

# Tidy Time Series & Forecasting in R

## 5. Time series features



# Outline

- 1 STL Features
- 2 Lab Session 9
- 3 Dimension reduction for features
- 4 Lab Session 10

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# Strength of seasonality and trend

## STL decomposition

$$y_t = T_t + S_t + R_t$$

## Seasonal strength

$$\max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(S_t + R_t)} \right)$$

## Trend strength

$$\max \left( 0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(T_t + R_t)} \right)$$

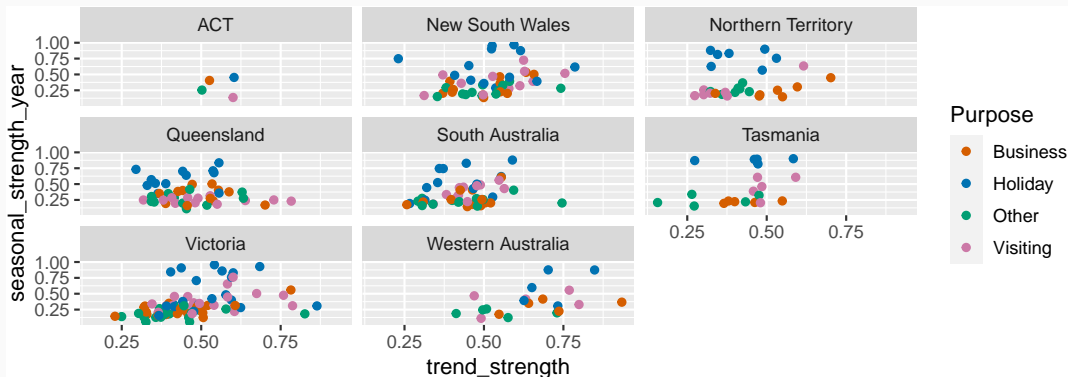
# Feature extraction and statistics

```
tourism %>% features(Trips, feat_stl)
```

```
## # A tibble: 304 x 12
##   Region      State Purpose trend_strength seasonal_streng~ seasonal_peak_y~
##   <chr>      <chr> <chr>          <dbl>          <dbl>          <dbl>
## 1 Adelaide Sout~ Busine~          0.464          0.407           3
## 2 Adelaide Sout~ Holiday          0.554          0.619           1
## 3 Adelaide Sout~ Other          0.746          0.202           2
## 4 Adelaide Sout~ Visiti~          0.435          0.452           1
## 5 Adelaide~ Sout~ Busine~          0.464          0.179           3
## 6 Adelaide~ Sout~ Holiday          0.528          0.296           2
## 7 Adelaide~ Sout~ Other          0.593          0.404           2
## 8 Adelaide~ Sout~ Visiti~          0.488          0.254           0
## 9 Alice Sp~ Nort~ Busine~          0.534          0.251           0
## 10 Alice Sp~ Nort~ Holiday          0.381          0.832           3
## # ... with 294 more rows, and 6 more variables:
## #   seasonal_trough_year <dbl>, spikiness <dbl>, linearity <dbl>,
## #   curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>
```

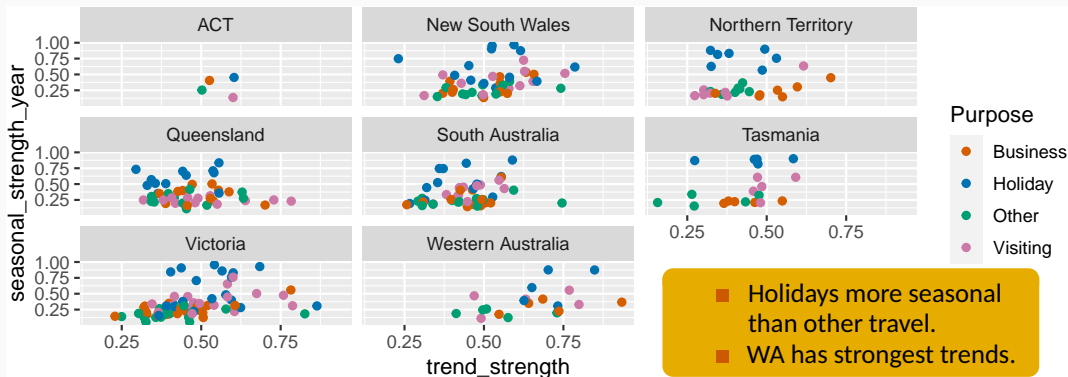
# Feature extraction and statistics

```
tourism %>%  
  features(Trips, feat_stl) %>%  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



# Feature extraction and statistics

```
tourism %>%  
  features(Trips, feat_stl) %>%  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



# Feature extraction and statistics

Find the most seasonal time series:

```
most_seasonal <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(seasonal_strength_year == max(seasonal_strength_year))
```

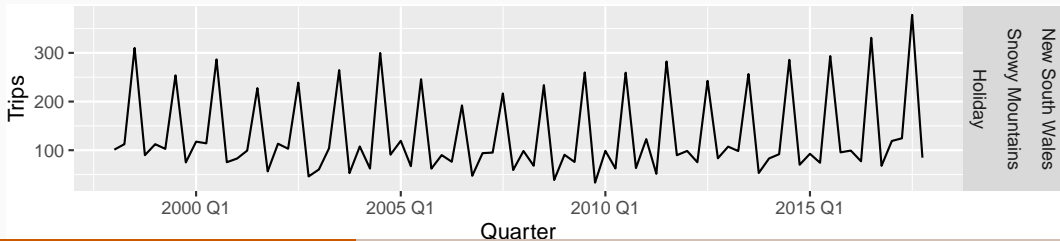


# Feature extraction and statistics

Find the most seasonal time series:

```
most_seasonal <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(seasonal_strength_year == max(seasonal_strength_year))
```

```
tourism %>%  
  right_join(most_seasonal, by = c("State", "Region", "Purpose")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(vars(State, Region, Purpose))
```



# Feature extraction and statistics

Find the most trended time series:

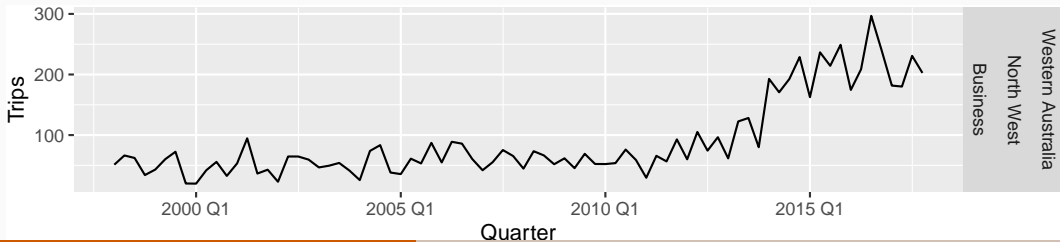
```
most_trended <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(trend_strength == max(trend_strength))
```

# Feature extraction and statistics

Find the most trended time series:

```
most_trended <- tourism %>%  
  features(Trips, feat_stl) %>%  
  filter(trend_strength == max(trend_strength))
```

```
tourism %>%  
  right_join(most_trended, by = c("State", "Region", "Purpose")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(vars(State, Region, Purpose))
```



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## Lab Session 9

- Use `GGally::ggpairs()` to look at the relationships between the STL-based features. You might wish to change `seasonal_peak_year` and `seasonal_trough_year` to factors.
- Which is the peak quarter for holidays in each state?

# Feature extraction and statistics

```
tourism %>% features(Trips, feat_acf)
```

```
## # A tibble: 304 x 10
##   Region      State Purpose      acf1 acf10 diff1_acf1 diff1_acf10 diff2_acf1
##   <chr>      <chr> <chr>      <dbl> <dbl>      <dbl>      <dbl>      <dbl>
## 1 Adelaide Sout~ Busine~  0.0333  0.131     -0.520      0.463     -0.676
## 2 Adelaide Sout~ Holiday 0.0456  0.372     -0.343      0.614     -0.487
## 3 Adelaide Sout~ Other    0.517    1.15     -0.409      0.383     -0.675
## 4 Adelaide Sout~ Visiti~  0.0684  0.294     -0.394      0.452     -0.518
## 5 Adelaide~ Sout~ Busine~  0.0709  0.134     -0.580      0.415     -0.750
## 6 Adelaide~ Sout~ Holiday 0.131    0.313     -0.536      0.500     -0.716
## 7 Adelaide~ Sout~ Other    0.261    0.330     -0.253      0.317     -0.457
## 8 Adelaide~ Sout~ Visiti~  0.139    0.117     -0.472      0.239     -0.626
## 9 Alice Sp~ Nort~ Busine~  0.217    0.367     -0.500      0.381     -0.658
## 10 Alice Sp~ Nort~ Holiday -0.00660 2.11     -0.153      2.11     -0.274
## # ... with 294 more rows, and 2 more variables: diff2_acf10 <dbl>,
## #   season_acf1 <dbl>
```

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# Feature extraction and statistics

```
tourism_features <- tourism %>%  
  features(Trips, feature_set(pkgs = "feasts"))
```

All features from the feasts package

```
## # A tibble: 304 x 51  
##   Region      State Purpose trend_strength seasonal_streng~ seasonal_peak_y~  
##   <chr>      <chr> <chr>          <dbl>          <dbl>          <dbl>  
## 1 Adelaide Sout~ Busine~         0.464         0.407           3  
## 2 Adelaide Sout~ Holiday       0.554         0.619           1  
## 3 Adelaide Sout~ Other         0.746         0.202           2  
## 4 Adelaide Sout~ Visiti~       0.435         0.452           1  
## 5 Adelaide~ Sout~ Busine~       0.464         0.179           3  
## 6 Adelaide~ Sout~ Holiday       0.528         0.296           2  
## 7 Adelaide~ Sout~ Other         0.593         0.404           2  
## 8 Adelaide~ Sout~ Visiti~       0.488         0.254           0  
## 9 Alice Sp~ Nort~ Busine~       0.534         0.251           0  
## 10 Alice Sp~ Nort~ Holiday       0.381         0.832           3  
## # ... with 294 more rows, and 45 more variables:  
## #   seasonal_trough_year <dbl>, spikiness <dbl>, linearity <dbl>,  
## #   curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>, acf1 <dbl>,  
## #   ...
```



# Feature extraction and statistics

```
pcs <- tourism_features %>%  
  select(-State, -Region, -Purpose) %>%  
  prcomp(scale = TRUE) %>%  
  broom::augment(tourism_features)
```

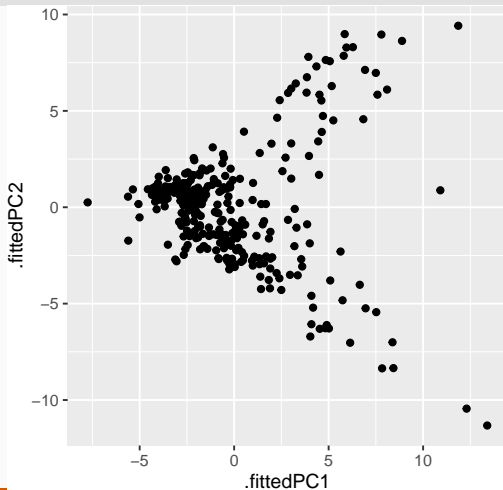
Principal components based on  
all features from the feasts  
package

```
## # A tibble: 304 x 100  
##   .rownames Region      State Purpose trend_strength seasonal_streng~  
##   <chr>      <chr>      <chr> <chr>      <dbl>      <dbl>  
## 1 1          Adelaide South ~ Busine~ 0.464      0.407  
## 2 2          Adelaide South ~ Holiday 0.554      0.619  
## 3 3          Adelaide South ~ Other 0.746      0.202  
## 4 4          Adelaide South ~ Visiti~ 0.435      0.452  
## 5 5          Adelaide Hills South ~ Busine~ 0.464      0.179  
## 6 6          Adelaide Hills South ~ Holiday 0.528      0.296  
## 7 7          Adelaide Hills South ~ Other 0.593      0.404  
## 8 8          Adelaide Hills South ~ Visiti~ 0.488      0.254  
## 9 9          Alice Springs Northe~ Busine~ 0.534      0.251  
## 10 10         Alice Springs Northe~ Holiday 0.381      0.832  
## # ... with 294 more rows, and 94 more variables: seasonal_peak_year <dbl>,
```

# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2)) +  
  geom_point() + theme(aspect.ratio=1)
```

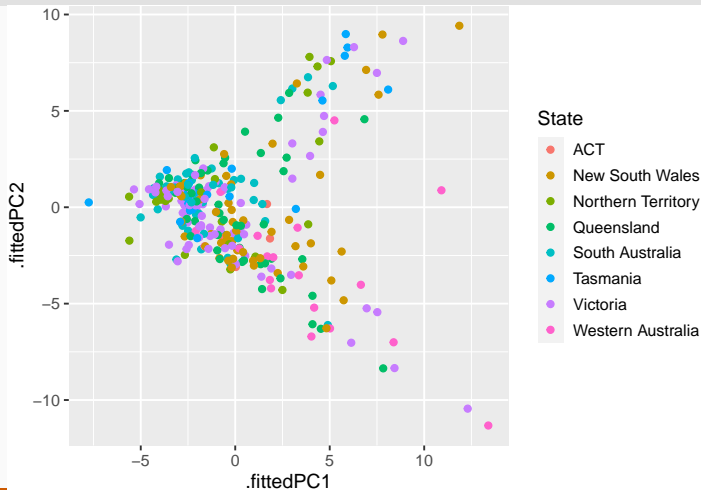
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=State)) +  
  geom_point() + theme(aspect.ratio=1)
```

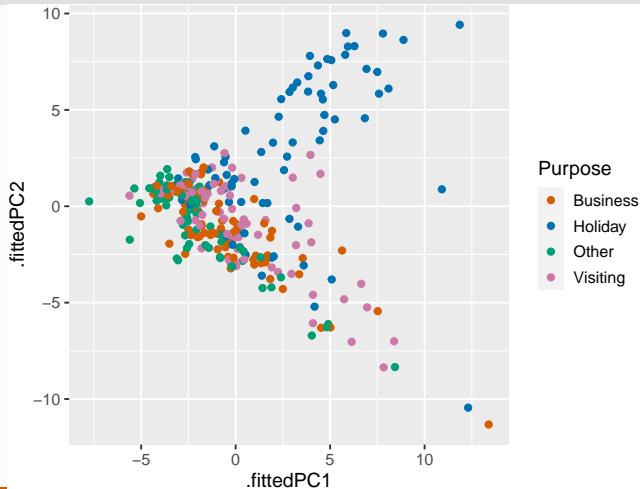
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

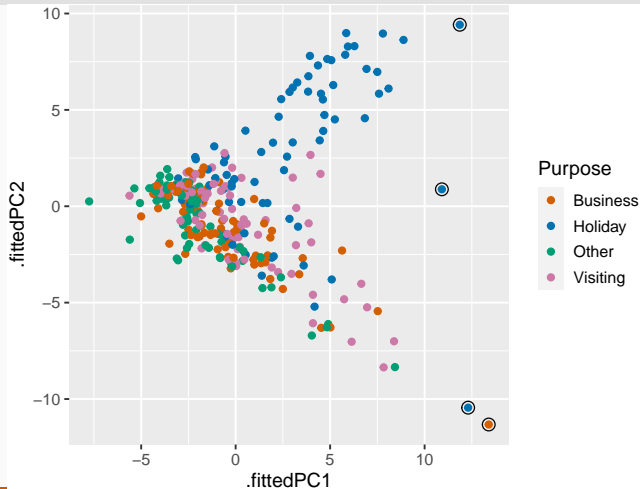
Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

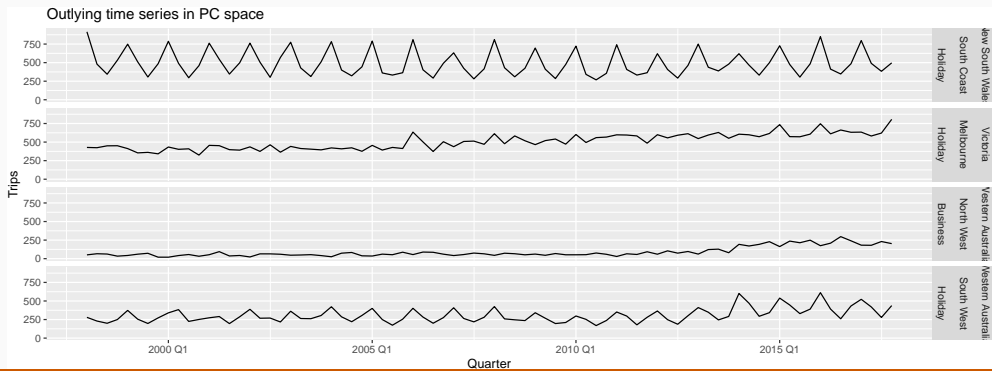
```
pcs %>% ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

Principal components  
based on all features  
from the feasts  
package



# Feature extraction and statistics

```
outliers %>%  
  left_join(tourism, by = c("State", "Region", "Purpose")) %>%  
  mutate(Series = glue("{State}", "{Region}", "{Purpose}", .sep = "\n\n")) %>%  
  ggplot(aes(x = Quarter, y = Trips)) + geom_line() +  
  facet_grid(Series ~ .) + ggtitle("Outlying time series in PC space")
```



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# Lab Session 10

- Use a feature-based approach to look for outlying series in PBS.
- What is unusual about the series you identify as outliers?