

CSI 2110 Tutorial (Section A)

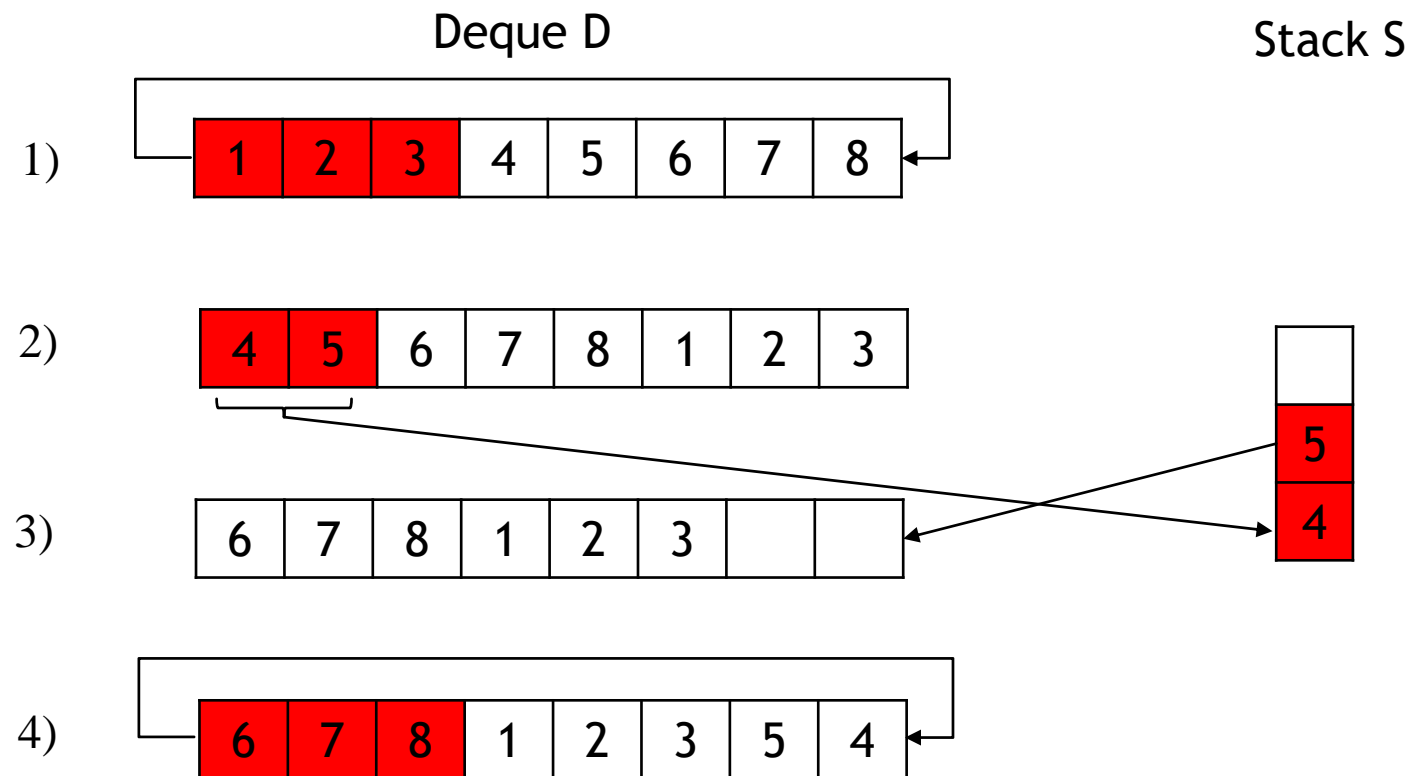
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Office hour: Fri 13:00 - 14:00

Place: STE 5000G

6.14 Suppose you have a deque D containing the numbers (1,2,3,4,5,6,7,8), in this order. Suppose further that you have an initially empty stack S. Give a code Fragment that uses only D and S (and no other variables) and results in D storing the elements in the order (1,2,3,5,4,6,7,8)



Tree: a connected graph with no cycles

Internal Node: has child

External Node: leaf

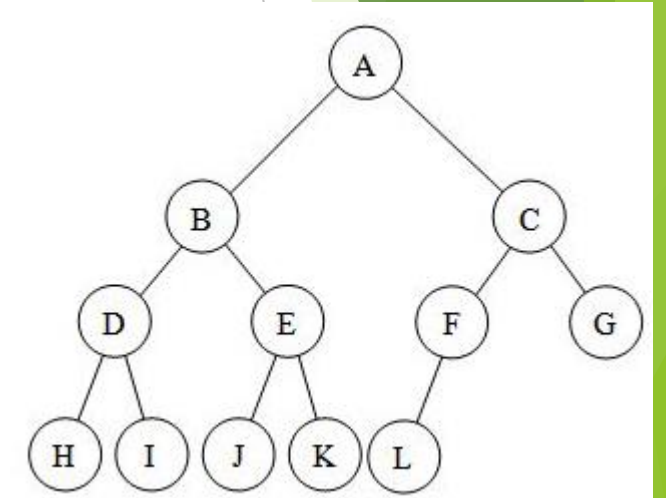
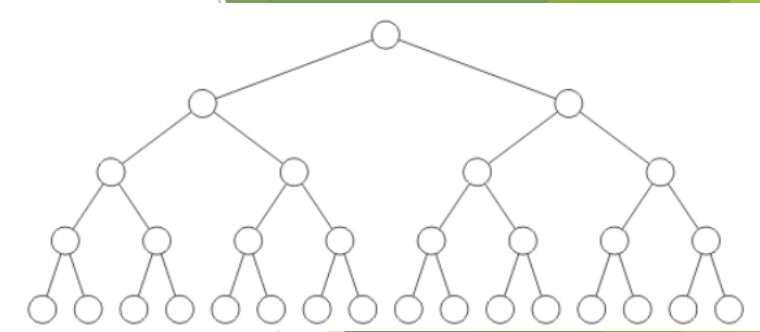
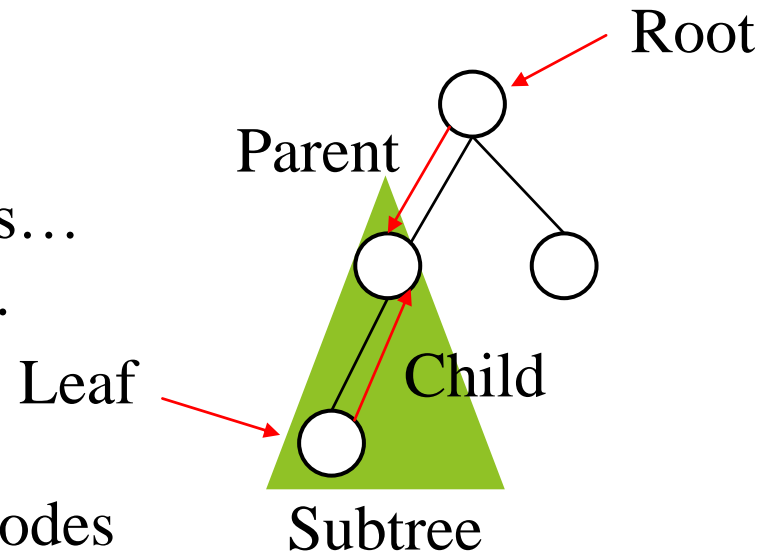
Ancestors: parents, grandparents...

Descendant: child, grandchild...

Distance: number of edges

Depth: number of ancestors

Height: maximum depth of all nodes



Binary Tree: each node has maximum two children

Full (proper) Binary Tree: each node has zero or two children

Perfect Binary Tree: all leaves are at the same depth

Complete Binary Tree: perfect binary tree + one or more leaves on the last level (left side)

Traveling in a tree

Pre-order: current \rightarrow children

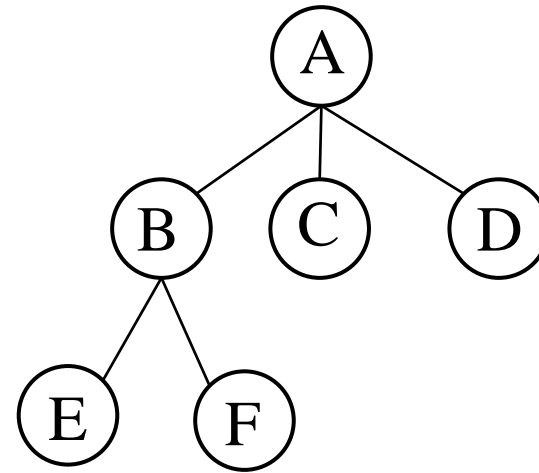
A, B, E, F, C, D

In-order: first child \rightarrow current \rightarrow other children

E, B, F, A, C, D

Post-order: children \rightarrow current

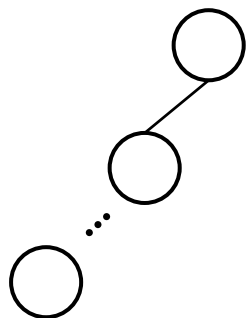
E, F, B, C, D, A



What are the minimum and maximum number of **internal** and **external** nodes in an **improper (not Full) binary tree** with n nodes?

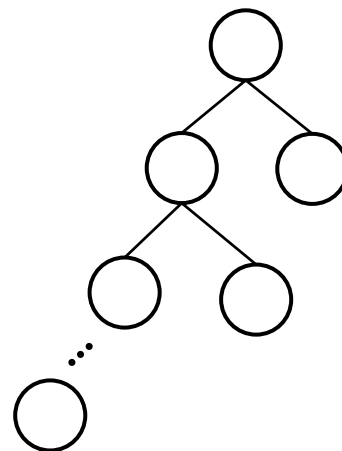
$$\text{Min: } n_e = 1$$

$$\text{Max: } n_i = n - 1$$



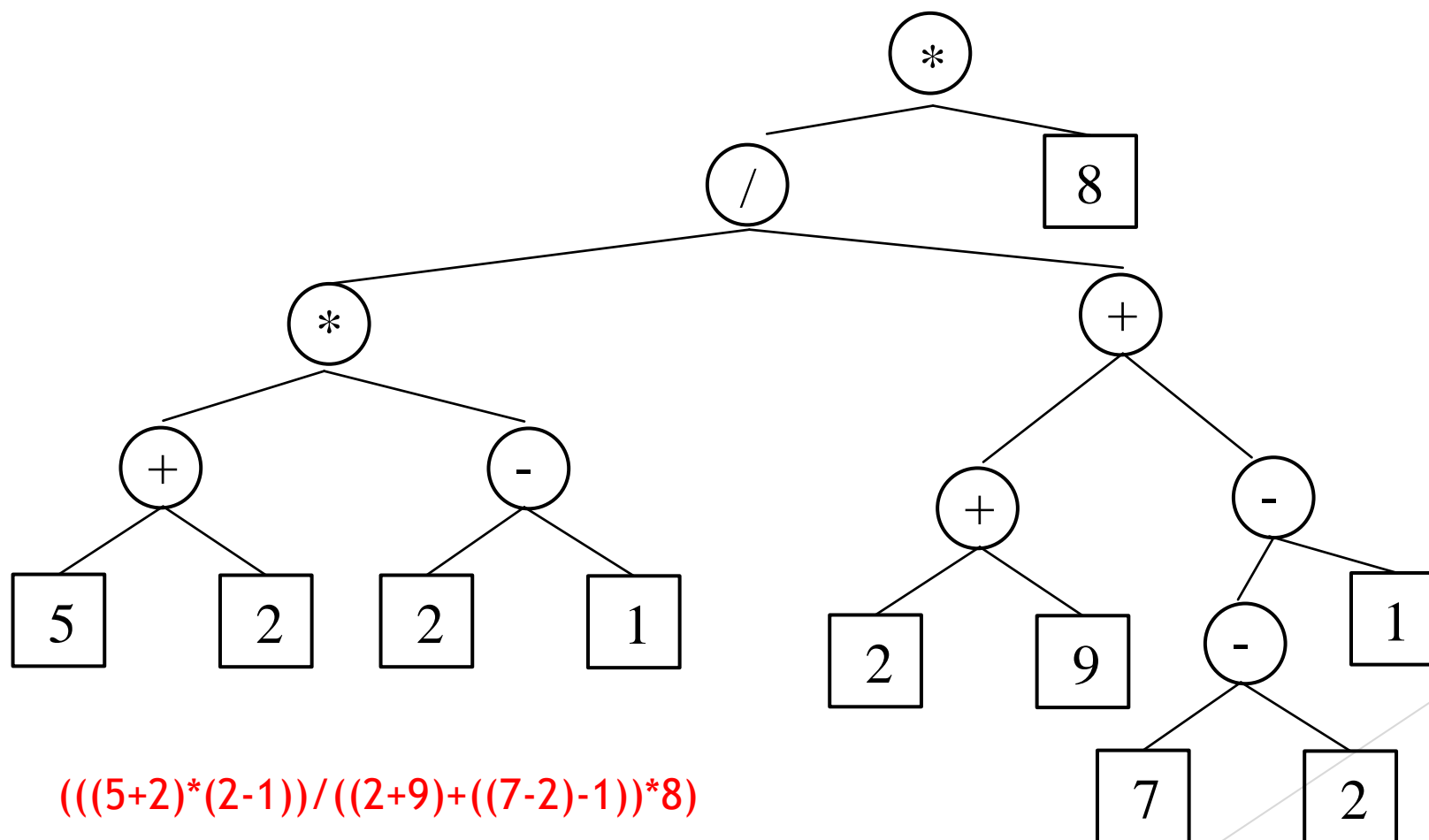
$$\text{Max: } n_e = \left\lceil \frac{n}{2} \right\rceil$$

$$\text{Min: } n_i = n - \left\lceil \frac{n}{2} \right\rceil$$

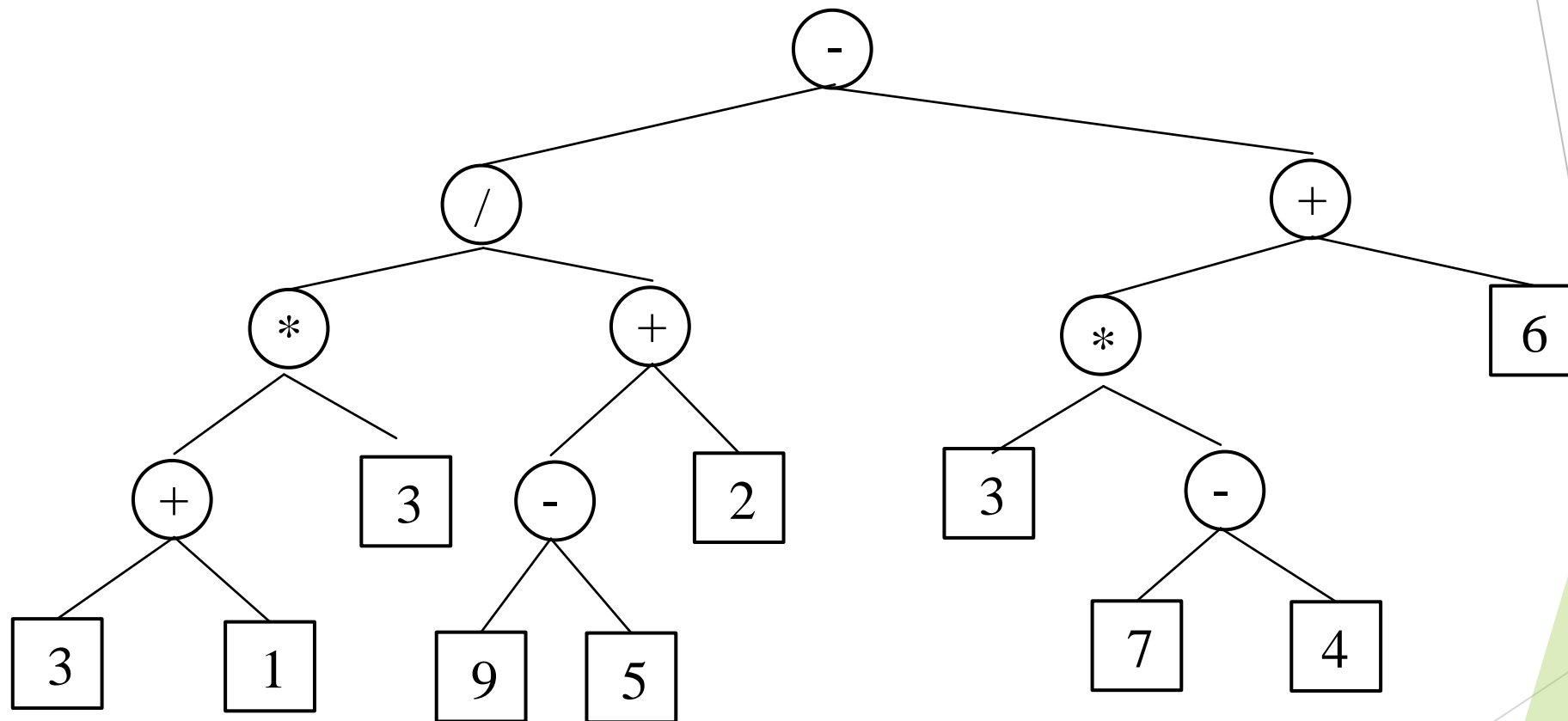


‘ $[x]$ ’ represents getting the largest integer of x

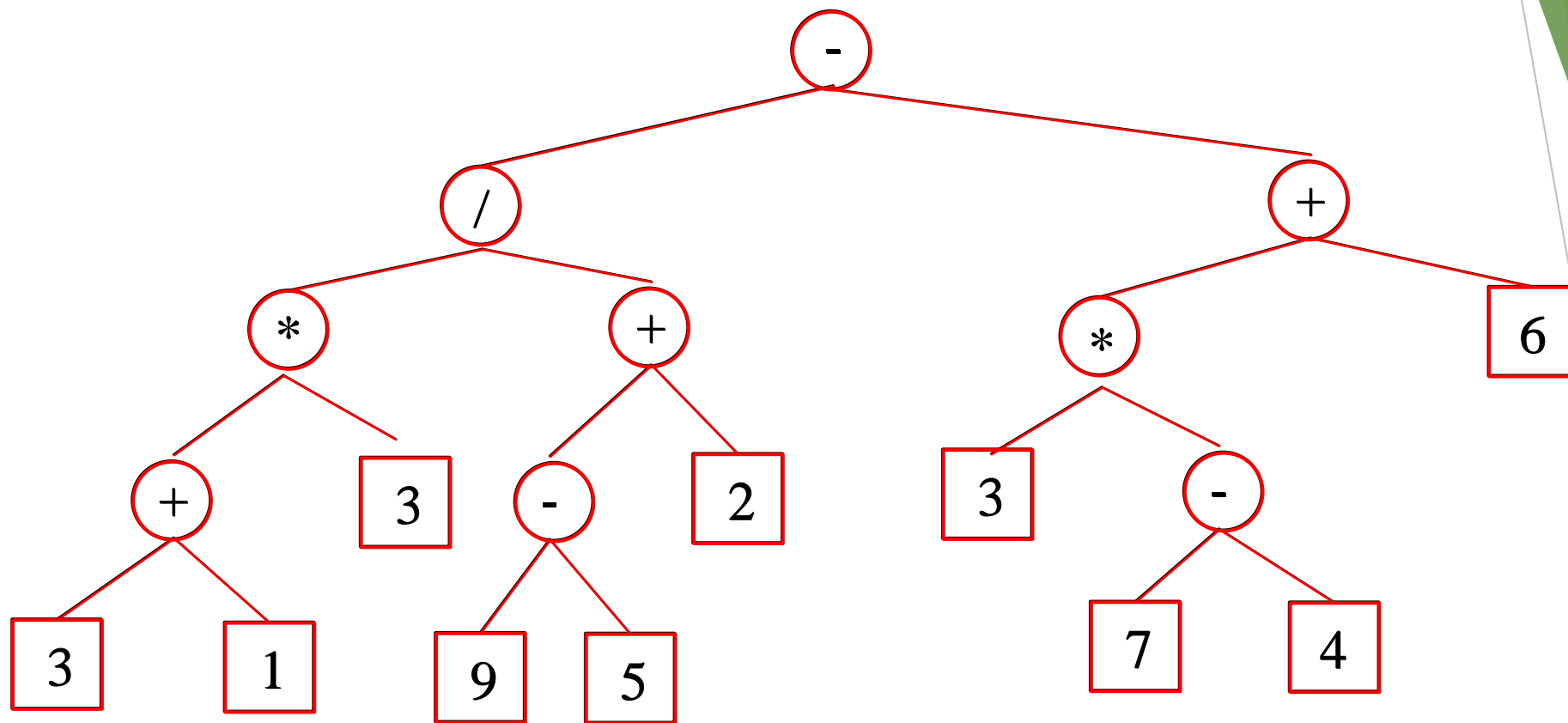
Draw the binary tree representation of the following arithmetic expression: “ $((5+2)*(2-1))/((2+9)+((7-2)-1))*8$ ”



In what order are positions visited during a **preorder** traversal of the tree below:

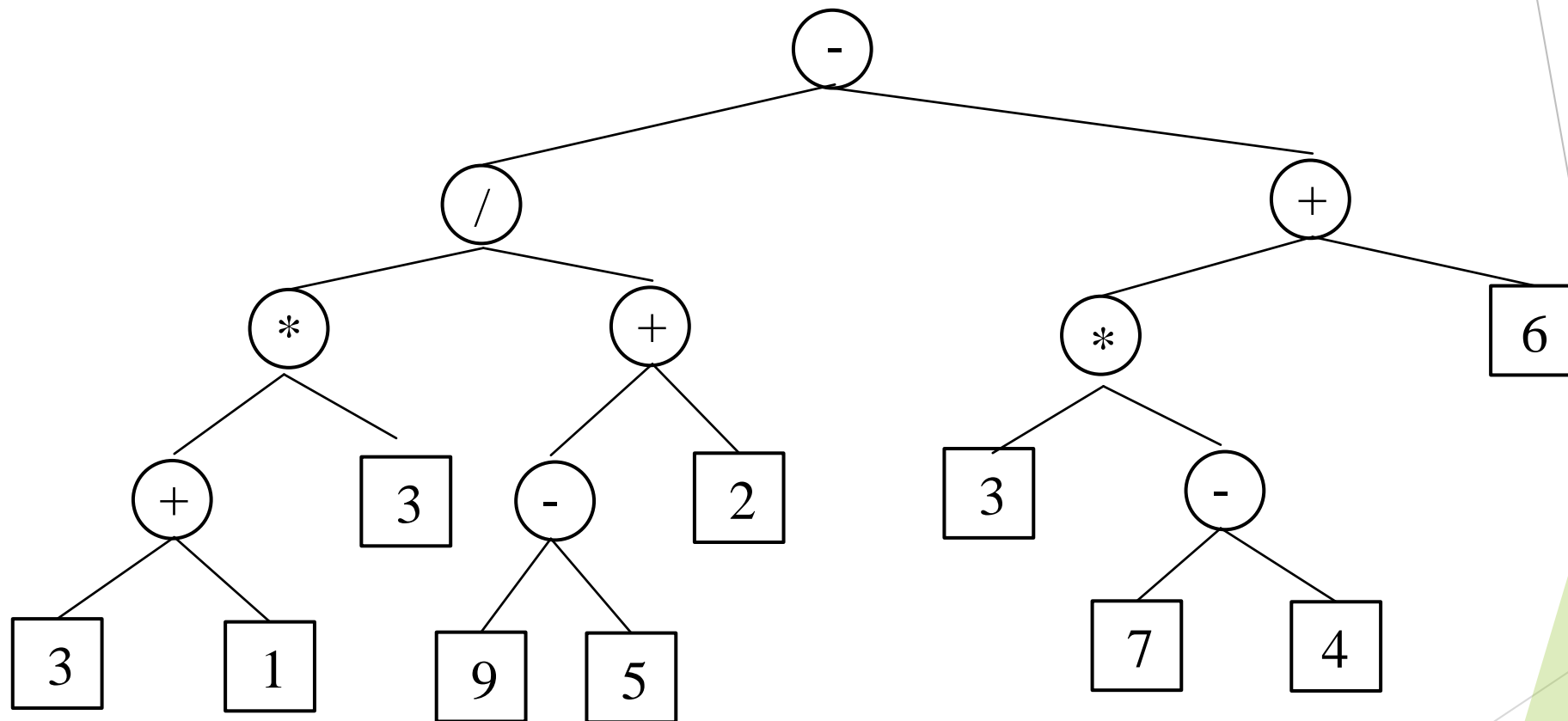


8.18:

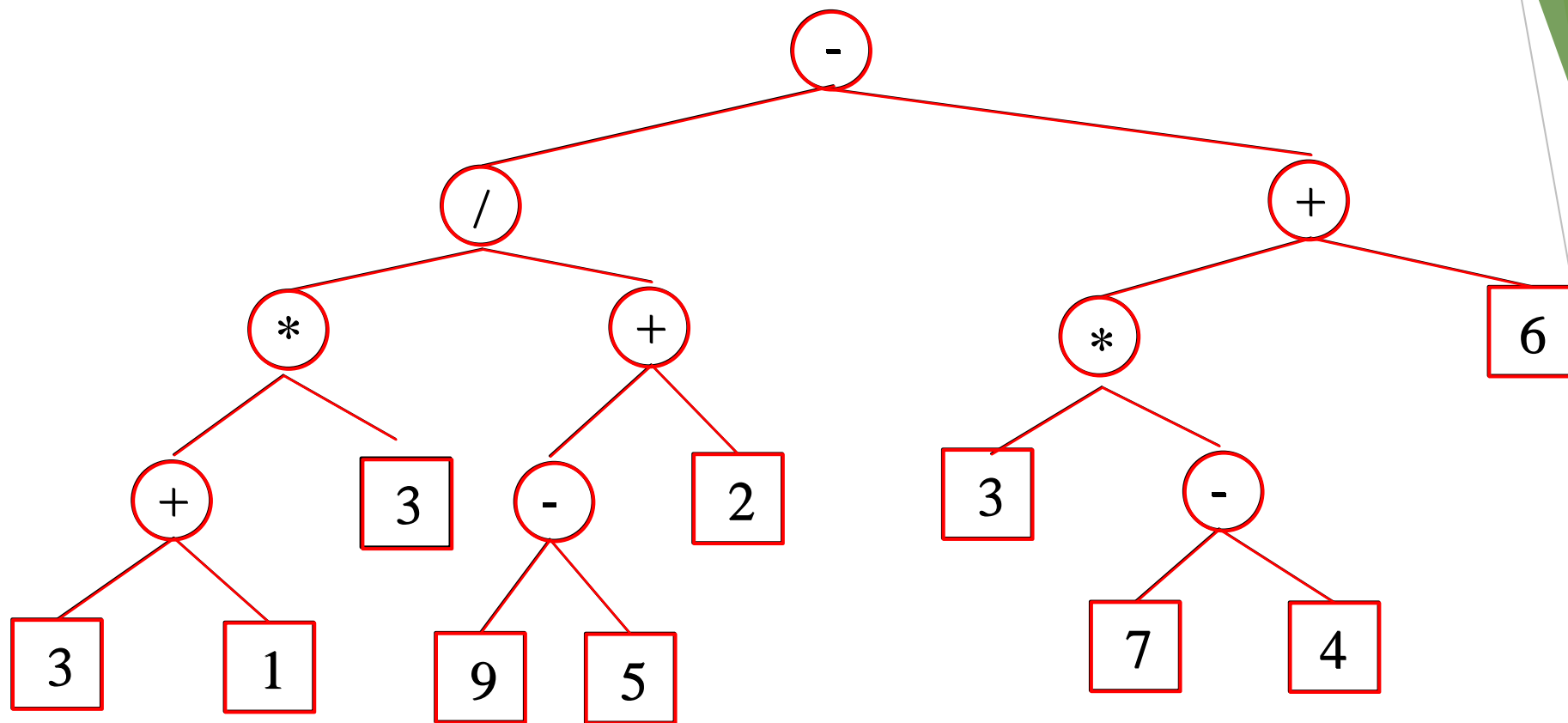


-/*+313+952+*3-746

In what order are positions visited during a **postorder** traversal of the tree below:



8.18:



$31+3*95-2+/374-*6+-$

8.22 Draw a binary tree T that

simultaneously satisfies the follows:

- 1) Each internal node of T stores a single character
- 2) A preorder traversal of yields EXAMFUN.
- 3) An inorder traversal of yields MAFXUEN.