

```

f1[y_, s_] := -Log[y]^s Integrate[ y^x (-x)^(s-1), {x, 0, 1}]
f2[y_, s_] := Gamma[s, 0, -Log[y]]

N[f1[10, 6]]

185.331

N[f2[10, 6]]

185.331 - 1.36179 × 10-13 i

f1a[y_, s_, n_] := -Log[y]^s Integrate[ y^(nx) (n (-x))^(s-1), {x, 0, 1}]
f2a[y_, s_, n_] := Gamma[s, 0, -n Log[y]] / n

f1b[y_, s_, n_] := -(n)^(s-1) Log[y]^s Integrate[ y^(nx) (-x)^(s-1), {x, 0, 1}]
f2b[y_, s_, n_] := Gamma[s, 0, -n Log[y]] / n

N[f1b[5, 4, 3]]

2735.03

N[f2b[5, 4, 3]]

2735.03 - 1.0041 × 10-12 i

f1c[y_, s_, n_] := -Log[y]^s Integrate[ y^(nx) (-x)^(s-1), {x, 0, 1}]
f2c[y_, s_, n_] := Gamma[s, 0, -n Log[y]] / n / n^(s-1)

N[f1c[5, 3, 4]]

-298.496

N[f2c[5, 3, 4]]

-298.496 + 7.3118 × 10-14 i

f1d[y_, s_, n_] := -Log[y]^s Integrate[ y^(nx) (-x)^(s-1), {x, 0, 1}]
f2d[y_, s_, n_] := Gamma[s, 0, -n Log[y]] / n^s

N[f1d[3, 3, 3]]

-6.19679

N[f2d[3, 3, 3]]

-6.19679 + 1.53592 × 10-15 i

f1e[y_, s_] := -Log[y]^s Integrate[Sum[ y^(nx), {n, 1, Infinity}]] (-x)^(s-1), {x, 0, 1}]
f2e[y_, s_] := Sum[ Gamma[s, 0, -n Log[y]] / n^s, {n, 1, 100000}]

N[f1e[.5, 3]]

0.189506

N[f2e[.5, 3]]

0.189506

```

```
f1f[y_, s_] := -Log[y]^s Integrate[ $\left(-\frac{y^x}{-1+y^x}\right) (-x)^{(s-1)}, \{x, 0, 1\}]$ 
```

```
f2f[y_, s_] := Sum[Gamma[s, 0, -n Log[y]] / n^s, {n, 1, 100 000}]
```

```
N[f1f[.5, 3]]
```

```
0.189506
```

```
N[f2f[.5, 3]]
```

```
0.189506
```

```
Sum[y^(n x), {n, 1, Infinity}]
```

```

$$-\frac{y^x}{-1+y^x}$$

```

```
N[Log[100]^s Integrate[100^x x^(s-1), {x, 0, 1}] /. s -> 2]
```

```
361.517 - 4.41506 × 10-14 i
```

```
N[Abs[Gamma[2, 0, -Log[100]]]]
```

```
361.517
```

```
FullSimplify[Log[100]^s Integrate[100^-x x^(s-1), {x, 0, 1}] /. s -> 2]
```

```
1 - Gamma[2, Log[100]]
```

```
Log[100]^s Integrate[100^x (-x)^(s-1), {x, 0, 1}] /. s -> 5
```

```
-24 + Gamma[5, -2 Log[10]]
```