

3
b

$$Lx = Pb$$

$$Ux = y$$

$$\begin{bmatrix} 1 & 0 & 0 \\ \frac{1}{5} & 1 & 0 \\ -\frac{1}{5} & \frac{2}{5} & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 2 \\ -2 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$x_1 = 2$$

$$x_2 = 1 + \frac{3}{5} \cdot 2 = \frac{11}{5} = x_2$$

$$x_3 = -2 + \frac{2}{5} \cdot \frac{2}{5} = -2 = x_3$$

$$x = \begin{bmatrix} 2 \\ \frac{11}{5} \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} -5 & 2 & -1 \\ 0 & \frac{11}{5} & \frac{27}{5} \\ 0 & 0 & \frac{30}{11} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 \\ \frac{11}{5} \\ -2 \end{bmatrix}$$

$$x_3 = -\frac{11}{10} \cdot 2 = -\frac{11}{10} = x_3$$

$$x_2 = \left(\frac{11}{5} + \frac{27}{5} \cdot \frac{11}{10} \right) \frac{5}{11} = 3.7 = x_2$$

$$x_1 = \left(2 - 2 \cdot 3.7 - \frac{11}{10} \right) = \left(-\frac{1}{5} \right) = 1.3$$

$$x = \begin{bmatrix} 1.3 \\ 3.7 \\ -\frac{11}{10} \end{bmatrix}$$