

4b

$$M_2(h/9) = \frac{9}{16} \left[\frac{3f(x_0+h) - 3f(x_0)}{h} - \frac{3f(x_0+h/3) - 3f(x_0)}{h} - \dots \right]$$

$$\dots - \frac{9f(x_0+h/3) - 9f(x_0)}{h} + \frac{9f(x_0+h/9) - 9f(x_0)}{h} \Big]$$

$$= \frac{27}{16h} \left[f(x_0+h) - f(x_0) - f(x_0+h/3) + f(x_0) - \dots \right]$$

$$\dots - 3f(x_0+h/3) + 3f(x_0) + 3f(x_0+h/9) - 3f(x_0) \Big]$$

$$= \frac{27}{16h} \left[f(x_0+h) - 4f(x_0+h/3) + 3f(x_0+h/9) \right]$$

$$= \frac{27}{16h} \left(f(x_0+h) - 4f(x_0+h/3) + 3f(x_0+h/9) \right) + O(h^3)$$

$\frac{df(x_0)}{dx}$