

Runge-Kutta Method (one-step)

THE 1ST STEP IS ALWAYS TO FIND

THE y_{n+1} ... $f(y(t)) = 2y(t) = 2e^t$

(RULE(?))

FOR IC THIS

IS $(y_0 = 1), (h = 0.1)$

$$\begin{aligned} y_1 &= (1) + \frac{0.1}{6} \left(\underbrace{2 \cdot 1}_{k_1} + \underbrace{2 \cdot \left(2 \left(1 + \frac{0.1}{2} (2 \cdot 1) \right) \right)}_{k_2} \right. \\ &\quad \left. + 2 \cdot \left(2 \cdot \left(1 + \frac{0.1}{2} \left(2 \cdot \left(2 \cdot \left(1 + \frac{0.1}{2} (2 \cdot 1) \right) \right) \right) \right) \right) \right. \\ &\quad \left. + 2 \cdot \left(1 + 0.1 \left(\left(2 \cdot \left(1 + \frac{0.1}{2} \left(2 \cdot \left(1 + \frac{0.1}{2} (2 \cdot 1) \right) \right) \right) \right) \right) \right) \right) \right) \\ &= 1 + (0.01667) (2 + 8.4) \\ &\quad + 2 \cdot (2 \cdot (1 + (0.01667) \cdot 4.4) \\ &\quad + 2 \cdot (1 + 0.1 (2 \cdot (1 + 0.01667 \cdot 2.067))) \end{aligned}$$