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K[n_] := If[n == 1, 0, FullSimplify[MangoldtLambda[n] / Log[n]]]
P[n_, k_] := P[n, k] = Sum[K[j] P[Floor[n / j], k - 1], {j, 2, n}]; P[n_, 0] := 1
DDa[n_, z_] := Sum[z^k / k! P[n, k], {k, 0, Log[2, n]}]

f[t_] := FullSimplify[DDa[100, t]]
f2[s_] := Integrate[FullSimplify[E^(-s t) f[t]], {t, 0, Infinity}]

Expand[f2[s]]

ConditionalExpression[ $\frac{7}{s^7} + \frac{67}{2 s^6} + \frac{611}{6 s^5} + \frac{993}{8 s^4} + \frac{16289}{180 s^3} + \frac{428}{15 s^2} + \frac{1}{s}$ , Re[s] > 0]

f3[s_] :=  $\frac{7}{s^7} + \frac{67}{2 s^6} + \frac{611}{6 s^5} + \frac{993}{8 s^4} + \frac{16289}{180 s^3} + \frac{428}{15 s^2} + \frac{1}{s}$ 

N[Roots[f3[x] == 0, x]]

x == -25.1214 || x == -1.78282 || x == -0.616185 - 0.940804 i ||
x == -0.616185 + 0.940804 i || x == -0.198375 - 0.290209 i || x == -0.198375 + 0.290209 i

Expand[f[t]]

 $1 + \frac{428 t}{15} + \frac{16289 t^2}{360} + \frac{331 t^3}{16} + \frac{611 t^4}{144} + \frac{67 t^5}{240} + \frac{7 t^6}{720}$ 

f4[t_, g_] := 1 / (2 Pi I) Limit[Integrate[E^(s t) f3[s], {s, g - I T, g + I T}], T -> Infinity]

Limit[(f4[z, 1] - 1) / z, z -> 0]

$Aborted

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