```
LL[n_{,} 1, x_{,}] := LL[n, 1, x] = Sum[Log[j], {j, 2, n}] - x Sum[Log[jx], {j, 1, Floor[n/x]}]
Sum[LL[n/j, k-1, x], {j, 2, n}] - xSum[LL[n/(jx), k-1, x], {j, 1, Floor[n/x]}]
\label{eq:chebyshevReference} ChebyshevReference[n\_] := Sum[\, MangoldtLambda[j]\,,\, \{j,\, 1,\, n\}\,]
Table[{n, N[Psi[n, 2]], N[Psi[n, 1.5]], N[Psi[n, 1.2]], N[ChebyshevReference[n]]},
  {n, 1, 100}] // TableForm
\texttt{Limit}[\; \texttt{Sum}[\; x^{k} \texttt{Log}[x] \,, \, \{k, \, 1, \, \texttt{Log}[x, \, n] \,\}] \,, \, x \rightarrow 1]
1
2
       0.693147
                   0.693147
                               0.693147
                                            0.693147
3
       1.79176
                   1.79176
                               1.79176
                                            1.79176
4
       2.48491
                   2.48491
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                                            2.48491
5
       4.09434
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7
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       6.7334
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       7.83201
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       43.6893
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46	43.6893	43.6893	43.6893	43.6893
47	47.5395	47.5395	47.5395	47.5395
48	47.5395	47.5395	47.5395	47.5395
49	49.4854	49.4854	49.4854	49.4854
50	49.4854	49.4854	49.4854	49.4854
51	49.4854	49.4854	49.4854	49.4854
52	49.4854	49.4854	49.4854	49.4854
53	53.4557	53.4557	53.4557	53.4557
54	53.4557	53.4557	53.4557	53.4557
55	53.4557	53.4557	53.4557	53.4557
56	53.4557	53.4557	53.4557	53.4557
57	53.4557	53.4557	53.4557	53.4557
58	53.4557	53.4557	53.4557	53.4557
59	57.5332	57.5332	57.5332	57.5332
60	57.5332	57.5332	57.5332	57.5332
61	61.6441	61.6441	61.6441	61.6441
62	61.6441	61.6441	61.6441	61.6441
63	61.6441	61.6441	61.6441	61.6441
64	62.3372	62.3372	62.3372	62.3372
65	62.3372	62.3372	62.3372	62.3372
66	62.3372	62.3372	62.3372	62.3372
67	66.5419	66.5419	66.5419	66.5419
68	66.5419	66.5419	66.5419	66.5419
69				
70	66.5419 66.5419	66.5419	66.5419	66.5419
		66.5419	66.5419	66.5419
71 72	70.8046	70.8046	70.8046	70.8046
	70.8046	70.8046	70.8046	70.8046
73 74	75.0951	75.0951	75.0951	75.0951
	75.0951	75.0951	75.0951	75.0951
75 76	75.0951	75.0951	75.0951	75.0951
	75.0951	75.0951	75.0951	75.0951
77	75.0951	75.0951	75.0951	75.0951
78 79	75.0951 79.4645	75.0951 79.4645	75.0951	75.0951 79.4645
	79.4645		79.4645	79.4645
80 81	80.5631	79.4645	79.4645 80.5631	
		80.5631		80.5631
82 83	80.5631 84.982	80.5631	80.5631 84.982	80.5631
		84.982 84.982		84.982
84	84.982		84.982	84.982
85	84.982	84.982	84.982	84.982
86	84.982 84.982	84.982 84.982	84.982 84.982	84.982
87				84.982
88	84.982	84.982	84.982	84.982
89	89.4706	89.4706	89.4706	89.4706
90	89.4706	89.4706	89.4706	89.4706
91	89.4706	89.4706	89.4706	89.4706
92	89.4706	89.4706	89.4706	89.4706
93	89.4706	89.4706	89.4706	89.4706
94	89.4706	89.4706	89.4706	89.4706
95	89.4706	89.4706	89.4706	89.4706
96	89.4706	89.4706	89.4706	89.4706
97	94.0453	94.0453	94.0453	94.0453
98	94.0453	94.0453	94.0453	94.0453
99	94.0453	94.0453	94.0453	94.0453
100	94.0453	94.0453	94.0453	94.0453