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By the theorem of uniqueness for polynomials as posted in lecture notes 21,

there is only one unique polynomial

in  $\mathcal{P}_n = \{a_0 + a_1x + a_2x^2 + a_3x^3 + a_4x^4 + a_5x^5\}$

satisfying

$x$	-2	-1	0	1	2	3
$P(x)$	-5	1	1	1	7	25

from the Lagrange form of polynomials,

$$P(x) = \sum_{k=0}^5 f(x_k) \cdot l_k(x) = f(x), \text{ for } x \in \{-2, -1, 0, 1, 2, 3\}$$