Time Series Analysis & Forecasting Using R

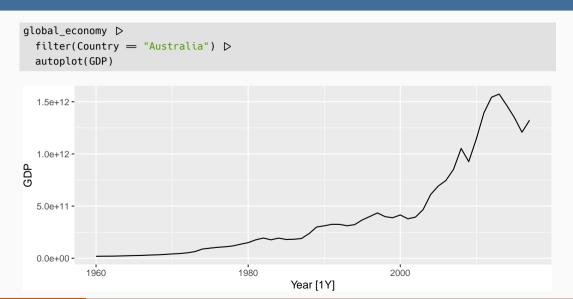
3. Transformations



- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

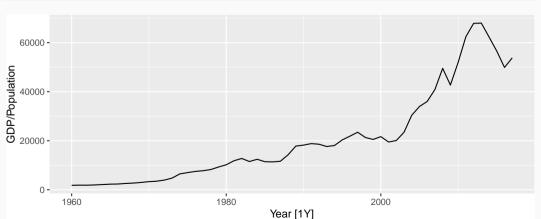
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Per capita adjustments



Per capita adjustments

```
global_economy ▷
  filter(Country = "Australia") ▷
  autoplot(GDP / Population)
```



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Lab Session 6

Consider the GDP information in global_economy. Plot the GDP per capita for each country over time. Which country has the highest GDP per capita? How has this changed over time?

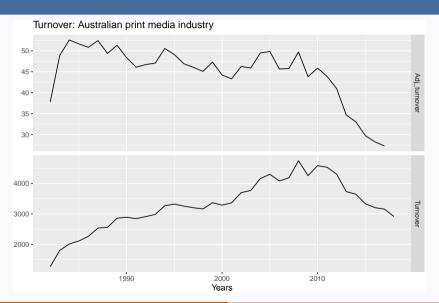
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Inflation adjustments

```
print retail <- aus retail ▷
 filter(Industry = "Newspaper and book retailing") ▷
  aroup bv(Industry) ▷
 index by(Year = year(Month)) ▷
  summarise(Turnover = sum(Turnover))
aus economy <- filter(global economy, Code = "AUS")
print retail ▷
  left_join(aus_economy, by = "Year") >
 mutate(Adj_turnover = Turnover / CPI) ▷
  pivot_longer(c(Turnover, Adj_turnover),
    names to = "Type", values to = "Turnover"
  ) >
  ggplot(aes(x = Year, y = Turnover)) +
  geom line() +
  facet_grid(vars(Type), scales = "free_y") +
  labs(x = "Years", y = NULL,
       title = "Turnover: Australian print media industry")
```

Inflation adjustments



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Mathematical transformations for stabilizing variation

Square root
$$w_t = \sqrt{y_t}$$

Cube root
$$w_t = \sqrt[3]{y_t}$$
 Increasing

Logarithm
$$w_t = \log(y_t)$$
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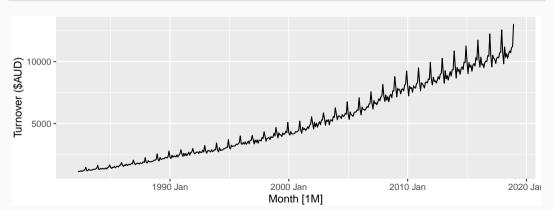
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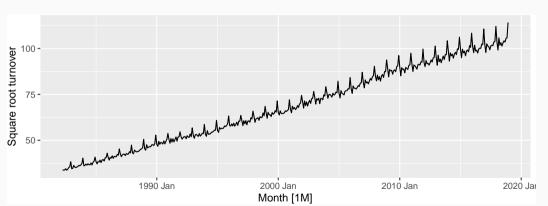
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Logarithms, in particular, are useful because they are more interpretable: changes in a log value are **relative (percent) changes on the original**

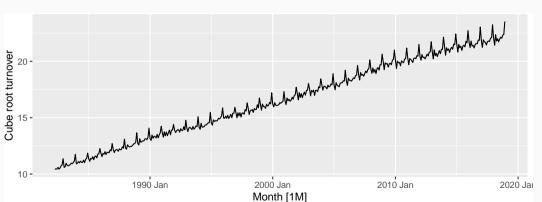
```
food <- aus_retail >
  filter(Industry = "Food retailing") >
  summarise(Turnover = sum(Turnover))
```

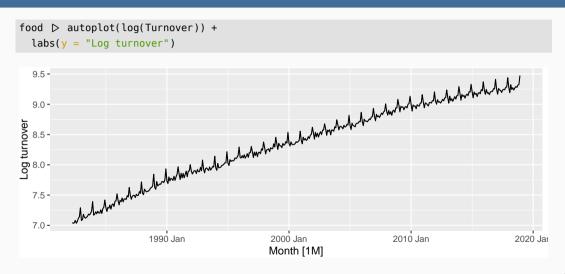


```
food ▷ autoplot(sqrt(Turnover)) +
  labs(y = "Square root turnover")
```

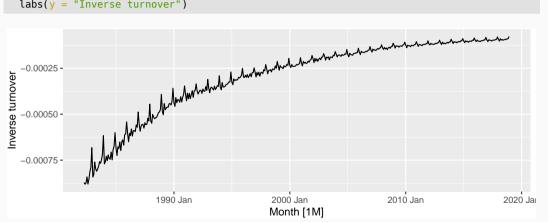


```
food ▷ autoplot(Turnover^(1 / 3)) +
  labs(y = "Cube root turnover")
```





```
food ▷ autoplot(-1 / Turnover) +
  labs(y = "Inverse turnover")
```



Each of these transformations is close to a member of the family of

Box-Cox transformations:

$$w_t = \left\{ egin{array}{ll} \log(y_t), & \lambda = 0; \\ (\operatorname{sign}(y_t)|y_t|^{\lambda} - 1)/\lambda, & \lambda
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- lacktriangle Actually the Bickel-Doksum transformation (allowing for $y_t < 0$)
- $\lambda = 1$: (No substantive transformation)
- $\lambda = \frac{1}{2}$: (Square root plus linear transformation)
- $\lambda = 0$: (Natural logarithm)
- $\lambda = -1$: (Inverse plus 1)

```
food D
  features(Turnover, features = guerrero)

### # A tibble: 1 x 1

## lambda_guerrero

### <dbl>
```

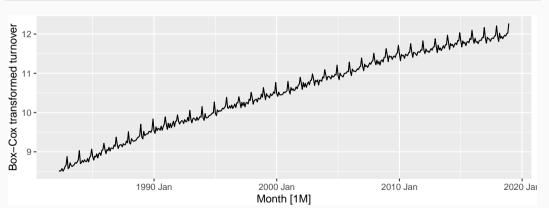
- This attempts to balance the seasonal fluctuations and random variation across the series.
- Always check the results.

0.0524

1

 \blacksquare A low value of λ can give extremely large prediction intervals.

```
food ▷ autoplot(box_cox(Turnover, 0.0524)) +
  labs(y = "Box-Cox transformed turnover")
```



Transformations

- Often no transformation needed.
- Simple transformations are easier to explain and work well enough.
- Transformations can have very large effect on PI.
- If some data are zero or negative, then use $\lambda > 0$.
- log1p() can also be useful for data with zeros.
- Choosing logs is a simple way to force forecasts to be positive
- Transformations must be reversed to obtain forecasts on the original scale. (Handled automatically by fable.)

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Lab Session 7

- For the following series, find an appropriate transformation in order to stabilise the variance.
 - United States GDP from global_economy
 - Slaughter of Victorian "Bulls, bullocks and steers" in aus_livestock
 - Victorian Electricity Demand from vic_elec.
 - Gas production from aus_production
- Why is a Box-Cox transformation unhelpful for the canadian_gas data?