# Tidy Time Series & Forecasting in R

4. Seasonality and trends



#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up

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#### Time series decomposition

Trend-Cycle aperiodic changes in level over time.

Seasonal (almost) periodic changes in level due to seasonal factors (e.g., the quarter of the year, the month, or day of the week).

#### **Additive decomposition**

$$y_t = S_t + T_t + R_t$$

where  $y_t$  = data at period t

 $T_t$  = trend-cycle component at period t

 $S_t$  = seasonal component at period t

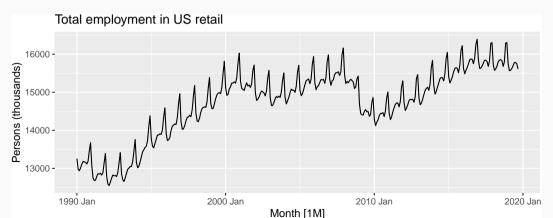
 $R_t$  = remainder component at period t

- STL: "Seasonal and Trend decomposition using Loess"
- Very versatile and robust.
- Seasonal component allowed to change over time, and rate of change controlled by user.
- Smoothness of trend-cycle also controlled by user.
- Optionally robust to outliers
- No trading day or calendar adjustments.
- Only additive.
- Take logs to get multiplicative decomposition.
- Use Box-Cox transformations to get other decompositions.

## 0 1000 C-- D-+--1 T---1-

```
us retail employment <- us employment |>
  filter(year(Month) >= 1990, Title == "Retail Trade") |>
  select(-Series_ID)
us_retail_employment
## # A tsibble: 357 x 3 [1M]
         Month Title
                             Employed
##
         <mth> <chr>
                                <dbl>
##
##
    1 1990 Jan Retail Trade
                               13256.
##
    2 1990 Feb Retail Trade
                               12966.
    3 1990 Mar Retail Trade
##
                               12938.
##
    4 1990 Apr Retail Trade
                               13012.
##
    5 1990 May Retail Trade
                               13108.
    6 1990 Jun Retail Trade
                               13183.
##
##
    7 1990 Jul Retail Trade
                               13170.
##
    8 1990 Aug Retail Trade
                               13160.
```

```
us_retail_employment |>
  autoplot(Employed) +
  labs(y="Persons (thousands)", title="Total employment in US retail")
```



```
dcmp <- us_retail_employment |>
    model(stl = STL(Employed))
dcmp

## # A mable: 1 x 1
## stl
## <model>
## 1 <STL>
```

#### components(dcmp)

##

9 stl

1990 Sep

```
## # A dable: 357 x 7 [1M]
            .model [1]
## # Key:
## # :
            Employed = trend + season_year + remainder
     .model
              Month Employed trend season_year remainder season_adjust
##
##
   <chr>
              <mth>
                       <dbl> <dbl>
                                        <dbl>
                                                  <dbl>
                                                               <dbl>
##
   1 stl
           1990 Jan 13256. 13288.
                                       -33.0
                                                  0.836
                                                              13289.
##
   2 stl
           1990 Feb
                     12966, 13269, -258,
                                                -44.6
                                                              13224.
##
   3 stl
           1990 Mar 12938, 13250, -290,
                                                -22.1
                                                              13228.
##
   4 stl
           1990 Apr
                     13012. 13231. -220. 1.05
                                                              13232.
   5 stl
##
            1990 Mav
                      13108. 13211.
                                      -114.
                                                11.3
                                                              13223.
   6 stl
                                       -24.3
                                                 15.5
##
            1990 Jun
                      13183. 13192.
                                                              13207.
   7 stl
           1990 Jul
                      13170. 13172.
                                       -23.2
                                                 21.6
##
                                                              13193.
##
   8 stl
            1990 Aug
                      13160. 13151.
                                       -9.52
                                                 17.8
                                                              13169.
```

-39.5

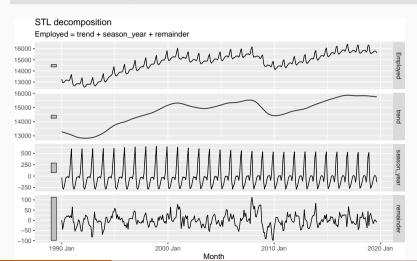
22.0

13113. 13131.

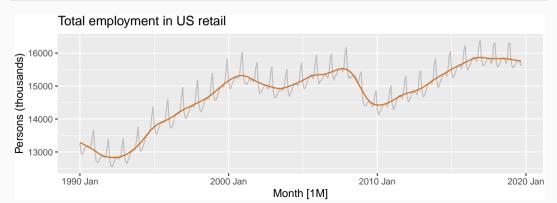
)

13153.

#### components(dcmp) |> autoplot()



```
us_retail_employment |>
autoplot(Employed, color='gray') +
autolayer(components(dcmp), trend, color='#D55E00') +
labs(y="Persons (thousands)", title="Total employment in US retail")
```





#### Seasonal adjustment

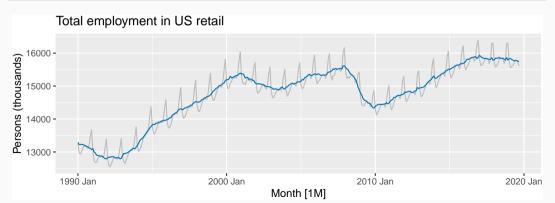
- Useful by-product of decomposition: an easy way to calculate seasonally adjusted data.
- Additive decomposition: seasonally adjusted data given by

$$y_t - S_t = T_t + R_t$$

Multiplicative decomposition: seasonally adjusted data given by

$$y_t/S_t = T_t \times R_t$$

```
us_retail_employment |>
autoplot(Employed, color='gray') +
autolayer(components(dcmp), season_adjust, color='#0072B2') +
labs(y="Persons (thousands)", title="Total employment in US retail")
```

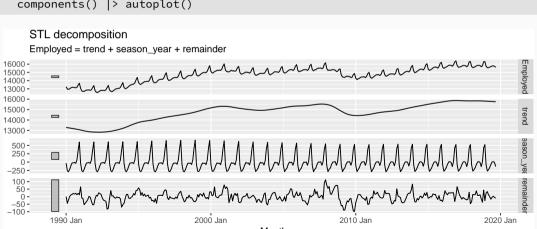


#### Seasonal adjustment

- We use estimates of S based on past values to seasonally adjust a current value.
- Seasonally adjusted series reflect remainders as well as trend. Therefore they are not "smooth" and "downturns" or "upturns" can be misleading.
- It is better to use the trend-cycle component to look for turning points.

- trend(window = ?) controls wiggliness of trend component.
- season(window = ?) controls variation on seasonal component.
- season(window = 'periodic') is equivalent to an infinite window.

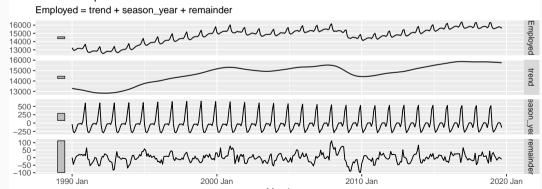
```
us_retail_employment |>
 model(STL(Employed)) |>
  components() |> autoplot()
```



STL() chooses season(window=13) by default

Can include transformations.

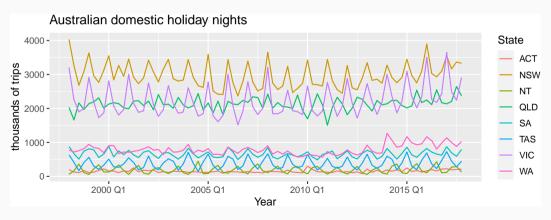
us\_retail\_employment |>
model(STL(Employed)) |>
components() |> autoplot()



- Algorithm that updates trend and seasonal components iteratively.
- Starts with  $\hat{T}_t = 0$
- Uses a mixture of loess and moving averages to successively refine the trend and seasonal estimates.
- The trend window controls loess bandwidth applied to deasonalised values.
- The season window controls loess bandwidth applied to detrended subseries.
- Robustness weights based on remainder.
- Default season window = 13
- Default trend window = nextodd(

## **Australian holidays**

```
holidays |> autoplot(Trips) +
  ylab("thousands of trips") + xlab("Year") +
  ggtitle("Australian domestic holiday nights")
```



#### **Decomposition plot**

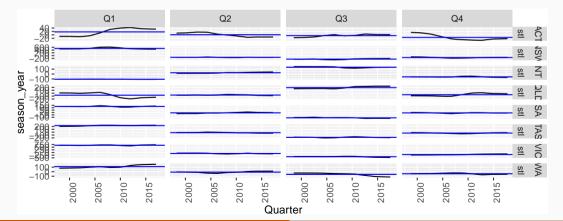
```
holidays |>
   model(stl = STL(Trips ~ season(window = 7))) |>
   components() |>
   autoplot()
     STL decomposition
     Trips = trend + season_year + remainder
4000 -
3000 -
2000 -
1000 -
0 -
                                                                                                           State/.model
                                                                                                               ACT/stl
                                                                                                               NSW/stl
3000 -
2000 -
                                                                                                               NT/stl
1000 -
   0 -
                                                                                                               QLD/stl
                                                                                                    ason_ye
 500 -
                                                                                                               SA/stI
   0 -
                                                                                                               TAS/stl
-500 -
                                                                                                    emainde
                                                                                                               VIC/stl
 200 -
   0 -
                                                                                                               WA/stl
-200 -
                                     2005 Q1
                                                           2010 Q1
                                                                                2015 Q1
                2000 Q1
                                                Quarter
```

#### **Decomposition plot**

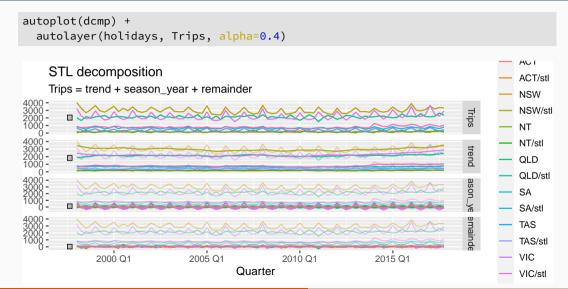
```
holidays |>
   model(stl = STL(Trips ~ season(window = "periodic"), robust = TRUE)) |>
   components() |>
   autoplot()
     STL decomposition
     Trips = trend + season_year + remainder
4000 -
3000 -
2000 -
1000 -
0 -
                                                                                                            State/.model
                                                                                                                ACT/stl
                                                                                                                NSW/stl
3000 -
2000 -
                                                                                                                NT/stl
1000 -
   ñ -
                                                                                                                QLD/stl
                                                                                                      ason_ye
                                                                                                                SA/stI
                                                                                                                TAS/stl
500 -
250 -
0 -
-250 -
-500 -
                                                                                                     emainde
                                                                                                                VIC/stl
                                                                                                                WA/stl
                                      2005 Q1
                                                                                 2015 Q1
                2000 Q1
                                                           2010 Q1
                                                 Quarter
```

#### **Decomposition subseries**

```
dcmp <- holidays |> model(stl = STL(Trips)) |>
  components()
dcmp |> gg_subseries(season_year)
```



#### **Decomposition trend**



```
holidays |>
model(stl = STL(Trips ~ trend(window=15) + season(window=13),
    robust = TRUE))
```

- trend(window = ?) controls wiggliness of trend component.
- season(window = ?) controls variation on seasonal component.
- STL() chooses season(window=13) by default
- A large seasonal window is equivalent to setting window="periodic".
- Odd numbers should be used for symmetry.

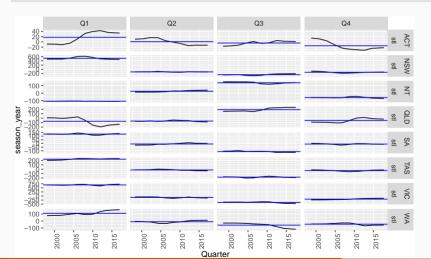
#### **Holidays decomposition**

```
dcmp <- holidays |> model(stl = STL(Trips)) |> components()
dcmp
```

```
# A dable: 640 x 8 [10]
  # Kev:
         State, .model [8]
##
##
        Trips = trend + season_year + remainder
     State .model Quarter Trips trend season_year remainder season_adjust
##
##
     <chr> <chr> <qtr> <dbl> <dbl>
                                          <dbl>
                                                    <dbl>
                                                                 <fdb>>
   1 ACT
           stl
                 1998 Q1 196. 172.
                                         -8.48
                                                   32.6
                                                                  205.
##
                                                   -40.6
##
   2 ACT
           stl
                 1998 02 127. 157. 10.3
                                                                  116.
##
   3 ACT
           stl
                 1998 03 111. 142.
                                         -16.8
                                                   -14.5
                                                                  128.
   4 ACT
           stl
                 1998 Q4 170.
                               130.
                                          14.6 25.6
                                                                  156.
##
##
   5 ACT
           stl
                 1999 Q1
                          108.
                               135.
                                         -8.63
                                                   -18.3
                                                                  116.
##
   6 ACT
           stl
                  1999 02
                          125.
                               148.
                                         11.0
                                                   -34.6
                                                                  114.
##
   7 ACT
           stl
                  1999 03
                          178.
                               166.
                                         -16.0
                                                   28.3
                                                                  194.
##
   8 ACT
           stl
                  1999 04
                          218.
                               177.
                                          13.2
                                                   27.5
                                                                  204.
##
   9 ACT
           stl
                  2000 01
                          158.
                               169.
                                          -8.75
                                                    -1.96
                                                                  167.
## 10 ACT
           c+1
                  2000 02 155 151
                                          11 7
                                                    -8 20
                                                                  143
```

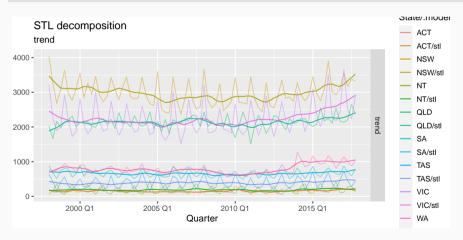
## **Holidays decomposition**

dcmp |> gg\_subseries(season\_year)



## **Holidays decomposition**

```
autoplot(dcmp, trend, scale_bars = FALSE) +
autolayer(holidays, alpha = 0.4)
```



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#### **Lab Session 8**

Produce the following decomposition

```
canadian_gas |>
  model(STL(Volume ~ season(window=7) + trend(window=11))) |>
  components() |>
  autoplot()
```

- What happens as you change the values of the two window arguments?
- How does the seasonal shape change over time? [Hint: Try plotting the seasonal component using gg\_season.]
- Can you produce a plausible seasonally adjusted series? [Hint: season\_adjust is one of the variables returned by STL.]

#### **Outline**

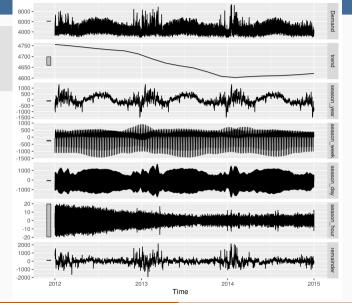
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## Multiple seasonality

```
vic_elec |>
  model(STL(Demand)) |>
  components() |>
  autoplot()
```



Demand = trend + season\_year + season\_week + season\_day + season\_hour + remainder



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#### Treasurer Joe Hockey calls for answers over Australian Bureau of Statistics jobs data

By Michael Vincent and Simon Frazer
Updated 9 Oct 2014, 12:17pm

Federal Treasurer Joe Hockey says he wants answers to the problems the Australian Bureau of Statistics (ABS) has had with unemployment figures.

Mr Hockey, who is in the US to discuss Australia's G20 agenda, said last month's unemployment figures were "extraordinary".

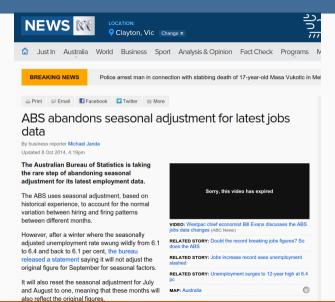
The rate was 6.1 per cent after jumping to a 12-year high of 6.4 per cent the previous month.

The ABS has now taken the rare step of abandoning seasonal adjustment for its latest employment data.



PHOTO: Joe Hockey says he is unhappy with the volatility of ABS unemployment figures. (AAP: Alan Porritt)

RELATED STORY: ABS abandons seasonal adjustment for



# ABS jobs and unemployment figures - key questions answered by an expert

A professor of statistics at Monash University explains exactly what is seasonal adjustment, why it matters and what went wrong in the July and August figures



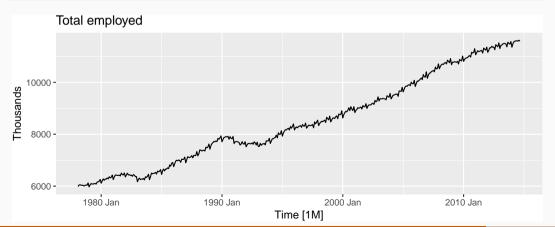
School leavers come on to the jobs market at the same time, causing a seasonal fluctuation. Photograph: Brian Snyder/Reuters

The Australian Bureau of Statistics has retracted its seasonally adjusted employment data for July and August, which recorded huge swings in the jobless rate. The ABS is also planning to review the methods it uses for seasonal adjustment to ensure its figures are as accurate as possible. Rob Hyndman, a professor of statistics at Monash University and member of the bureau's methodology advisory board. answers our questions:

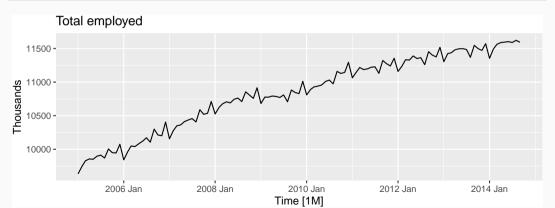
#### employed

```
# A tsibble: 440 x 4 [1M]
##
         Time Month Year Employed
        <mth> <ord> <dbl>
                             <dbl>
##
##
   1 1978 Feb Feb 1978
                             5986.
##
   2 1978 Mar Mar 1978
                             6041.
##
   3 1978 Apr Apr 1978
                             6054.
   4 1978 May May 1978
                             6038.
##
   5 1978 Jun Jun 1978
##
                             6031.
##
   6 1978 Jul Jul 1978
                             6036.
##
   7 1978 Aug Aug 1978
                             6005.
                     1978
##
   8 1978 Sep Sep
                             6024.
   9 1978 Oct Oct
                     1978
                             6046.
##
  10 1978 Nov Nov
                  1978
                             6034.
  # ... with 430 more rows
```

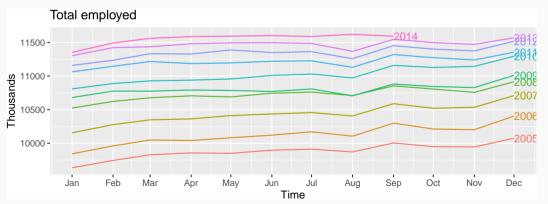
```
employed |>
  autoplot(Employed) +
  labs(title = "Total employed", y = "Thousands")
```



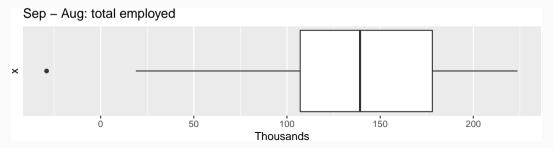
```
employed |>
  filter(Year >= 2005) |>
  autoplot(Employed) +
  labs(title = "Total employed", y = "Thousands")
```



```
employed |>
  filter(Year >= 2005) |>
  gg_season(Employed, labels = "right") +
  labs(title = "Total employed", y = "Thousands")
```

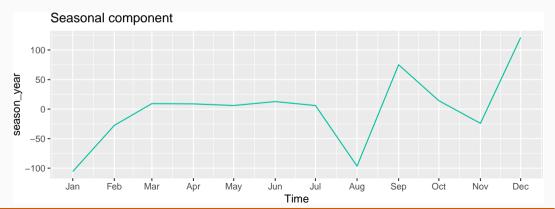


```
employed |>
  mutate(diff = difference(Employed)) |>
  filter(Month == "Sep") |>
  ggplot(aes(y = diff, x = 1)) +
  geom_boxplot() + coord_flip() +
  labs(title = "Sep - Aug: total employed", y = "Thousands") +
  scale_x_continuous(breaks = NULL, labels = NULL)
```

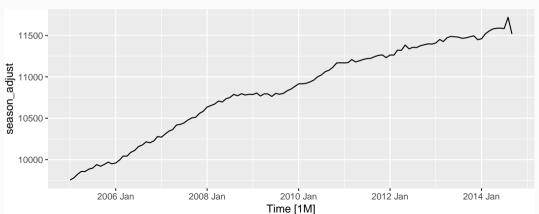


```
dcmp <- employed |>
  filter(Year >= 2005) |>
  model(stl = STL(Employed ~ season(window = 11), robust = TRUE))
components(dcmp) |> autoplot()
    STL decomposition
     Employed = trend + season_year + remainder
                                                                                        mploye
                                                                                        trend
                              2008 Jan
                                              2010 Jan
                                                             2012 Jan
                                            Time
```

```
components(dcmp) |>
  filter(year(Time) == 2013) |>
  gg_season(season_year) +
  labs(title = "Seasonal component") + guides(colour = "none")
```



```
components(dcmp) |>
  as_tsibble() |>
  autoplot(season_adjust)
```



- August 2014 employment numbers higher than expected.
- Supplementary survey usually conducted in August for employed people.
- Most likely, some employed people were claiming to be unemployed in August to avoid supplementary questions.
- Supplementary survey not run in 2014, so no motivation to lie about employment.
- In previous years, seasonal adjustment fixed the problem.
- The ABS has now adopted a new method to avoid the bias.