COMS12200 problem set #1

Within this problem slot, the idea is that you attempt to solve the set of pencil-and-paper, exam-style questions presented below; in doing so, you can (optionally) use an interactive system to anonymously register your solutions. More concretely, optionally start by installing the Socrative client, e.g.,

• for Chrome

http://chrome.google.com/webstore/detail/socrative-student/nblhpecglllndfihipmpdoikimcmgkha

• for Android

http://play.google.com/store/apps/details?id=com.socrative.student

• for iOS

http://itunes.apple.com/gb/app/socrative-student/id477618130

or using the web-based application at

http://www.socrative.com,

then entering the 9-character "room name" which should be displayed top-center on the projector screen. Then, we will alternate as follows:

- 1. solve the current question, and optionally register your solution using Socrative,
- 2. wait until everyone is finished (or say ~ 5 minutes elapse), at which point we will discuss the questions and solutions using any collated Socrative results as a starting point.

Q1. From the following list

- A: $(x \wedge y) \oplus z$
- B: $(\neg x \lor y) \oplus z$
- C: $(x \lor \neg y) \oplus z$
- D: $\neg(x \lor y) \oplus z$
- E: $\neg \neg (x \lor y) \oplus z$

identify **each** Boolean expression that evaluates to 1 given the assignment x = 0, y = 0 and z = 1.

Q2. One of the following equivalences

- A: $(x \wedge y) \wedge z \equiv x \wedge (y \wedge z)$
- B: $x \lor 1 \equiv x$
- C: $x \lor \neg x \equiv 1$
- D: $\neg(x \lor y) \equiv \neg x \land \neg y$
- E: $\neg \neg x \equiv x$

is incorrect: identify which.

Q3. The Boolean expression

$$(x \lor (z \lor y)) \land \neg(\neg y \land \neg z)$$

is equivalent to which of the following alternatives?

- A: $y \lor z$
- B: $((x \lor z) \lor y)) \land (x \lor z)$
- C: $(x \wedge y) \vee (x \wedge z)$
- D: $(x \lor y) \land \neg(x \lor z)$
- E: $(x \wedge z) \vee (x \wedge y)$

Q4. The Boolean expression

$$(x \lor y) \lor (x \land z)$$

is equivalent to which of the following alternatives?

- A: $(x \lor y) \land (x \lor z)$
- B: $(x \lor y) \land z$
- C: $(x \lor y) \land (x \land z)$
- D: $x \vee y$
- E: $(x \wedge y) \vee x$
- **Q5.** A given set of Boolean operators may be termed functionally complete (or universal): this means *any* Boolean function can be expressed using a Boolean expression involving elements of the set alone. For example, because we know the NAND operator is functionally complete, we can also term the sets $\{ \overline{\land} \}$ and $\{ \land, \neg \}$ functionally complete. Noting that \neq and \Rightarrow denote the inverse of equivalence and implication respectively (i.e., not equivalent, and does not imply), which of the following sets
 - A: $\{\oplus, \vee\}$
 - B: {⇒, ≢}
 - C: {⇒, ⇒}
 - D: all of the above
 - E: none of the above

is/are functionally complete?

- **Q6.** How many *n*-input, 1-output Boolean functions are there?
 - A: 1
 - B: *n*
 - C: 2^n
 - D: 2^{2^n}
 - E: $2^{2^{2^n}}$