$\mathtt{DApprox[j_]} := (-1) \land j + \mathtt{Sum[(-1) \land (j-k+1) / (k!) n (Log[n]) \land k, \{k, 0, j-1\}]}$

DApprox[j]

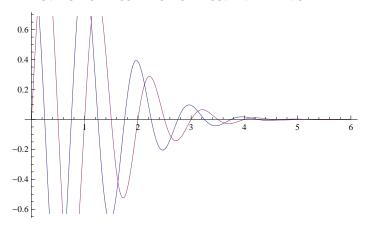
$$\left(-1\right)^{j}-rac{\left(-1\right)^{j}\operatorname{Gamma}\left[j,-\operatorname{Log}\left[n
ight]
ight]}{\operatorname{Gamma}\left[j\right]}$$

$$FF[n_{,},j_{]} := (-1)^{j} - \frac{(-1)^{j} Gamma[j,-Log[n]]}{Gamma[j]}$$

FF[n, -1]

- 1

Plot[{Re[FF[2, j]], Im[FF[2, j]]}, {j, 0, 6}]



$$FF2[n_{-}, j_{-}] := \left(\left((-1)^{j} - \frac{(-1)^{j} Gamma[j, -Log[n]]}{Gamma[j]} \right) - 1 \right) / j$$

Expand[FF2[n, 0.000000000000001]]

$$(0. + 3.14159 i) - (1. + 3.14159 \times 10^{-16} i)$$
 Gamma $[1. \times 10^{-16}, -Log[n]]$

 $FF3a[n_] := -Gamma[0, -Log[n]]$

FF3a[n]

-Gamma[0, -Log[n]]

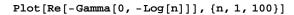
N[FF3a[a = 100]]

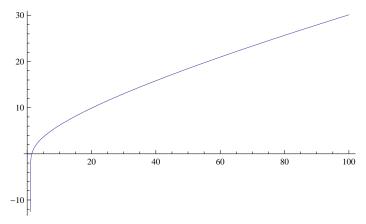
N[LogIntegral[a]]

30.1261 + 3.14159 i

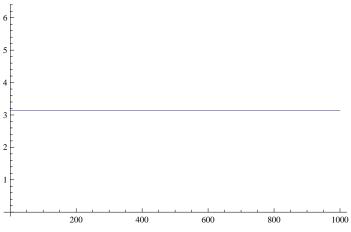
30.1261

30.1261





$Plot[Im[1-Gamma[0, -Log[n]]], {n, 1, 1000}]$



-Gamma[0,-n]

-Gamma[0, -n]

Gamma[0]

 ${\tt ComplexInfinity}$

 ${\tt FullSimplify[(1/Gamma[z])\ (1/z)]}$

 $\frac{1}{\text{Gamma}[1+z]}$ $\frac{1}{\text{Gamma}[1+0]}$

1