

```
ClearAll["Global`*"]
```

```
d1[n_, k_, s_] := Sum[j^s d1[n / j, k - 1, s], {j, 1, n}]; d1[n_, 0, s_] := 1
d1a[n_, k_, a_, s_] := Sum[j^s a d1a[n / j, k - 1, a, s], {j, a, n / (a^(k - 1))}, a];
d1a[n_, 0, a_, s_] := 1
d1b[n_, k_, a_, s_] := Sum[(j a)^s a d1b[n / (j a), k - 1, a, s], {j, 1, n / (a^k)}];
d1b[n_, 0, a_, s_] := 1
d1c[n_, k_, a_, s_] := (a^(1 + s))^k d1[na^-k, k, s]
d11[n_, k_, a_, s_] := (a^(1 + s))^-k d1a[na^k, k, a, s]
```

```
N[d1b[100, 3, 1.31, -1]]
```

```
26.6256
```

```
N[d1c[100, 3, 1.31, -1]]
```

```
26.6256
```

```
N[d1a[100, 1, 3 / 4, 1]]
```

```
5012.44
```

```
N[d1c[100, 1, 3 / 4, 1]]
```

```
5012.44
```

```
d1[100, 2, 2]
```

```
1867051
```

```
d11[100, 2, 1 / 3, 2]
```

```
1867051
```

```
a a^s
```

```
a1+s
```

```
FullSimplify[(a^(1 + s))^k]
```

$$(a^{1+s})^k$$

```
(a^(1 + s))^k /. s -> -2
```

$$\left(\frac{1}{a}\right)^k$$

```
d1[100, 1, 1, -1]
```

```
(1 / 2)^(1 / 2) N[d1[200, 1, -1 / 2]]
```

```
18.9924
```

```
N[d1b[100, 1, 1 / 2, -1 / 2]]
```

```
18.9924
```

```
N[d1[200, 1, -2]]
```

```
1.63995
```

```
N[d1b[100, 1, 1 / 8, -2]] / 8
```

```
1.64368
```

