

Lesson 1: Week 5

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Exercise 1: Fibonacci maker

Recall the Fibonacci numbers from practice exercise Week 3 Exercise 3: Fibonacci lister: 0, 1, 1, 2, 3, 5, 8, 13, ... Write a program that returns a requested Fibonacci number, this time using a recursive function. Examples: Which Fibonacci number would you like? 1 It is 0. Which Fibonacci number would you like? 8 It is 13. Which Fibonacci number would you like? 12 It is 89.

Exercise 2: Prime factoriser

Write a program that asks the user for a number and then factorises the number into primes. Examples: Enter a number: 345 345 = 3 x 5 x 23 Enter a number: 612 612 = 2 x 2 x 3 x 3 x 17 Enter a number: 127 127 = 127

Exercise 3: Longest sequence of consecutive letters

Write a program `longest_sequence.py` that prompts the user for a string `w` of lowercase letters and outputs the longest sequence of consecutive letters that occur in `w`, but with possibly other letters in between, starting as close as possible to the beginning of `w`. Insert your code into `longest_sequence.py`. If you are stuck, but only when you are stuck, then use `longest_sequence_scaffold.py`. Examples: Please input a string of lowercase letters: a The solution is: a Please input a string of lowercase letters: abcefg The solution is: efgh Please input a string of lowercase letters: abcefg The solution is: abc Please input a string of lowercase letters: ablccmdnneoffpg The solution is: abcdefg Please input a string of lowercase letters: abcdiijwkaalbmbz The solution is: ijklm Please input a string of lowercase letters: abcqqrstuvwxbcbcddeffghijklrst The solution is: abcdefghijkl

Exercise 4: A triangle of characters

Write a program `characters_triangle.py` that gets a strictly positive integer `N` as input and outputs a triangle of height `N`. For instance, when `N = 5`, the triangle looks like this: Two built-in functions are useful for this exercise: `ord()` returns the integer that encodes the character provided as argument; `chr()` returns the character encoded by the integer provided as argument. For instance: `>>> ord('A') 65 >>> chr(65) 'A'` Consecutive uppercase letters are encoded by consecutive integers. For instance: `>>> ord('A'), ord('B'), ord('C') (65, 66, 67)` Insert your code into `characters_triangle.py`. If you are stuck, but only when you are stuck, then use `characters_triangle_scaffold_1.py`.

Exercise 5: Pascal triangle

Write a program `pascal_triangle.py` that prompts the user for a number `N` and prints out the first `N + 1` lines of Pascal triangle, making sure the numbers are nicely aligned, as illustrated below for `N = 3`, `7` and `11` respectively: Insert your code into `pascal_triangle.py`. If you are stuck, but only when you are stuck, then use `pascal_triangle_scaffold_1.py`.

Exercise 6: Hasse diagrams

Let a strictly positive integer `n` be given. Let `D` be the set of divisors of `n`. Let `k` be the number of prime divisors of `n` (that is, the number of prime numbers in `D`). The members of `D` can be arranged as the vertices of a solid in a `k`-dimensional space as illustrated below for `n = 12` (in which case `D = {1, 2, 3, 4, 6, 12}` and `k = 2`) and for `n = 30` (in which case `D = {1, 2, 3, 5, 6, 10, 15, 30}` and `k = 3`). Each of the solids' vertices is associated with two collections of nodes: those "directly below" it, and those "directly above" it. In particular, the prime divisors of `n` are "directly above" 1, and no vertex is below 1; `n` has exactly `k` vertices "directly below" it, and no vertex is above `n`. This suggests considering a dictionary whose keys are the members of `D` (inserted from smallest to largest), and as value for a given key `d`, the pair of ordered lists of members of `D` "directly below" `d` and "directly above" `d`, respectively. The solids exhibit `k` distinct "edge directions", one for each prime divisor of `n`, defining a partition of the solids' edges. One can represent this partition as a dictionary whose keys are the prime divisors of `n` (inserted from smallest to largest), and as value for a given key `p`, the ordered list of ordered pairs of members of `D` that make up the endpoints of the

edges whose "direction" is associated with p . The program `hasse_diagram.py` defines a function `make_hasse_diagram()` that returns a named tuple `HasseDiagram` with three attributes: `factors`, for a dictionary whose keys are the members of D , and as value for a given key d (1 excepted), a string that represents the prime decomposition of d , using x for multiplication and $^$ for exponentiation, displaying only exponents greater than 1; `vertices`, for the first dictionary previously defined; `edges`, for the second dictionary previously defined. Replace `pass` in `hasse_diagram.py` with your code. Except for `namedtuple`, `hasse_diagram.py` imports a number of classes and functions from various modules that are used in the solution, but that other good solutions will make no use of.

Exercise 7: Encoding pairs of integers as natural numbers

Complete the program `plane_encoding.py` that implements a function `encode(a, b)` and a function `decode(n)` for the one-to-one mapping from the set of pairs of integers onto the set of natural numbers, that can be graphically described as follows: That is, starting from the point $(0, 0)$ of the plane, we move to $(1, 0)$ and then spiral counterclockwise: `encode(0,0)` returns 0 and `decode(0)` returns $(0,0)$; `encode(1,0)` returns 1 and `decode(1)` returns $(1,0)$; `encode(1,1)` returns 2 and `decode(2)` returns $(1,1)$; `encode(0,1)` returns 3 and `decode(3)` returns $(0,1)$; `encode(-1,1)` returns 4 and `decode(4)` returns $(-1,1)$; `encode(-1,0)` returns 5 and `decode(5)` returns $(-1,0)$; `encode(-1,-1)` returns 6 and `decode(6)` returns $(-1,-1)$; `encode(0,-1)` returns 7 and `decode(7)` returns $(0,-1)$; `encode(1,-1)` returns 8 and `decode(8)` returns $(1,-1)$; `encode(2,-1)` returns 9 and `decode(9)` returns $(2,-1)$. . .

Exercise 8: Decoding a multiplication

We want to decode all multiplications of the form such that the sum of all digits in all 4 columns is constant. Insert your code into `decoded_multiplication.py`. There are actually two solutions, see expected output for details on what it should be. If you are stuck, but only when you are stuck, then use `decoded_multiplication_scaffold.py`.