Time Series Analysis & Forecasting Using R

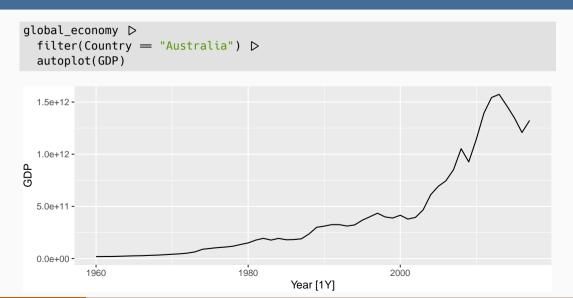
3. Transformations



- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

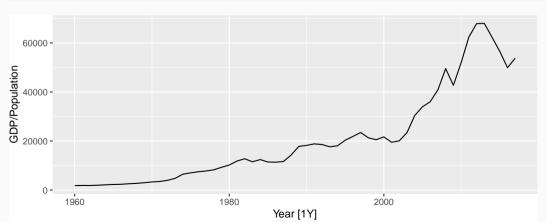
- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

Per capita adjustments



Per capita adjustments

```
global_economy ▷
  filter(Country = "Australia") ▷
  autoplot(GDP / Population)
```



- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

Lab Session 6

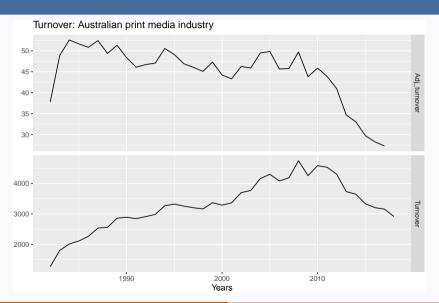
Consider the GDP information in global_economy. Plot the GDP per capita for each country over time. Which country has the highest GDP per capita? How has this changed over time?

- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

Inflation adjustments

```
print retail <- aus retail ▷
 filter(Industry = "Newspaper and book retailing") ▷
 group by(Industry) ▷
 index by(Year = year(Month)) ▷
  summarise(Turnover = sum(Turnover))
aus economy <- filter(global economy, Code = "AUS")
print retail ▷
 left join(aus economy, by = "Year") ▷
 mutate(Adj turnover = Turnover / CPI) ▷
 pivot longer(c(Turnover, Adj turnover),
   names to = "Type", values to = "Turnover"
  ) >
 ggplot(aes(x = Year, y = Turnover)) +
 geom line() +
 facet_grid(vars(Type), scales = "free_y") +
  labs(x = "Years", y = NULL,
      title = "Turnover: Australian print media industry")
```

Inflation adjustments



- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

If the data show different variation at different levels of the series, then a transformation can be useful.

If the data show different variation at different levels of the series, then a transformation can be useful.

Denote original observations as y_1, \ldots, y_n and transformed observations as w_1, \ldots, w_n .

If the data show different variation at different levels of the series, then a transformation can be useful.

Denote original observations as y_1, \ldots, y_n and transformed observations as w_1, \ldots, w_n .

Mathematical transformations for stabilizing variation

Square root
$$w_t = \sqrt{y_t}$$

Cube root
$$w_t = \sqrt[3]{y_t}$$
 Increasing

Logarithm
$$w_t = \log(y_t)$$
 strength

If the data show different variation at different levels of the series, then a transformation can be useful.

Denote original observations as y_1, \ldots, y_n and transformed observations as w_1, \ldots, w_n .

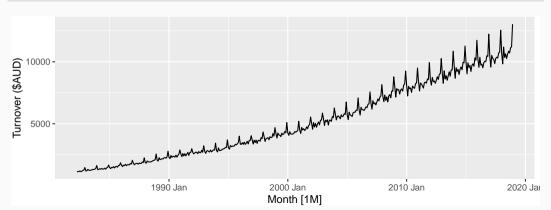
Mathematical transformations for stabilizing variation

Square root
$$w_t = \sqrt{y_t}$$
 \downarrow Cube root $w_t = \sqrt[3]{y_t}$ Increasing

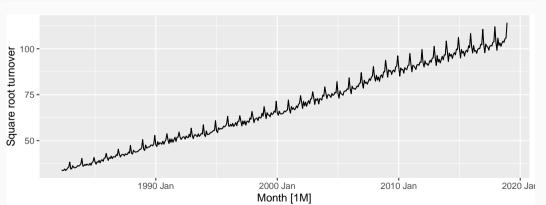
Logarithm
$$w_t = \log(y_t)$$
 strength

Logarithms, in particular, are useful because they are more interpretable: changes in a log value are **relative (percent) changes on the original**

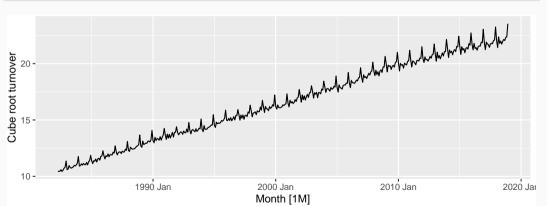
```
food <- aus_retail >
  filter(Industry = "Food retailing") >
  summarise(Turnover = sum(Turnover))
```



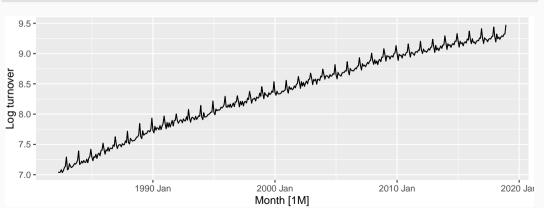
```
food ▷ autoplot(sqrt(Turnover)) +
  labs(y = "Square root turnover")
```



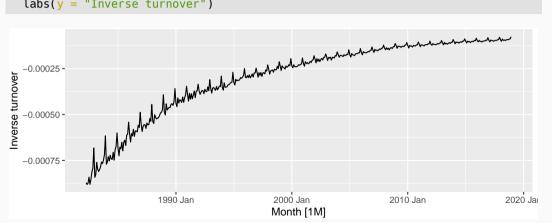
```
food ▷ autoplot(Turnover^(1 / 3)) +
  labs(y = "Cube root turnover")
```



```
food ▷ autoplot(log(Turnover)) +
  labs(y = "Log turnover")
```



```
food ▷ autoplot(-1 / Turnover) +
  labs(y = "Inverse turnover")
```



Each of these transformations is close to a member of the family of

$$w_t = \left\{ egin{array}{ll} \log(y_t), & \lambda = 0; \\ (\operatorname{sign}(y_t)|y_t|^{\lambda} - 1)/\lambda, & \lambda
eq 0. \end{array}
ight.$$

Each of these transformations is close to a member of the family of

$$w_t = \left\{ egin{array}{ll} \log(y_t), & \lambda = 0; \\ (\operatorname{sign}(y_t)|y_t|^{\lambda} - 1)/\lambda, & \lambda
eq 0. \end{array}
ight.$$

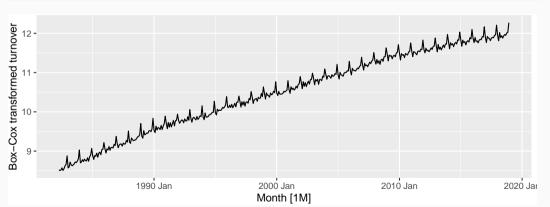
- lacktriangle Actually the Bickel-Doksum transformation (allowing for $y_t < 0$)
- $\lambda = 1$: (No substantive transformation)
- $\lambda = \frac{1}{2}$: (Square root plus linear transformation)
- $\lambda = 0$: (Natural logarithm)
- $\lambda = -1$: (Inverse plus 1)

```
food ▷
  features(Turnover, features = guerrero)
```

```
## # A tibble: 1 x 1
## lambda_guerrero
## <dbl>
## 1 0.0524
```

- This attempts to balance the seasonal fluctuations and random variation across the series.
- Always check the results.
- \blacksquare A low value of λ can give extremely large prediction intervals.

```
food ▷ autoplot(box_cox(Turnover, 0.0524)) +
  labs(y = "Box-Cox transformed turnover")
```



Transformations

- Often no transformation needed.
- Simple transformations are easier to explain and work well enough.
- Transformations can have very large effect on PI.
- If some data are zero or negative, then use $\lambda > 0$.
- log1p() can also be useful for data with zeros.
- Choosing logs is a simple way to force forecasts to be positive
- Transformations must be reversed to obtain forecasts on the original scale. (Handled automatically by fable.)

- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

Lab Session 7

- For the following series, find an appropriate transformation in order to stabilise the variance.
 - United States GDP from global_economy
 - Slaughter of Victorian "Bulls, bullocks and steers" in aus_livestock
 - Victorian Electricity Demand from vic_elec.
 - Gas production from aus_production
- Why is a Box-Cox transformation unhelpful for the canadian_gas data?