

# Tidy Time Series & Forecasting in R

## 5. Time series features



# Outline

- 1 STL Features
- 2 Lab Session 9
- 3 Dimension reduction for features
- 4 Lab Session 10

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# Strength of seasonality and trend

## STL decomposition

$$y_t = T_t + S_t + R_t$$

## Seasonal strength

$$\max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(S_t + R_t)} \right)$$

## Trend strength

$$\max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(T_t + R_t)} \right)$$

# Feature extraction and statistics

```
tourism %>% features(Trips, feat_stl)
```

```
## # A tibble: 304 x 12
```

```
##   Region      State Purpose trend~1 seaso~2 seaso~3 seaso~4
##   <chr>      <chr> <chr>    <dbl>  <dbl>  <dbl>  <dbl>
## 1 Adelaide Sout~ Busine~ 0.464  0.407      3      1
## 2 Adelaide Sout~ Holiday 0.554  0.619      1      2
## 3 Adelaide Sout~ Other    0.746  0.202      2      1
## 4 Adelaide Sout~ Visiti~ 0.435  0.452      1      3
## 5 Adelaide H~ Sout~ Busine~ 0.464  0.179      3      0
## 6 Adelaide H~ Sout~ Holiday 0.528  0.296      2      1
## 7 Adelaide H~ Sout~ Other    0.593  0.404      2      2
## 8 Adelaide H~ Sout~ Visiti~ 0.488  0.254      0      3
## 9 Alice Spri~ Nort~ Busine~ 0.534  0.251      0      1
## 10 Alice Spri~ Nort~ Holiday 0.381  0.832      3      1
```

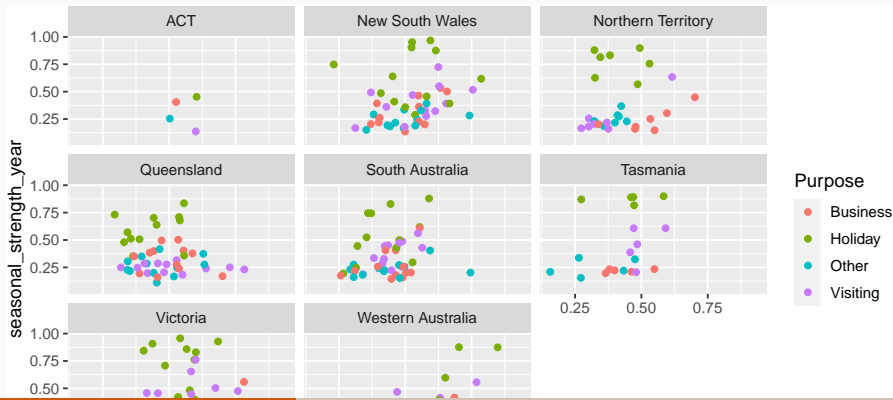
```
## # ... with 294 more rows, 5 more variables:
```

```
## #   spikiness <dbl>, linearity <dbl>, curvature <dbl>,
```

```
## #   stl_e acf1 <dbl> stl_e acf10 <dbl> and abbreviated
```

# Feature extraction and statistics

```
tourism %>%  
  features(Trips, feat_stl) %>%  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



# Feature extraction and statistics

```
tourism %>%  
  features(Trips, feat_stl) %>%  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



# Feature extraction and statistics

Find the most seasonal time series:

```
most_seasonal <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(seasonal_strength_year == max(seasonal_strength_year))
```

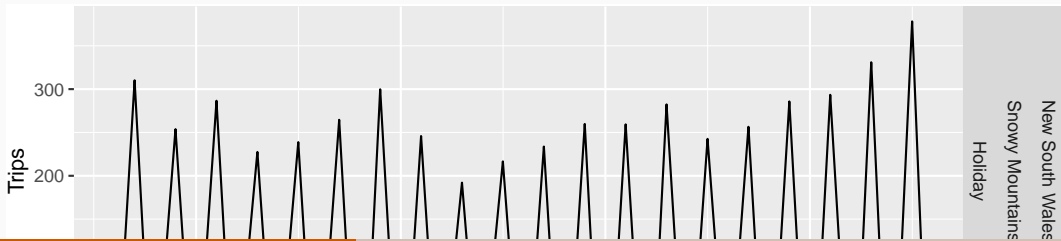


# Feature extraction and statistics

Find the most seasonal time series:

```
most_seasonal <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(seasonal_strength_year == max(seasonal_strength_year))
```

```
tourism %>%  
  right_join(most_seasonal, by = c("State", "Region", "Purpose")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(vars(State, Region, Purpose))
```



# Feature extraction and statistics

Find the most trended time series:

```
most_trended <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(trend_strength == max(trend_strength))
```

# Feature extraction and statistics

Find the most trended time series:

```
most_trended <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(trend_strength == max(trend_strength))
```

```
tourism %>%  
  right_join(most_trended, by = c("State", "Region", "Purpose")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(vars(State, Region, Purpose))
```



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## Lab Session 9

- Use `GGally::ggpairs()` to look at the relationships between the STL-based features. You might wish to change `seasonal_peak_year` and `seasonal_trough_year` to factors.
- Which is the peak quarter for holidays in each state?

# Feature extraction and statistics

```
tourism %>% features(Trips, feat_acf)
```

```
## # A tibble: 304 x 10
##   Region      State Purpose      acf1 acf10 diff1~1 diff1~2
##   <chr>      <chr> <chr>      <dbl> <dbl>   <dbl>   <dbl>
## 1 Adelaide Sout~ Busine~  0.0333  0.131  -0.520  0.463
## 2 Adelaide Sout~ Holiday 0.0456  0.372  -0.343  0.614
## 3 Adelaide Sout~ Other    0.517   1.15   -0.409  0.383
## 4 Adelaide Sout~ Visiti~  0.0684  0.294  -0.394  0.452
## 5 Adelaide Hi~ Sout~ Busine~  0.0709  0.134  -0.580  0.415
## 6 Adelaide Hi~ Sout~ Holiday 0.131   0.313  -0.536  0.500
## 7 Adelaide Hi~ Sout~ Other    0.261   0.330  -0.253  0.317
## 8 Adelaide Hi~ Sout~ Visiti~  0.139   0.117  -0.472  0.239
## 9 Alice Sprin~ Nort~ Busine~  0.217   0.367  -0.500  0.381
## 10 Alice Sprin~ Nort~ Holiday -0.00660 2.11   -0.153  2.11
## # ... with 294 more rows, 3 more variables:
## #   diff2_acf1 <dbl>, diff2_acf10 <dbl>, season_acf1 <dbl>,
## #   and abbreviated variable names 1: diff1 acf1
```

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# Feature extraction and statistics

```
tourism_features <- tourism %>%  
  features(Trips, feature_set(pkgs = "feasts"))
```

All features from  
the feasts  
package

```
## # A tibble: 304 x 51  
##   Region      State Purpose trend~1 seaso~2 seaso~3 seaso~4  
##   <chr>      <chr> <chr>    <dbl>    <dbl>    <dbl>    <dbl>  
## 1 Adelaide Sout~ Busine~ 0.464    0.407      3      1  
## 2 Adelaide Sout~ Holiday 0.554    0.619      1      2  
## 3 Adelaide Sout~ Other    0.746    0.202      2      1  
## 4 Adelaide Sout~ Visiti~ 0.435    0.452      1      3  
## 5 Adelaide H~ Sout~ Busine~ 0.464    0.179      3      0  
## 6 Adelaide H~ Sout~ Holiday 0.528    0.296      2      1  
## 7 Adelaide H~ Sout~ Other    0.593    0.404      2      2  
## 8 Adelaide H~ Sout~ Visiti~ 0.488    0.254      0      3  
## 9 Alice Spri~ Nort~ Busine~ 0.534    0.251      0      1  
## 10 Alice Spri~ Nort~ Holiday 0.381    0.832      3      1  
## # ... with 294 more rows, 44 more variables:  
## #   spikiness <dbl>, linearity <dbl>, curvature <dbl>,  
## #   stl_e_acf1 <dbl>, stl_e_acf10 <dbl>, acf1 <dbl>,  
## #   ...
```



# Feature extraction and statistics

```
pcs <- tourism_features %>%  
  select(-State, -Region, -Purpose) %>%  
  prcomp(scale = TRUE) %>%  
  broom::augment(tourism_features)
```

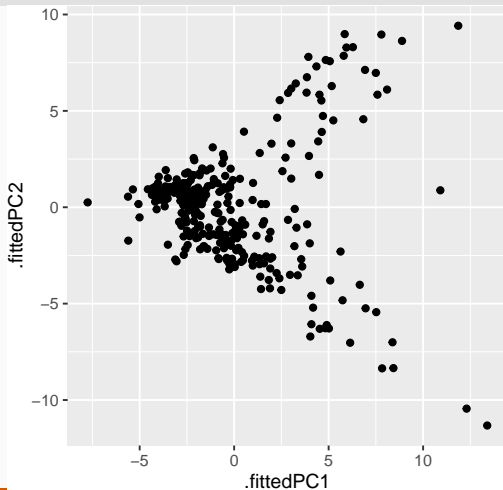
```
## # A tibble: 304 x 100  
##   .rownames Region State Purpose trend~1 season~1  
##   <chr>      <chr> <chr> <chr>    <dbl>    <dbl>  
## 1 1 Adelaide Sout~ Busine~ 0.464 0.4  
## 2 2 Adelaide Sout~ Holiday 0.554 0.6  
## 3 3 Adelaide Sout~ Other 0.746 0.202  
## 4 4 Adelaide Sout~ Visiti~ 0.435 0.452  
## 5 5 Adelaide~ Sout~ Busine~ 0.464 0.179  
## 6 6 Adelaide~ Sout~ Holiday 0.528 0.296  
## 7 7 Adelaide~ Sout~ Other 0.593 0.404  
## 8 8 Adelaide~ Sout~ Visiti~ 0.488 0.254  
## 9 9 Alice Sp~ Nort~ Busine~ 0.534 0.251  
## 10 10 Alice Sp~ Nort~ Holiday 0.381 0.832  
## # ... with 294 more rows, 93 more variables:
```

Principal  
components  
based on all  
features from the  
feasts package

# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2)) +  
  geom_point() + theme(aspect.ratio=1)
```

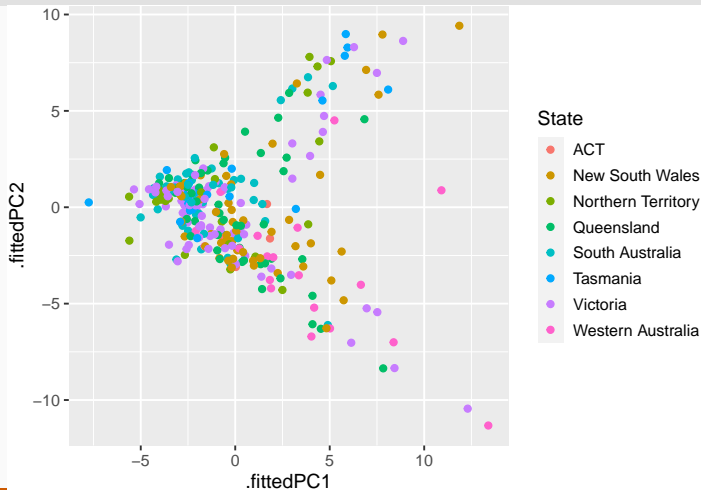
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=State)) +  
  geom_point() + theme(aspect.ratio=1)
```

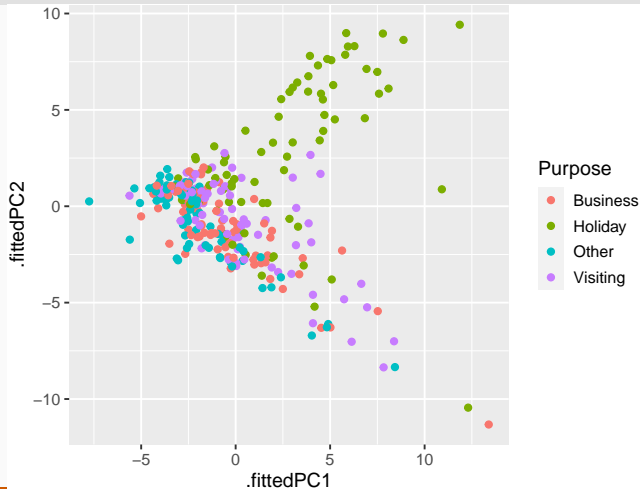
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

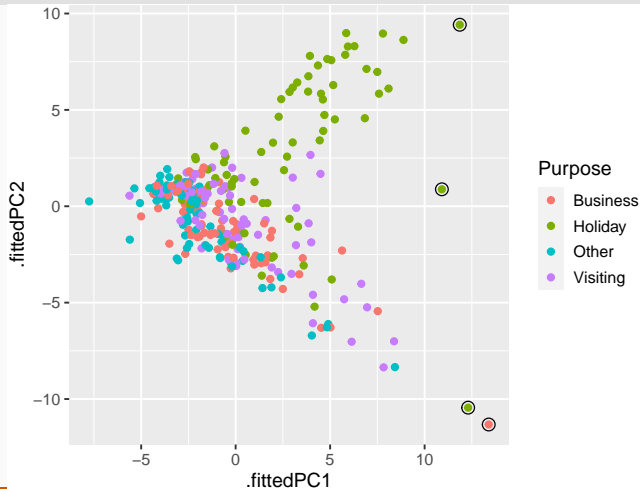
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

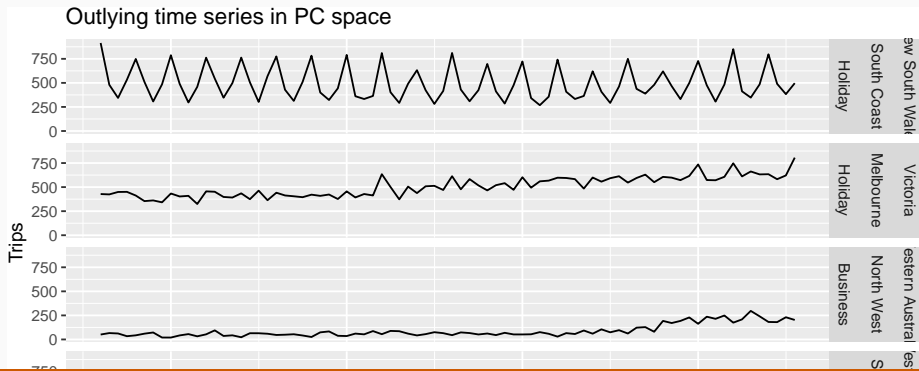
```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
outliers %>%  
  left_join(tourism, by = c("State", "Region", "Purpose")) %>%  
  mutate(Series = glue("{State}", "{Region}", "{Purpose}", .sep = "\n\n")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(Series ~ .) + ggtitle("Outlying time series in PC space")
```



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# Lab Session 10

- Use a feature-based approach to look for outlying series in PBS.
- What is unusual about the series you identify as outliers?