

```

N[10^ZetaZero[1]]
1.34784 + 2.86065 i

N[ExpIntegralEi[(1 - ZetaZero[1]) Log[10]]]
0.0880046 - 3.10063 i

N[-Gamma[0, -(1 - ZetaZero[1]) Log[10]]] - Pi I
0.0880046 - 3.10063 i

N[-Sum[1/j (1 - Gamma[j, -ZetaZero[1] Log[10]] / Gamma[j]), {j, 1, 1360}]]
-4.54189 + 1.57113 i

N[LogIntegral[10^ZetaZero[1]]]
1.97481 + 2.7126 i

N[-Sum[1/j ((Gamma[j, 0, -(1 - ZetaZero[1]) Log[10]] - Pi I) / Gamma[j]), {j, 1, 1360}]]
-4.54219 + 3.8269 i

fp[n_, a_] := Sum[(a^(1 - ZetaZero[1]))^k - 1 / k, {k, 1, Log[a, n]}] +
  Log[(1 - ZetaZero[1]) Log[n]] + EulerGamma
fp[10, 1.0001]
0.0879872 - 3.09999 i

se[n_, a_, s_] := Sum[(a^(1 - s))^k - 1 / k, {k, 1, Log[a, n]}]
s = N[ZetaZero[1]]; {se[nn = 10, 1.00001, s] + EulerGamma + Log[(1 - s) Log[nn]],
  N[ExpIntegralEi[(1 - s) Log[nn]]], -Gamma[0, -(1 - s) Log[nn]] - Pi I}
{0.0880018 - 3.10056 i, 0.0880046 - 3.10063 i, 0.0880046 - 3.10063 i}

se[10, 1.00001, N[ZetaZero[1]]] + EulerGamma + Log[(1 - ZetaZero[1]) Log[10]]
0.0880018 - 3.10056 i

N[ExpIntegralEi[(1 - ZetaZero[1]) Log[10]]]
0.0880046 - 3.10063 i

Limit[(Gamma[a, 0, -Log[n^(1 - ZetaZero[1])]] / Gamma[a] - 1) / a, {a -> 0}]
{-Gamma[0, -Log[n^(1 - ZetaZero[1])]]}

Limit[(Gamma[a, 0, -(1 - ZetaZero[1]) Log[n]] / Gamma[a] - 1) / a, {a -> 0}]
{-Gamma[0, Log[n] (-1 + ZetaZero[1])]}

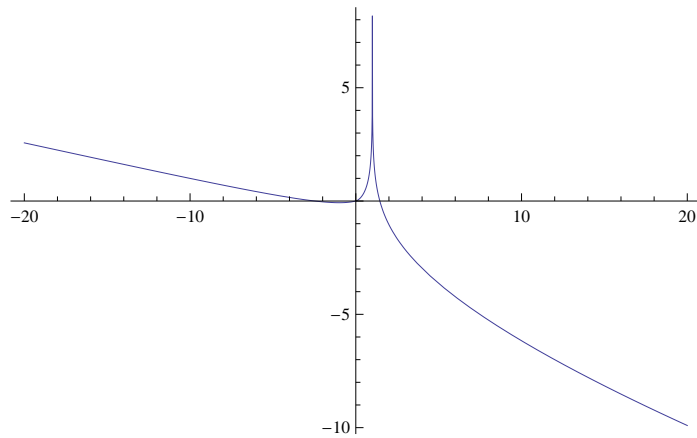
Limit[(Gamma[a, 0, -Log[n^(1 - ZetaZero[1])]] / Gamma[a] - 1) / a, {a -> 2}]
{-1/2 Gamma[2, -Log[n^(1 - ZetaZero[1])]]}

N[Gamma[3, 0, Log[99]] / Gamma[3]] + N[Gamma[3, Log[99]] / Gamma[3]]
1.

N[Gamma[3, 0, -Log[99]] / Gamma[3]] + N[Gamma[3, -Log[99]] / Gamma[3]]
1. + 0. i

```

```
Plot[{Re[Gamma[aa = 0, -Log[n]]], Re[Gamma[aa, 0, -Log[n]]]}, {n, -20, 20}]
```



$(-1)!$

ComplexInfinity

```
Integrate[t^(-1) E^(-t), {t, -Log[x], Infinity}]
```

```
ConditionalExpression[Gamma[0, -Log[x]] + Log[-Log[x]], Im[Log[x]] != 0 || Log[x] < 0]
```

```
Integrate[(E^(-t) - 1) / t, {t, 0, -Log[n]}]
```

```
ConditionalExpression[-EulerGamma + ExpIntegralEi[Log[n]] - Log[-Log[n]], Log[n] < 0]
```