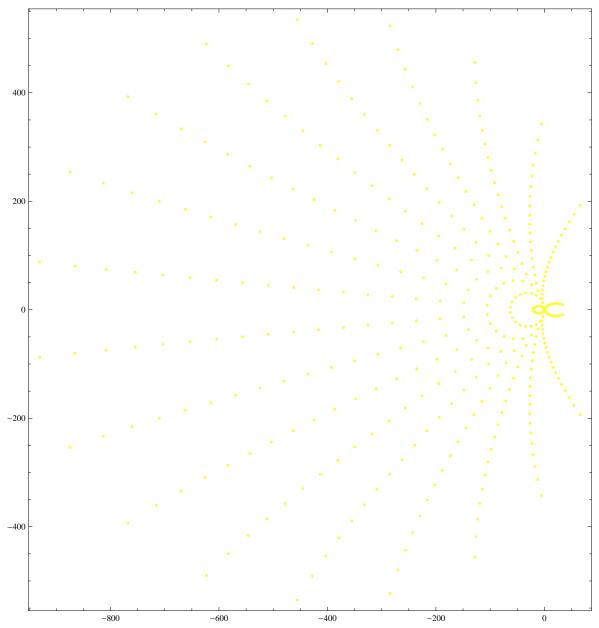
Graphics[  $Frame \rightarrow True]$ 



Graphics[ Frame → True]



Graphics[  $Frame \rightarrow True]$ 



# poccrootsa[8]

$$\{\,-\,8\;,\;\,-\,7\;,\;\,-\,6\;,\;\,-\,5\;,\;\,-\,4\;,\;\,-\,3\;,\;\,-\,2\;,\;\,-\,1\,\}$$

## Expand@pocc[8, z]

$$1 + \frac{761\,z}{280} + \frac{29\,531\,z^2}{10\,080} + \frac{267\,z^3}{160} + \frac{1069\,z^4}{1920} + \frac{9\,z^5}{80} + \frac{13\,z^6}{960} + \frac{z^7}{1120} + \frac{z^8}{40\,320} + \frac{1069\,z^4}{1120} + \frac{1069\,z^4}{1120}$$

Expand@ (Product[ (z+k),  $\{k, 1, 8\}$ ] / 8!)

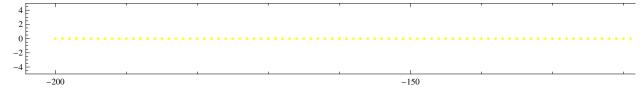
$$1 + \frac{761 \text{ z}}{280} + \frac{29531 \text{ z}^2}{10080} + \frac{267 \text{ z}^3}{160} + \frac{1069 \text{ z}^4}{1920} + \frac{9 \text{ z}^5}{80} + \frac{13 \text{ z}^6}{960} + \frac{\text{z}^7}{1120} + \frac{\text{z}^8}{40320}$$

Expand[Pochhammer[z+1, 8] / 8!]

$$1 + \frac{761 z}{280} + \frac{29531 z^2}{10080} + \frac{267 z^3}{160} + \frac{1069 z^4}{1920} + \frac{9 z^5}{80} + \frac{13 z^6}{960} + \frac{z^7}{1120} + \frac{z^8}{40320}$$

Graphics[Table[{colfunc[100], Point[{Re[#], Im[#]}]} & /@ N@poccrootsa[200], {n, 1, 1}],

Frame → True]



Graphics[

```
Table[{colfunc[100], Point[{Re[#], Im[#]}]} & /@ N@pocxrootsa[20, 20, 1], {n, 1, 1}],
Frame \rightarrow True]
```

```
pts4 = Table[{Point[{Re[#], Im[#]}]} & /@ pocxrootsa[n, 12, 1], {n, 1, 200}];
\texttt{ListAnimate[Table[Graphics[pts4[[k]], Frame} \rightarrow \texttt{True, Axes} \rightarrow \texttt{True,}
    AxesOrigin \rightarrow {0, 0}, PlotRange \rightarrow {{-1000, 100}, {-500, 500}}], {k, 1, Length[pts4]}]]
```

pts4

pocx[50, 1, 2, -4]

16