

$$\underline{y'} = 2y, \quad y(0) = 1 = u_0$$

$$u_{n+1} = u_n + hf(u_n)$$

$$f(y) = 2y, \quad y(t) = e^{2t}, \quad h = 0.1$$

$$u_1 = u_0 + hf(u_0)$$

$$= u_0(1 + 2h) = 1.0(1 + 0.2) = 1.2$$

$$u_2 = u_1 + hf(u_1)$$

$$= u_1(1 + 2h) = 1.2 \cdot (1 + 0.2) = 1.44$$

$$h = 0.05$$

$$u_1 = 1.0(1 + 0.1) = 1.1$$

$$u_2 = 1.1(1 + 0.1) = 1.21$$

$$h = 0.001$$

$$u_1 = 1.0(1 + 0.002) = 1.002$$

$$u_2 = 1.002(1 + 0.002) \approx 1.004$$