

3a

$$\begin{aligned}l_1(x) &= \prod_{\substack{i=0 \\ i \neq 1}}^3 \frac{x-x_i}{x_1-x_i} = \frac{x-x_0}{x_1-x_0} \cdot \frac{x-x_2}{x_1-x_2} \cdot \frac{x-x_3}{x_1-x_3} \\&= x \cdot \frac{x-2}{1} \cdot \frac{x-3}{-2} = \frac{1}{2}x(x^2-5x+6) \\&= \frac{1}{2}(x^3-5x^2+6x)\end{aligned}$$

$$\begin{aligned}l_2(x) &= \prod_{\substack{i=0 \\ i \neq 2}}^3 \frac{x-x_i}{x_2-x_i} = \frac{x-x_0}{x_2-x_0} \cdot \frac{x-x_1}{x_2-x_1} \cdot \frac{x-x_3}{x_2-x_3} \\&= \frac{1}{2}x \cdot \frac{x-1}{1} \cdot \frac{x-3}{-1} = -\frac{1}{2}(x^3-4x^2+3x)\end{aligned}$$

$$\begin{aligned}l_3(x) &= \prod_{\substack{i=0 \\ i \neq 3}}^3 \frac{x-x_i}{x_3-x_i} = \frac{x-x_0}{x_3-x_0} \cdot \frac{x-x_1}{x_3-x_1} \cdot \frac{x-x_2}{x_3-x_2} \\&= \frac{1}{3}x \cdot \frac{1}{2}(x-1)(x-2) = \frac{1}{6}(x^3-3x^2+2x)\end{aligned}$$