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486.52871826165125, 488.38056709001745, 489.66176157795616, 491.398821593663,
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549.4975675626614, 550.9700100394839, 552.0495722005649, 553.7649721191589,
555.7920205616825, 556.8994764068553, 557.5646591720586, 559.3162370286822,
560.2408074972957`, 562.5592076160458`, 564.1608791107861`, 564.5060559381499`,
566.698787682808`, 567.7317579011769`, 568.9239551796294`, 570.0511147824636`,
572.4199841324528`, 573.6146105267582`, 575.0938860144948`, 575.8072471409288`,
```

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577.0390034720982, 579.0988346720366, 580.1369593623846, 581.9465762659016,
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   627.268396850783, 628.3258623594604, 630.4738874382921, 630.8057809271976,
  632.2251411671159, 633.5468582522518, 635.5238003106055, 637.3971931598373,
   637.9255139808225, 638.9279382668568, 640.6947946688257, 641.9454996657053,
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   654.3019205863194, 655.7094630223556, 656.9640845994606, 658.1756144186054,
   659.663845972964, 660.7167325952793, 662.2965864311004, 664.244604652273,
   665.342763095599`, 666.5151477041729`, 667.1484948945555`, 668.9758488202351`,
   670.3235852058626, 672.4581835841698, 673.0435782861476, 674.3558978101232,
   676.1396743636268, 677.230180668764, 677.8004447462214, 679.7421978825282]
Expand [(f1[n] E^t - f2[n] E^t(-t)) / E^t]
f1[n] - e^{-2t} f2[n]
Cosh[0]
1
Sinh[0]
r1[s_{-}, t_{-}, j_{-}, n_{-}] := 2(s+tI) Cos[(s+tI) Log[j/n]] + Sin[(s+tI) Log[j/n]]
1/(2I)(E^{(s+tI)Log[j/n]})-E^{(-I((s+tI)Log[j/n]))}
(E^{(j)}([s+t]) + E^{(j)}([j/n])) + E^{(j)}([s+t]) + E^
     1/(2I)(E^{(s+tI)Log[j/n]))-E^{(-I((s+tI)Log[j/n]))}
r1c[s_{t_{1}}, t_{t_{2}}, t_{t_{3}}] := (s+tI)(E^{(I((s)Log[j/n])})E^{(I((tI)Log[j/n])}) +
             E^{(-I((s) Log[j/n]))} E^{(-I((tI) Log[j/n]))} +
     1/(2I)(E^{(i)}(I((s)Log[j/n]))E^{(i)}(I((tI)Log[j/n]))-
             E^{(-I((s) Log[j/n]))} E^{(-I((tI) Log[j/n]))}
r1d[s_{-}, t_{-}, j_{-}, n_{-}] := (s+tI) (E^{(IsLog[j/n])} E^{(-tLog[j/n])} +
             E^{(-1sLog[j/n])} E^{(tLog[j/n])} +
     1/(2I) (E^{(IsLog[j/n])} E^{(-tLog[j/n])} - E^{(-IsLog[j/n])} E^{(tLog[j/n])}
rle[s_{-}, t_{-}, j_{-}, n_{-}] := (s+tI) ((Cos[sLog[j/n]] + ISin[sLog[j/n]]) E^{(-tLog[j/n])} +
              (Cos[sLog[j/n]] - ISin[sLog[j/n]]) E^{(tLog[j/n])) +
     1/(2I)((Cos[sLog[j/n]] + ISin[sLog[j/n]])E^{(-tLog[j/n])} -
              (\mathsf{Cos}[\,\mathsf{sLog}[\,\mathsf{j}\,/\,\mathsf{n}]\,]\,-\,\mathsf{I}\,\,\mathsf{Sin}[\,\mathsf{sLog}[\,\mathsf{j}\,/\,\mathsf{n}]\,])\,\,\mathsf{E}^{\,\mathsf{h}}\,(\mathsf{tLog}[\,\mathsf{j}\,/\,\mathsf{n}]\,))
(\texttt{Cos[sLog[j/n]]} - \texttt{ISin[sLog[j/n]]}) \; \texttt{E^(tLog[j/n])}) \; + \\
      ((Cos[sLog[j/n]] + ISin[sLog[j/n]]) 1 / (2I) E^(-tLog[j/n]) -
           (\cos[s\log[j/n]] - I \sin[s\log[j/n]]) 1/(2I) E^{(t\log[j/n]))
rlg[s_{-}, t_{-}, j_{-}, n_{-}] := (s+tI) ((Cos[sLog[j/n]] + ISin[sLog[j/n]]) E^{-}(-tLog[j/n]) + ISin[sLog[j/n]] + ISin[sLog[j/n]] E^{-}(-tLog[j/n]) + ISin[sLog[j/n]] + IS
```

 $(\texttt{Cos[sLog[j/n]]} - \texttt{ISin[sLog[j/n]]}) \; \texttt{E^(tLog[j/n])}) \; + \\$

 $(Cos[sLog[j/n]]) 1 / (2I) E^{-tLog[j/n]) +$

```
(I Sin[s Log[j/n]]) 1/(2I) E^{-t Log[j/n]) -
    (\cos[sLog[j/n]]) 1/(2I) E^{(tLog[j/n]) +
    (I Sin[sLog[j/n]]) 1/(2I) E^(tLog[j/n])
r1h[s_{,t_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{n_}}}}}}}}}}}}}}}}}}}r_i}}}}}}}r_i)}}}}}
          (Cos[sLog[j/n]] - ISin[sLog[j/n]]) E^{(tLog[j/n])) +
    (\text{Cos[sLog[j/n]]}) \; 1 \; / \; (2 \; \text{I}) \; (\text{E^(-tLog[j/n]}) \; - \; \text{E^(tLog[j/n])}) \; + \;
     (I Sin[s Log[j/n]]) 1/(2I) (E^{-t Log[j/n]}) + E^{-t Log[j/n]})
(Cos[sLog[j/n]] - ISin[sLog[j/n]]) E^{(tLog[j/n])) +
    -I \cos[s \log[j/n]] \sinh[-t \log[j/n]] + \sin[s \log[j/n]] \cosh[t \log[j/n]]
r1j[s_, t_, j_, n_] := (s+tI) (
       Cos[sLog[j/n]] E^{(-tLog[j/n])} +
          I Sin[s Log[j/n]] E^{-t Log[j/n]} +
          Cos[sLog[j/n]]E^{(tLog[j/n])}
          I Sin[s Log[j/n]] E^{(t Log[j/n])}
      ) +
    -I \cos[s \log[j/n]] \sinh[-t \log[j/n]] + \sin[s \log[j/n]] \cosh[t \log[j/n]]
\texttt{Cos[sLog[j/n]] (E^{-tLog[j/n])} + E^{-tLog[j/n])) + E^{-tLog[j/n])) + E^{-tLog[j/n])) + E^{-tLog[j/n])}}
          I Sin[sLog[j/n]] (E^{-tLog[j/n]}) - E^{-tLog[j/n]})
      ) +
    -I \cos[s \log[j/n]] \sinh[-t \log[j/n]] + \sin[s \log[j/n]] \cosh[t \log[j/n]]
r1l[s_, t_, j_, n_] :=
  2 (s+t I) (Cos[s Log[j/n]] Cosh[t Log[j/n]] - I Sin[s Log[j/n]] Sinh[t Log[j/n]]) +
    +I \cos[s \log[j/n]] \sinh[t \log[j/n]] + \sin[s \log[j/n]] \cosh[t \log[j/n]]
r1m[s_, t_, j_, n_] :=
  2 t Sin[sLog[j/n]] Sinh[tLog[j/n]] - 2 s I Sin[sLog[j/n]] Sinh[tLog[j/n]] + 2 s I
    I Cos[s Log[j/n]] Sinh[t Log[j/n]] + Sin[s Log[j/n]] Cosh[t Log[j/n]]
rln[s_{,t_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{,n_{,j_{n_{,j_{n_}}}}}}}}}}}}}}cosh(j,j,j)}}}}}}}runln[s]}}}}}}}rlnjnjrunln[s]}}}}
    2 t Sin[sLog[j/n]] Sinh[tLog[j/n]] + Sin[sLog[j/n]] Cosh[tLog[j/n]] +
    I (2 t Cos[s Log[j/n]] Cosh[t Log[j/n]] -
          2 	ext{ Sin}[sLog[j/n]] Sinh[tLog[j/n]] + Cos[sLog[j/n]] Sinh[tLog[j/n]])
N@r1n[2, 3, 6, 11]
18.332 - 5.63168 i
N@r1[2, 3, 6, 11]
18.332 - 5.63168 i
FullSimplify[2 s Cos[s Log[j/n]] Cosh[t Log[j/n]] +
    2 t Sin[sLog[j/n]] Sinh[tLog[j/n]] + Sin[sLog[j/n]] Cosh[tLog[j/n]]

\cosh\left[\mathsf{t}\,\log\left[\frac{\mathsf{j}}{\mathsf{n}}\right]\right]\left(2\,\mathsf{s}\,\cos\left[\mathsf{s}\,\log\left[\frac{\mathsf{j}}{\mathsf{n}}\right]\right] + \sin\left[\mathsf{s}\,\log\left[\frac{\mathsf{j}}{\mathsf{n}}\right]\right]\right) + 2\,\mathsf{t}\,\sin\left[\mathsf{s}\,\log\left[\frac{\mathsf{j}}{\mathsf{n}}\right]\right] \,\mathrm{Sinh}\left[\mathsf{t}\,\log\left[\frac{\mathsf{j}}{\mathsf{n}}\right]\right]

FullSimplify[I (2 t Cos[sLog[j/n]] Cosh[tLog[j/n]] -
        2 s \, Sin[s \, Log[j/n]] \, Sinh[t \, Log[j/n]] + Cos[s \, Log[j/n]] \, Sinh[t \, Log[j/n]]))]
i\left(2 t \cos\left[s \log\left[\frac{1}{n}\right]\right] \cosh\left[t \log\left[\frac{1}{n}\right]\right] + \left(\cos\left[s \log\left[\frac{1}{n}\right]\right] - 2 s \sin\left[s \log\left[\frac{1}{n}\right]\right]\right) \sinh\left[t \log\left[\frac{1}{n}\right]\right]\right)
```

```
Sum[1/j^{(1/2)}N@rln[N@Im@ZetaZero@1, 0, j, 10000], {j, 1, 10000}]
0.141347 + 0.i
N@Sinh[-10]
-11013.2
N@Cos[3+4I]
-27.0349 - 3.85115 i
N[Cos[3] Cos[4I] - Sin[3] Sin[4I]]
-27.0349 - 3.85115 i
N[Cos[3] Cosh[4] - I Sin[3] Sinh[4]]
-27.0349 - 3.85115 i
Sum[j^{(-1/2)}Sin[(s+tI)Log[j]], {j, 1, n}] +
       (2 (s+tI) Cos[(s+tI) Log[n]] - Sin[(s+tI) Log[n]])
          Sum[j^{(-1/2)}Cos[(s+tI)Log[j]], {j, 1, n}]
slo[n_{, s_{, t_{, l}}} := Sin[(s + t I) Log[n]]
s1[n_, s_, t_] := Sin[sLog[n]] Cosh[tLog[n]] + ICos[sLog[n]] Sinh[tLog[n]]
s2[n_-, s_-, t_-] := Cos[sLog[n]] Cosh[tLog[n]] - ISin[sLog[n]] Sinh[tLog[n]]
ra2[n_, s_, t_] :=
    (2ss1[n, s, t] + 2tIs1[n, s, t] + s2[n, s, t]) Sum[j^{(-1/2)}s1[j, s, t], {j, 1, n}] +
        (2 ss2[n, s, t] + 2tIs2[n, s, t] - s1[n, s, t]) Sum[j^(-1/2) s2[j, s, t], {j, 1, n}]
ra3[n\_, s\_, t\_] := (2s(Sin[sLog[n]] Cosh[tLog[n]] + ICos[sLog[n]] Sinh[tLog[n]]) + ICos[sLog[n]] Sinh[tLog[n]]) + ICos[sLog[n]] Sinh[tLog[n]] + ICos[sLog[n]] + ICos[s
                2 t I (Sin[sLog[n]] Cosh[tLog[n]] + I Cos[sLog[n]] Sinh[tLog[n]]) +
                 (\texttt{Cos}[\, \texttt{sLog}[n]] \, \, \texttt{Cosh}[\texttt{tLog}[n]] \, - \, \texttt{ISin}[\texttt{sLog}[n]] \, \, \texttt{Sinh}[\texttt{tLog}[n]]))
           \begin{aligned} & \text{Sum}[j^{-1}/2) \left( \text{Sin}[s \text{Log}[j]] \text{Cosh}[t \text{Log}[j]] + I \text{Cos}[s \text{Log}[j]] \text{Sinh}[t \text{Log}[j]] \right), \left\{ j, 1, n \right\} ] + \end{aligned} 
       (2 \ s \ (Cos[\ s \ Log[n]] \ Cosh[t \ Log[n]] \ - \ I \ Sin[s \ Log[n]] \ Sinh[t \ Log[n]]) \ +
                2 t I (Cos[sLog[n]] Cosh[tLog[n]] - I Sin[sLog[n]] Sinh[tLog[n]]) -
                 (Sin[sLog[n]]Cosh[tLog[n]] + ICos[sLog[n]]Sinh[tLog[n]]))
           \begin{aligned} & \text{Sum}[\ j^{-1/2}) \ (\text{Cos}[\ s \ \text{Log}[\ j]] \ |\ Cosh[t \ \text{Log}[\ j]] - I \ Sin[s \ \text{Log}[\ j]] \ Sinh[t \ \text{Log}[\ j]]) \, , \, \{j,1,n\}] \end{aligned}
2 s Cosh[t Log[n]] Sin[s Log[n]] - 2 t Cos[s Log[n]] Sinh[t Log[n]] +
                2 i t Cosh[t Log[n]] Sin[s Log[n]] + 2 i s Cos[s Log[n]] Sinh[t Log[n]] -
                iSin[sLog[n]]Sinh[tLog[n]]
          ) Sum[j^{(-1/2)} (Sin[sLog[j]] Cosh[tLog[j]] + ICos[sLog[j]] Sinh[tLog[j]]),
             {j, 1, n} +
       (2 s Cos[s Log[n]] Cosh[t Log[n]] - Cosh[t Log[n]] Sin[s Log[n]] +
                2 t Sin[s Log[n]] Sinh[t Log[n]] +
                 2 \ it \ Cos[s Log[n]] \ Cosh[t Log[n]] - it \ Cos[s Log[n]] \ Sinh[t Log[n]] - it \ Cos[s Log[n]] \ Sinh[t Log[n]] - it \ Cos[s Log[n]] \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] \ Sinh[t Log[n]] \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] \ Sinh[t Log[n]] - it \ Sinh[t Log[n]] \ Sinh
                2 is Sin[s Log[n]] Sinh[t Log[n]])
          Sum[j^{(-1/2)}(Cos[sLog[j]]Cosh[tLog[j]]-ISin[sLog[j]]Sinh[tLog[j]]), \{j, 1, n\}]
ra5[n_{-}, s_{-}, t_{-}] := (Cos[sLog[n]] Cosh[tLog[n]] +
                2 \ s \ Cosh[t \ Log[n]] \ Sin[s \ Log[n]] \ - 2 \ t \ Cos[s \ Log[n]] \ Sinh[t \ Log[n]] \ +
                I(2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
                          Sin[sLog[n]] Sinh[tLog[n]])
          ) (Sum[j^{(-1/2)} Sin[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
                ISum[j^{(-1/2)}Cos[sLog[j]]Sinh[tLog[j]], {j, 1, n}]) +
```

```
(2 \text{ s Cos}[\text{s Log}[n]] \text{ Cosh}[\text{t Log}[n]] - \text{Cosh}[\text{t Log}[n]] \text{ Sin}[\text{s Log}[n]] +
      2 t Sin[s Log[n]] Sinh[t Log[n]] +
       \verb|I (2tCos[sLog[n]] Cosh[tLog[n]] - Cos[sLog[n]] Sinh[tLog[n]] - \\
          2 s Sin[s Log[n]] Sinh[t Log[n]])
    ) (Sum[j^{(-1/2)}Cos[sLog[j]]Cosh[tLog[j]], {j, 1, n}] -
      I Sum[j^{(-1/2)} Sin[s Log[j]] Sinh[t Log[j]], {j, 1, n}])
2 t Cos[s Log[n]] Sinh[t Log[n]] +
      I(2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
          Sin[s Log[n]] Sinh[t Log[n]])
    ) (Sum[j^{(-1/2)}Sin[sLog[j]]Cosh[tLog[j]], {j, 1, n}]) +
   (Cos[sLog[n]]Cosh[tLog[n]] +
      2 \times Cosh[t Log[n]] Sin[s Log[n]] - 2 t Cos[s Log[n]] Sinh[t Log[n]] +
      I(2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
          Sin[sLog[n]] Sinh[tLog[n]])
    ) I Sum[j^{(-1/2)} Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
   (2 s Cos[s Log[n]] Cosh[t Log[n]] -
      Cosh[t Log[n]] Sin[s Log[n]] + 2 t Sin[s Log[n]] Sinh[t Log[n]] +
      I(2tCos[sLog[n]]Cosh[tLog[n]] - Cos[sLog[n]]Sinh[tLog[n]] -
          2 s Sin[s Log[n]] Sinh[t Log[n]])
    ) (Sum[j^{(-1/2)} Cos[sLog[j]] Cosh[tLog[j]], {j, 1, n}]) +
   (2 s Cos[s Log[n]] Cosh[t Log[n]] -
      Cosh[t Log[n]] Sin[s Log[n]] + 2 t Sin[s Log[n]] Sinh[t Log[n]] +
       \verb|I (2tCos[sLog[n]] Cosh[tLog[n]] - Cos[sLog[n]] Sinh[tLog[n]] - \\
          2 sSin[sLog[n]] Sinh[tLog[n]])
    ) (-I Sum[j^(-1/2) Sin[s Log[j]] Sinh[t Log[j]], {j, 1, n}])
ra7[n_, s_, t_] :=
 (\cos[s Log[n]] Cosh[t Log[n]] + 2 s Cosh[t Log[n]] Sin[s Log[n]] - 2 t Cos[s Log[n]]
       Sinh[tLog[n]]) Sum[j^{-1/2}] Sin[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
    (I (2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] - 
         Sin[sLog[n]] Sinh[tLog[n]])
   ) Sum[j^{(-1/2)} Sin[s Log[j]] Cosh[t Log[j]], {j, 1, n}] +
   (Cos[sLog[n]]Cosh[tLog[n]] +
      2 s Cosh[t Log[n]] Sin[s Log[n]] - 2 t Cos[s Log[n]] Sinh[t Log[n]])
    ISum[j^{(-1/2)} Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
    (\texttt{I (2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] - } \\
         Sin[sLog[n]] Sinh[tLog[n]])
   ) I Sum[j^{(-1/2)} Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
   (2 s Cos[s Log[n]] Cosh[t Log[n]] -
      Cosh[tLog[n]] Sin[sLog[n]] + 2tSin[sLog[n]] Sinh[tLog[n]])
    Sum[j^{(-1/2)}Cos[sLog[j]]Cosh[tLog[j]], {j, 1, n}] +
   (I (2 t Cos[s Log[n]] Cosh[t Log[n]] - Cos[s Log[n]] Sinh[t Log[n]] -
         2 s Sin[s Log[n]] Sinh[t Log[n]])
   ) Sum[j^{(-1/2)} Cos[s Log[j]] Cosh[t Log[j]], {j, 1, n}] +
   (2 s Cos[s Log[n]] Cosh[t Log[n]] -
      Cosh[tLog[n]] Sin[sLog[n]] + 2 t Sin[sLog[n]] Sinh[tLog[n]])
    (-I Sum[j^{(-1/2)} Sin[s Log[j]] Sinh[t Log[j]], {j, 1, n}]) +
    (\texttt{I} (2 \texttt{t} \texttt{Cos}[\texttt{s} \texttt{Log}[\texttt{n}]] \texttt{Cosh}[\texttt{t} \texttt{Log}[\texttt{n}]] - \texttt{Cos}[\texttt{s} \texttt{Log}[\texttt{n}]] \texttt{Sinh}[\texttt{t} \texttt{Log}[\texttt{n}]] - \\
         2 sSin[sLog[n]] Sinh[tLog[n]])
    ) (-I Sum[j^{(-1/2)} Sin[s Log[j]] Sinh[t Log[j]], {j, 1, n}])
ra8[n_, s_, t_] :=
 (\cos[s \log[n]] \cosh[t \log[n]] + 2 s \cosh[t \log[n]] \sin[s \log[n]] - 2 t \cos[s \log[n]]
```

```
Sinh[tLog[n]]) Sum[j^{-1/2}] Sin[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
  (2 \text{ s Cos}[s \text{ Log}[n]] \text{ Cosh}[t \text{ Log}[n]] - \text{Cosh}[t \text{ Log}[n]] \text{ Sin}[s \text{ Log}[n]] + 2 t \text{ Sin}[s \text{ Log}[n]]
       Sinh[tLog[n]]) Sum[j^{-1/2}) Cos[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
  ((2 t Cos[s Log[n]] Cosh[t Log[n]] - Cos[s Log[n]] Sinh[t Log[n]] -
       2 s Sin[s Log[n]] Sinh[t Log[n]]))
   (Sum[j^{(-1/2)}Sin[sLog[j]]Sinh[tLog[j]], {j, 1, n}]) +
  -((2 \text{ t} Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
        Sin[sLog[n]] Sinh[tLog[n]]))
   Sum[j^{(-1/2)} Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
  I (Cos[sLog[n]] Cosh[tLog[n]] + 2 sCosh[tLog[n]] Sin[sLog[n]] - 2 tCos[sLog[n]]
       Sinh[tLog[n]]) Sum[j^{-1/2}] Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
  -I (2 s Cos[s Log[n]] Cosh[t Log[n]] - Cosh[t Log[n]] Sin[s Log[n]] +
      2 t Sin[s Log[n]] Sinh[t Log[n]])
   (Sum[j^{(-1/2)}Sin[sLog[j]]Sinh[tLog[j]], {j, 1, n}]) +
  I((2 t Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
       Sin[sLog[n]] Sinh[tLog[n]]))
   Sum[j^{(-1/2)} Sin[s Log[j]] Cosh[t Log[j]], {j, 1, n}] +
  I((2 t Cos[s Log[n]] Cosh[t Log[n]] - Cos[s Log[n]] Sinh[t Log[n]] -
       2 sSin[sLog[n]] Sinh[tLog[n]]))
   Sum[j^{(-1/2)} Cos[sLog[j]] Cosh[tLog[j]], \{j, 1, n\}]
Sum[j^{(-1/2)}Sin[sLog[j]]Cosh[tLog[j]], {j, 1, n}] +
  (2 s Cos[s Log[n]] Cosh[t Log[n]] - Cosh[t Log[n]] Sin[s Log[n]] + 2 t Sin[s Log[n]]
       Sinh[tLog[n]]) Sum[j^{-1/2}] Cos[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
  ((2 t Cos[s Log[n]] Cosh[t Log[n]] - Cos[s Log[n]] Sinh[t Log[n]] -
       2 s Sin[s Log[n]] Sinh[t Log[n]]))
   (Sum[j^{(-1/2)}Sin[sLog[j]]Sinh[tLog[j]], {j, 1, n}]) +
  -((2 \text{ t} Cosh[t Log[n]] Sin[s Log[n]] + 2 s Cos[s Log[n]] Sinh[t Log[n]] -
        Sin[sLog[n]] Sinh[tLog[n]]))
   Sum[j^{(-1/2)} Cos[sLog[j]] Sinh[tLog[j]], {j, 1, n}] +
  I ((Cos[sLog[n]] Cosh[tLog[n]] + 2 sCosh[tLog[n]] Sin[sLog[n]] - 2 tCos[sLog[n]]
          Sinh[tLog[n]]) Sum[j^{-1/2}) Cos[sLog[j]] Sinh[tLog[j]], \{j, 1, n\}] +
      -(2 s Cos[s Log[n]] Cosh[t Log[n]] - Cosh[t Log[n]] Sin[s Log[n]] + 2 t Sin[s Log[n]]
           Sinh[tLog[n]]) (Sum[j^{-1/2})Sin[sLog[j]]Sinh[tLog[j]], {j, 1, n}]) +
      ((2 \text{ t} Cosh[t Log[n]] Sin[s Log[n]] + 2 \text{ s} Cos[s Log[n]] Sinh[t Log[n]] - Sin[s Log[n]]
           Sinh[tLog[n]])) Sum[j^{-1/2}) Sin[sLog[j]] Cosh[tLog[j]], {j, 1, n}] +
      ((2 t Cos[s Log[n]] Cosh[t Log[n]] - Cos[s Log[n]] Sinh[t Log[n]] - 2 s Sin[s Log[n]]
           Sinh[tLog[n]])) Sum[j^{-1/2}) Cos[sLog[j]] Cosh[tLog[j]], {j, 1, n}])
ra9[1000, .5, .3]
-4.22662 - 5.82755 i
ra1[1000, .5, .3]
-4.226624969204295 -5.8275475674013535 i
```

```
2\,t\,\mathtt{I}\,\left(\mathtt{Cos}\,[\,\mathtt{s}\,\mathtt{Log}\,[\mathtt{n}]\,]\,\mathtt{Cosh}\,[\,\mathtt{t}\,\mathtt{Log}\,[\mathtt{n}]\,]\,-\,\mathtt{I}\,\mathtt{Sin}\,[\,\mathtt{s}\,\mathtt{Log}\,[\mathtt{n}]\,]\,\,\mathtt{Sinh}\,[\,\mathtt{t}\,\mathtt{Log}\,[\mathtt{n}]\,]\right)\,-\,
   (Sin[\,s\,Log[n]]\,Cosh[t\,Log[n]]\,+\,I\,Cos[s\,Log[n]]\,Sinh[t\,Log[n]])\,]
2 \; s \; Cos[s \; Log[n]] \; Cosh[t \; Log[n]] \; + \; 2 \; i \; t \; Cos[s \; Log[n]] \; Cosh[t \; Log[n]] \; -
 Cosh[t Log[n]] Sin[s Log[n]] - i Cos[s Log[n]] Sinh[t Log[n]] -
 2 i s Sin[s Log[n]] Sinh[t Log[n]] + 2 t Sin[s Log[n]] Sinh[t Log[n]]
-II
1
Sinh[0]
0
```

```
N@E^(3 I)
-0.989992 + 0.14112 i
N@E^(-3I)
-0.989992 - 0.14112 i
```