ising-class.py

```
# We create a 'master' Ising class, with options to gap the spectrum or use mixed correlator
1
        information.
    import bootstrap
2
    import matplotlib.pyplot as plt
3
    import time, datetime
4
    import datetime
5
    import numpy as np
6
    from matplotlib.backends.backend_pdf import PdfPages
7
8
9
    sig_defaults = np.arange(0.5, 0.85, 0.05).tolist()
    eps_defaults = np.arange(1.0,2.2,0.2).tolist()
10
11
    class Grid(object):
12
13
      def __init__(self, kmax, lmax, mmax, nmax, allowed_points, disallowed_points, run_time,
          cpu_time):
14
        self.kmax = kmax
        self.lmax = lmax
15
        self.mmax = mmax
16
        self.nmax = nmax
17
        self.allowed_points = allowed_points
18
        self.disallowed_points = disallowed_points
19
20
        self.run_time = run_time
        self.cpu_time = cpu_time
21
22
    class Ising(object):
23
24
      def __init__(self, dim = 3, gap = 3, name, sig_values = sig_defaults, eps_values = eps_defaults
          ):
        self.dim = dim
25
        self.qap = qap
26
        self.sig_values = sig_values
27
28
        self.eps_values = eps_values
29
        self.table = []
        self.name = name
30
31
      # For a given set of conformal blocks, set by kmax and lmax, generate a grids for a specified
32
          range of mmax and nmax.
33
      # If we obtain a grid of entirely dissallowed points, fill in the rest of the grids for that
          kmax and lmax.
      def iterate_parameters(self, kmax_range, lmax_range, mmax_range, nmax_range):
34
        keys = self.generate_keys(kmax_range, lmax_range, mmax_range)
35
36
37
        while len(keys) > 0:
38
          # Used keys will store the keys for which there is already a grid in table.
          used_keys = []
39
          \#null_keys = []
40
41
          for key in keys:
42
            if self.get_grid_index(key) != -1:
43
               used_keys.append(key)
44
               continue
45
            print("Trying kmax = " + str(key[0]) + ", lmax = " + str(key[1]) + ", mmax = " + str(key[1])
46
                [2]) + ", nmax = " + str(key[3]))
            self.determine_grid(key)
47
             used_keys.append(key)
48
```

```
49
50
             # If the grid has only disallowed points...
             if self.table[self.get_grid_index(key)].allowed_points == []:
51
               print ("In the if statement.")
52
               k = key[0]
53
               l = key[1]
54
55
               m = key[2]
               n = key[3]
56
57
               null_keys = [key for key in keys if key not in used_keys and key[0] == k and key[1] ==
58
                   l and key[2] >= m and key[3] >= n]
59
               for key in null_keys:
60
                  if self.get_grid_index(key) != -1:
61
                    used_keys.append(key)
62
                    continue
63
64
                  #grid = Grid(*key, [], [])
                  grid = Grid(*(key + [[], [], 0, 0]))
65
66
                  for sig in self.sig_values:
67
                    for eps in self.eps_values:
68
69
                      grid.disallowed_points.append((sig, eps))
70
71
                  self.table.append(grid)
                  self.save_grid(grid, self.name)
72
73
               break
74
75
           # We remove all keys from the list that we are done with.
76
           keys = [key for key in keys if key not in null_keys and key not in used_keys]
77
           null_keys = []
78
79
80
       ,,,
81
       # Saves the data as an executable file that will repopulate the table attribute.
82
       # Note, we now do this as we go, instead of at the end, to avoid loss of mass data.
83
       def save_to_file(self, name):
84
         with open(name + ".py", 'w') as file:
85
           file.write("self.table = []\n")
86
           for grid in self.table:
87
              file.write("kmax = " + str(grid.kmax) + "\n")
88
              file.write("lmax = " + str(grid.lmax) + "\n")
89
              file.write("mmax = " + str(grid.mmax) + "\n")
90
              file.write("nmax = " + str(grid.nmax) + "\n")
91
              file.write("allowed_points = " + str(grid.allowed_points) + "\n")
92
             file.write("disallowed_points = " + str(grid.disallowed_points) + "\n")
93
             file.write("self.table.append(Grid(kmax, lmax, mmax, nmax, allowed_points,
94
                 disallowed_points))" + "\n")
95
96
       def save_grid(self, grid, name):
97
         with open(name + ".py", 'a') as file:
98
           file.write("kmax = " + str(grid.kmax) + "\n")
99
           file.write("lmax = " + str(grid.lmax) + "\n")
100
           file.write("mmax = " + str(grid.mmax) + "\n")
101
           file.write("nmax = " + str(grid.nmax) + "\n")
102
           file.write("allowed_points = " + str(grid.allowed_points) + "\n")
103
           file.write("disallowed_points = " + str(grid.disallowed_points) + "\n")
104
```

```
file.write("run_time = " + str(grid.run_time) + "\n")
105
106
           file.write("cpu_time = " + str(grid.cpu_time) + "\n")
           file.write("self.table.append(Grid(kmax, lmax, mmax, nmax, allowed_points,
107
               disallowed_points, run_time, cpu_time))" + "\n")
108
       # Recoveres a table stored to a file.
109
110
       def recover_table(self, file_name):
         exec(open(file_name + ".py").read())
111
112
113
       \# Searches table of grids for index matching the input key. Returns -1 if not found.
114
       def get_grid_index(self, key):
115
116
         for i in range(0, len(self.table)):
           if self.table[i].kmax == key[0] and self.table[i].lmax == key[1] and self.table[i].mmax ==
117
               key[2] and self.table[i].nmax == key[3]:
              return i
118
         return -1
119
120
       # Plots and saves a series of grids to an output PDF file.
121
       # Takes as input parameter values for which we want plotted grids, and the desired PDF file
122
           name.
123
       def plot_grids(self, keys, file_name):
         table = self.generate_table(keys)
124
         pdf_pages = PdfPages(file_name + ".pdf")
125
126
         # Define the number of plots per page and the size of the grid board.
127
         nb_plots = len(table)
128
129
         nb_plots_per_page = 6
         nb_pages = int(np.ceil(nb_plots / float(nb_plots_per_page)))
130
131
         grid_size=(3,2)
132
         # This will define which row of the grid we are on.
133
134
         row_index = 0
135
         # We go through each 'grid' in 'table', generating a plot for each.
136
137
         for i in range(nb_plots):
           # To begin, declare a new figure / page if we have exceeded limit of the last page.
138
           if i % nb_plots_per_page == 0:
139
             fig = plt.figure(figsize=(8.27, 11.69), dpi=100)
140
141
           # Now, add a plot for the current grid on the grid board.
142
           plt.subplot2grid(grid_size, (row_index, i % grid_size[1]))
143
           if i % grid_size[1] == 1:
144
             row_index += 1
145
146
           # Handle our data. Retrieve isolated points for plotting from out input table of Grid
147
               obiects.
           allowed_sig = [points[0] for points in table[i].allowed_points]
148
           allowed_eps = [points[1] for points in table[i].allowed_points]
149
           disallowed_sig = [points[0] for points in table[i].disallowed_points]
150
           disallowed_eps = [points[1] for points in table[i].disallowed_points]
151
152
           # Plot a grid.
153
           plt.plot(allowed_sig, allowed_eps, 'r+')
154
155
           plt.plot(disallowed_sig, disallowed_eps, 'b+')
           plt.title('kmax : ' + table[i].kmax.__str__() + " " +
156
                'lmax : ' + table[i].lmax.__str__() + " " +
157
                'mmax : ' + table[i].mmax.__str__() + " " +
158
```

```
159
                'nmax : ' + table[i].nmax.__str__())
160
           # If we have filled a page, or have reached the end of our plots, tight-pack and save the
161
               page.
           if (i + 1) % nb_plots_per_page == 0 or (i + 1) == nb_plots:
162
163
             plt.tight_layout()
164
             pdf_pages.savefig(fig)
             row_index = 0
165
166
         pdf_pages.close()
167
168
       # Returns a key or list of keys generated by the input parameter ranges.
169
170
       def generate_keys(self, kmax_range, lmax_range, mmax_range, nmax_range):
         if type(kmax_range) == int:
171
           kmax_range = [kmax_range]
172
         if type(lmax_range) == int:
173
174
           lmax_range = [lmax_range]
         if type(mmax_range) == int:
175
176
           mmax_range = [mmax_range]
         if type(nmax_range) == int:
177
           nmax_range = [nmax_range]
178
179
         keys = []
         for kmax in kmax_range:
180
181
           for lmax in lmax_range:
             for mmax in mmax_range:
182
                for nmax in nmax_range:
183
                  key = [kmax, lmax, mmax, nmax]
184
185
                  keys.append(key)
         return keys
186
187
       # Generates a subtable table of desired, already determined grids from main table.
188
       # Gives a warning message if a grid isn't found.
189
190
       def generate_table(self, keys):
191
         # table to store the resulting grids.
         table = []
192
193
         for key in keys:
           if self.get_grid_index(key) == -1:
194
             print("Grid at kmax = " + str(key[0]) + ", " +
195
                "lmax = " + str(key[1]) + ", " +
196
                "mmax = " + str(key[2]) + "
197
                "nmax = " + str(key[3]) + ", " + "does not exist.")
198
199
           else:
             table.append(self.table[self.get_grid_index(key)])
200
201
         return table
202
203
       # Takes two keys and returns a dictionary with the direction of every point.
204
       def changes(self, key1, key2):
205
206
         changes = \{\}
         allowed_one = self.table[self.get_grid_index(key1)].allowed_points
207
         allowed_two = self.table[self.get_grid_index(key2)].allowed_points
208
209
         for sig in self.sig_values:
210
211
           for eps in self.eps_values:
212
             if (sig, eps) in allowed_one and (sig, eps) in allowed_two:
                changes[(sig, eps)] = 0
213
             if (sig, eps) not in allowed_one and (sig, eps) not in allowed_two:
214
                changes[(siq, eps)] = 0
215
```

```
216
             if (sig, eps) in allowed_one and (sig, eps) not in allowed_two:
217
               changes[(sig, eps)] = -1
             if (sig, eps) not in allowed_one and (sig, eps) in allowed_two:
218
               changes[(sig, eps)] = 1
219
220
         return changes
221
222
       def plot_changes(self, keys, file_name):
223
         pdf_pages = PdfPages(file_name + ".pdf")
224
         # Define the number of plots per page and the size of the grid board.
225
         # We have one less plots than grids.
226
         nb_plots = len(keys)
227
228
         nb_plots_per_page = 6
         nb_pages = int(np.ceil(nb_plots / float(nb_plots_per_page)))
229
         grid_size=(3,2)
230
231
         # This will define which row of the grid we are on.
232
         row_index = 0
233
234
         # We go through each 'grid' in 'table', generating a plot for each.
235
         for i in range(nb_plots):
236
           # To begin, declare a new figure / page if we have exceeded limit of the last page.
237
           # 8.27 x 11.69 dimensions of A4 page in inches. DPI - dots per inch (resolution.)
238
239
           if i % nb_plots_per_page == 0:
             fig = plt.figure(figsize=(8.27, 11.69), dpi=100)
240
241
           # Now, add a plot for the current grid on the grid board.
242
243
           plt.subplot2grid(grid_size, (row_index, i % grid_size[1]))
           if i % grid_size[1] == 1:
244
             row_index += 1
245
246
           # We want the first grid to compare all changes to.
247
248
           if i == 0:
             grid = self.table[self.get_grid_index(keys[i])]
249
             allowed_sig = [points[0] for points in grid.allowed_points]
250
             allowed_eps = [points[1] for points in grid.allowed_points]
251
             disallowed_sig = [points[0] for points in grid.disallowed_points]
252
             disallowed_eps = [points[1] for points in grid.disallowed_points]
253
254
             # Plot the grid.
255
             plt.plot(allowed_sig, allowed_eps, 'r+')
256
257
             plt.plot(disallowed_sig, disallowed_eps, 'b+')
             plt.title('kmax : ' + grid.kmax.__str__() + " " +
258
                  'lmax : ' + grid.lmax.__str__() + " " +
259
                  'mmax : ' + grid.mmax.__str__() + " " +
260
                  'nmax : ' + grid.nmax.__str__())
261
262
             y_range = plt.ylim()
263
264
             x_range = plt.xlim()
265
266
           else:
             changes = self.changes(keys[i-1], keys[i])
267
268
             unchanged_points = []
             to_allowed_points = []
269
270
             to_disallowed_points = []
             for point in changes:
271
               if changes[point] == 0:
272
                 unchanged_points.append(point)
273
```

```
274
                if changes[point] == 1:
                  to_allowed_points.append(point)
275
                if changes[point] == -1:
276
                  to_disallowed_points.append(point)
277
278
             unchanged_sig = [points[0] for points in unchanged_points]
279
280
             unchanged_eps = [points[1] for points in unchanged_points]
281
             to_disallowed_sig = [points[0] for points in to_disallowed_points]
             to_disallowed_eps = [points[1] for points in to_disallowed_points]
282
             to_allowed_sig = [points[0] for points in to_allowed_points]
283
             to_allowed_eps = [points[1] for points in to_allowed_points]
284
285
286
             # Plot a grid.
             plt.plot(to_allowed_sig, to_allowed_eps, 'r+')
287
             plt.plot(to_disallowed_sig, to_disallowed_eps, 'b+')
288
             plt.xlim(x_range)
289
290
             plt.ylim(y_range)
             plt.title('kmax : ' + self.table[self.get_grid_index(keys[i])].kmax.__str__() + " " +
291
                  'lmax : ' + self.table[self.get_grid_index(keys[i])].lmax.__str__() + " " +
292
                  'mmax : ' + self.table[self.get_grid_index(keys[i])].mmax.__str__() + " " +
293
                  'nmax : ' + self.table[self.get_grid_index(keys[i])].nmax.__str__())
294
295
           # If we have filled a page, or have reached the end of our plots, tight-pack and save the
296
           if (i + 1) % nb_plots_per_page == 0 or (i + 1) == nb_plots:
297
             plt.tight_layout()
298
             pdf_pages.savefig(fig)
299
300
             row_index = 0
301
         pdf_pages.close()
302
303
304
     class SingleCorrelator(Ising):
305
       bootstrap.cutoff=1e-10
       def __init__(self, dim = 3, gap = 3, name, sig_values = sig_defaults, eps_values = eps_defaults
306
           ):
307
         self.dim = dim
         self.gap = gap
308
         self.sig_values = sig_values
309
         self.eps_values = eps_values
310
         self.table = []
311
         self.name = name
312
313
314
       # Determines allowed and disallowed scaling dimensions for whatever the parameters are.
       def determine_grid(self, key):
315
         #if self.get_grid_index(key) != -1:
316
         start_time=time.time()
317
         start_cpu=time.clock()
318
         tab1 = bootstrap.ConformalBlockTable(self.dim, *key)
319
         tab2 = bootstrap.ConvolvedBlockTable(tab1)
320
321
         # Instantiate a Grid object with appropriate input values.
322
         # grid=Grid(*key, [], [])
323
324
         grid = Grid(*(key + [[], [], 0, 0]))
325
326
         for sig in self.sig_values:
           for eps in self.eps_values:
327
             sdp = bootstrap.SDP(sig, tab2)
328
             # SDPB will naturally try to parallelize across 4 cores / slots.
329
```

```
330
             # To prevent this, we set its 'maxThreads' option to 1.
331
             # See 'common.py' for the list of SDPB option strings, as well as their default values.
             sdp.set_option("maxThreads", 1)
332
             sdp.set_bound(0, float(self.gap))
333
             sdp.add_point(0, eps)
334
335
             result = sdp.iterate()
336
             if result:
                grid.allowed_points.append((sig, eps))
337
             else:
338
                grid.disallowed_points.append((sig, eps))
339
340
         # Now append this grid object to the IsingGap table.
341
342
         # Note we will need to implement a look up table to retrieve desired data.
         end_time=time.time()
343
         end_cpu=time.clock()
344
         run_time=end_time-start_time
345
346
         cpu_time=end_cpu-start_cpu
         run_time = datetime.timedelta(seconds = int(end_time - start_time))
347
         cpu_time = datetime.timedelta(seconds = int(end_cpu - start_cpu))
348
349
         grid.run_time = run_time
350
351
         grid.cpu_time = cpu_time
         self.table.append(grid)
352
353
         self.save_grid(grid, self.name)
354
     # For mixed correlator, we pass pairs of external scaling dimensions to the SDP.
355
     # We copy the content of the triples entering the SDP from the tutorial, same case.
356
357
     # We want to scan over all possible [sig, eps], assuming only one relevant Z2-even and Z2-odd
         operator.
     # Use a protoype to use the same basis for all SDPs, so we don't need to recaculate bases.
358
     # Dump the ConformalBlockTable objects once we have used them to save memory.
359
     # Set dualThresholdError to 1e-15.
360
361
     # Use 16 cores for all SDP runs - set maxThreads = 16, speed up the SDP.
362
     class MixedCorrelator(Ising):
       bootstrap.cutoff=0
363
364
       def __init__(self, dim = 3, gap = 3, name, sig_values = sig_defaults, eps_values = eps_defaults
           ):
         self.dim = dim
365
         self.gap = gap
366
         self.sig_values = sig_values
367
         self.eps_values = eps_values
368
         self.table = []
369
370
         self.name = name
371
       # Determines allowed and disallowed scaling dimensions for whatever the parameters are.
372
       def determine_grid(self, key):
373
         #if self.get_grid_index(key) != -1:
374
         reference_sdp = None
375
376
         start_time=time.time()
         start_cpu=time.clock()
377
378
         # Instantiate a Grid object with appropriate input values.
379
         # grid=Grid(*key, [], [])
380
381
         grid = Grid(*(key + [[], [], 0, 0]))
382
         for sig in self.sig_values:
383
           for eps in self.eps_values:
384
             # Generates three tables, two of which depend on the dimension differences.
385
```

```
386
               g_tab1 = bootstrap.ConformalBlockTable(self.dim, *key)
387
               g_tab2 = bootstrap.ConformalBlockTable(self.dim, *key, eps-sig, sig-eps, odd_spins =
               g_tab3 = bootstrap.ConformalBlockTable(self.dim, *key, sig-eps, sig-eps, odd_spins =
388
                   True)
               # Uses the function above to return the 5 ConvolvedConformalBlocks we need.
389
390
               # The ConvolvedConformalBlock objects inherits the dimension differences from
                   ConformalBlockTable.
               # We set odd_spins = True for odd those ConvolvedConformalBlocks appearing in odd-
391
                   sector-odd-spins.
               # We set symmetric = True where required.
392
               tab_list = convolved_table_list(g_tab1, g_tab2, g_tab3)
393
394
               # Here, we will sava and delete conformal blocks. Think aboout their recycling.
               # Otherwise, massive redundancy, same blocks will be used many times.
395
396
               # N.B vec3 & vec2 are 'raw' quads, which will be converted to 1x1 matrices
397
                   automatically.
               # Third vector: 0, 0, 1 st table4 with one of each dimension, -1 st table2 with only pair
398
                   [0] dimensions, 1 * table3 with only pair[0] dimensions
               vec3 = [[0, 0, 0, 0], [0, 0, 0, 0], [1, 4, 1, 0], [-1, 2, 0, 0], [1, 3, 0, 0]]
399
               # Second vector: 0, 0, 1 st table4 with one of each dimension, 1 st table2 with only pair
400
                   [0] dimensions, -1 * table3 with only pair[0] dimensions
               vec2 = [[0, 0, 0, 0], [0, 0, 0, 0], [1, 4, 1, 0], [1, 2, 0, 0], [-1, 3, 0, 0]]
401
402
               # The first vector has five components as well but they are matrices of quads, not just
                    the quads themselves.
               m1 = [[[1, 0, 0, 0], [0, 0, 0, 0]], [[0, 0, 0, 0], [0, 0, 0, 0]]]
403
               m2 = [[[0, 0, 0, 0], [0, 0, 0, 0]], [[0, 0, 0, 0], [1, 0, 1, 1]]]
404
405
               m3 = [[[0, 0, 0, 0], [0, 0, 0, 0]], [[0, 0, 0, 0], [0, 0, 0, 0]]]
               m4 = [[[0, 0, 0, 0], [0.5, 0, 0, 1]], [[0.5, 0, 0, 1], [0, 0, 0, 0]]]
406
               m5 = [[[0, 1, 0, 0], [0.5, 1, 0, 1]], [[0.5, 1, 0, 1], [0, 1, 0, 0]]]
407
               vec1 = [m1, m2, m3, m4, m5]
408
409
410
               # The first rep must be the singlet even channel, where the unit operator resides.
411
               # After this, the order doesn't matter.
               # Spins for these again go even, even, odd.
412
               # The Z2 even sector has only even spins, Z2 odd sector runs over even and odd spins.
413
               info = [[vec1, 0, "z2-even-l-even"], [vec2, 0, "z2-odd-l-even"], [vec3, 1, "z2-odd-l-
414
                   odd"]]
415
               # We instantiate the SDP object, inputting our vectorial sum info.
416
               # dim_list, convolved_block_table_list, vector_types (how they combine to compose sum
417
                   rule).
               # We use the first calculated SDP object as a prototype for all the rest.
418
               # This is because some bounds remain unchanged, no need to recalculate basis.
419
               # Basis is independent of external scaling dimensions, cares only of the bounds on
420
                   particular operators.
               if reference_sdp == None:
421
               sdp = bootstrap.SDP([sig, eps], tab_list, vector_types = info)
422
423
               reference_sdp = sdp
               else:
424
                 sdp = bootstrap.SDP([sig, eps], tab_list, vector_types = info, protoype =
425
                     reference_sdp)
426
               # We assume the continuum in both Z2 odd / even sectors begins at the dimension=3.
427
               sdp.set_bound([0, "z2-even-l-even"], self.dim)
428
               sdp.set_bound([0, "z2-odd-l-even"], self.dim)
429
430
```

Except for the two lowest dimension scalar operators in each sector.

431

```
sdp.add_point([0, "z2-even-l-even"], eps)
432
433
               sdp.add_point([0, "z2-odd-l-even"], sig)
434
               # We expect these calculations to be computationally intensive.
435
               # We set maxThreads=16 to parallelise SDPB for all runs.
436
             # See 'common.py' for the list of SDPB option strings, as well as their default values.
437
438
             sdp.set_option("maxThreads", 16)
             sdp.set_option("dualErrorThreshold", 1e-15)
439
440
             # Run the SDP to determine if the current operator spectrum is permissable.
441
             result = sdp.iterate()
442
             if result:
443
444
               grid.allowed_points.append((sig, eps))
             else:
445
               grid.disallowed_points.append((sig, eps))
446
447
         # Now append this grid object to the IsingGap table.
448
         # Note we will need to implement a look up table to retrieve desired data.
449
450
         end_time=time.time()
         end_cpu=time.clock()
451
         run_time=end_time-start_time
452
453
         cpu_time=end_cpu-start_cpu
         run_time = datetime.timedelta(seconds = int(end_time - start_time))
454
455
         cpu_time = datetime.timedelta(seconds = int(end_cpu - start_cpu))
456
         grid.run_time = run_time
457
         grid.cpu_time = cpu_time
458
459
         self.table.append(grid)
         self.save_grid(grid, self.name)
460
461
       # A function used for the multi-correlator 3D Ising example.
462
       # Note default is antisymmetrised convolved conformal blocks.
463
       def convolved_table_list(self, tab1, tab2, tab3):
464
           f_tabla = bootstrap.ConvolvedBlockTable(tab1)
465
           f_tab1s = bootstrap.ConvolvedBlockTable(tab1, symmetric = True)
466
467
           f_tab2a = bootstrap.ConvolvedBlockTable(tab2)
           f_tab2s = bootstrap.ConvolvedBlockTable(tab2, symmetric = True)
468
           f_tab3 = bootstrap.ConvolvedBlockTable(tab3)
469
           return [f_tabla, f_tabls, f_tab2a, f_tab2s, f_tab3]
470
471
     ,,,
472
473
     # We define a class with imposes a gap in the Z_2-even operator sector.
474
     # The continuum starts at a specified value, and we add an operator between this and unitarity
         bound.
     class IsingGap(object):
475
       bootstrap.cutoff=1e-10
476
       def __init__(self, dim = 3, gap = 3, sig_values = sig_defaults, eps_values = eps_defaults):
477
         self.dim = dim
478
479
         self.gap = gap
         self.sig_values = sig_values
480
481
         self.eps_values = eps_values
         self.table = []
482
         self.name = "name"
483
         # if from_file == True:
484
         # self.recover_table(file_name)
485
         # else:
486
         # self.table = []
487
488
```