

AN ALTERNATIVE FORM OF THE GAUSS-SEIDEL ITERATIVE METHOD FOR SOLVING LINEAR SYSTEMS OF EQUATIONS IS:

$Dx_{k+1} = D x_k - (L x_{k+1} + (D+U)x_k - b)$
 IF A SOLUTION CAN BE FOUND BY THIS, CONVERGENCE CAN BE ACCELERATED W/ AN APLY TERMED 'ACCELERATION PARAMETER' ω

$$\rightarrow Dx_{k+1} = D x_k - \omega (L x_{k+1} + (D+U)x_k - b) \quad (1)$$

REARRANGE (1) TO THE FORM:

$$(\omega L + D) x_{k+1} = D x_k - \omega (D+U)x_k + \omega b$$

$$\rightarrow Dx_{k+1} = D x_k - \omega L x_{k+1} - \omega (D+U)x_k + \omega b$$

$$D x_{k+1} + \omega L x_{k+1} = D x_k - \omega (D+U)x_k + \omega b$$

$$(\omega L + D) x_{k+1} = D x_k - \omega (D+U)x_k + \omega b \quad (2)$$

REARRANGE (2) TO THE FORM:

$$(\omega L + D) x_{k+1} = ((1-\omega)D - \omega U) x_k + \omega b$$

$$= (D - \omega(D+U)) x_k + \omega b$$

$$= (D - \omega D + \omega U) x_k + \omega b$$

$$(\omega L + D) x_{k+1} = ((1-\omega)D - \omega U) x_k + \omega b$$