

Goals

We have a dataset contain axon diameters of neurons from the optic nerve of control and mutant zebrafish. We'd like to know if the mean axon diameter, or the distribution of axon diameters, differs between groups. We want to implement tests that take account of within and between animal variance.

Here, we focus on the myRF data set.

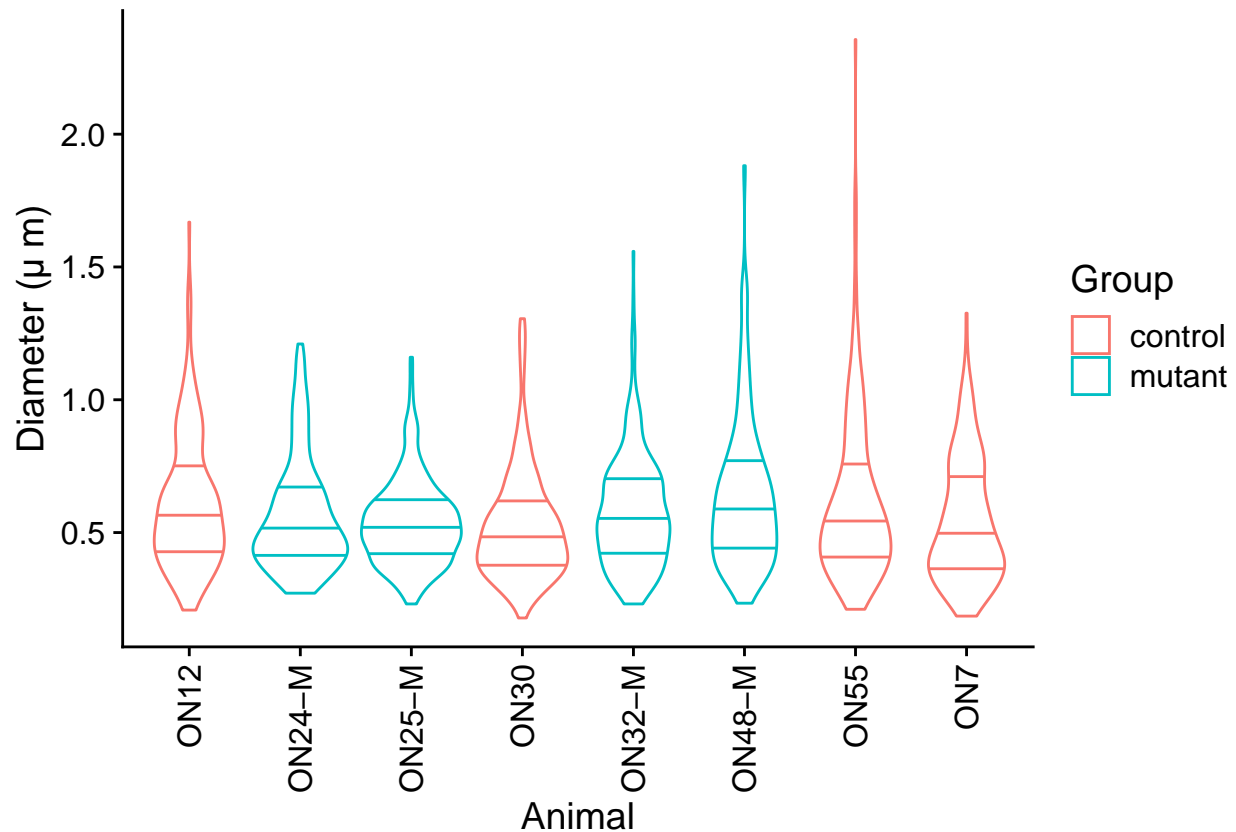
Load and format data

```
df <- read_excel("MyRF Axon Diameter Measurements 20240709.xlsx", range = "A3:H328") %>%
  pivot_longer(cols = 1:8) %>%
  drop_na() %>%
  mutate(group = as_factor(ifelse(name %in% c("ON7", "ON12", "ON30", "ON55"), "control", "mutant")),
         litter = as_factor(ifelse(name %in% c("ON7", "ON12"), "litter1",
                                             ifelse(name %in% c("ON24-M", "ON25-M", "ON30"), "litter2",
                                                    ifelse(name %in% c("ON32-M"), "litter3",
                                                           ifelse(name %in% c("ON48-M"), "litter4",
                                                                ifelse(name %in% c("ON55"), "litter5", "error"))))))),
         processed = as_factor(ifelse(litter %in% c("litter1", "litter2"), "processed1", "processed2"))),
         df$group <- as.factor(df$group)
df$name <- as.factor(df$name)
```

Plot the data

Focus here on plot of individual mice, colour coded by group.

```
(plot_by_id <- ggplot(data = df, aes(name, value)) +
  geom_violin(aes(colour = group), draw_quantiles = c(0.25, 0.5, 0.75)) +
  theme_cowplot(font_size = 14) +
  theme(axis.text.x = element_text(angle = 90, vjust = 0.5, hjust=1)) +
  labs(x = 'Animal', y = 'Diameter (\u00B5 m)', colour = "Group"))
```



```
ggsave('Plots/violins.jpeg', plot_by_id)
```

```
## Saving 6.5 x 4.5 in image
```

Tests for differences in means

```
mm <- lmer(value ~ group + (1 | name), data = df)
mm_null <- lmer(value ~ (1 | name), data = df)
summary(mm)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: value ~ group + (1 | name)
## Data: df
##
## REML criterion at convergence: -75.2
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -1.6912 -0.7023 -0.1939  0.4556  7.3979
##
## Random effects:
## Groups Name Variance Std.Dev.
## name (Intercept) 0.001786 0.04226
## Residual 0.055828 0.23628
## Number of obs: 2160, groups: name, 8
##
```

```

## Fixed effects:
##           Estimate Std. Error t value
## (Intercept) 0.571517  0.022377  25.540
## groupmutant 0.007131  0.031583   0.226
##
## Correlation of Fixed Effects:
##           (Intr)
## groupmutant -0.709
anova(mm, mm_null)

## refitting model(s) with ML (instead of REML)

## Data: df
## Models:
## mm_null: value ~ (1 | name)
## mm: value ~ group + (1 | name)
##           npar      AIC      BIC logLik deviance Chisq Df Pr(>Chisq)
## mm_null      3 -80.980 -63.946 43.490  -86.980
## mm           4 -79.046 -56.335 43.523  -87.046 0.0664  1    0.7966

mm_t <- lmer(log(value) ~ group + (1 | name), data = df)
mm_t_null <- lmer(log(value) ~ (1 | name), data = df)
summary(mm_t)

## Linear mixed model fit by REML ['lmerMod']
## Formula: log(value) ~ group + (1 | name)
## Data: df
##
## REML criterion at convergence: 1997.2
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -2.6621 -0.7026 -0.0217  0.6423  3.8142
##
## Random effects:
## Groups Name Variance Std.Dev.
## name (Intercept) 0.003713 0.06094
## Residual 0.145934 0.38201
## Number of obs: 2160, groups: name, 8
##
## Fixed effects:
##           Estimate Std. Error t value
## (Intercept) -0.64693  0.03271 -19.777
## groupmutant 0.03399  0.04615  0.737
##
## Correlation of Fixed Effects:
##           (Intr)
## groupmutant -0.709
anova(mm_t, mm_t_null)

## refitting model(s) with ML (instead of REML)

## Data: df
## Models:
## mm_t_null: log(value) ~ (1 | name)

```

```
## mm_t: log(value) ~ group + (1 | name)
##          npar      AIC      BIC logLik deviance Chisq Df Pr(>Chisq)
## mm_t_null    3 1993.5 2010.6 -993.77   1987.5
## mm_t         4 1994.8 2017.6 -993.42   1986.8 0.6906  1      0.406
```

Test again with more complicated random effects stuctures

```
mm_t_2 <- lmer(log(value) ~ group + (1 | litter/name), data = df)
mm_t_null_2 <- lmer(log(value) ~ (1 | litter/name), data = df)
summary(mm_t_2)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: log(value) ~ group + (1 | litter/name)
## Data: df
##
## REML criterion at convergence: 1996.8
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -2.6577 -0.7005 -0.0188  0.6393  3.8127
##
## Random effects:
## Groups      Name      Variance Std.Dev.
## name:litter (Intercept) 0.002358 0.04856
## litter      (Intercept) 0.001445 0.03802
## Residual                    0.145938 0.38202
## Number of obs: 2160, groups: name:litter, 8; litter, 5
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept) -0.64303    0.03472 -18.522
## groupmutant  0.04355    0.04461   0.976
##
## Correlation of Fixed Effects:
##              (Intr)
## groupmutant -0.654
```

```
anova(mm_t_2, mm_t_null_2)
```

```
## refitting model(s) with ML (instead of REML)
## Data: df
## Models:
## mm_t_null_2: log(value) ~ (1 | litter/name)
## mm_t_2: log(value) ~ group + (1 | litter/name)
##          npar      AIC      BIC logLik deviance Chisq Df Pr(>Chisq)
## mm_t_null_2    4 1995.5 2018.2 -993.77   1987.5
## mm_t_2         5 1996.6 2025.0 -993.31   1986.6 0.9227  1      0.3368
```

```
mm_t_3 <- lmer(log(value) ~ group + (1 | processed/name), data = df)
mm_t_null_3 <- lmer(log(value) ~ (1 | processed/name), data = df)
summary(mm_t_3)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: log(value) ~ group + (1 | processed/name)
```

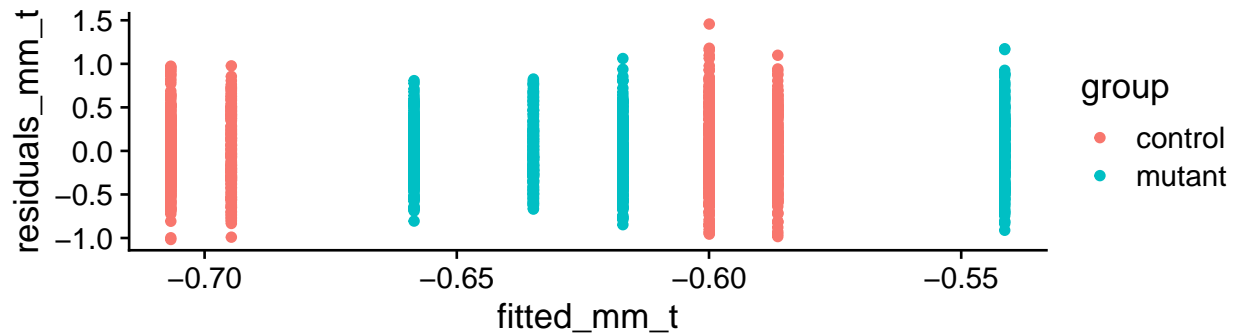
```
## Data: df
##
## REML criterion at convergence: 1996.5
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -2.6643 -0.7015 -0.0129  0.6368  3.8046
##
## Random effects:
##   Groups             Name             Variance Std.Dev.
## name:processed (Intercept) 0.002588 0.05087
## processed      (Intercept) 0.001885 0.04342
## Residual                0.145936 0.38202
## Number of obs: 2160, groups: name:processed, 8; processed, 2
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept) -0.63456    0.04246 -14.947
## groupmutant  0.02162    0.04047   0.534
##
## Correlation of Fixed Effects:
##              (Intr)
## groupmutant -0.500
anova(mm_t_2, mm_t_null_3)

## refitting model(s) with ML (instead of REML)

## Data: df
## Models:
## mm_t_null_3: log(value) ~ (1 | processed/name)
## mm_t_2: log(value) ~ group + (1 | litter/name)
##              npar      AIC      BIC  logLik deviance Chisq Df Pr(>Chisq)
## mm_t_null_3     4 1995.1 2017.8 -993.54   1987.1
## mm_t_2          5 1996.6 2025.0 -993.31   1986.6 0.474  1    0.4912
```

Evaluate residuals

```
df$residuals_mm_t <- resid(mm_t)
df$fitted_mm_t <- fitted(mm_t)
(res_t_plot <- ggplot(data = df, aes(x = fitted_mm_t, y = residuals_mm_t)) +
  geom_point(aes(colour = group)) +
  theme_cowplot())
```



Compare residual distributions between groups, for the untransformed data first and then for the log-transformed data.

```
### We could use a KS test:
ks.test(residuals_mm_t ~ group, data = df)
```

```
## Warning in ks.test.default(x = DATA[[1L]], y = DATA[[2L]], ...): p-value will be
## approximate in the presence of ties
```

```
##
## Asymptotic two-sample Kolmogorov-Smirnov test
##
## data: residuals_mm_t by group
## D = 0.071709, p-value = 0.007785
## alternative hypothesis: two-sided
```

This suggests differences between groups in the variance, but doesn't account for within vs between subject effects in the residuals. But worry here is that we don't treat animals as independent. Instead calculate SD for each animal and compare groups:

```
gr_t <- df %>% group_by(group, name) %>% summarize(avg_r = sd(residuals_mm_t))
```

```
## `summarise()` has grouped output by 'group'. You can override using the `.groups`
## argument.
```

```
t.test(avg_r ~ group, data = gr_t)
```

```
##
## Welch Two Sample t-test
##
## data: avg_r by group
## t = 1.9909, df = 5.4795, p-value = 0.09813
## alternative hypothesis: true difference in means between group control and group mutant is not equal
## 95 percent confidence interval:
## -0.01468272 0.12853729
## sample estimates:
## mean in group control mean in group mutant
## 0.4089329 0.3520056
```

Hard to interpret because group sizes are small. No firm evidence for difference in distributions.

Generate histograms for all animals

```

### Make histograms for each animal
### Use log transformed data
names = unique(df$name)
### If submean = 1 then will subtract means before making histograms
histfun <- function(name, df, submean = 0) {
  sub <- ifelse(submean == 1, mean(df$value[df$name==name]), 0)
  hist(log(df$value[df$name==name]-sub), seq(-2,2,0.1), plot = FALSE)
}
hists <- sapply(names, histfun, df, submean=0)

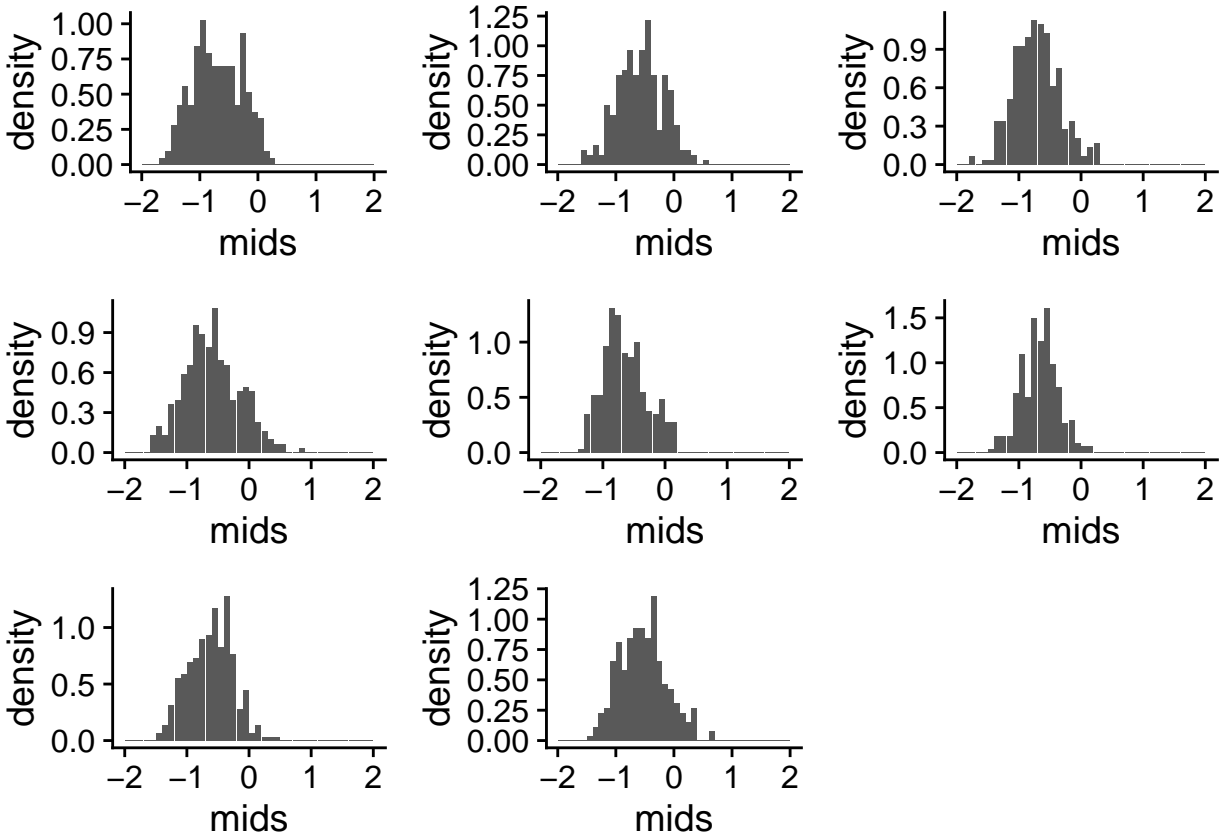
### Convert results to tibble for use with tidyverse functions
rns <- rownames(hists)
hists_tib <- as_tibble(hists) %>%
  rownames_to_column(var = "rowname") %>%
  pivot_longer(-rowname, names_to = "column", values_to = "value") %>%
  pivot_wider(names_from = rowname, values_from = value)
colnames(hists_tib) <- c("animal", rns)

ggconvfun <- function(mids, density) {
  gghist <- cbind(mids, density)
  ggplot(gghist, aes(mids, density)) +
    geom_col() +
    theme_cowplot()
}

gghists <- map2(hists_tib$mids, hists_tib$density, ggconvfun)

plot_grid(plotlist = gghists)

```



Evaluate distributions

```
fit.lqmm <- lqmm(fixed = value ~ group, random = ~1, group = name, tau = c(0.25, 0.5, 0.75), nK = 7, type = "normal", data = df, control = c(method = "df", summary(fit.lqmm, R = 500, seed = 2)
```

```
## Call: lqmm(fixed = value ~ group, random = ~1, group = name, tau = c(0.25,
##      0.5, 0.75), nK = 7, type = "normal", data = df, control = c(method = "df",
##      LP_max_iter = 5000))
##
## tau = 0.25
##
## Fixed effects:
##              Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept) 0.372273   0.025789   0.321605   0.4229 < 2.2e-16 ***
## groupmutant 0.105470   0.037054   0.032669   0.1783  0.004604 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## tau = 0.5
##
## Fixed effects:
##              Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept) 0.5722731  0.0355788   0.5023704   0.6422 <2e-16 ***
## groupmutant 0.0054705  0.0361782  -0.0656098   0.0766  0.8799
## ---
```



```

## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## tau = 0.75
##
## Fixed effects:
##               Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept)  0.692258   0.031817   0.629747   0.7548   <2e-16 ***
## groupmutant -0.010545   0.041330  -0.091747   0.0707   0.7987
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## AIC:
## [1] -443.5 (df = 4) -63.3 (df = 4) 768.8 (df = 4)
fit.log.lqmm <- lqmm(fixed = log(value) ~ group, random = ~1, group = name, tau = c(0.25,0.5, 0.75), nK
summary(fit.log.lqmm, R = 500, seed = 2)

## Call: lqmm(fixed = log(value) ~ group, random = ~1, group = name, tau = c(0.25,
##         0.5, 0.75), nK = 7, type = "normal", data = df, control = c(method = "df",
##         LP_max_iter = 5000))
##
## tau = 0.25
##
## Fixed effects:
##               Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept) -0.9393497  0.0344783  -1.0070903   -0.8716   < 2e-16 ***
## groupmutant  0.0676887  0.0393206  -0.0095657    0.1449   0.08579 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## tau = 0.5
##
## Fixed effects:
##               Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept) -0.666737   0.037753  -0.740912   -0.5926   <2e-16 ***
## groupmutant  0.041693   0.049686  -0.055927    0.1393   0.4018
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## tau = 0.75
##
## Fixed effects:
##               Value Std. Error lower bound upper bound Pr(>|t|)
## (Intercept) -0.366817   0.046582  -0.458338   -0.2753  2.148e-14 ***
## groupmutant -0.016329   0.060507  -0.135210    0.1026   0.7874
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## AIC:
## [1] 2372 (df = 4) 2264 (df = 4) 2633 (df = 4)

```