

$$\underline{3} \quad f(x) = e^x, \quad x_0 = 0, \quad x_1 = 1, \quad x_2 = 2, \quad x_3 = 3 \quad n = 3$$

$$p_3(x) = f(x_0)l_0(x) + f(x_1)l_1(x) + f(x_2)l_2(x) + f(x_3)l_3(x)$$

$$l_0(x) = \prod_{i=1}^3 \frac{x-x_i}{x_0-x_i} = \frac{x-x_1}{x_0-x_1} \frac{x-x_2}{x_0-x_2} \frac{x-x_3}{x_0-x_3} = \frac{x-1}{0-1} \frac{x-2}{0-2} \frac{x-3}{0-3}$$

$$= -\frac{1}{6}(x-1)(x^2-5x+6) = -\frac{1}{6}(x^3-6x^2+12x-6)$$

$$l_1(x) = \prod_{\substack{i=0 \\ i \neq 1}}^3 \frac{x-x_i}{x_1-x_i} = \frac{x-x_0}{x_1-x_0} \frac{x-x_2}{x_1-x_2} \frac{x-x_3}{x_1-x_3} = \frac{x-0}{1-0} \frac{x-2}{1-2} \frac{x-3}{1-3}$$

$$= \frac{1}{2}x(x^2-5x+6) = \frac{1}{2}(x^3-5x^2+6x)$$

$$l_2(x) = \prod_{\substack{i=0 \\ i \neq 2}}^3 \frac{x-x_i}{x_2-x_i} = \frac{x-x_0}{x_2-x_0} \frac{x-x_1}{x_2-x_1} \frac{x-x_3}{x_2-x_3} = \frac{x-0}{2-0} \frac{x-1}{2-1} \frac{x-3}{2-3}$$

$$= -\frac{1}{2}x(x^2-4x+3) = -\frac{1}{2}(x^3-4x^2+3x)$$