### Lesson 1: Week 10

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#### **Exercise 1: Word ladders**

Write a program word ladder.py that computes all transformations of a word word 1 into a word word 2, consisting of sequences of words of minimal length, starting with word\_1, endingin word\_2, and such that two consecutive words in the sequence differ by at most one letter. All words have to occur in a dictionary with name dictionary.txt, stored in the working directory.It is convenient and effective to first create a dictionary whose keys are all words in the dictionary dictionary.txt with one letter replaced by a "slot", the value for a given key being the list of words that match the key with the "slot" being replaced by an appropriate letter. From this dictionary, one can then build a dictionary with words as keys, and as value for a given key the list of words that differ in only one letter from the key. The program implements a function word ladder(word 1, word 2) that returns the list of all solutions, a solution being as previously described.Below is a possible interaction:\$ python3 ... >>> from word\_ladder import \* >>> for ladder in word\_ladder('cold', 'warm'): print(ladder) ... ['COLD', 'CORD', 'CARD', 'WARD', 'WARM'] ['COLD', 'CORD', 'WORD', 'WORM', 'WARM'] ['COLD', 'CORD', 'WORD', 'WARD', 'WARM'] >>> for ladder in word\_ladder('three', 'seven'): print(ladder) ... ['THREE', 'THREW', 'SHREW', 'SHRED', 'SIRED', 'SITED', 'SATED', 'SAVED', 'SAVER', 'SEVER', 'SEVEN'] >>> for ladder in word\_ladder('train', 'bikes'): print(ladder) ... ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'BORES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'CAKES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'PORES', 'POKES', 'PIKES', 'BIKES', I'TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'PIKES', 'PIKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'CAKES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'BORES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'CAKES', 'BAKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'PORES', 'POKES', 'PIKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'POKES', 'PIKES', 'BIKES'] ['TRAIN', 'GRAIN', 'GROIN', 'GROWN', 'GROWS', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'CAKES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DRAWS', 'DRAGS', 'BRAGS', 'BRATS', 'BEATS', 'BELTS', 'BELLS', 'BALLS', 'BALES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DRAWS', 'DRAGS', 'BRAGS', 'BRATS', 'BEATS', 'BESTS', 'BUSTS', 'BUSES', 'BASES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'BORES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'BARES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'CARES', 'CAKES', 'BAKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'PORES', 'POKES', 'PIKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'POKES', 'PIKES', 'BIKES'] ['TRAIN', 'DRAIN', 'DRAWN', 'DROWN', 'CROWN', 'CROWS', 'CROPS', 'COOPS', 'CORPS', 'CORES', 'COKES', 'CAKE...

## **Exercise 2: Word search puzzle**

Word search puzzle consists of a grid of letters and a number of words, that have to be read horizontally, vertically or diagonally, in either direction. Write a program word\_search.py that defines a class WordSearch with the following properties:To create a WordSearch object, the name of a file has to be provided. This file is meant to store a number of lines all with the same number of uppercase letters, those lines possibly containing spaces anywhere, and the file possibly containing extra blank lines.\_\_str\_\_() is implemented.It has a method number\_of\_solutions() to display the number of solutions for each word length for which a solution exists.It has a method locate\_word\_in\_grid() that takes a word as argument; it returns None if the word cannot be read in the grid, and otherwise returns the x and y coordinates of an occurrence of the first letter of the word in the grid and the direction to follow (N, NE, E, SE, S, SW, W, or

NW) to read the whole word from that point onwards. Coordinates start from 0, with the x-axis pointing East, and the y-axis pointing South. It has a method locate words in grid() that takes any number of words as arguments, and returns a dictionary whose keys are those words and whose values are None or the triple returned by locate\_word\_in\_grid() when called with that word as argument.It has a method display\_word\_in\_grid() that takes a word as argument and in case the word can be read from the grid, prints out the grid with all characters being displayed in lowercase, except for those that make up word, displayed in uppercase. Here is a possible interaction: \$ python3 ... >>> from word search import \* >>> import pprint >>> ws = WordSearch('word search 1.txt') >>> print(ws) N D A O E L D L O G B M N E I T D CMEAINRUTSLCLUUEICGGGOLIIKMUIMUIDIRIALTEURTUNGSTENBV HLILSLTTULRUOEIC MATETIUR DR CRUIDS CAMAGNESIUM MAM PD MUI NATITIPCNPLATINUMDLLHZEMANGANESEIGMGITINRUNORITCRIAN N A M E R C U R Y N U O T C C R E P P O C E E R >>> metal = 'PLATINUM' >>> print(f'{metal}: {ws.locate word in grid(metal)}') PLATINUM: (3, 9, 'E') >>> metal = 'SODIUM' >>> print(f'{metal}: {ws.locate word in grid(metal)}') SODIUM: None >>> metals = ('PLATINUM', 'COPPER', 'MERCURY', 'TUNGSTEN', 'MAGNESIUM', 'ZINC', 'MANGANESE', ... 'TITANIUM', 'TIN', 'IRON', 'LITHIUM', 'CADMIUM', 'GOLD', 'COBALT', 'SILVER', ... 'NICKEL', 'LEAD', 'IRIDIUM', 'URANIUM', 'SODIUM') >>> located metals = ws.locate words in grid(\*metals) >>> pprint.pprint(located metals) ('CADMIUM': (1, 9, 'N'), 'COBALT': (11, 6, 'N'), 'COPPER': (10, 13, 'W'), 'GOLD': (9, 0, 'W'), 'IRIDIUM': (10, 3, 'W'), 'IRON': (11, 11, 'W'), 'LEAD': (4, 5, 'S'), 'LITHIUM': (13, 1, 'S'), 'MAGNESIUM': (5, 7, 'E'), 'MANGANESE': (3, 10, 'E'), 'MERCURY': (6, 12, 'E'), 'NICKEL': (0, 0, 'S'), 'PLATINUM': (3, 9, 'E'), 'SILVER': (12, 1, 'S'), 'SODIUM': None, 'TIN': (6, 9, 'NE'), 'TITANIUM': (12, 8, 'W'), 'TUNGSTEN': (3, 4, 'E'), 'URANIUM': None, 'ZINC': (1, 10, 'SE')} >>> for metal in metals: ... print(metal, end = ':\n') ... ws.display\_word\_in\_grid(metal) ... print() ... PLATINUM: ndaoeldlogbmneitdcmeainrutslcluueicgggoliikmuimuidirialte urtungstenbvhlilslttulruoeicmatetiurdrcruidscamagnesiummampdmui natitipcnPLATINUMdllhzemanganeseigmgitinrunoritcriannamercuryn uotccreppoceer COPPER: ndaoeldlogbmneitdcmeainruts Icluueicgggoliik muimuidirialteurtungstenbvhlilslttulruoeicmatetiurdrcruidscamagnes ium mampdmuinatitip cnplatinum dllhzemangane seigm gitinrunorit crian namercurynuotc...

### Exercise 3: Possible subtractions yielding a given sum

# Exercise 4: Voting systems

Find out (e.g., in Wikipedia) about these voting systems: (a) one round method, (b) two round method, (c) elimination method, (d) De Borda count, and (e) De Condorcet count. The elimination method works as follows. One adds up the tallies of all candidates who rank 1st and eliminate the candidate(s) who get the minimal number of votes (as ranked 1st candidates). For a given ordering, the candidates who remain and were ranked after the eliminated candidate(s) see their ranking go up so that the ordering is preserved, and rankings range from 1 up to the number of candidates that remain. For instance, if to start with, there are 5 candidates, A, B, C, D, and E who are ranked 1, 2, 3, 4, and 5, respectively, and if B and D are eliminated because they get the least number of votes as 1st candidates across all rankings, then for that particular ranking, A remains ranked 1st, C becomes ranked 2nd, and E becomes ranked third. The process is repeated until there is only one candidate left, or all candidates that remain get exactly the same number of votes as preferred candidates. Then design a program election.py that defines a class

Election, with objects of this class created from Excel files of the kind provided as examples, to which the methods:one round winners(),two round winners(),elimination winner(),de borda winners(), andde\_condorcet\_winners()can be applied. Also, the \_\_str\_\_() method is implemented so as to display in textual form the election results recorded in the Excel file.Below is a possible interaction:\$ python3 ... >>> from election import \* >>> election = Election('election\_1.xlsx') >>> print(election) Number of votes Albert Emily Oscar Maria Max 3273 1 5 4 2 3 2182 5 1 4 3 2 1818 5 2 1 4 3 1636 5 4 2 1 3 727 5 2 4 3 1 364 5 4 2 3 1 >>> election.one round winners() The winner is Albert. >>> election.two round winners() The winner is Emily. >>> election.elimination winners() The winner is Oscar. >>> election.de borda winners() The winner is Maria. >>> election.de condorcet winners() The winner is Max. >>> election = Election('election 2.xlsx') >>> print(election) Number of votes Albert Emily Oscar Maria Max 1000 1 2 3 4 5 >>> election.one\_round\_winners() The winner is Albert. >>> election.two\_round\_winners() The winner is Albert. >>> election.elimination\_winners() The winner is Max. >>> election.de\_borda\_winners() The winner is Albert. >>> election.de condorcet winners() The winner is Albert. >>> election = Election('election\_3.xlsx') >>> print(election) Number of votes Albert 1000 1 1000 1 1000 1 1000 1 1000 1 1000 1 >>> election.one\_round\_winners() All candidates are winners. >>> election.two\_round\_winners() All candidates are winners. >>> election.elimination\_winners() All candidates are winners. >>> election.de borda winners() All candidates are winners. >>> election.de condorcet winners() All candidates are winners. >>> election = Election('election 4.xlsx') >>> print(election) Number of votes Albert Emily Oscar 1000 1 2 3 1000 2 1 3 >>> election.one round winners() The winners is Albert and Emily. >>> election.two round winners() The winners is Albert and Emily. >>> election.elimination winners() The winner is Oscar. >>> election.de borda winners() The winners is Albert and Emily. >>> election.de\_condorcet\_winners() The winners is Albert and Emily. >>> election = Election('election\_5.xlsx') >>> print(election) Number of votes Albert Emily Oscar Maria 1000 1 2 3 4 1000 2 3 1 4 1000 3 1 2 4 >>> election.one round winners() The winners are Albert, Emily and Oscar. >>> election.two\_round\_winners() The winners are Albert, Emily and Oscar. >>> election.elimination\_winners() The winner is Maria. >>> election.de\_borda\_winners() The winners are Albert, Emily and Oscar. >>> election.de condorcet winners() There is no winner. >>> election = Election('election 6.xlsx') >>> print(election) Number of votes Albert Emily Oscar 1000 1 2 3 1000 2 1 3 250 2 3 1 250 3 2 1 >>> election.one\_r...

#### **Exercise 5: Context free grammars**

A context free grammar is a set of production rules of the form:\symbol\_0\\$ --> \symbol\_1\\$ ...  $symbol_n$ where  $symbol_0$ , . . . ,  $symbol_n$  are either terminal or nonterminal symbols, with \$symbol\_0\$ being necessarily nonterminal. A symbol is a nonterminal symbol iff it is denoted by a word built from underscores or uppercase letters. A special nonterminal symbol is called the start symbol. The language generated by the grammar is the set of sequences of terminal symbols obtained by replacing a nonterminal symbol by the sequence on the right hand side of a rule having that nonterminal symbol on the left hand side, starting with the start symbol. For instance, the following, where EXPRESSION is the start symbol, is a context free grammar for a set of arithmetic expressions: EXPRESSION --> EXPRESSION TERM\_OPERATOR TERMEXPRESSION --> TERMTERM --> TERM FACTOR OPERATOR FACTORTERM --> FACTORFACTOR --> NUMBERFACTOR --> (EXPRESSION)NUMBER --> DIGIT NUMBER | DIGITDIGIT --> 0...DIGIT --> 9TERM\_OPERATOR --> +TERM\_OPERATOR --> -FACTOR\_OPERATOR --> \*ACTOR\_OPERATOR --> /Moreover, blank characters (spaces or tabs) can be inserted anywhere except inside a number. For instance, (2 + 3) \* (10 -2) - 12 \* (1000 + 15) is an arithmetic expression generated by the grammar. Note that operators associate to the left. The grammar is unambiguous, in the sense that every expression generated by the grammar has a unique evaluation. Write down a program context\_free\_grammar.py that implements a function evaluate() which takes a string representing an expression as an argument, checks whether the expression can be generated by the grammar, and in case the answer is yes, returns the value of the expression, provided that no division by 0 is attempted; otherwise, the function returns None.Below is a possible interaction:\$ python3 ... >>> from context\_free\_grammar import \* >>> evaluate('100') 100 >>> evaluate('(100)') 100 >>> evaluate('1 - 20 + 300') 281 >>> evaluate('(((((1))-((20))+((300)))))') 281 >>> evaluate('20 \* 4 / 5') 16.0 >>> evaluate('(((((20))\*((4))/((5)))))') 16.0 >>> evaluate('1 + 20 \* 30 - 400 / 500') 600.2 >>> evaluate('1 + (20\*30-400) / 500') 1.4 >>> evaluate('1+(20 / 30 \* 400)- 500') -232.33333333333337 >>> evaluate('1 + 2 \* (3+4\*5) / (6\*7-8/9)') 2.1189189189189186 >>> evaluate('100)') >>> evaluate('100 + ') >>> evaluate('100 + -3') >>> evaluate('100 ÷ 50') >>> evaluate('100 / 0') Before you tackle the exercise, find out about recursive descent parsers. To easily tokenise the string, check out the findall() function from the re module. See also related content Week 10 - Notes 15 Context Free Grammars discussed in Week 10 Tuesday Lecture.