

$$Lz = Pb$$

$$b = \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$Pb = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$\begin{bmatrix} 3/5 & 0 & 0 \\ 0 & 1 & 0 \\ 1/5 & 2/11 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$x_1 = 2$$

$$-\frac{3}{5}x_1 + x_2 = 1$$

$$x_2 = 1 + \frac{3}{5} \cdot 2 = \frac{5}{5} + \frac{6}{5} = \frac{11}{5} = x_2$$

$$-\frac{1}{5} \cdot 2 + \frac{2}{11} \cdot \frac{11}{5} + x_3 = -2$$

$$x_3 = -2 + \frac{2}{5} - \frac{2}{5} = -2 = x_3$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$-1 + 2 \cdot 3 + (-1 \cdot 2) = -1 + 6 - 2 = 3$$

$$Ux = y \rightarrow \begin{bmatrix} -5 & 2 & -1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

$$\frac{20}{11}x_3 = -2$$

$$x_3 = -\frac{11}{20} \cdot 2 = -\frac{22}{20} = -\frac{11}{10} = x_3$$

$$\frac{11}{5}x_2 + \frac{27}{5}x_3 = \frac{11}{5}$$

$$-\frac{3}{5}x_1 + x_2 = 1$$

$$-\frac{3}{5} \cdot 2 + x_2 = 1$$

$$x_2 = 1 + \frac{6}{5} = \frac{5}{5} + \frac{6}{5} = \frac{11}{5} = x_2$$

$$x_2 = \left(\frac{11}{5} + \frac{27}{5} \cdot \frac{11}{10} \right) \frac{5}{11} = 3.7 = x_2$$

$$-5x_1 + 2x_2 - x_3 = 2$$

$$x_1 = (2 - 2x_2 + x_3) \cdot \left(-\frac{1}{5} \right)$$

$$= (2 - 2(3.7) - \frac{11}{10}) \cdot \left(-\frac{1}{5} \right)$$

$$= 1.3 = x_3$$

$$-\frac{1}{5}x_1 + \frac{2}{11}x_2 + x_3 = -2$$

$$x_3 = -2 + \frac{2}{5} - \frac{2}{5} = -2$$

$$= -2 \checkmark$$

$$-5 \cdot (1.3) + 2 \cdot (3.7) + \left(-\frac{11}{10} \right) =$$