```
Ela[n_, k_, a_, s_] := Ela[n, k, a, s] = Sum[j^(-s) Ela[n/j, k-1, a, s], {j, 1, n}] -
    a Sum[(ja)^(-s) Ela[n/(aj), k-1, a, s], {j, 1, n/a}]; Ela[n_, 0, a_, s_] := 1

DDa[n_, k_, s_] := DDa[n, k, s] = Sum[j^(-s) DDa[Floor[n/j], k-1, s], {j, 1, n}];

DDa[n_, 0, s_] := 1

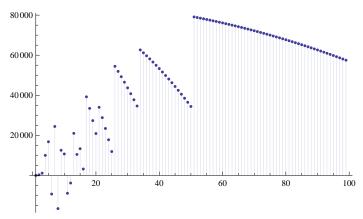
DDc[n_, k_, b_, s_] :=
    Sum[Binomial[k+j-1, k-1] b^(j(1-s)) Ela[n/(b^j), k, b, s], {j, 0, Log[b, n]}]

Elc[n_, k_, b_, s_] := Sum[(-1)^jBinomial[k, j] b^(j(1-s)) DDa[n/b^j, k, s], {j, 0, k}]

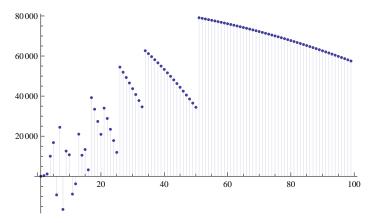
Ela[100, 1, 100, -1]
-4950

Elc[100, 1, 100, -1]
```

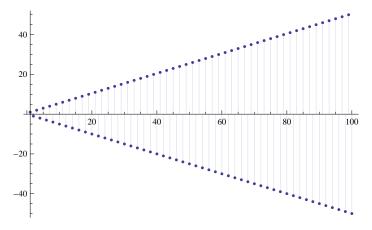
DiscretePlot[ E1a[100, 3, n, -1], {n, 1, 99}]



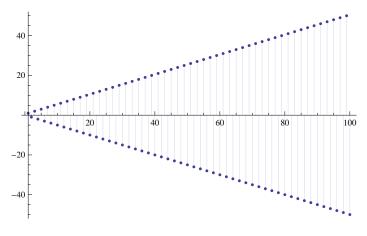
#### DiscretePlot[E1c[100, 3, n, -1], {n, 1, 99}]



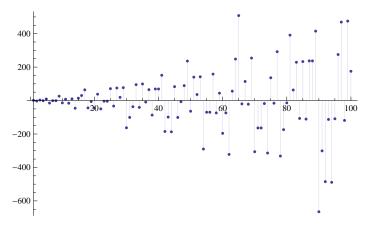
# ${\tt DiscretePlot[\ Ela[n, 1, 2, -1], \{n, 1, 100\}]}$



### ${\tt DiscretePlot[\,DDa[n,\,1,\,-1]\,-4\,DDa[Floor[n\,/\,2]\,,\,1,\,-1]\,,\,\{n,\,1,\,100\}]}$

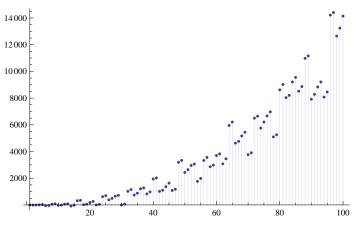


### DiscretePlot[ E1a[n, 2, 2, -1], $\{n, 1, 100\}$ ]

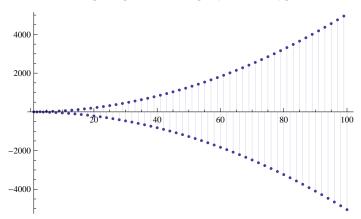


#### DiscretePlot[

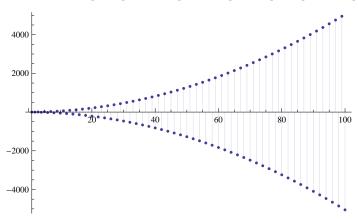
 $(\ DDa[n,\,2,\,-1]\,-16\,DDa[Floor[n\,/\,2]\,,\,2,\,-1]\,+64\,DDa[Floor[n\,/\,4]\,,\,2,\,-1])\,,\,\{n,\,1,\,100\}]$ 



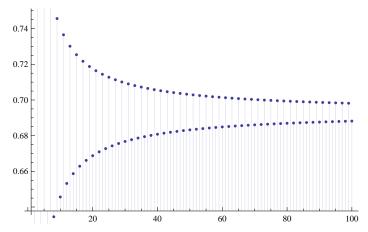
DiscretePlot[Ela[n, 1, 2, -2], {n, 1, 100}]



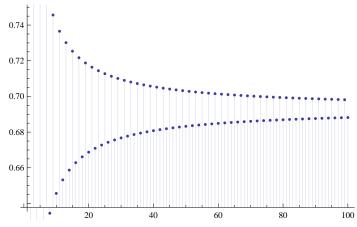
 $\label{eq:defDDa} \ \, \text{DiscretePlot} \ \, [ \ \, \text{DDa} \left[ n, \, 1, \, -2 \right] \, - \, 8 \, \, \text{DDa} \left[ \text{Floor} \left[ n \, / \, 2 \right] \, , \, 1, \, -2 \right] \, , \, \left\{ n, \, 1, \, 100 \right\} \right]$ 



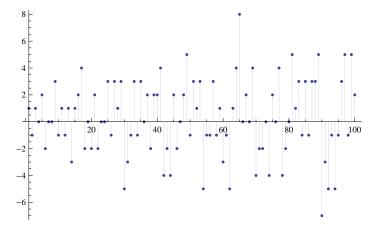
# ${\tt DiscretePlot[\,Ela[n,\,1,\,2,\,1]\,,\,\{n,\,1,\,100\}]}$



# ${\tt DiscretePlot[\,DDa[n,\,1,\,1]\,-1\,DDa[Floor[n\,/\,2]\,,\,1,\,1]\,,\,\{n,\,1,\,100\}]}$

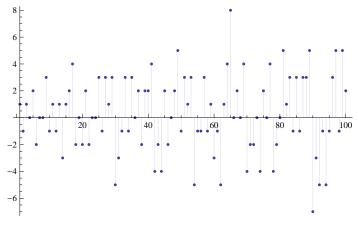


# ${\tt DiscretePlot[\,Ela[n,\,2,\,2,\,0]\,,\,\{n,\,1,\,100\}]}$

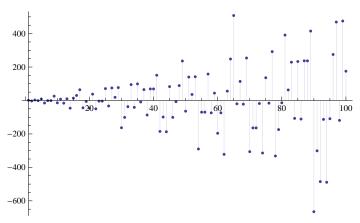


#### DiscretePlot[

 $(\ DDa[n, 2, 0] - (2 \times 2) \ DDa[Floor[n / 2], 2, 0] + (1 \times 4) \ DDa[Floor[n / 4], 2, 0]) \, , \, \{n, 1, 100\}]$ 

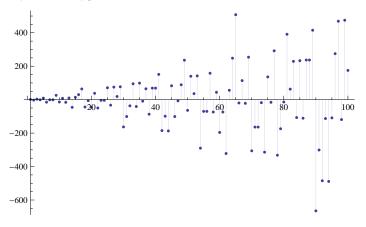


### DiscretePlot[ $E1a[n, 2, 2, -1], \{n, 1, 100\}$ ]

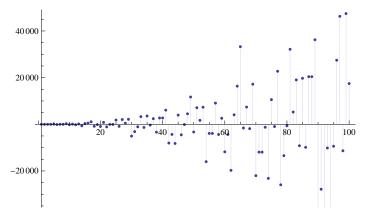


#### DiscretePlot[

 $(\; DDa\,[n,\,2,\,-1]\,-\,(2\times2\times2)\; DDa\,[Floor\,[n\,/\,2]\,,\,2,\,-1]\,+\,(1\times4\times4)\; DDa\,[Floor\,[n\,/\,4]\,,\,2,\,-1])\,, \\$ {n, 1, 100}]

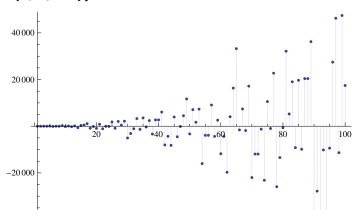


### DiscretePlot[ E1a[n, 2, 2, -2], $\{n, 1, 100\}$ ]

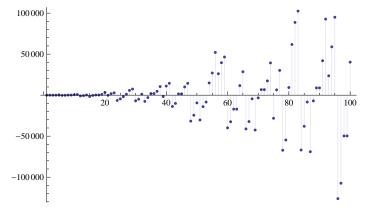


### DiscretePlot[

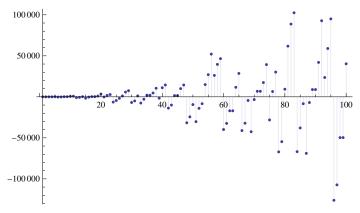
(  $DDa[n, 2, -2] - (2 \times 2 \times 4) DDa[Floor[n/2], 2, -2] + (1 \times 4 \times 16) DDa[Floor[n/4], 2, -2])$ , {n, 1, 100}]



## DiscretePlot[ $E1a[n, 2, 3, -2], \{n, 1, 100\}$ ]



 $\begin{tabular}{ll} $(\ DDa[n,\ 2,\ -2] - (2 \times 3 \times 9)\ DDa[Floor[n/3],\ 2,\ -2] + (1 \times 9 \times 81)\ DDa[Floor[n/9],\ 2,\ -2]), \\ $(n,\ 1,\ 100)] \end{tabular}$ 



FullSimplify[b^jb^(-js)]

 $b^{j-j\,s}$ 

DDc[100, 3, 1.5, -1]

86914.

DDa[100, 3, -1]

86 914