Notes on NEWUOA

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June 7, 2021 7pm

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Algorithm 0.1

Input $\Delta_0 \in (0, +\infty)$, $m \in \{n+2, n+3, \ldots, (n+1)(n+2)/2\}$, and $\mathcal{X}_0 \subset \mathbb{R}^n$ with $x_0 \in \mathcal{X}_0$ and $|\mathcal{X}_0| = m$. Set $Q_{-1} = 0$ and $k = 0$.

1. $Q_k = \operatorname{argmin}\{\|\nabla^2 Q - \nabla^2 Q_{k-1}\|_{\mathrm{F}} : Q \in \mathcal{Q} \text{ and } Q(x) = f(x) \text{ for } x \in \mathcal{X}_k\}$.
2. $x_k = \operatorname{argmin}\{f(x) : x \in \mathcal{X}_k\}$, $x_k^+ = \operatorname{argmin}\{Q_k(x) : \|x - x_k\| \le \Delta_k\}$.
3. $\rho_k = [f(x_k) - f(x_k^+)]/[Q_k(x_k) - Q_k(x_k^+)]$; update Δ_k according to ρ_k.
4. $x_k^- = \operatorname{argmin}\{K(\mathcal{X}_k \cup \{x_k^+\} \setminus \{x\}) : x \in \mathcal{X}_k\}$

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