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### The Anatomy of a Large-Scale Hypertextual Web Search Engine

#### Sergey Brin and Lawrence Page

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#### Abstract

In this paper, we present Google, a prototype of a large-scale search engine which makes heavy use of the structure present in hypertext. Google is designed to crawl and index the Web efficiently and produce much more satisfying search results than existing systems. The prototype with a full text and hyperlink database of at least 24 million pages is available at <a href="http://google.stanford.edu/">http://google.stanford.edu/</a>

To engineer a search engine is a challenging task. Search engines index tens to hundreds of millions of web pages involving a comparable number of distinct terms. They answer tens of millions of queries every day. Despite the importance of large-scale search engines on the web, very little academic research has been done on them. Furthermore, due to rapid advance in technology and web proliferation, creating a web search engine today is very different from three years ago. This paper provides an in-depth description of our large-scale web search engine -- the first such detailed public description we know of to date.

Apart from the problems of scaling traditional search techniques to data of this magnitude, there are new technical challenges involved with using the additional information present in hypertext to produce better search results. This paper addresses this question of how to build a practical large-scale system which can exploit the additional information present in hypertext. Also we look at the problem of how to effectively deal with uncontrolled hypertext collections where anyone can publish anything they want.

Keywords: World Wide Web, Search Engines, Information Retrieval, PageRank, Google

#### 1. Introduction

(Note: There are two versions of this paper -- a longer full version and a shorter printed version. The full version is available on the web and the conference CD-ROM.)

The web creates new challenges for information retrieval. The amount of information on the web is growing rapidly, as well as the number of new users inexperienced in the art of vits link graph, often starting with high quality human maintained indices such as <u>Yahoo!</u> or with search engines. Human maintained lists cover popular topics effectively but are subjimprove, and cannot cover all esoteric topics. Automated search engines that rely on keyword matching usually return too many low quality matches. To make matters worse, some taking measures meant to mislead automated search engines. We have built a large-scale search engine which addresses many of the problems of existing systems. It makes especial hypertext to provide much higher quality search results. We chose our system name, Google, because it is a common spelling of googol, or 10<sup>100</sup> and fits well with our goal of build

### 1.1 Web Search Engines -- Scaling Up: 1994 - 2000

Search engine technology has had to scale dramatically to keep up with the growth of the web. In 1994, one of the first web search engines, the World Wide Web Worm (WWWW) | web accessible documents. As of November, 1997, the top search engines claim to index from 2 million (WebCrawler) to 100 million web documents (from Search Engine Watch). It comprehensive index of the Web will contain over a billion documents. At the same time, the number of queries search engines handle has grown incredibly too. In March and April



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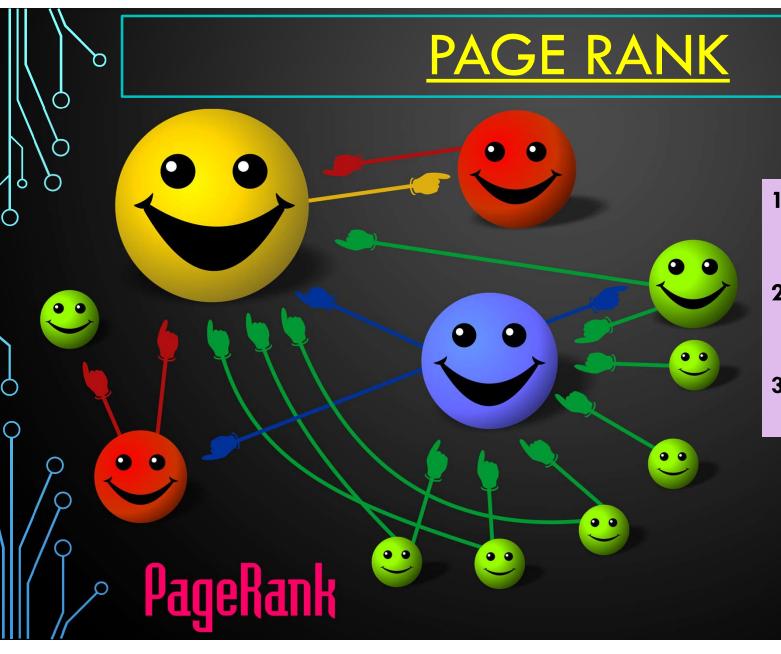
Apart from the problems of scaling traditional search techniques to data of this magnitude, there are new technical challenges involved with using the additional information present in hypertext to produce letter search

Neste artigo, apresentamos o Google, um protótipo de um motor de busca de larga escala que faz uso da estrutura presente nos hipertextos. O Google foi projetado para rastrear e indexar a web de forma eficiente e produzir resultados de pesquisa muito mais satisfatórios do que os sistemas existentes.

1.1 Web Search Engines -- Scaling Up: 1994 - 2000

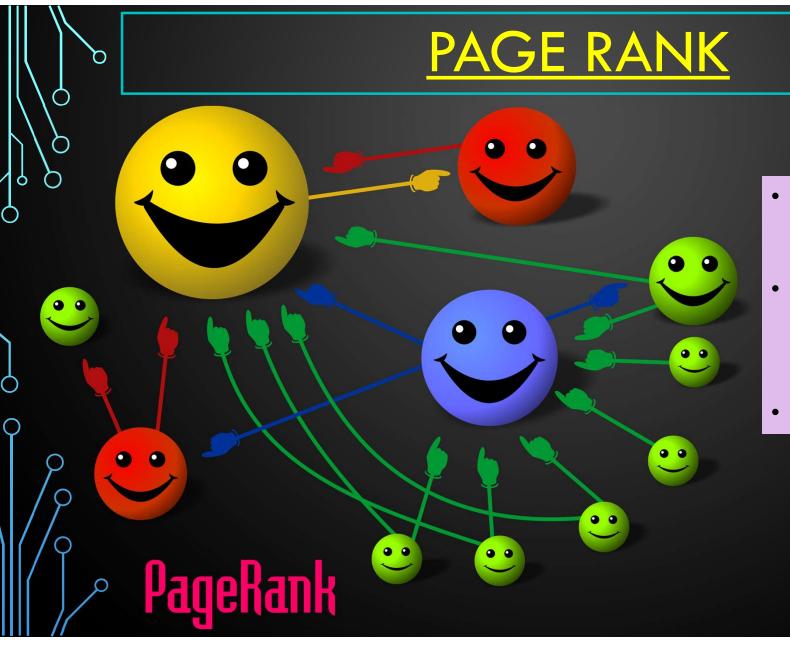
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- 1) Quantidade de links que recebe;
- 2) Links de sites com PageRank alto valem mais;
- 3) Quanto mais links envia, menor o peso de cada.





- Não será levado em consideração links para a própria página (sem laços);
- Vários links de uma página para outra, será considerado como uma (sem arestas múltiplas);
- Grafo Simples



# PAGE RANK MODELO SIMPLIFICADO

Em um dado um grafo G com n vértices, temos que o Page Rank do vértice p na iteração t ( PR(p,t) ) é dado por:

$$PR(p,0) = \frac{1}{n}$$

$$PR(p,t) = \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$

## Em que:

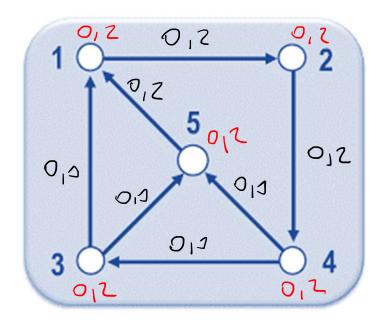
C(p) é o conjunto de página que tem links para p NumLinks(p') é a quantidade de links na página p'

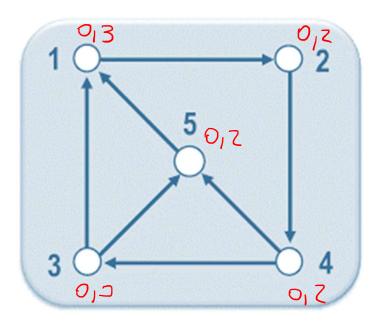


$$t = 0$$

Nó	Page Rank
1	0,2
2	0,1
3	0,2
4	0,1
5	012

$$N=5$$
  $\frac{1}{5}=0.12$ 





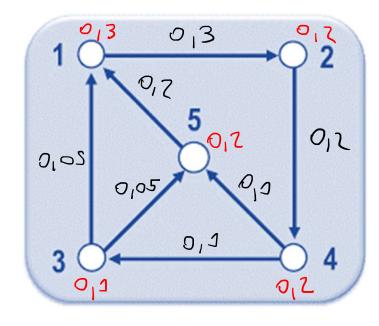
$$PR(p,0) = \frac{1}{n}$$

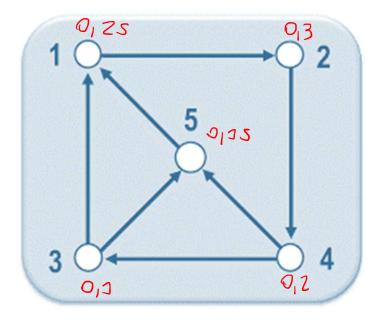
$$PR(p,t) = \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$



$$t = 1$$

Nó	Page Rank
1	0,3
2	0,2
3	013
4	012
5	0,2





$$PR(p,0)=\frac{1}{n}$$

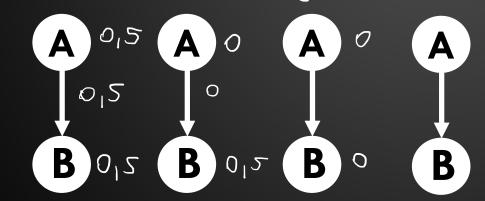
$$PR(p,t) = \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$



# PAGE RANK PROBLEMA DO MODELO SIMPLIFICADO

Páginas sem links de saída podem drenar os Page Ranks do sistema: t = 0 t = 1

$$n=2$$



Vértices/Iteração	t=0	t=1	t=2	t=3
Α	015	0	Ø	0
В	0,5	0,5	0	O



# <u>PAGE RANK</u> FÓRMULA ORIGINAL

Em um dado um grafo G com n vértices, temos que o Page Rank do vértice p na iteração t ( PR(p,t) ) é dado por:

$$PR(p,0)=\frac{1}{n}$$

$$PR(p,t) = (1-d) + d. \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$

## Em que:

C(p) é o conjunto de página que tem links para p NumLinks(p') é a quantidade de links na página p' d é o fator de amortecimento (usualmente 0.85)



# PAGE RANK COM FATOR DE AMORTECIMENTO

Em um dado um grafo G com n vértices, temos que o Page Rank do vértice p na iteração t ( PR(p,t) ) é dado por:

$$PR(p,0)=\frac{1}{n}$$

$$PR(p,t) = \frac{(1-d)}{n} + d. \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$

## Em que:

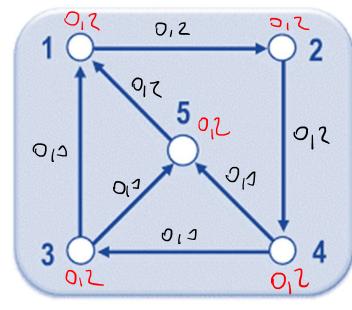
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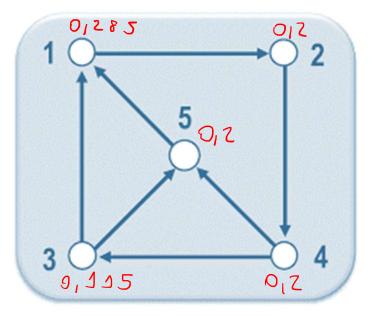


$$t = 0$$

Nó	Page Rank
1	0,2
2	0,2
3	0,2
4	0,1
5	0,2

$$N = 2$$
  $E = 0$   $\frac{1}{2} = 0$ 





$$\frac{d = 0,85}{1-d} = \frac{0,15}{5} = 0,03$$

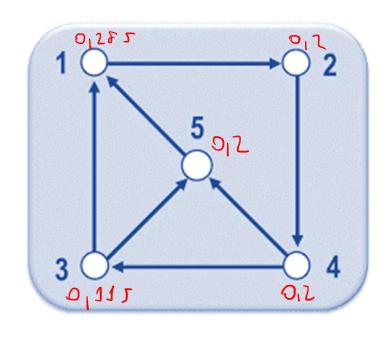
$$PR(p,0)=\frac{1}{n}$$

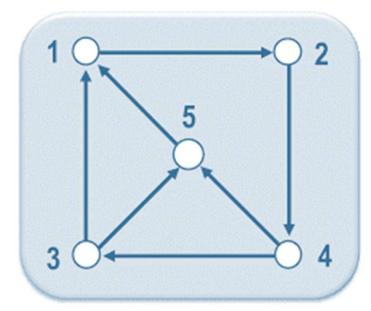
$$PR(p,t) = \frac{(1-d)}{n} + d. \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$



$$t = 1$$

Nó	Page Rank
1	0,285
2	0,2
3	01772
4	0,2
5	0,2





$$\frac{d=0,85}{n} = \frac{0,15}{5} = 0,03$$

$$PR(p,0)=\frac{1}{n}$$

$$PR(p,t) = \frac{(1-d)}{n} + d. \sum_{p' \in C(p)} \frac{PR(p',t-1)}{NumLinks(p')}$$

