

Assignment 3 - Solutions

Q1 a) A possible solution:

```
InsertionSort(arr):  
    int [] sorted-a;  
    int j ← 0;  
    int k ← arr.size-1;  
    for (int i=0; i < arr.size; i++):  
        if (arr[i] == 0)  
            sorted-a[j] ← arr[i];  
            j++;  
        else  
            sorted-a[k] ← arr[i];  
            k--;  
    return sorted-a;
```

Another possible solution:

```
InsertionSort(arr):  
    int [] sorted-a;  
    int j ← 0;  
    for (int i=0; i < arr.size; i++):  
        if (arr[i] == 0)  
            sorted-a[j] ← arr[i];  
            j++;  
        while (j < arr.size):  
            sorted-a[j] ← 1;  
            j++;  
    return sorted-a;
```

b) A possible solution:

InsertionSort(arr):

```
int [] sorted ← arr;  
int i ← 0;  
int j ← arr.size - 1;  
while (j > i):  
    if (arr[i] > arr[j])  
        swap(sorted, i, j);  
        i++;  
        j--;  
    else if (arr[j] > arr[i])  
        i++;  
        j--;  
    else if (arr[j] == 0)  
        i++;  
    else if (arr[i] == 1)  
        j--;
```

```
swap(arr, i, j):  
    int temp ← arr[i];  
    arr[i] ← arr[j];  
    arr[j] ← temp;
```

Hibroy

Q₂

We use a Stack to Traverse the tree non-recursively.
The algorithm is shown below, where T is a non-empty binary tree with n nodes

Algorithm 1, A possible solution

```
let node be the root of  $T$ ;  
let  $S$  be an initially empty Stack;  
flag  $\leftarrow$  True  
while flag do  
    if node  $\neq$  None then  
         $S.push(node)$ ;  
        node  $\leftarrow$  node.left;  
    else  
        if  $\neg (S.empty())$  then  
            node  $\leftarrow S.pop()$ ;  
            print (node.item);  
            node  $\leftarrow$  node.right;  
        else  
            flag  $\leftarrow$  False
```

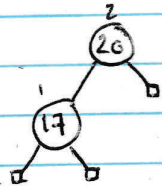
Each node of T is pushed into S once and will be eventually removed from S .

Since each statement inside the while-loop can be done in $O(1)$ the algorithm runs in $O(n)$ overall time

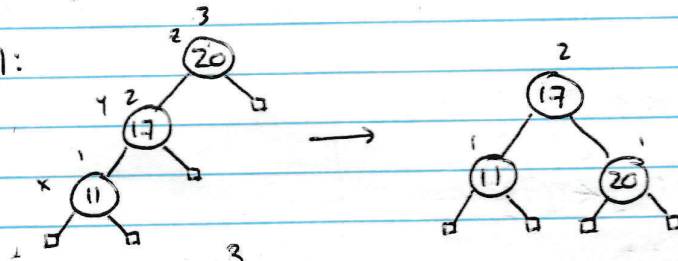
Q3a) Insert 20:



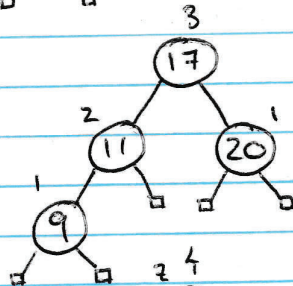
Insert 17:



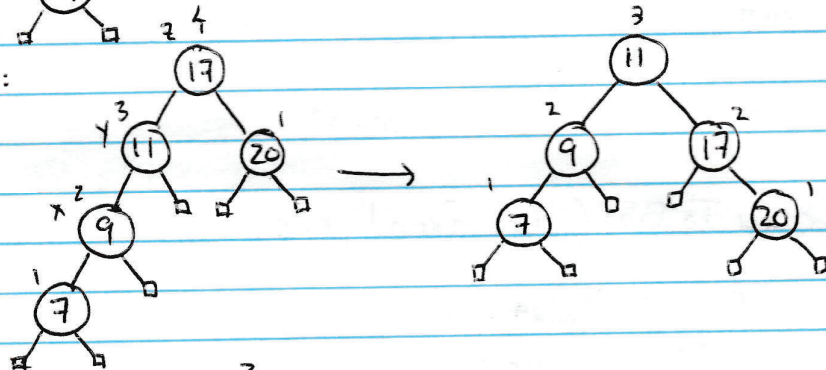
Insert 11:



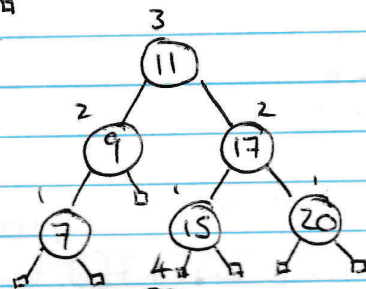
Insert 9:



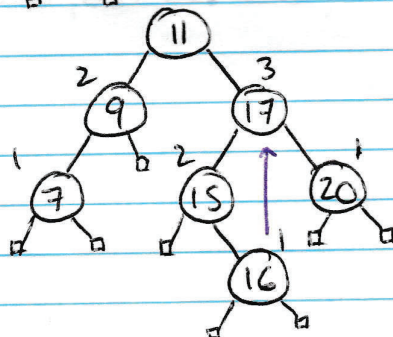
Insert 7:



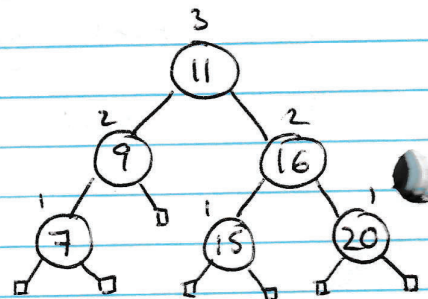
Insert 15:



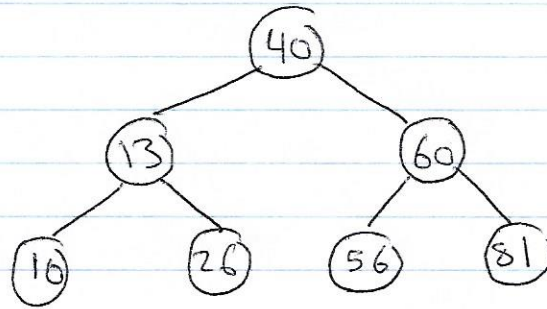
Insert 16:



b)

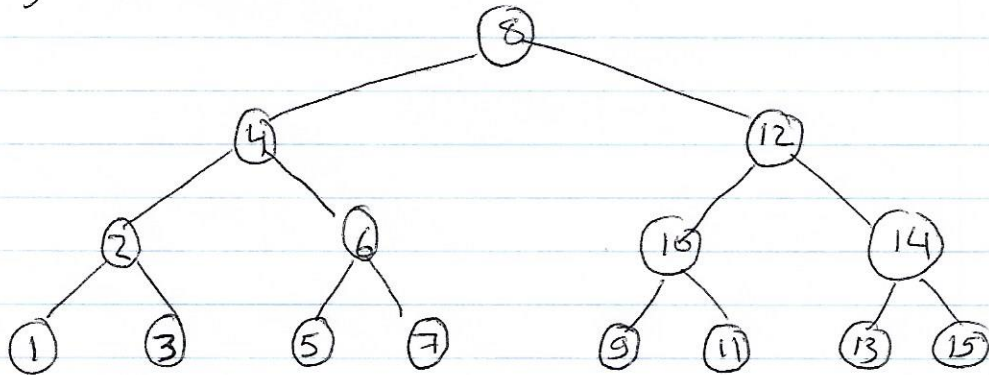


Q4

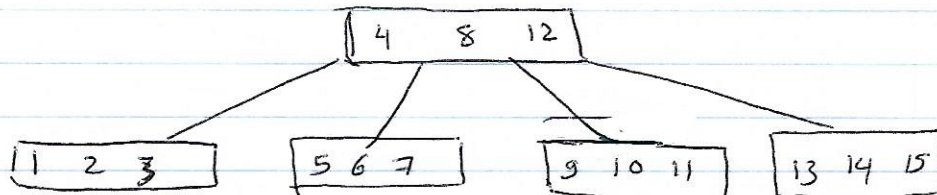


Q5

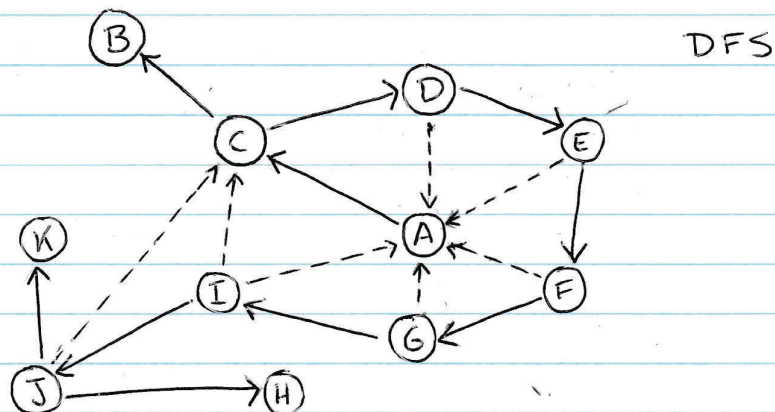
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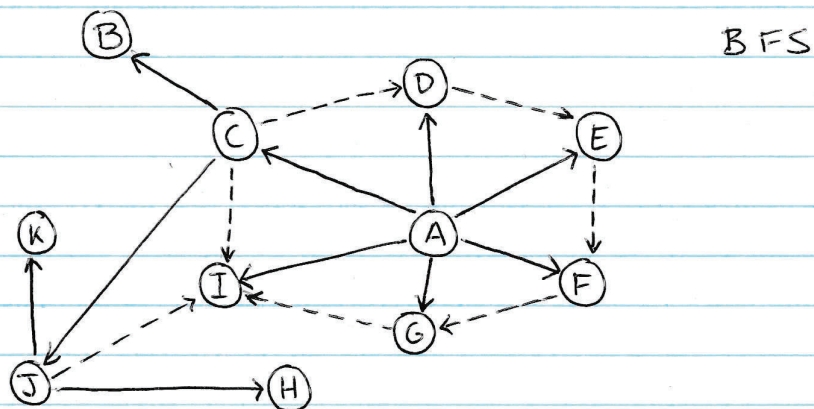
max height



Q6 b) A, C, B, D, E, F, G, I, J, H, K



a) A, C, D, E, F, G, I, B, J, H, K



c) A, G, I, D, F, E, J, C, H, K, B

