# **Tidy Time Series & Forecasting in R**

4. Seasonality and trends



#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up

#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up

#### **Time series decomposition**

**Trend-Cycle** aperiodic changes in level over time.

Seasonal (almost) periodic changes in level due to seasonal factors (e.g., the quarter of the year, the month, or day of the week).

#### **Additive decomposition**

$$y_t = S_t + T_t + R_t$$

where  $y_t = \text{data at period } t$ 

 $T_t = \text{trend-cycle component at period } t$ 

 $S_t =$  seasonal component at period t

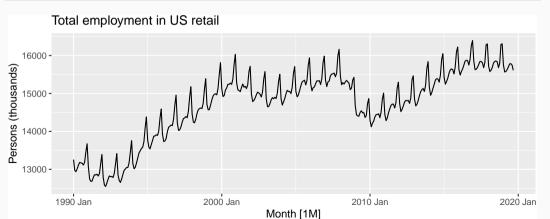
 $R_t$  = remainder component at period t

- STL: "Seasonal and Trend decomposition using Loess"
- Very versatile and robust.
- Seasonal component allowed to change over time, and rate of change controlled by user.
- Smoothness of trend-cycle also controlled by user.
- Optionally robust to outliers
- No trading day or calendar adjustments.
- Only additive.
- Take logs to get multiplicative decomposition.
- Use Box-Cox transformations to get other decompositions.

```
us_retail_employment <- us_employment ▷
  filter(year(Month) ≥ 1990, Title = "Retail Trade") ▷
  select(-Series_ID)
us_retail_employment</pre>
```

```
## # A tsibble: 357 x 3 [1M]
         Month Title
###
                             Employed
###
         <mth> <chr>
                                <fdb1>
###
    1 1990 Jan Retail Trade
                               13256.
    2 1990 Feb Retail Trade
                               12966.
###
    3 1990 Mar Retail Trade
                               12938.
###
##
    4 1990 Apr Retail Trade
                               13012.
    5 1990 May Retail Trade
                               13108.
##
    6 1990 Jun Retail Trade
###
                               13183.
    7 1990 Jul Retail Trade
                               13170.
###
###
    8 1990 Aug Retail Trade
                               13160.
## 0 1000 Con Dotail Trado
                               12112
```

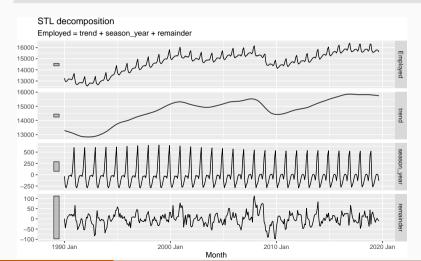
```
us_retail_employment ▷
  autoplot(Employed) +
  labs(y="Persons (thousands)", title="Total employment in US retail")
```



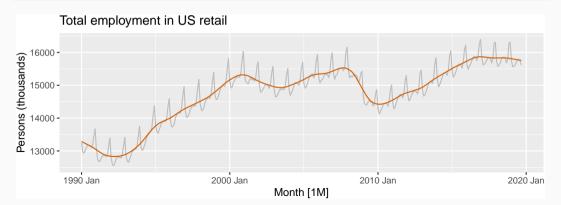
#### components(dcmp)

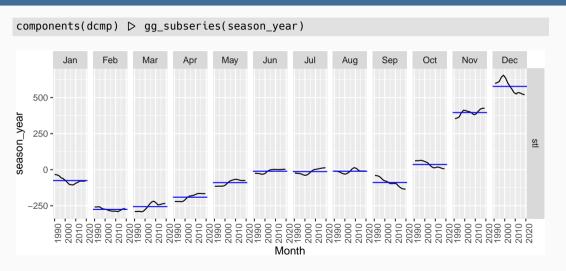
```
## # A dable: 357 x 7 [1M]
##
  # Kev:
             .model [1]
## # :
             Employed = trend + season_year + remainder
     .model
               Month Employed trend season year remainder season adjust
###
##
     <chr>
               <mth>
                       <dbl> <dbl>
                                         <dbl>
                                                   <dbl>
                                                                <dbl>
##
   1 stl
            1990 Jan 13256. 13288.
                                        -33.0
                                                   0.836
                                                               13289.
            1990 Feb 12966, 13269, -258,
##
   2 stl
                                                 -44.6
                                                               13224.
            1990 Mar 12938, 13250, -290,
                                                 -22.1
                                                               13228.
###
   3 stl
###
   4 stl
            1990 Apr 13012, 13231.
                                       -220.
                                                   1.05
                                                               13232.
            1990 May 13108, 13211.
                                                  11.3
                                                               13223.
###
   5 stl
                                       -114.
   6 stl
            1990 Jun
                      13183. 13192.
                                        -24.3
                                                  15.5
                                                               13207.
###
   7 stl
            1990 Jul
                      13170. 13172.
                                        -23.2
                                                  21.6
                                                               13193.
###
            1990 Aug 13160. 13151.
                                         -9.52
###
   8 stl
                                                  17.8
                                                               13169.
            1990 Sep
                                                  22.0
##
   9 stl
                      13113. 13131.
                                        -39.5
                                                               13153.
```

#### components(dcmp) ▷ autoplot()



```
us_retail_employment ▷
  autoplot(Employed, color='gray') +
  autolayer(components(dcmp), trend, color='#D55E00') +
  labs(y="Persons (thousands)", title="Total employment in US retail")
```





#### Seasonal adjustment

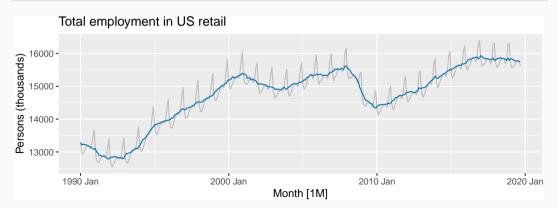
- Useful by-product of decomposition: an easy way to calculate seasonally adjusted data.
- Additive decomposition: seasonally adjusted data given by

$$y_t - S_t = T_t + R_t$$

 Multiplicative decomposition: seasonally adjusted data given by

$$y_t/S_t = T_t \times R_t$$

```
us_retail_employment >
  autoplot(Employed, color='gray') +
  autolayer(components(dcmp), season_adjust, color='#0072B2') +
  labs(y="Persons (thousands)", title="Total employment in US retail")
```

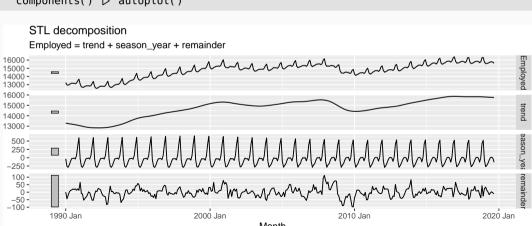


#### Seasonal adjustment

- We use estimates of S based on past values to seasonally adjust a current value.
- Seasonally adjusted series reflect remainders as well as trend. Therefore they are not "smooth" and "downturns" or "upturns" can be misleading.
- It is better to use the trend-cycle component to look for turning points.

- trend(window = ?) controls wiggliness of trend component.
- season(window = ?) controls variation on seasonal component.
- season(window = 'periodic') is equivalent to an infinite window.

```
us retail employment ▷
  model(STL(Employed)) ▷
  components() ▷ autoplot()
```

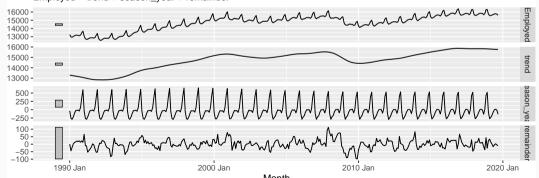


- STL() chooses season(window=13) by default
- Can include transformations.

us retail employment ▷ model(STL(Employed)) ▷ components() ▷ autoplot()

#### STL decomposition

Employed = trend + season\_year + remainder

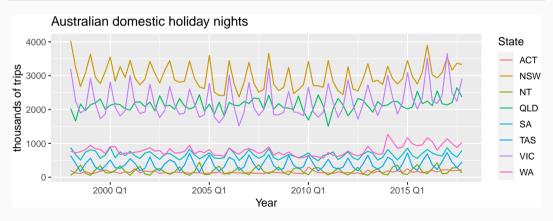


- Algorithm that updates trend and seasonal components iteratively.
- Starts with  $\hat{T}_t = 0$
- Uses a mixture of loess and moving averages to successively refine the trend and seasonal estimates.
- The trend window controls loess bandwidth applied to deasonalised values.
- The season window controls loess bandwidth applied to detrended subseries.
- Robustness weights based on remainder.
- Default season window = 13
- Default trend window = nextodd(

```
ceiling((1.5*period)/(1-(1.5/s.window)))
```

#### **Australian holidays**

```
holidays ▷ autoplot(Trips) +
ylab("thousands of trips") + xlab("Year") +
ggtitle("Australian domestic holiday nights")
```



#### **Decomposition plot**

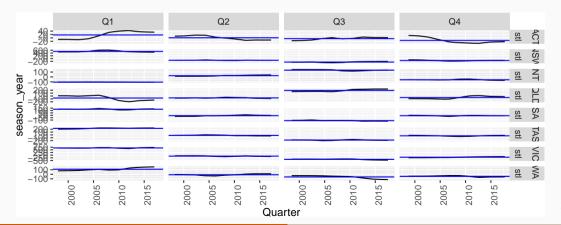
```
holidays ▷
  model(stl = STL(Trips ~ season(window = 7))) ▷
  components() ▷
  autoplot()
     STL decomposition
     Trips = trend + season year + remainder
4000 -
3000 -
                                                                                                    State/.model
                                                                                                        ACT/stl
                                                                                                        NSW/stl
3000 -
2000 -
                                                                                                        NT/stl
1000 -
  0 -
                                                                                                        QLD/stl
 500 -
                                                                                                        SA/stl
  0 -
                                                                                                         TAS/stl
-500 -
                                                                                              emainde
                                                                                                        VIC/stl
 200 -
                                                                                                        WA/stl
-200 -
                                                       2010 Q1
                                                                           2015 Q1
               2000 Q1
                                   2005 Q1
                                             Quarter
```

#### **Decomposition plot**

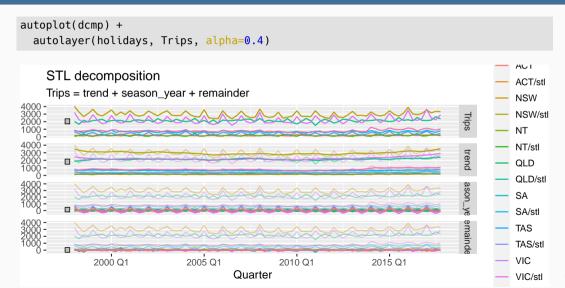
```
holidays ▷
  model(stl = STL(Trips ~ season(window = "periodic"), robust = TRUE)) ▷
  components() ▷
  autoplot()
     STL decomposition
     Trips = trend + season year + remainder
                                                                                                    State/.model
                                                                                                        ACT/stl
                                                                                                        NSW/stl
3000 -
         П
2000 -
                                                                                                        NT/stl
1000 -
  0 -
                                                                                                        QLD/stl
                                                                                                        SA/stl
                                                                                                         TAS/stl
500 -
250 -
0 -
-250 -
-500 -
                                                                                              emainde
                                                                                                        VIC/stl
                                                                                                        WA/stl
                                   2005 Q1
                                                                           2015 Q1
               2000 Q1
                                                       2010 Q1
                                             Quarter
```

### **Decomposition subseries**

```
dcmp <- holidays > model(stl = STL(Trips)) >
  components()
dcmp > gg_subseries(season_year)
```



#### **Decomposition trend**



```
holidays ▷
model(stl = STL(Trips ~ trend(window=15) + season(window=13),
    robust = TRUE))
```

- trend(window = ?) controls wiggliness of trend component.
- season(window = ?) controls variation on seasonal component.
- STL() chooses season(window=13) by default
- A large seasonal window is equivalent to setting window="periodic".
- Odd numbers should be used for symmetry.

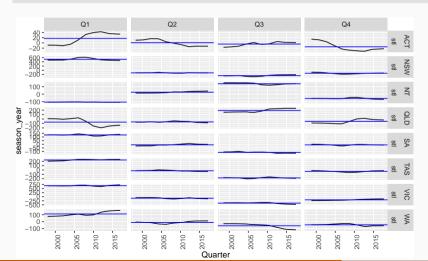
#### **Holidays decomposition**

```
dcmp <- holidays \triangleright model(stl = STL(Trips)) \triangleright components() dcmp
```

```
## # A dable: 640 x 8 [10]
## # Key:
         State, .model [8]
         Trips = trend + season year + remainder
###
###
     State .model Quarter Trips trend season year remainder season adjust
     <chr> <chr> <qtr> <dbl> <dbl>
                                           <dbl>
                                                     <dbl>
###
                                                                   <dbl>
                  1998 01 196. 172.
                                                  32.6
                                                                    205.
##
   1 ACT
           stl
                                          -8.48
###
   2 ACT
           stl
                  1998 02 127. 157.
                                           10.3
                                                    -40.6
                                                                    116.
   3 ACT
           stl
                  1998 Q3
                          111. 142.
                                          -16.8
                                                    -14.5
                                                                    128.
###
   4 ACT
                  1998 04
                          170. 130.
                                           14.6
                                                   25.6
                                                                    156.
##
           stl
                  1999 Q1
   5 ACT
           stl
                          108.
                                135.
                                           -8.63
                                                    -18.3
                                                                    116.
##
   6 ACT
           stl
                  1999 Q2
                          125.
                                148.
                                           11.0
                                                    -34.6
                                                                    114.
##
   7 ACT
                  1999 Q3
                          178.
                                 166.
                                                     28.3
                                                                    194.
###
           stl
                                          -16.0
                  1999 Q4
                                                     27.5
###
   8 ACT
           stl
                          218.
                                177.
                                           13.2
                                                                    204.
###
   9 ACT
           stl
                  2000 01
                          158.
                                169.
                                           -8.75
                                                     -1.96
                                                                    167.
## 10 ACT
           s+1
                  2000 02 155
                                 151
                                           11 7
                                                     -8 20
                                                                    143
```

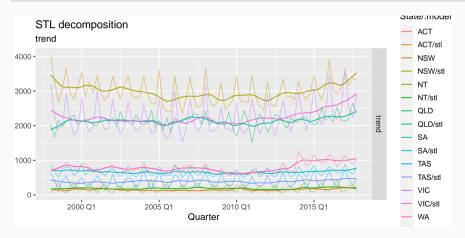
## **Holidays decomposition**

dcmp ▷ gg\_subseries(season\_year)



### **Holidays decomposition**

```
autoplot(dcmp, trend, scale_bars = FALSE) +
  autolayer(holidays, alpha = 0.4)
```



#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up

#### **Lab Session 8**

Produce the following decomposition

```
canadian_gas >
  model(STL(Volume ~ season(window=7) + trend(window=11))) >
  components() >
  autoplot()
```

- What happens as you change the values of the two window arguments?
- How does the seasonal shape change over time? [Hint: Try plotting the seasonal component using gg\_season.]
- Can you produce a plausible seasonally adjusted series? [Hint: season\_adjust is one of the variables returned by STL.]

#### **Outline**

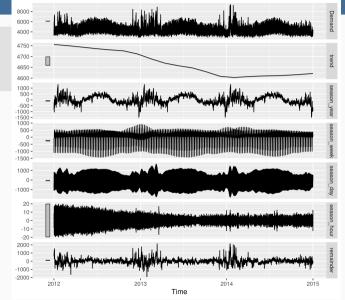
- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up

## **Multiple seasonality**

vic\_elec ▷
 model(STL(Demand)) ▷
 components() ▷
 autoplot()



Demand = trend + season\_year + season\_week + season\_day + season\_hour + remainder



#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Multiple seasonality
- 4 The ABS stuff-up



#### Treasurer Joe Hockey calls for answers over Australian Bureau of Statistics jobs data

By Michael Vincent and Simon Frazer
Undated 9 Oct 2014, 12:17pm

Federal Treasurer Joe Hockey says he wants answers to the problems the Australian Bureau of Statistics (ABS) has had with unemployment figures.

Mr Hockey, who is in the US to discuss Australia's G20 agenda, said last month's unemployment figures were "extraordinary"

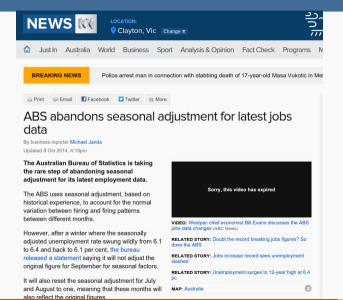
The rate was 6.1 per cent after jumping to a 12-year high of 6.4 per cent the previous month.

The ABS has now taken the rare step of abandoning seasonal adjustment for its latest employment data.



PHOTO: Joe Hockey says he is unhappy with the volatility of ABS unemployment figures. (AAP: Alan Porritt)

RELATED STORY: ABS abandons seasonal adjustment for



## ABS jobs and unemployment figures - key questions answered by an expert

A professor of statistics at Monash University explains exactly what is seasonal adjustment, why it matters and what went wrong in the July and August figures



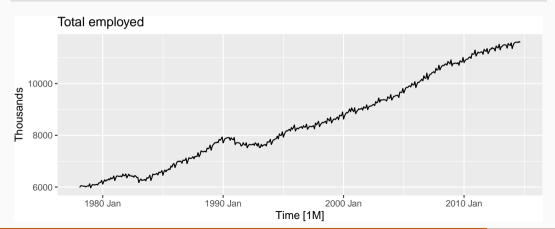
School leavers come on to the jobs market at the same time, causing a seasonal fluctuation. Photograph: Brian Snyder/Reuters

## The Australian Bureau of Statistics has retracted its seasonally adjusted employment data for July and August, which recorded huge swings in the jobless rate. The ABS is also planning to review the methods it uses for seasonal adjustment to ensure its figures are as accurate as possible. Rob Hyndman, a professor of statistics at Monash University and member of the bureau's methodology advisory board. answers our questions:

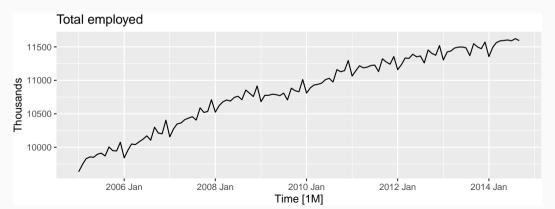
#### employed

```
# A tsibble: 440 \times 4 \lceil 1M \rceil
###
          Time Month Year Employed
         <mth> <ord> <dbl>
                                <dbl>
###
    1 1978 Feb Feb
                        1978
                                5986.
###
##
    2 1978 Mar Mar
                        1978
                                6041.
##
    3 1978 Apr Apr
                        1978
                                6054.
##
    4 1978 May May
                        1978
                                 6038.
    5 1978 Jun Jun
                        1978
                                6031.
##
###
    6 1978 Jul Jul
                        1978
                                6036.
                        1978
##
    7 1978 Aug Aug
                                 6005.
    8 1978 Sep Sep
                        1978
                                 6024.
###
##
    9 1978 Oct Oct
                        1978
                                 6046.
  10 1978 Nov Nov
                        1978
                                 6034.
  # ... with 430 more rows
```

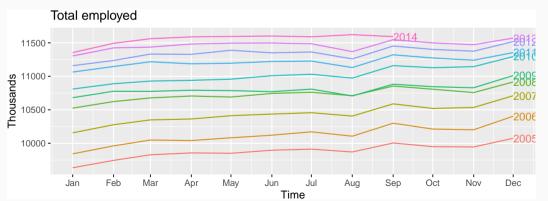
```
employed >
  autoplot(Employed) +
  labs(title = "Total employed", y = "Thousands")
```



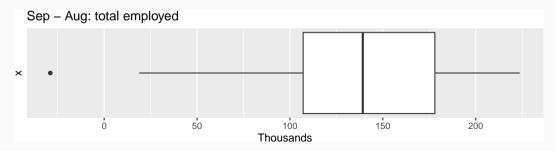
```
employed ▷
  filter(Year ≥ 2005) ▷
  autoplot(Employed) +
  labs(title = "Total employed", y = "Thousands")
```



```
employed ▷
  filter(Year ≥ 2005) ▷
  gg_season(Employed, labels = "right") +
  labs(title = "Total employed", y = "Thousands")
```

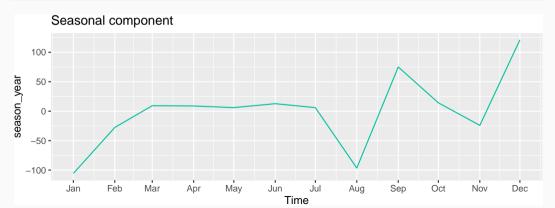


```
employed >
  mutate(diff = difference(Employed)) >
  filter(Month = "Sep") >
  ggplot(aes(y = diff, x = 1)) +
  geom_boxplot() + coord_flip() +
  labs(title = "Sep - Aug: total employed", y = "Thousands") +
  scale_x_continuous(breaks = NULL, labels = NULL)
```

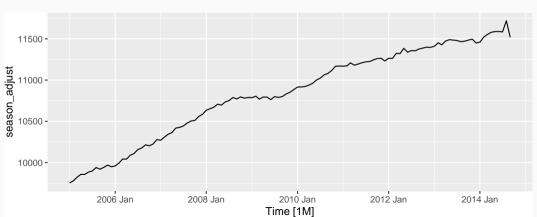


```
dcmp <- employed ▷
  filter(Year ≥ 2005) ▷
  model(stl = STL(Employed ~ season(window = 11), robust = TRUE))
components(dcmp) ▷ autoplot()
    STL decomposition
     Employed = trend + season_year + remainder
                                                                                      mploye
        2010 Jan
                                                                          2014 Jan
                                           Time
```

```
components(dcmp) >
  filter(year(Time) = 2013) >
  gg_season(season_year) +
  labs(title = "Seasonal component") + guides(colour = "none")
```







- August 2014 employment numbers higher than expected.
- Supplementary survey usually conducted in August for employed people.
- Most likely, some employed people were claiming to be unemployed in August to avoid supplementary questions.
- Supplementary survey not run in 2014, so no motivation to lie about employment.
- In previous years, seasonal adjustment fixed the problem.
- The ABS has now adopted a new method to avoid the bias.