

7

a

$$M_1 A = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 3/4 & 1 & 0 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dots \\ \dots \\ \dots \\ \dots \end{bmatrix} = \begin{bmatrix} 4 & 1 & 0 & 0 \\ 0 & 3/4 & 1 & 0 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$M_2 M_1 A = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 4/3 & 1 & 0 \\ 0 & 0 & 3/8 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dots \\ \dots \\ \dots \\ \dots \end{bmatrix} = \begin{bmatrix} 4 & 1 & 0 & 0 \\ 0 & 3/4 & 1 & 0 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} = MA = U$$

$$Mb = \begin{bmatrix} \dots \\ \dots \\ \dots \\ \dots \end{bmatrix} \begin{bmatrix} 3 \\ 3 \\ 3 \\ -25/8 \end{bmatrix} = \begin{bmatrix} 2 \\ 5/2 \\ 7 \\ -25/8 \end{bmatrix} = y$$

$$MA = y$$

$$\downarrow$$

$$\begin{bmatrix} 4 & 3/4 & 0 & 0 \\ 0 & 3/4 & 1 & 0 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 2 \\ 5/2 \\ 7 \\ -25/8 \end{bmatrix}$$

$$\begin{cases} 4x_1 + x_2 = 2 \\ 3/4 x_2 - x_3 = 5/2 \\ 8/3 x_3 - x_4 = 7 \\ 29/8 x_4 = -25/8 \end{cases}$$

NOW I WOULD
SOLVE FOR
X BY
BACK-SUB