

```

Expand[Sum[ 1 / ((3 k - 2) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((3 k - 1) ^ 3), {k, 1, Infinity}]]
Expand[Sum[ 1 / ((4 k - 3) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((4 k - 1) ^ 3), {k, 1, Infinity}]]
Expand[Sum[ 1 / ((6 k - 4) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((6 k - 2) ^ 3), {k, 1, Infinity}]]
Expand[Sum[ 1 / ((6 k - 5) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((6 k - 1) ^ 3), {k, 1, Infinity}]]
Expand[Sum[ 1 / ((8 k - 2) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((8 k - 6) ^ 3), {k, 1, Infinity}]]
Expand[Sum[ 1 / ((9 k - 6) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((9 k - 3) ^ 3), {k, 1, Infinity}]]
Expand[ Sum[ 1 / ((12 k - 2) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((12 k - 10) ^ 3), {k, 1, Infinity}]]
Expand[ Sum[ 1 / ((12 k - 3) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((12 k - 9) ^ 3), {k, 1, Infinity}]]
Expand[ Sum[ 1 / ((12 k - 4) ^ 3), {k, 1, Infinity}] - Sum[ 1 / ((12 k - 8) ^ 3), {k, 1, Infinity}]]

```

$$\begin{aligned}
& \frac{4 \pi^3}{81 \sqrt{3}} \\
& \frac{\pi^3}{32} \\
& \frac{\pi^3}{162 \sqrt{3}} \\
& \frac{\pi^3}{18 \sqrt{3}} \\
& - \frac{\pi^3}{256} \\
& \frac{4 \pi^3}{2187 \sqrt{3}} \\
& - \frac{\pi^3}{144 \sqrt{3}} \\
& - \frac{\pi^3}{864} \\
& - \frac{\pi^3}{1296 \sqrt{3}}
\end{aligned}$$