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a IF L_n IS ORTHOGONAL TO L_{n+1}

THEN, $\langle L_n, L_{n+1} \rangle = 0$

$$\longrightarrow \int_0^{\infty} L_n \cdot L_{n+1} e^{-x} dx = \int_0^{\infty} 1 \cdot (1-x) e^{-x} dx$$

$$= \int_0^{\infty} (e^{-x} - x e^{-x}) dx = \int_0^{\infty} e^{-x} dx - \int_0^{\infty} x e^{-x} dx$$

$$= 1 - 1$$

$$= 0$$

$\longrightarrow L_0 \text{ \& } L_1$
ARE ORTHOGONAL