

$$C \approx \frac{\|x_k - x_{k-1}\|}{\|x_{k-1} - x_{k-2}\|}$$

$$C \approx \frac{\|x_2 - x_1\|}{\|x_1 - x_0\|} = \frac{\frac{1}{4} + \frac{1}{4}}{\frac{1}{4} - \frac{1}{4}} = \frac{1}{0} = \infty$$

$$\begin{aligned} x_1^{(k+1)} &= \frac{1}{a_{11}} [b_1 - a_{12}x_2^{(k)} - a_{13}x_3^{(k)}] \\ x_2^{(k+1)} &= \frac{1}{a_{22}} [b_2 - a_{21}x_1^{(k)} - a_{23}x_3^{(k)}] \\ x_3^{(k+1)} &= \frac{1}{a_{33}} [b_3 - a_{31}x_1^{(k)} - a_{32}x_2^{(k)}] \end{aligned}$$

$$A = \begin{bmatrix} 4 & -1 & 0 \\ -1 & 4 & 1 \\ 0 & -1 & 4 \end{bmatrix}; b = \begin{bmatrix} 2 \\ 4 \\ 10 \end{bmatrix}$$

$$x^{(0)} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}; x^{(1)} = \frac{1}{4} \begin{bmatrix} 2 \\ 4 \\ 10 \end{bmatrix} = \begin{bmatrix} 0.5 \\ 1.0 \\ 2.5 \end{bmatrix} = x^{(1)}$$

$$\begin{aligned} x^{(2)} &= \frac{1}{4} \begin{bmatrix} 2 - (-1 \cdot 1.0 + 0 \cdot 2.5) \\ 4 - (-1 \cdot 0.5 + -1 \cdot 2.5) \\ 10 - (0 \cdot 0.5 + -1 \cdot 1.0) \end{bmatrix} \\ &= \frac{1}{4} \begin{bmatrix} 2 - (-1.0) \\ 4 - (-0.5 - 2.5) \\ 10 - (-1.0) \end{bmatrix} \\ &= \frac{1}{4} \begin{bmatrix} 2 + 1.0 \\ 4 + 3.0 \\ 10 + 1.0 \end{bmatrix} \end{aligned}$$

$$= \frac{1}{4} \begin{bmatrix} 3.0 \\ 7.0 \\ 11.0 \end{bmatrix} = \begin{bmatrix} 0.75 \\ 1.75 \\ 2.75 \end{bmatrix} = x^{(2)}$$

CHECK  $x^{(0)}, x^{(1)}, x^{(2)}$   
ARE CORRECT IN  
CODE

→ THEY ARE

NOW CHECK C'S  
ARE CORRECT

GAUSS - SEIDEL

$$(L+D)x_{n+1} = -Ux_n + b$$