DAE_8 Problem 2.5

Given:

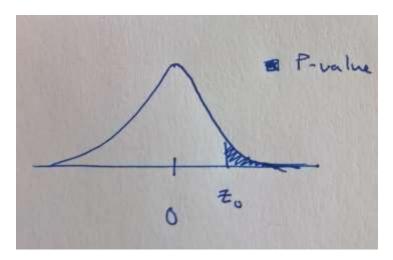
2.5. Suppose that we are testing H_0 : $\mu = \mu_0$ versus H_1 : $\mu > \mu_0$. Calculate the *P*-value for the following observed values of the test statistic:

(a)
$$Z_0 = 2.25$$
 (b) $Z_0 = -1.65$ (c) $Z_0 = 2.05$

(d)
$$Z_0 = 1.90$$
 (e) $Z_0 = -2.25$

Solution:

The Z statistic is related to the standard normal distribution $N(\mu, sigma) = N(0,1)$. The test is one sided as only more extremely larger values are considered under H1 (see figure below).



The P-value the probability of more extreme cases than Z0, P(z>Z0), i.e.

P=P(z>Z0)

This probability in turn is derived from the CDF as

$$P(z>Z0)=1-P(z\leq Z0)=1-CDF(Z0)$$

The CDF of the normal distribution is determined by the error function, which does not have an analytical solution for the 1-D case. Using MATLAB/OCTAVE the following code will determine the P-values.