



# Time Series Analysis & Forecasting Using R

3. Transformations

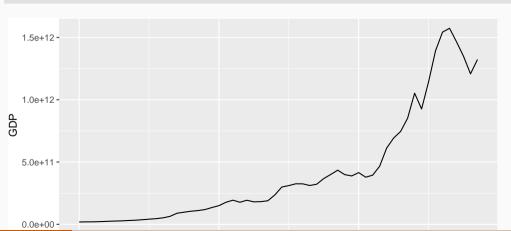


- 1 Per capita adjustments
- 2 Lab Session 6
- 3 Inflation adjustments
- 4 Mathematical transformations
- 5 Lab Session 7

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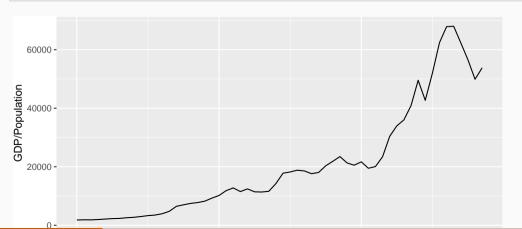
# Per capita adjustments

```
global_economy %>%
  filter(Country == "Australia") %>%
  autoplot(GDP)
```



# Per capita adjustments

```
global_economy %>%
  filter(Country == "Australia") %>%
  autoplot(GDP / Population)
```



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## **Lab Session 6**

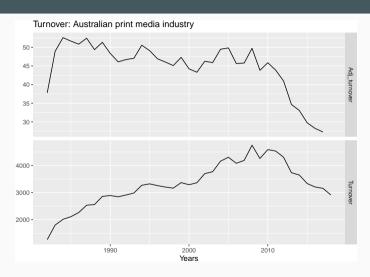
Consider the GDP information in global\_economy. Plot the GDP per capita for each country over time. Which country has the highest GDP per capita? How has this changed over time?

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# **Inflation adjustments**

```
print retail <- aus retail %>%
  filter(Industry == "Newspaper and book retailing") %>%
  group by(Industry) %>%
  index_by(Year = year(Month)) %>%
  summarise(Turnover = sum(Turnover))
aus economy <- filter(global economy, Code == "AUS")
print retail %>%
  left_join(aus_economy, by = "Year") %>%
  mutate(Adj_turnover = Turnover / CPI) %>%
  pivot longer(c(Turnover, Adi turnover),
    names_to = "Type", values_to = "Turnover"
  ) %>%
  ggplot(aes(x = Year, y = Turnover)) +
  geom line() +
  facet_grid(vars(Type), scales = "free_y") +
  xlab("Years") + ylab(NULL) +
  ggtitle("Turnover: Australian print media industry")
```

# **Inflation adjustments**



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Denote original observations as  $y_1, \ldots, y_n$  and transformed observations as  $w_1, \ldots, w_n$ .

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#### Mathematical transformations for stabilizing variation

Square root 
$$w_t = \sqrt{y_t}$$

Cube root 
$$w_t = \sqrt[3]{y_t}$$
 Increasing

Logarithm 
$$w_t = \log(y_t)$$
 strength

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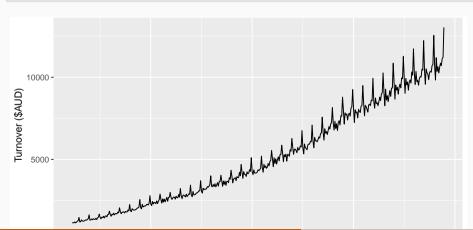
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#### Mathematical transformations for stabilizing variation

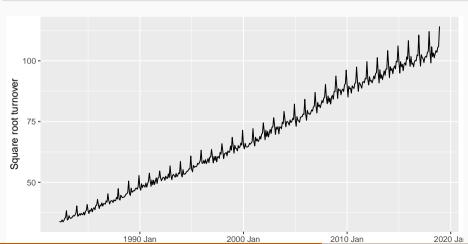
Square root 
$$w_t = \sqrt{y_t}$$
  $\downarrow$  Cube root  $w_t = \sqrt[3]{y_t}$  Increasing Logarithm  $w_t = \log(y_t)$  strength

Logarithms, in particular, are useful because they are more interpretable: changes in a log value are **relative (percent) changes on the original scale**.

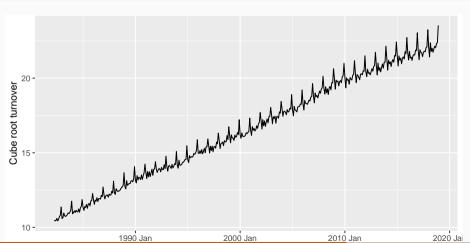
```
food <- aus_retail %>%
  filter(Industry == "Food retailing") %>%
  summarise(Turnover = sum(Turnover))
```



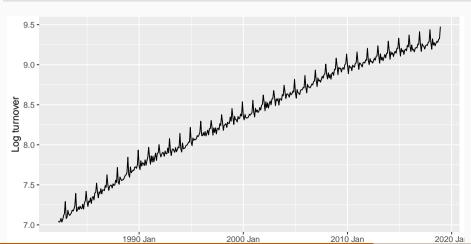
```
food %>% autoplot(sqrt(Turnover)) +
  labs(y = "Square root turnover")
```



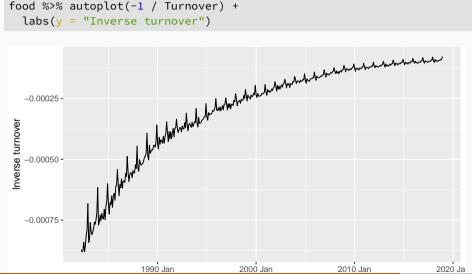
```
food %>% autoplot(Turnover^(1 / 3)) +
  labs(y = "Cube root turnover")
```



```
food %>% autoplot(log(Turnover)) +
  labs(y = "Log turnover")
```



```
food %>% autoplot(-1 / Turnover) +
 labs(y = "Inverse turnover")
```



Each of these transformations is close to a member of the family of **Box-Cox transformations**:

$$w_t = \begin{cases} \log(y_t), & \lambda = 0; \\ (y_t^{\lambda} - 1)/\lambda, & \lambda \neq 0. \end{cases}$$

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#### **Box-Cox transformations:**

$$w_t = \begin{cases} \log(y_t), & \lambda = 0; \\ (y_t^{\lambda} - 1)/\lambda, & \lambda \neq 0. \end{cases}$$

- $\lambda$  = 1: (No substantive transformation)
- $\lambda = \frac{1}{2}$ : (Square root plus linear transformation)
- $\lambda$  = 0: (Natural logarithm)
- $\lambda = -1$ : (Inverse plus 1)

```
food %>%
  features(Turnover, features = guerrero)

## # A tibble: 1 x 1
## lambda_guerrero
## <dbl>
```

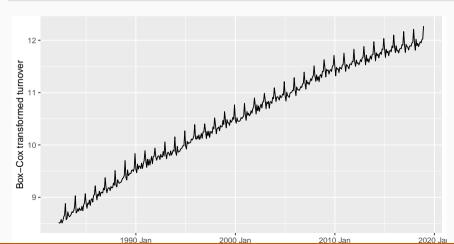
- This attempts to balance the seasonal fluctuations and random variation across the series.
- Always check the results.

0.0895

## 1

lacksquare A low value of  $\lambda$  can give extremely large prediction intervals.

```
food %>% autoplot(box_cox(Turnover, 0.0524)) +
  labs(y = "Box-Cox transformed turnover")
```



#### **Transformations**

- Often no transformation needed.
- Simple transformations are easier to explain and work well enough.
- Transformations can have very large effect on PI.
- If the data contains zeros, then don't take logs.
- logp1() can be useful for data with zeros.
- If some data are negative, no power transformation is possible unless a constant is added to all values.
- Choosing logs is a simple way to force forecasts to be positive
- Transformations must be reversed to obtain forecasts on the original scale. (Handled automatically by fable.)

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#### **Lab Session 7**

- For the following series, find an appropriate transformation in order to stabilise the variance.
  - United States GDP from global\_economy
  - Slaughter of Victorian "Bulls, bullocks and steers" in aus\_livestock
  - Victorian Electricity Demand from vic\_elec.
  - Gas production from aus\_production
- Why is a Box-Cox transformation unhelpful for the canadian\_gas data?