

# Getting Started with Whiley

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April 15, 2014

## Abstract

The aim of this document is to provide a short introduction to the Whiley programming language, in order to get you up and running quickly. However, it is not intended to be a definitive reference. We'll walk through a number of simple examples illustrating the most interesting features of Whiley, and show you how to get it up and running. We will be assuming some rudimentary knowledge of programming.

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# 1 Introduction

The Whiley programming language has been in active development since 2009. The language was designed specifically to help the programmer eliminate bugs from his/her software. The key feature is that Whiley allows programmers to write *specifications* for their functions, which are then checked by the compiler. For example, here is the specification for the `max()` function which returns the maximum of two integers:

```
function max(int x, int y) => (int z)
// must return either x or y
ensures x == z || y == z
// return must be as large as x and y
ensures x <= z && y <= z:
    // implementation
    if x > y:
        return x
    else:
        return y
```

Here, we see our first piece of Whiley code. This declares a function called `max` which accepts two integers `x` and `y`, and returns an integer `z`. The body of the function simply compares the two parameters and returns the largest. The two **requires** clauses form the function's *post-condition*, which is a guarantee made to any caller of this function. In this case, the `max` function guarantees to return one of the two parameters, and that the return will be as large as both of them. In plain English, this means it will return the maximum of the two parameter values.

When verification is enabled the Whiley compiler will check that every function meets its specification. For our `max()` function, this means it will check that body of the function guarantees to return a value which meets the function's post-condition. To do this, it will explore the two execution paths of the function and check each one separately. If it finds a path which does not meet the post-condition, the compiler will report an error. In this case, the `max()` function above is implemented correctly and so it will find no errors. The advantage of providing specifications is that they can help uncover bugs and other, more serious, problems earlier in the development cycle. This leads to software which is both more reliable and more easily maintained (since the specifications provide important documentation).

## 1.1 Objectives

Although the primary purpose of Whiley is to allow us to write specifications on functions, we will not talk about that again until later in the document. Furthermore, we will not consider this aspect in detail and, for more, the reader is referred to our tutorial on verification<sup>[2]</sup>.

The primary goal of this article is to introduce the core language of Whiley without worrying about verification (since this presents many challenges and adds complexity). Indeed, it is only once we've understood the basics of Whiley that we will be ready to investigate verification. Furthermore, Whiley's core language turns out to be rather interesting even without considering verification!

## 1.2 Installation

There are currently three ways to get setup with the Whiley programming language:

- **Web Browser.** By far the simplest way to get started with Whiley is by running it in your web browser (see Figure 1). Go to <http://whiley.org/play/> and you can get started straight away!
- **Eclipse Plugin.** If you're familiar with the Eclipse IDE or want to develop more serious programs in Whiley, then installing the Eclipse plugin is easy to do. From within Eclipse, choose

*Help*→*Install New Software* from the menu. Enter <http://whiley.org/eclipse> as the site, select the “Whiley Eclipse Plugin” and follow the on-screen instructions (see Figure 2).

- **Development Kit.** For those familiar with the command-line, installing the Whiley Development Kit (WDK) is another option. Furthermore, you’ll be able to explore the source code for the Whiley system, and see how it all works! To do this, visit <http://whiley.org/downloads/>.

More information of getting started with Whiley can be found at <http://whiley.org/getting-started/>. Finally, the Whiley system is completely free and released under an open source license (BSD), and you can get the latest code from <http://github.com/Whiley>.

### 1.3 Running Whiley

Illustrate Hello World



Figure 1: Compiling a Whiley program using a web browser (Mozilla Firefox). At the moment, the user's program is not correct and the system is reporting this as an error in red.



Figure 2: Installing the Whiley Eclipse Plugin from within Eclipse.

## 2 Quick Walkthrough

This section provides a quick walk through of the main concepts and ideas in the Whiley language. Through a series of short examples, we'll introduce the basic building blocks of the language.

### 2.1 Booleans and Numbers

As found in many languages, Whiley supports a range of primitive datatypes for representing boolean, integers, real numbers, bytes, characters, etc. Of these, the most commonly used are:

- **Booleans** are denoted by the type `bool`. This is the simplest of the primitive datatypes, and has only two possible values: `true` or `false`.
- **Integers** are denoted by the type `int`. Integers in Whiley are *unbounded*. This means that, in theory at least, a variable of type `int` can take on *any possible integer value*; this differs from many other languages (e.g. Java), which limit the number of possible values (e.g. following 32-bit two's complement).
- **Real Numbers** are denoted by the type `real`. Reals in Whiley are *unbounded rationals*. This means that, in theory at least, a variable of type `real` can take on *any possible rational value*. Again, this offers significantly better precision than, for example, `float` or `double` types based on IEEE754 as found in other languages (e.g. Java).

A very simple example which illustrates the `int` and `bool` types is the following:

```
function isLessThan(int x, int y) => bool:
//
  if x < y:
    return true
  else:
    return false
```

This declares a simple function which returns `true` if the first parameter, `x`, is less than the second, `y`, and `false` otherwise.

?

**Indentation Syntax.** From the above example you should notice that Whiley, unlike many languages, does not use curly braces (i.e. `{ ... }`) to demarcate blocks of code. Instead, Whiley uses *indentation syntax* which was popularised by the Python programming language. The start of a new code block is signalled by a preceding `:` on the previous line. The new block must be indented by at least one space (the actual amount doesn't matter) and all subsequent statements with the same indentation are included.

?

**Ints versus Reals.** Unlike many other languages, Whiley provides a strong relationship between values of type `int` and those of type `real`. Specifically, every `int` value can be represented precisely as a `real` value. Although it may seem surprising, this is not true for many other languages (e.g. Java), where there are `int` (resp. `long`) values which cannot be represented using `float` (resp. `double`)<sup>[1]</sup>.

## 2.2 Sets, Lists and Maps

Like many modern programming languages, Whiley provides built-in types for representing collections. The following illustrates a short function which multiplies a vector by a scalar:

```
function vectorMultiply([real] vector, real scalar) => [real]:  
  //  
  for i in 0 .. |vector|:  
    vector[i] = vector[i] * scalar  
  return vector
```

This illustrates a few of the common collection operations. Firstly, the size of a collection is obtained using the *length* operator (i.e. `|vector|` returns the length of `vector`). Secondly, the **for** loop is useful for iterating over the elements of a collection. In this case, `0 .. |vector|` returns a *list* of consecutive integers from 0 up to (but not including) `|vector|`. Finally, the *list access* operator, `vector[i]`, returns the element at index `i`. The three different kinds of collections supported in Whiley are:

- **Sets** (e.g. `{int}`) provide the simplest form of collection, and are constructed using a *set constructor* (e.g. `{1, 2, 3}`). They support the *set union* (e.g. `xs + ys`), *set intersection* (e.g. `xs & ys`) and *set difference* (e.g. `xs - ys`) operators. One can test for inclusion using the *element of* operator (e.g. `x in xs`), or the *subset* (e.g. `xs  $\subset$  ys`) and *subset or equal* (e.g. `xs  $\subseteq$  ys`) operators.
- **Maps** (e.g. `{int=>string}`) provide a halfway point between sets and lists. They are similar to dictionaries in Python or the `Map` interface in Java. They can be viewed as a set of *key*×*value* pairs, where every key maps to exactly one value. Maps are constructed using a *map constructor* (e.g. `{1=>"hello", 2=>"world"}`), and elements are accessed using the *map access* operator (e.g. `map[i]`).
- **Lists** (e.g. `[int]`) are similar to arrays (e.g. in Java), but they can also be resized. As can be seen above, they support the *list access* operator (e.g. `vector[i]`). They also support the *list append* operator (e.g. `[1, 2, 3] ++ [4, 5, 6]`) and *sublist* operator (e.g. `vector[0..2]`). Finally, lists are constructed using a *list constructor* (e.g. `[1, 2, 3]`).

All collection kinds can be iterated using the built-in **for** loop construct. For example, here is a function to iterate a map looking for a particular value:

```
// Return the set of all keys which map to a given value  
function keysOf({int=>string} map, string value) => {string}:  
  //  
  {string} result = {} // initialise result with empty set  
  for k, v in map:      // loop over every key,value pair in map  
    if v == value:  
      result = result + {k} // add matching keys to result set  
  // return result  
  return result
```

This function iterates over each key×value pair (i.e. `k, v`) in a from integers to strings (i.e. `{int=>string}`) using the **for** statement.

## 2.3 Records and Tuples

Aside from collection types, Whiley also allows provides *records* and *tuples* for grouping items together. Records are similar to `structs` (as found in C) and `objects` (as found in JavaScript). A record is constructed from one or more *fields*, each of which has a unique name and type. For example, the following defines a simple record type for representing 2D points and a function for translating their position:

```

// A point has two integer fields named x and y
type Point is {int x, int y}

// Translate a given point by an x and y delta
function translate(Point p, int dx, int dy) => Point:
    return {
        x: p.x + dx, // new x value is old value plus dx
        y: p.y + dy  // new y value is old value plus dy
    }

```

Here, a *user-defined type* named `Point` has been defined. This is a record type containing two `int` fields, `x` and `y`. In the `translate()` function, a *record literal* is used to construct a new `Point` to be returned.

Records are an important mechanism for giving meaning to data in Whiley. For example, consider the following declaration of a rectangle:

```

// A rectangle has a position, and a width and height
type Rectangle is {
    Point position, // position of top-left corner
    int width,      // width of the rectangle
    int height      // height of the rectangle
}

```

Here, we see that a rectangle has a position, a width and a height. The names of the fields are important for conveying their meaning in the real-world.

Sometimes, using a record type is a little more than necessary because the data being described is really quite simple. In such cases we can use a *tuple* in Whiley, which provide a lightweight mechanism for grouping data. For example, we might consider that using a record to defined our `Point` is a little verbose. Instead, we could rework the example to use a tuple as follows:

```

// A point has two integer components; the first represents x, the second represents y.
type Point is (int,int)

// Translate a given point by an x and y delta
function translate(Point p, int dx, int dy) => Point:
    return p.x+dx, p.y+dy

```

Since there is a widely used notation for describing 2D points — namely  $(x, y)$  — it makes sense in this case to use a tuple over a record. Tuples are also useful for describing functions which return multiple values. For example, the following illustrates a simple function which swaps the order of its parameters:

```

function swap(int x, int y) => (int, int):
    return y, x

```

Here, we see that the return type is a tuple and this provides a convenient and lightweight mechanism for returning multiple values. Following on from this, Tuple types in Whiley also supports *destructuring syntax* (e.g. as found in Python). The following example illustrates this:

```

int x
int y
...
x, y = swap(x, y) // destructuring assignment
...

```

Here, we see that variables `x` and `y` are assigned their respective component of the tuple returned from `swap`. Again, this syntax simplifies the use of functions with multiple return values.



## 2.4 Strings and Characters

Encodings?

Like most programming languages, Whiley provides explicit support for dealing with strings and characters. This is achieved through the **char** and **string** data types. Here, **char** represents unicode characters, whilst **string** is a list of **chars** and supports all list operations (recall §2.2). Here's a simple example illustrating the well-known `replace()` function:

```
function replace(string str, char old, char n) => string:
    //
    int i = 0
    while i < |str|:
        if str[i] == old:
            str[i] = n
            i = i + 1
    return str
```

This function simply iterates through the elements of a string replacing every occurrence of the character `old` with the character `n`.

## 3 Flexible Types

The previous section introduced us to the basic types found in Whiley, such as integers (`int`), rationals (`real`) and booleans (`bool`). However, unlike many languages, Whiley provides a flexible and powerful approach to typing which go well beyond the basic forms. In this section, we will examine this in more detail.

### 3.1 Flow Typing

To improve the programmer experience and reduce unnecessary tedium, Whiley employs a *flow typing* system. What this means is that the type of a variable can vary at different points within a function. To make this work, Whiley employs *union types*<sup>[2;3]</sup> along with *variable retyping*. The following example illustrates how this works (where the body of `indexOf()` is left out for brevity):

```
function indexOf(string str, char c) => null|int:
    ...

function split(string str, char c) => [string]:
    var idx = indexOf(str,c)
    //idx has type null|int
    if idx is int:
        //idx now has type int
        int below = str[0..idx]
        int above = str[idx..]
        return [below,above]
    else:
        //idx now has type null
        return [str] //no occurrence
```

Here, `indexOf()` returns the first index of a character in the string, or `null` if there is none. The type `null|int` is a *union type*, meaning it is either an `int` or `null`. The `split()` function splits a string into two pieces based on the first occurrence of a given character `c`, or leaves the string as is otherwise. It calls `indexOf()` to determine the first occurrence of `c` in `str`. Observe that variable `idx` has been declared as type `var`, meaning the compiler will automatically infer the best possible type for it.

In the above example, Whiley’s flow typing system seamlessly ensures that `null` is never dereferenced. This is because the type `null|int` cannot be treated as an `int`. Instead, one must first check it is an `int` using a type test, such as “`idx is int`”. Whiley automatically *retypes* `idx` to `int` when this is known to be true, thereby avoiding any awkward and unnecessary syntax (e.g. a cast as required in many languages).

? **Null References.** In many languages (e.g. C/C++, Java, etc) the use of `null` is a significant source of error (see e.g.<sup>[4]</sup>). For example, in Java dereferencing the `null` value gives rise to a `NullPointerException`, which is regarded as the most common form of error in Java<sup>[2]</sup>. The issue is that, in such languages, one can treat *nullable* references as though they are *non-null* references<sup>[5]</sup>. In the research literature, there have been many proposals to solve this problem using static type systems (e.g. <sup>[6;7;8;9;10;11;12;13]</sup>). Unfortunately, at the time of writing, very few languages have incorporated such ideas.

? **Intersections and Negations.** Whiley also supports so-called *intersection* and *negation* types. Whilst these can be expressed directly in source code, they are generally less useful than unions.

## 3.2 Recursive Types

To represent tree-like structures, Whiley provides *recursive types* which are similar to the algebraic data types found in functional languages (e.g. Haskell, ML, etc). For example:

```
// A linked list is either the empty list or a link
type LinkedList is EmptyList | Link

// The empty list contains no links
type EmptyList is null

// A single link in a linked list
type Link is {int data, LinkedList next}

// Return the length of a linked list (i.e. the number of links it contains)
int length(LinkedList l):
  if l is null:
    return 0 // l now has type null
  else:
    return 1 + length(l.next) // l now has type {int data, LinkedList next}
```

Here, `LinkedList` is a recursive type representing a linked list (i.e. a sequence of zero or more links). The empty list is defined as `null`, whilst each link contains a `data` field. The type `LinkedList` is defined in terms of itself (i.e. it is recursive) and describes linked lists of arbitrary size.

?

**Value Semantics.** As discussed in §5.2 all compound structures in Whiley are passed by value, *including recursive types*. This differs from common languages (e.g. Java), where linked structures are typically composed from *references* to link objects. This means, for example, that linked structures in such languages can share substructures, leading to subtle and hard-to-find bugs. In Whiley linked structures, such as `LinkedList`, can never share substructure.

The above example also serves as another illustration of flow typing in Whiley. More specifically, on the false branch of the type test “`l is null`”, variable `l` is automatically retyped to `{int data, LinkedList next}` — thus ensuring the subsequent dereference of `l.next` is safe. No casts are required as would be needed for a conventional imperative language (e.g. Java). Finally, like all compound structures, the semantics of Whiley dictates that recursive data types are passed by value (or, at least, appear to be from the programmer’s perspective).

## 3.3 Structural vs Nominal Types

Statically typed languages, such as Java, employ *nominal typing* for recursive data types. This means that two otherwise identical types with different names are considered distinct and, for example, a variable of one type cannot flow into the other. In contrast, Whiley employs *structural typing* of records<sup>[?]1</sup> to give greater flexibility. This means that the name of a type is, generally speaking, unimportant. Instead, identical types (i.e. those with identical *structure*) with different names are still considered identical in Whiley. For example:

```
// Define the notion of a "rectangle"
type Rectangle is { int x, int y, int width, int height }
// Define the notion of a "bounding box"
type BoundingBox is { int x, int y, int width, int height }

// Define a function for computing the area of a rectangle
function area(Rectangle rect) => int:
  return rect.width * rect.height
```

In this example, the types `Rectangle` and `BoundingBox` are *identical* and can be used interchangeably. For example, if we have a variable of type `BoundingBox`, we can safely pass it to the `area()` function above to compute its area.

### 3.4 Coercions

A *coercion* converts a value of one type into a corresponding value of another type. For example, in *Whiley*, we can coerce the `int` value “0” into the `real` value “0.0”. Many programming languages permit both *implicit* and *explicit* coercions, with the latter more commonly referred to as *casting*. Implicit coercions occur without explicit direction from the programmer, and are often considered dangerous because of this.

**? Lossless Coercions?** The Java programming language attempts to enforce a requirement that implicit coercions are *lossless*. Thus, any coercion which may result in a loss of information must be made explicit through the use of a cast. Unfortunately, Java does permit implicit lossy coercions by, for example, allowing `int` values to be implicitly coerced into `float` values — because not every `int` value can be represented by a `float` in Java.

To address the issues surrounding implicit coercions, *Whiley* only permits implicit coercions which are lossless. That is, which do not result in a loss of information. In contrast, *lossy* coercions require an explicit cast be used to “force” the coercion. The following example illustrates:

```
type Link is {int data, LinkedList next}
type LinkedList is null | Link
type OrderedList is null | {
    int data, int order, OrderedList next
}
```

Here, we have defined a standard linked list and a specialised “ordered” list. The intuition is that `order < next.order` for each node in an `OrderedList` (although the details of how this is done are unimportant here). These two types are not considered identical because they have different structure (i.e. `OrderedList` has an additional field, `order`). However, there is still a subtyping relationship between them (i.e. `OrderedList` subtypes `LinkedList`). Thus, an instance of `OrderedList` can be used where a `LinkedList` was expected. For example:

```
function sum(LinkedList l) => int:
    if l is null:
        return 0
    else:
        return l.data + sum(l.next)
```

This defines a simple recursive function for computing the length of a `LinkedList`. Instances of `OrderedList` can be passed into this function by *coercing* them to instances of `LinkedList`:

```
function sum(OrderedList l) => int:
    return sum((LinkedList) l)
```

Here, we have used an explicit coercion (i.e. a cast) from `OrderedList` to `LinkedList`. This must be done explicitly because the coercion is lossy because the field `order` is discarded during the coercion.

**? Lossless Coercions.** *Whiley* (unlike Java) supports lossless coercion from `int` values to `real` values. This is because arithmetic in *Whiley* is unbounded and, hence, every value of `int` type has a corresponding value of `real` type (though not vice-versa).

### 3.5 Subtyping

An important concept in many modern programming languages is that of *subtyping*. This defines a relationship between otherwise different types (i.e. which do not have identical structure). Subtyping allows data from a variable of one type to flow into a variable of another. However, unlike a coercion, subtyping does not physically change the value itself.

The most common form of subtyping in Whiley is through the use of union types. Indeed, we have encountered this already. The following illustrates a very simple example:

```
// A circle is defined by its position and radius
type Circle is { int x, int y, int radius }

// A rectangle is defined by its position and dimensions
type Rectangle is { int x, int y, int width, int height }

// A shape is either a circle or a rectangle
type Shape is Circle | Rectangle

// Determine the area of a shape
function area(Shape s) => real:
  //
  if s is Rectangle:
    // case for rectangle
    return s.width * s.height
  else:
    // case for circle
    return Math.PI * s.radius * s.radius
```

Here, we see that a Shape is either a Rectangle or Circle. We say that Rectangle and Circle are subtypes of Shape. The Whiley compiler knows that there are only two possibilities and, hence, automatically retypes variable `s` to Circle on the false branch.

? A useful analogy to help understanding the concept of a subtype is that of a *subset*. In this way, we think of types as representing the set of values that their variables may hold. Then, one type is a subtype of another if its set of values is a subset of the other's. Conversely, one type is a *supertype* of another if its set of values is a *superset* of the other's. Furthermore, a union type "`T1 | T2`" corresponds to a set union of those values represented by "`T1`" and "`T2`".

Another situation where subtyping occurs in Whiley is with the types **any** and **void**. Specifically, every type is a subtype of **any**, whilst every type is a *supertype* of **void**. To understand this, consider the following:

```
function toInteger(Any x) => int:
  if x is int:
    return x
  else if x is real:
    return Math.round(x)
  else if x is [any]:
    return |x|
  else:
    return 0 // default value
```

In this function, parameter `x` can hold *any possible value on entry*. It could be an integer, a real, a list, a set, a record, etc. In this case, we have picked a few examples which we can easily convert

into **int** values. Note that the type **[any]** describes all possible lists, including e.g. instances of **[int]**, **[[int]]**, **[char]**, etc.

## 4 Example: Minesweeper

In this section, we will develop a simple implementation of the well-known *Minesweeper* game. Typically the minesweeper game is played through a graphical user interface, illustrated as follows:



Here, we can see the main aspects of the game. The *game board* is a two-dimensional grid of *squares*. Each square holds *nothing* or a *bomb* and is in one of the three states: *hidden*, *exposed* or *flagged* (with a flag). An exposed square shows either the total number of bombs in the nine adjacent squares, referred to as its *rank*. If an exposed square contains a bomb, then the game is over and the player has lost. Flagged squares are protected and cannot be exposed unless they are *unflagged*. The intuition here, is that the player marks those squares believed to contain a bomb.

Let's analyse the above board. In the following diagram of the above minesweeper game, gray squares represent hidden squares in the game. For our benefit here, we've split them into two categories: those which contain a bomb (dark gray); and, those which don't:

	0	1	2	3	4	5	6	7	8
0									
1									
2				1	1	1			
3		1	1	2	⚡	2	1	1	
4		1	⚡	3	2	⚡	⚡	1	
5		2						2	
6	1	2						1	
7							3	1	
8							1		

In our discussion, we'll use  $(x, y)$  to indicate a position on the board where  $x$  gives the horizontal component, and  $y$  the vertical component. So, for example, the squares  $(2, 4)$ ,  $(4, 3)$  and  $(6, 4)$  are all marked with a flag. Indeed, we can see that the above player has correctly flagged the three bombs in these squares, and that there are seven remaining to be identified and flagged. Of course, unlike us, the player cannot see exactly where the bombs are. However, he/she can easily determine that the square  $(2, 6)$  must contain a bomb. This is because the exposed square at  $(1, 4)$  has a rank of 1, and a bomb is flagged at  $(2, 4)$ . Therefore, there can be no bomb in square  $(2, 5)$  as this mean the rank of square  $(1, 4)$  was incorrect. Finally, the rank of the square at  $(1, 5)$  is 2 with only three unexposed squares, of which one is known already to contain a bomb and the other is known *not* to contain a bomb. Therefore, the  $(2, 6)$  must contain a bomb.

The player plays the game by repeatedly selecting a square to expose. When all squares are exposed, except for those containing bombs, the game is over and the player wins. However, if a

square holding a bomb is exposed, then the game is over immediately and the player loses. A *blank* square is one with no adjacent bombs. When a blank square is exposed, every adjacent blank square is recursively exposed.

## 4.1 Squares

We're now going to begin implementing the game of Minesweeper in Whiley. To start with, we'll implement the game board in Whiley and provide functions for manipulating it; then, we'll implement the gameplay itself.

The first aspect of the game board we'll implement is the concept of a *square*. There are essentially two broad categories of square in the game: *exposed squares* and *hidden squares*. Therefore, our implementation will reflect this. Exposed squares either have a *rank* or are *blank* (i.e. have a rank of zero). Furthermore, they may or may not hold a bomb. We can implement this in Whiley like so:

```
type ExposedSquare is {  
  int rank,           // Number of bombs in adjacent squares  
  bool holdsBomb      // true if the square holds a bomb  
}
```

Here, we can see that an integer field called `rank` is used to store the rank of the square. Likewise, a boolean field called `holdsBomb` is used to indicate whether or not the square holds a bomb.

Hidden squares may or may not hold a bomb, and may or may not have been flagged. We can implement this in Whiley as follows:

```
type HiddenSquare is {  
  bool holdsBomb,     // true if the square holds a bomb  
  bool flagged        // true if the square is flagged  
}
```

As before, a boolean field called `holdsBomb` is used to signal whether or not the square holds a bomb. Likewise, a boolean field called `flagged` signals whether or not the square is flagged.

We can now define the concept of a square in our Whiley implementation by combining the notions of exposed and hidden squares together as follows:

```
type Square is ExposedSquare | HiddenSquare
```

Here, the type `Square` is a union of the types `ExposedSquare` and `HiddenSquare`. In other words, it is either an `ExposedSquare` or a `HiddenSquare`.

## 4.2 Board

Using our above `Square` data type, we can now define the game board in our Whiley implementation as follows:

```
type Board is {  
  [Square] squares,    // List of squares making up the board  
  int width,           // Width of the game board (in squares)  
  int height,          // Height of the game board (in squares)  
  int numberFlagged,   // Number of Squares which are flagged  
  int numberOfBombs    // Number of Bombs on the board  
}
```

The main component of `Board` is the `squares` list. Although this is a one-dimensional list, we'll see shortly that it is treated a two dimensional way. The remaining fields provide additional



information, such as the width and height of board. Also, the number of flagged squares and the number of bombs on the board. Technically speaking, the latter two can be calculated directly from the `squares` list; however, for simplicity, we provide them as fields here.

```
// Create a board of given dimensions which contains no bombs, and  
// where all squares are hidden.  
Board createEmptyBoard(int width, int height):  
    [Square] squares = []  
    //  
    for i in 0 .. width * height:  
        squares = squares ++ [HiddenSquare(false,false)]  
    //  
    return {  
        squares: rows,  
        width: width,  
        height: height,  
        numberFlagged: 0,  
        numberOfBombs: 0  
    }
```

## 5 Functions, Methods and Objects

### 5.1 Function Purity

Much research has been done on functional purity for object-oriented languages (e.g. <sup>[2 14;15;16]</sup>), because it makes many things more tractable, including: *automatic parallelisation*<sup>[2 ? ? 1]</sup>, *software verification*<sup>[2 ? ? ? 1]</sup>, *query systems*<sup>[2 17]</sup>, *compiler optimisations*<sup>[2 ? ? ? 1]</sup> and more.

### 5.2 Value Semantics

In Whiley, all compound structures (e.g. lists, sets, and records) have *value semantics*. This means they are passed and returned by-value (as in Pascal, MATLAB or most functional languages). But, unlike functional languages (and like Pascal), values of compound types can be updated in place.

Value semantics implies that updates to a variable only affects that variable, and that information can only flow out of a function through its return value. Whiley has no general, mutable heap comparable to those found in object-oriented languages. Consider:

```
int f ([int] xs) :  
  ys = xs  
  xs[0] = 1  
  ...
```

The semantics of Whiley dictate that, having assigned `xs` to `ys` as above, the subsequent update to `xs` does not affect `ys`. Arguments are also passed by value, hence `xs` is updated inside `f()` and this does not affect `f`'s caller. That is, `xs` is not a *reference* to a list of `int`; rather, it *is* a list of `int`s and assignments to it do not affect state visible outside of `f()`.

Whilst this approach may seem inefficient, a variety of techniques exist (e.g. reference counting) to ensure efficiency (see e.g. <sup>[18;19;20]</sup>). Indeed, the underlying implementation does pass compound structures by reference and copies them only when absolutely necessary.

### 5.3 Objects and References

### 5.4 Simulating Interfaces

### 5.5 Concurrency

## 6 Modules, Packages and Versioning

Basically discuss the hierarchy of things:

- **Compilation Units.**
- **Packages.**
- **Modules.**

And how modules can be versioned.

## 7 Verification

As discussed in the introduction, an important feature of Whiley is *verification*. That is made up of two aspects: firstly, the ability to write specifications for functions and methods in Whiley; secondly, the ability of the compiler to check the body of a function or method meets its specification.

Unfortunately, specification is not always straightforward and can require considerable attention to detail. Nevertheless, with practice, it can easily fit into the routine of day-to-day development. In this section, we'll explore the basics of verification in Whiley using some small examples. In the following sections, we'll look at larger and more realistic examples.

### 7.1 Preconditions and Postconditions

A *precondition* is a condition over the parameters of a function that is required to be true when the function is called. The body of the function can then use this to make assumptions about the possible values of the parameters. Likewise, a *postcondition* is a condition over the return values of a function which is required to be true after the function is called. As a very simple example, consider the following function which accepts a positive integer and returns a non-negative integer (i.e. natural number):

```
function decrement(int x) => (int y)
// Parameter x must be greater than zero
requires x > 0
// Return must be greater or equal to zero
ensures y >= 0:
//
    return x - 1
```

Here, the **requires** and **ensures** clauses define the function's precondition and postcondition. With verification enabled, the Whiley compiler will verify that the implementation of this function meets its specification. In fact, we can see this for ourselves by manually constructing an appropriate *verification condition* (that is, a logical condition whose truth establishes that the implementation meets its specification). In this case, the appropriate verification condition is  $x > 0 \implies x-1 \geq 0$ . Unfortunately, although constructing a verification condition by hand was possible in this case, in general it's difficult if not impossible for more complex functions.

The Whiley compiler reasons about functions by exploring the different control-flow paths through their bodies. Furthermore, as it learns more about the variables used in the function, it automatically takes this into account. For example:

```
function abs(int x) => (int y)
// Return value cannot be negative
ensures y >= 0:
//
    if x >= 0:
        return x
    else:
        return -x
```

The Whiley compiler verifies that the implementation of this function meets its specification. At this point, it is worth considering in more detail what this really means. Since the Whiley compiler performs verification at *compile-time*, it does not consider specific values when reasoning about a function's implementation. Instead, it considers all possible input values for the function which satisfy its precondition. In other words, when the Whiley compiler verifies a function's implementation meets its specification, this means it does so *for all possible input values*.

## 7.2 Data Type Invariants

The above illustrates a function specification given through explicit pre- and post-conditions. However, we may also employ *constrained types* to simplify it as follows:

```
type nat is (int n) where n >= 0
type pos is (int p) where p > 0

function f(pos x) => (nat n)
// Return must differ from parameter
ensures n != x:
//
return x-1
```

Here, the **type** declaration includes a **where** clause constraining the permissible values for the type (\$ represents the variable whose type this will be). Thus, `nat` defines the type of non-negative integers (i.e. the natural numbers). Likewise, `pos` gives the type of positive integers and is implicitly a subtype of `nat` (since the constraint on `pos` implies that of `nat`). We consider that good use of constrained types is critical to ensuring that function specifications remain as readable as possible.

The notion of type in Whiley is more fluid than found in typical languages. In particular, if two types  $T_1$  and  $T_2$  have the same *underlying* type, then  $T_1$  is a subtype of  $T_2$  iff the constraint on  $T_1$  implies that of  $T_2$ . Consider the following:

```
type anat is (int x) where x >= 0
type bnat is (int x) where 2*x >= x

function f(anat x) => bnat:
return x
```

In this case, we have two alternate (and completely equivalent) definitions for a natural number (we can see that `bnat` is equivalent to `anat` by subtracting  $x$  from both sides). The Whiley compiler is able to reason that these types are equivalent and statically verifies that this function is correct.

## 7.3 Quantification

## 7.4 Loop Invariants

A loop invariant is a property which holds before and after each iteration of the loop. There are three key points about loop invariants:

1. The loop invariant must hold on entry to the loop.
2. Assuming the loop invariant holds at the start of the loop body (along with the condition), it must hold at the end.
3. The loop invariant (along with the negated condition) can be assumed to hold immediately after the loop.

To illustrate these three aspects, we'll use some simple loop examples. For example, consider the following example:

```
function f(int x) => (int y)
// return cannot be negative
ensures y >= 0:
//
int i = 0
while i < x where i > 0:
i = i + 1
```

```
//
return i
```

Loop invariants in Whiley are indicated by the **where** clause. Thus, in the above example, the loop invariant is “ $i > 0$ ”. Compiling the above program with verification enabled will fail with an error. This is because the loop invariant does not hold on entry to the loop (item 1 above).

## 7.5 Strategies for Loop Invariants

Loop invariants can be tricky to get right, and there are some useful tricks which can simplify things. We’ll now consider some examples to illustrate this.

**Example 1.** Summing over a list of natural numbers is guaranteed to produce a natural number. The following Whiley program illustrates this:

```
type nat is (int x) where x >= 0

function sum([nat] items) => nat:
    int r = 0
    int i = 0
    //
    while i < |items| where i >= 0 && r >= 0:
        r = r + items[i]
        i = i + 1
    //
    return r
```

The Whiley compiler statically verifies that `sum()` does indeed meet this specification. This is true in Whiley because integer arithmetic is *unbounded* — meaning it does not suffer from overflow as other languages do (e.g. Java). The loop invariant is necessary to help the Whiley compiler verify this function. However, we can avoid the need for a loop invariant by declaring variables `i` and `r` more precisely:

```
function sum([nat] items) => nat:
    nat r = 0
    nat i = 0
    //
    while i < |items|:
        ...
```

This time, we have declared the variables `i` and `r` as having type `nat`. The Whiley compiler will now enforce the `nat` property for `i` and `r` at all points in the function, and the loop invariant is no longer required.

**Example 2.** Generally speaking, the loop condition and invariant are used independently to increase knowledge. However, sometimes they need to be used in concert. Consider the following function for initialising a list of a given size:

```
function create(int count, int value) => ([int] r)
// Cannot create negatively sized lists!
requires count >= 0,
// Returned list must have count elements
ensures |r| == count:
    //
    int i = 0
    [int] r = []
```

```

while i < count:
    r = r + [value]
    i = i + 1
//
return r

```

This example uses the list append operator (i.e. `r + [value]`) and is surprisingly challenging to verify. An obvious approach is to connect the size of `r` with `i` as follows:

```

...
while i < count where |r| == i:
    ...

```

Unfortunately, this loop invariant is not strong enough to allow this function to be verified. To understand this, recall from §7.4 that, after a loop is complete, the loop invariant holds along with the *negated* condition. Thus, after the above loop, we have `i >= count && |r| == i` which is insufficient to establish `|r| == count`. In fact, we can resolve this by using an *overriding loop invariant* as follows:

```

...
while i < count where i <= count && |r| == i:
    ...

```

In this case, `i >= count && i <= count && |r| == i` holds after the loop and, hence, it follows that `|r| == count`.

## 7.6 Explicit Assumptions

## 7.7 Function Invocation

To keep verification tractable, the Whiley compiler verifies each function in a program one at a time, independently of others.<sup>1</sup> Thus, when verifying a given function, it assumes that all other functions correctly meet their specification. Of course, if this is not the case, then this will eventually be discovered as the compiler progresses through the program. For example, consider this program:

```

function f(int x) => (int y)
// Return cannot be negative
ensures y >= 0:
    //
    return x

function g() => (int y)
// Return cannot be negative
ensures y >= 0:
    //
    return f(1)

```

This program will not verify because the implementation of `f()` does not meet its specification. For example, `f(-1)` gives `-1` but the post-condition for `f()` allows only non-negative integers to be returned. However, the Whiley compiler will verify that the implementation of `g()` meets its specification as, when doing this, it assumes that `f()` meets its specification.

<sup>1</sup>This corresponds to performing an *intra-procedural* analysis, compared with a more involved *inter-procedural* analysis.

## 8 Example: IndexOf Function

To better illustrate verification in Whiley, we'll develop the specification for a slightly more challenging function. This is the `indexOf()` function, described as follows:

```
// Return the lowest index in the items list which equals the given item.  
// If no such index exists, returns null.  
function indexOf([int] items, int item) => int|null:  
    ...
```

This is a common function found in the standard libraries of many programming languages. The body of the function examines each element of the `items` list and check whether or not it equals `item`. To start with, we won't worry too much about the body of the `indexOf()` function. Instead, we'll progressively build up the specification until we are happy with it. Then, we'll give an implementation of the function which meets this specification.

To specify this function, we want to ensure three properties:

1. If the return is an integer `i`, then `items[i] == item`.
2. If the return is `null`, there is no index `j` where `items[j] == item`.
3. If the return is an integer `i`, then there is no index `j` where `j < i` and `items[j] == item`.

These properties determine how a correct implementation of the `indexOf()` function should behave. We refer to them as the *specification* of the `indexOf()` function.

### 8.1 Specifying Property 1 — Return Valid Index

The first of the above properties is the easiest, so let's start by specifying that in Whiley. At the same time, we'll also give an initial implementation which satisfies this partial specification:

```
function indexOf([int] items, int item) => (int|null r)  
// If return value is an int i, then items[i] == item  
ensures i is int ==> items[i] == item:  
    //  
    if |items| > 0 && items[0] == item:  
        return 0  
    else:  
        return null
```

Here, we can see property (1) above written as an **ensures** clause in Whiley. In particular, the phrase “the return value is an integer” is translated into the condition “`i is int`”. Likewise, the implication operator (i.e. `==>`) is used to say “If ... then ...”. We've also given an initial implementation for the `indexOf()` function which simply checks whether or not `items[0] == item`. This implementation meets the specification we have so far although, obviously, this is an incomplete implementation of the `indexOf` function!

### 8.2 Specifying Property 2 — Return Null if No Match

Property (2) from our list above is more difficult to specify, because it requires *quantification*. There are several quantifiers available in Whiley, including: **all**, which allows us to say “for all elements in a list something is true”; and **no**, which allows us to say “there is no element in the list where something is true”.

In Whiley, we can express property (2) from above in several different ways. The most direct translation would be:

```

...
// If return is null, there is no index j where items[j] == item
ensures i is null ==> no { j in 0..|items| | items[j] == item }:
...

```

Here, the expression `|items|` gives the length of the `items` list, whilst the range expression `0..|items|` returns a list of consecutive integers from 0 up to, but not including, `|items|`. Instead of using the **no** quantifier, we could have equally used the **all** quantifier, like so:

```

...
// If return is null, there is no index j where items[j] == item
ensures i is null ==> all { j in 0..|items| | items[j] != item }:
...

```

The above, however, is perhaps not as clear as the first translation. Finally we can, in this case, avoid talking about indices altogether like so:

```

...
// If return is null, there is no index j where items[j] == item
ensures i is null ==> no { x in items | x == item }:
...

```

The above simply says “there is no element `x` in `items` where `x == item`”. Although this is also not the most direct translation of the original property, it is a rather convenient translation which achieves the same thing.

### 8.3 Specifying Property 3 — Return Least Index

### 8.4 Working Implementation

At this point, we can now give the complete specification for the `indexOf()` function, along with an initial implementation:

```

function indexOf([int] items, int item) => (int|null i)
// If return is an int r, then items[r] == item
ensures i is int ==> items[i] == item
// If return is null, then no element x in items where x == item
ensures i is null ==> no { x in items | x == item }
// If return is an int i, then no index j where j < i and items[j] == item
ensures i is int ==> no { j in 0 .. i | items[j] == item }:
//
i = 0
while i < |items|:
    if items[i] == item:
        return i
    i = i + 1
//
return null

```

The implementation of `indexOf()` given above meets the function’s specification. Unfortunately, whilst this is true, the `Whiley` compiler needs help to determine this. Figure 3 illustrates what happens when we compile the above code with verification enabled.

### 8.5 Verified Implementation

Although our implementation of `indexOf()` given above is correct, it currently does not verify. Although this distinction may seem unimportant, it goes to the heart of what verification is about.



```

1 int| null indexOf([int] items, int item)
2 // If return is an int r, then items[r] == item
3 ensures !($ is int) || items[$] == item,
4 // If return is null, then no element x in items where x == item
5 ensures !($ is null) || no { x in items | x == item },
6 // If return is an int i, then no index j where j < $ i and items[j] == item
7 ensures !($ is int) || no { j in 0 .. $ | items[j] == item }:
8 //
9 i = 0
10 while i < |items|:
11     if items[i] == item:
12         return i
13     i = i + 1
14 //
15 return null
16

```

"index out of bounds (negative)"

Figure 3: Illustrating our first working version of the `indexOf` function being compiled with verification enabled. The compiler is reporting an error stating “*index out of bounds (negative)*”. This is because the compiler believes `i` may be negative at this point. Although we know this is not true, we must write a *loop invariant* to help the compiler see this.

That is, we know the implementation of `indexOf()` is correct because we, *as humans*, have looked at it and believe it is. Whilst may be a reasonable approach for small examples, it certainly is not for larger and more complex programs. Humans are fallible and we can easily believe something is true when it is not. Therefore, we want a mechanical system which can examine a program and report “*Yes, I agree that this is correct*”. Whiley provides such a system when verification is enabled.

Unfortunately, Whiley is not as smart as a human and often there will be things we know that it does not. In such cases, we need to help Whiley by adding hints into our programs. In this case, we need to add some loop invariants (recall §7.4) to help Whiley verify our implementation of `indexOf()`. The first part of the loop invariant we need is straightforward. Since `i` is modified in the loop, we need an invariant to ensure `i >= 0` when `items[i]` is accessed:

```

...
i = 0
while i < |items| where i >= 0:
    ...
    i = i + 1

```

We can see that this invariant holds on entry to the loop (i.e. since `i = 0` on entry). Furthermore, if `i >= 0` then `i+1 >= 0` follows and, hence, the loop invariant holds after each iteration.

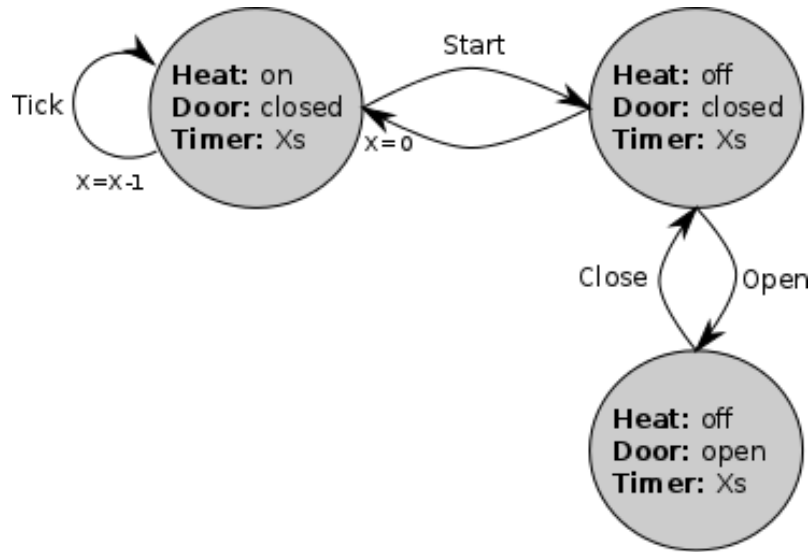


Figure 4: A state-machine diagram for the microwave oven

## 9 Example: Microwave Oven

For the next case study, we examine the classic and well-known *microwave oven* problem. In essence, we have a microwave oven with a door and a heating element. An important safety condition is that the heating element cannot be on when the door is open, to protect against burns. This example is interesting, because it demonstrates that Whiley can operate effectively as a modelling language, as well as a general-purpose programming language.

### 9.1 Overview

Figure 4 provides a state-machine diagram of the microwave oven. The microwave state has three components: a heating element, which is set either *on* or *off*; a door which (via a sensor) is reported either *open* or *closed*; and, finally, a timer value indicating how for many seconds heating should occur.

In addition to the microwave state, a number of external events are permitted. First, a start button is used to signal the microwave should begin heating; second, the door may be opened or closed; finally, an internal clock is used to signal time passing (in one second intervals) to the state machine.

### 9.2 Microwave State

The state of the microwave is represented in Whiley using a record containing the main three components, along with an appropriate invariant. The following illustrates:

```

type nat is (int x) where x >= 0

// First, define the state of the microwave.
type Microwave is {
    bool heatOn, // if true, the oven is cooking
    bool doorOpen, // if true, the door is open
    nat timer // timer setting (in seconds)
} where !doorOpen || !heatOn

```

Here, boolean values are used to represent the state of the heating element, and the door sensor, whilst a natural number represents the timer value. The invariant states that either the door is closed, or the heating element is off.

### 9.3 Events

Events are represented in Whiley using functions which map one microwave state to another. Here are the two functions representing the *open* and *close* events:

```
// A door closed event is triggered when the sensor detects that the door is closed.
function doorClosed(Microwave m) => Microwave
requires m.doorOpen:
    //
    m.doorOpen = false
    return m

// A door opened event is triggered when the sensor detects that the door is opened.
function doorOpened(Microwave m) => Microwave
requires !m.doorOpen:
    //
    m.doorOpen = true
    m.heatOn = false
    return m
```

Here, we can see that preconditions on the functions act as guards restricting when the events may fire. The Whiley compiler will statically verify that the `Microwave` invariant holds for the turn value, assuming it held for the parameter. Thus, failing to set `m.heatOn = false` in `doorOpened()` results in a compile time error which signal that the safety property is not be enforced.

Likewise, we can specify the *start* event and, in doing so, we must ensure the safety property is enforced. Specifically, when the heating element is turned on, the door must be closed:

```
// Signals that the "start cooking" button has been pressed.
function startCooking(Microwave m) => Microwave:
    //
    // Here, we check the all important safety property
    if !m.doorOpen:
        m.heatOn = true
    return m
```

Here we can see that, if the door is open when the start button is pressed, nothing happens. Again, failing to check whether the door is open in `startCooking()` results in a compile time error which signal that the safety property is not be enforced.

## A Foreign Function Interface

## B Verification Conditions

Talk about how to generate and see verification conditions.

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