**Noise promotes independent control of gamma oscillations and grid firing within recurrent attractor networks**

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**Abstract (150 words)**

Neural computations underlying cognitive functions require calibration of the strength of excitatory and inhibitory synaptic connections and are associated with modulation of gamma frequency oscillations in network activity. However, principles relating gamma oscillations, synaptic strength and circuit computations are unclear. We address this in attractor network models that account for grid firing and theta-nested gamma oscillations in the medial entorhinal cortex. We show that moderate intrinsic noise massively increases the range of synaptic strengths supporting gamma oscillations and grid computation. With moderate noise, variation in excitatory or inhibitory synaptic strength tunes the amplitude and frequency of gamma activity without disrupting grid firing. This beneficial role for noise results from disruption of epileptic-like network states. Thus, moderate noise promotes independent control of multiplexed firing rate- and gamma-based computational mechanisms. Our results have implications for tuning of normal circuit function and for disorders associated with changes in gamma oscillations and synaptic strength.

**Introduction**

**Cognitive processes are mediated by computations in neural circuits and are often associated with gamma frequency oscillations in circuit activity. Gamma activity and cognitive performance often co-vary within tasks and between individuals, while cognitive deficits in psychiatric disorders such as autism and schizophrenia are linked to altered gamma frequency network dynamics** (Spellman and Gordon, 2014; Uhlhaas and Singer, 2012)**. Such disorders are also linked to changes in the efficacy of excitatory glutamatergic and inhibitory GABAergic synapses** (Lewis et al., 2012; Rubenstein and Merzenich, 2003)**. A critical and unresolved issue is the mechanistic relationship between gamma oscillations, the strength of excitation and inhibition, and circuit computations. On the one hand, neural codes based on firing rates may be sufficient for circuit computations** (Histed and Maunsell, 2014; Shadlen and Newsome, 1994)**. In this scenario gamma oscillations might index circuit activation, but would not be required for computation. Evidence that rate coded computations and gamma oscillations arise from shared circuit mechanisms could be interpreted to support this view** (Lundqvist et al., 2010; Pastoll et al., 2013)**, which predicts that when synaptic properties of a circuit are altered then gamma activity and the output of the rate-coded computation will co-vary. Alternatively, gamma oscillations, while sharing cellular substrates with rate-coded computations, may nevertheless support independent or multiplexed computational modes. For example, according to the communication through coherence hypothesis, tuning of gamma frequency activity may facilitate selective interactions between distant brain regions** (Fries, 2009)**. In this scenario independent control of rate coded computation and gamma activity would be beneficial, for example by allowing tuning of coherence without disrupting multiplexed rate-coded computations. However, it is unclear how this could be achieved in circuits where gamma and rate-coded computations share common synaptic mechanisms, as this would require variation in synaptic properties to differentially affect gamma activity and the rate coded computation.**

**We address these issues using a model that accounts, through a common synaptic mechanism, for gamma oscillations and spatial computation by neurons in layer II of the medial entorhinal cortex (MEC)** (Pastoll et al., 2013)**. The rate-coded firing of grid cells in the MEC is a well-studied feature of neural circuits for spatial cognition** (Moser and Moser, 2013)**. During exploration of an environment individual grid cells are active at multiple locations that together follow a hexagonal grid-like organization. At the same time MEC circuits generate periods of activity in the high gamma frequency range (60 – 120 Hz) nested within a slower theta (8 – 12 Hz) frequency network oscillation** (Chrobak and Buzsaki, 1998)**. Analysis of spatial correlations in grid firing, of manipulations to grid circuits, and recording of grid cell membrane potential in behaving animals, collectively point towards continuous two-dimensional network attractor states as explanations for grid firing** (Bonnevie et al., 2013; Domnisoru et al., 2013; Schmidt-Hieber and Häusser, 2013; Yoon et al., 2013)**. In layer II of the MEC, which has the highest known density of grid cells** (Sargolini et al., 2006)**, stellate cells that project to the dentate gyrus of the hippocampus are the major population of excitatory neurons** (Gatome et al., 2010)**. These excitatory (E) neurons do not contact one another directly but instead interact via intermediate inhibitory (I) neurons** (Couey et al., 2013; Dhillon and Jones, 2000; Pastoll et al., 2013)**. Models that explicitly incorporate this recurrent E-I-E connectivity can account for grid firing through velocity-dependent update of network attractor states** (Pastoll et al., 2013)**. When these models are implemented with excitable spiking neurons they also account for theta-nested gamma frequency network oscillations** (Pastoll et al., 2013)**. The influence in these, or other classes of attractor network models, of the strength of E-I or I-E connections on gamma oscillations and grid firing, or other attractor computations, has not been systematically investigated.**

**We find that while gamma oscillations and grid firing are both sensitive to the strength of excitatory and inhibitory connections, their relationship differs. Although their underlying synaptic substrates are identical, gamma activity nevertheless provides little information about grid firing or the presence of underlying network attractor states. Thus, gamma activity is not a good predictor of rate-coded computation. Unexpectedly, we find the range of E- and I- synaptic strengths that support gamma and grid firing is massively increased by moderate intrinsic noise through a mechanism involving suppression of seizure-like events. In the presence of moderate noise differences in synaptic strength can tune the amplitude and frequency of gamma across a wide range with little effect on grid firing. We obtain similar results in implementations of E-I models in which connectivity is probabilistic and in models extended to include additional I to I and E to E connections. Our results suggest constraints for extrapolation of differences in gamma activity to mechanisms for cognition, identify noise as a critical factor for successful circuit computation, and suggest that tuning of excitatory or inhibitory synaptic strength could be used to control gamma-dependent processes multiplexed within circuits carrying out rate coded computations.**

**Results**

**To systematically explore relationships between strengths of excitatory and inhibitory synapses, computations and gamma activity, we initially take advantage of models that account for both grid firing and theta-nested gamma oscillations through E-I-E interactions** (Pastoll et al., 2013)**. In these models a layer of E cells sends synaptic connections to a layer of I cells, which in turn feedback onto the E cell layer (Figure 1A). For attractor dynamics to emerge the strength of E and I connections are set to depend on the relative locations of neurons in network space (Figure 1B). While suitable connectivity could arise during development through spike timing-dependent synaptic plasticity** (Widloski and Fiete, 2014)**, here the connection profiles are fixed** (Pastoll et al., 2013)**. To vary the strength of excitatory or inhibitory connections in the network as a whole we scale the strength of all connections relative to a maximum conductance value (gE or gI for excitation and inhibition respectively)(Figure 1B). We also consider networks in which the connection probability, rather than its strength, varies according to the relative position of neurons in the network (Figure 1 – figure supplement 1). Each E and I cell is implemented as an exponential integrate and fire neuron and so its membrane potential approximates the dynamics of a real neuron, as opposed to models in which synaptic input directly updates a spike rate parameter. Addition of noise to a single E or I cell increases variability in its membrane potential trajectory approximating that seen in vivo (Figure 1C). Given that all neurons in the model are implemented as exponential integrate-and-fire neurons and that in total the model contains > 1.5 million synaptic connections, we optimized a version of the model to enable relatively fast simulation and automated extraction and analysis of generated data (see Methods). In this way the effect on grid firing of 31 x 31 combinations of gE and gI could be evaluated on a computer cluster in approximately one week.**

**Intrinsic noise increases the range of synaptic strengths that support grid firing**

**What happens to grid firing patterns when the strengths of excitatory and / or inhibitory synaptic connections in the model are modified? To address this we first evaluated grid firing while simulating exploration within a circular environment with a network from which noise sources were absent (Figure 2A). When we reduce the strength of connections from I cells by 3-fold and increase the strength of connections from E cells by 3-fold we find that grid firing is abolished (Figure 2Ab vs 2Aa). Exploring the parameter space of gE and gI more systematically reveals a relatively restricted region that supports grid firing (Figure 2D and Figure 2 – figure supplement 1A-D). Rather than the required gI and gE being proportional to one another, this region is shifted towards low values of gI and high gE. Thus, the ability of recurrently connected networks to generate grid fields requires specific tuning of synaptic connection strengths.**

**Because neural activity in the brain is noisy** (Faisal et al., 2008; Shadlen and Newsome, 1994)**, we wanted to know if the ability of the circuit to compute location is affected by noise intrinsic to each neuron (Figure 1C). Given that continuous attractor networks are often highly sensitive to noise** (Eliasmith, 2005; Zhang, 1996)**, we expected that intrinsic noise would reduce the parameter space in which computation is successful. In contrast, when we added noise with standard deviation of 150 pA to the intrinsic dynamics of each neuron, we found that both configurations from Figure 2Aa,b now supported grid firing patterns (Figure 2Ba,b). When we considered the full space of E and I synaptic strengths in the presence of this moderate noise we now found a much larger region that supports grid firing (Figure 2E and Figure 2 – figure supplement 1E-H). This region has a crescent-like shape, with arms of relatively high gI and low gE, and low gI and high gE. Thus, while tuning of gI and gE continues to be required for grid firing, moderate noise massively increases the range of gE and gI over which grid fields are generated.**

**When intrinsic noise was increased further, to 300 pA, the parameter space that supports grid firing was reduced in line with our initial expectations (Figure 2Ca,b, F and Figure 2 – figure supplement 1I-L). To systematically explore the range of gE and gI over which the network is most sensitive to the beneficial effects of noise we subtracted grid scores for simulations with 150 pA noise from scores with deterministic simulations (Figure 2G). This revealed that the unexpected beneficial effect of noise was primarily in the region of the parameter space where recurrent inhibition was strong. In this region, increasing noise above a threshold led to high grid scores, while further increases in noise progressively impaired grid firing (Figure 2H). In probabilistically connected networks, the range of gE and gI supporting grid firing was reduced, but the shape of the parameter space and dependence on noise was similar to the standard networks (Figure 2 – figure supplement 2), indicating that the dependence of grid firing on gE and gI, and the effects of noise, are independent of the detailed implementation of the E-I attractor networks.**

**How closely does the firing of I cells in the simulated networks correspond to inhibitory activity in behaving animals, and to what extent is the pattern of I cell firing affected by gE, gI and noise? While there is little data on the spatial firing of interneurons in the MEC, recent evidence indicates that the majority of parvalbumin positive interneurons have firing fields with significant spatial stability, but low spatial sparsity and grid scores compared to excitatory grid cells** (Buetfering et al., 2014)**. A possible interpretation of these data is that parvalbumin positive cells are unlikely to fulfill the roles of I cells predicted in E-I models. However, in networks that we evaluate here in which E cells have grid firing fields in the presence of moderate noise, I cell firing fields also have a much lower spatial information content and spatial sparsity than the corresponding E cell firing fields (E cells: spatial sparsity 0.788 ± 0.061, spatial information: 1.749 ± 0.32 bits/spike; I cells: spatial sparsity 0.239 ± 0.018, spatial information 0.243 ± 0.024 bits/spike; p < 10-16 for comparisons of both spatial sparsity and information; paired t-test; data range is indicated as mean ± standard deviation)(Figure 2A-C and Figure 2 – figure supplement 3). Spatial autocorrelograms of simulated I cell firing fields also do not contain the six hexagonally organized peaks that are characteristic of grid fields (Figure 2A-C). Nevertheless, I cell spatial autocorrelograms produce positive grid scores (0.39 ± 0.16; Figure 2 – figure supplement 4), although these are reduced compared to scores for the E cells in the same networks (E cells: 0.796 ± 0.157; p < 10-16; paired t-test; mean ± SD) and in many networks are below the threshold considered previously to qualify as grid like (cf. figure 4B of Buetfering et al., 2014). When we evaluated the dependence of I cell spatial firing on gE, gI and noise, it appeared to be similar to that of E cells (Figure 2 – figure supplement 4). To assess whether grid scores of I cells can be reduced further in E-I networks while maintaining grid firing by E cells, we investigated networks in which uncorrelated spatial input is applied to each I cell (Figure 2 – figure supplement 5). In these simulations E cells had grid scores of 0.57 ± 0.25, spatial sparsity of 0.78 ± 0.03 and spatial information of 1.69 ± 0.18 bits/spike, whereas I cells have grid scores of 0.16 ± 0.2 (p < 10-16, paired t-test), spatial sparsity of 0.21 ± 0.01 (p < 10-16, paired t-test) and spatial information of 0.2 ± 0.01 bits/spike (p < 10-16, paired t-test; range of all data sets is mean ± SD). Thus, spatial firing of I cells has a similar dependence on noise, gE and gI to grid cells, conventional indices of spatial firing are nevertheless much lower for I cells in E-I networks compared to E cells, and grid firing by E cells in E-I networks is relatively robust to disruption of the rotational symmetry of I cell firing fields.**

**Together these simulations demonstrate that attractor circuit computations that generate grid firing fields require specific tuning of gE and gI. In the absence of noise grid firing is supported in relatively restricted regions of parameter space. Optimal levels of noise, which produce single cell membrane potential fluctuations of a similar amplitude to experimental observations, promote grid firing by reducing the sensitivity of grid computations to the strength of recurrent synaptic connections, particularly when inhibition is relatively strong and excitation is weak.**

**Differential sensitivity of gamma oscillations and grid firing to the strength of E and I synapses**

**Is the sensitivity of gamma frequency oscillations to synaptic strength and to noise similar to that of grid firing? To evaluate gamma activity we recorded synaptic currents from single E and I cells across multiple theta cycles (Figure 3A-C). For the network configurations illustrated in Figure 2Aa,b and in which intrinsic noise is absent, we observed synaptic events entrained to theta cycles (Figure 3Aa,b). However, the timing and amplitude of synaptic events typically differed between theta cycles and no consistent gamma rhythm was apparent. In contrast, in the presence of noise with standard deviation 150 pA we observed nested gamma frequency synaptic activity with timing that was consistent between theta cycles (Figure 3Ba). In this condition the frequency of the gamma oscillations was reduced and their amplitude increased by raising gI and lowering gE (Figure 3Bb). With a further increase in noise to 300 pA, gamma activity remained entrained to theta cycles, but became less ordered (Figure 3Ca,b).**

**To explore gamma activity across a wider range of gI and gE we automated quantification of the strength and frequency of oscillatory input to E cells (see Methods). In the absence of noise gamma frequency activity only occurred for a narrow range of gI and gE (Figure 3D). Strikingly, following addition of moderate noise the region of parameter space that supports gamma activity was massively expanded (Figure 3E). Within this space, the amplitude of gamma increased with increasing inhibition, whereas the frequency was reduced. As noise is increased further the amplitude and frequency of gamma oscillations are reduced (Figure 3F). We found a similar dependence of gamma oscillations on noise, gE and gI in networks with probabilistic connectivity (Figure 3 – figure supplement 1). Thus, intrinsic noise modifies the amplitude and frequency of nested gamma oscillations.**

**To determine whether there is a systematic relationship between values of gE and gI that generate gamma and grid firing we compared the gridness score and gamma scores for each circuit configuration (Figure 3G, Figure 3 – figure supplements 2 and 3). We found this relationship to be complex and highly sensitive to noise. However, we did not find any evidence for strong linear relationships between gamma amplitude or gamma frequency and grid score (R2 < 0.12 for all comparisons), while gamma amplitude and frequency provided only modest amounts of information about grid scores (0.27 < MIC < 0.33 and 0.27 < MIC < 0.37 respectively). The relationship between noise intensity and gamma differed from that for grid computations. Whereas, grids emerged above a sharp noise threshold (Figure 2H), for the same regions in parameter space the frequency and amplitude of gamma oscillations varied smoothly as a function of noise (Figure 3H). Thus, neither the frequency nor the power of gamma appears to be a good predictor of grid firing.**

When we considered only regions of parameter space that generate robust grid fields (grid score > 0.5), we found circuits generating almost the complete observed range of gamma amplitudes (0.02 < autocorrelation peak < 0.59) and frequencies (31 Hz < frequency < 102 Hz)( **Figure 3 – figure supplement 4**). For example, considering the crescent shaped region of E-I space that supports grid firing in the presence of intermediate noise (the region within the isocline in Figure 3E), when **gI** is high and **gE** low then the amplitude of gamma is relatively low and the frequency high. Moving towards the region where **gI** is high and **gE** is low, the amplitude of gamma is increased and the frequency is reduced. Thus, variation of synaptic strength across this region of E-I space can be used to tune the properties of gamma activity while maintaining the ability of the network to generate grid fields.

**Together these data indicate that an optimal level of noise promotes emergence of gamma oscillations, while the properties of oscillations may depend on the relative strength of synaptic connections. The relationship between gamma and synaptic strength differs to that for grid computations. Strikingly, while gamma activity provides relatively little information about grid firing, differential sensitivity of gamma and grid firing to gE and gI provides a mechanism for circuits to tune gamma frequency activity while maintaining the ability to compute rate coded grid firing fields.**

**Noise promotes attractor computation by opposing seizures**

Given the emergence of a large parameter space that supports grid firing following introduction of moderate noise, we were interested to understand how noise influences the dynamics of the E-I circuits. One possibility is that in networks that fail to generate grid firing fields network attractor states form, but their activity bumps are unable to track movement. In this scenario disrupted grid firing would reflect incorrect control of network activity by velocity signals. Alternatively, deficits in grid firing may reflect failure of network attractor states to emerge. To distinguish these possibilities we investigated formation of activity bumps in network space over the first 10 s following initialization of each network (Figure 4).

Our analysis suggests that the deficit in grid firing in deterministic compared to noisy networks reflects a failure of attractor states to emerge. For deterministic simulation of the points in parameter space considered in Figure 2Aa, which are able to generate grid patterns, we found that a single stable bump of activity emerged over the first 2.5 s of simulated time (Figure 4Aa). In contrast, for deterministic simulation of the point considered in 2Ab, which in deterministic simulations did not generate grid patterns, a single stable bump fails to emerge (Figure 4Ab). Quantification across the wider space of **gE** and **gI** values (see Methods) indicated that when **gI** is low there is a high probability of a bump formation as well as grid firing, whereas when **gI** is high the probability of both is reduced (Figure 4B). In contrast to the deterministic condition, for circuits with intrinsically noisy neurons activity bumps emerged in the first 1.25 s following initialization of the network (Figure 4Ac-e) and the area of parameter space that supported bump formation was much larger than that supporting grid firing (Figure 4B). Plotting gridness scores as a function of bump probability indicated that bump formation was necessary, although not sufficient for grid formation (Figure 4C), while plotting the first autocorrelation peak as a function of bump probability supported our conclusion that grid computation and gamma activity are not closely related (Figure 4D). Together, these data indicate that noise promotes formation of attractor bumps in network activity and in deterministic simulations the failure of the circuit to generate attractor states largely accounts for disrupted grid firing.

In noisy networks the presence of low grid scores for networks with high bump scores (Figure 4C) is explained by sensitivity of these network configurations to noise-induced drift. This is illustrated by the region of parameter space from Figure 2Ab, where **gI** is relatively high and **gE** relatively low, and which in deterministic simulations fails to generate bumps or grids. With moderate noise, this point generates bumps that show little drift (Figure 4Ac), whereas as noise is increased further the bump begins to drift (Figure 4Ae). In contrast, at the point illustrated in Figure 2Aa, which forms grids and bumps in the presence or absence of noise, activity bumps are stable in each condition (Figure 4Aa). Thus, intrinsic noise has two opposing effects on bump formation. For much of the parameter space we consider moderate noise promotes emergence of bumps and grids, while across all of parameter space noise reduces bump stability leading to deterioration of grids.

To investigate how addition of noise promotes emergence of network attractor states we investigated the dynamics of neurons in the simulated circuits. We focus initially on the point in parameter space identified in Figure 2Ab, where grids are found in the presence of moderate noise, and bumps are found when noise is moderate or high. When we examined times of action potentials generated by all neurons in this circuit, we find that in the absence of noise the network generates hyper-synchronous seizure-like states at the start of each theta cycle (Figure 5A and **Figure 5 – figure supplement 1A**). The number of E cells active on each theta cycle differs, but their activity is typically restricted to the rising phase of theta, and there is no consistent structure in the pattern of activated neurons. The number of simultaneously active I cells is also greatest at the start of each theta cycle. The I-cells continue to fire over the theta cycle, but their synchronization declines. When moderate noise is added to the circuit only a subset of E-cells are active on each theta cycle, forming an activity bump (Figure 5B and **Figure 5 – figure supplement 1B**). The I-cells are active at gamma frequency and the formation of an activity bump in the E-cell population is reflected by an inverted bump in the I-cell population activity (Figure 5B). With increased noise there is a similar overall pattern of activity, but spike timing becomes more variable, causing the bumps to drift and reducing the degree of synchronization at gamma frequencies (Figure 5C and **Figure 5 – figure supplement 1C**).

To determine whether these changes in network dynamics are seen across wider regions of parameter space we first quantified the presence of seizure like events from the maximum population firing rate in any 2 ms window over 10 s of simulation time (E-ratemax). Strikingly, we found that in the absence of noise epochs with highly synchronized activity were found for almost all combinations of **gE** and **gI**, whereas these seizure-like events were absent in simulations where noise was present (Figure 5D). Interestingly, while grids emerge in deterministic networks in regions of E-I space where E-ratemax is relatively low, there is a substantial region of parameter space in which E-ratemax is > 400 Hz, but grids are nevertheless formed. It is possible that seizure-like states may be rare in this region of parameter space and so do not interfere sufficiently with attractor dynamics to prevent grid firing. To test this we calculated for each combination of **gE** and **gI** the probability per theta cycle of events with population-average rate > 300 Hz (PE-rate > 300). For values of **gE** and **gI** where grid fields are present PE-rate > 300 was relatively low, indicating that seizure-like events are indeed rare (Figure 5E). Consistent with this, when we plotted grid score as a function of PE-rate > 300, we found that P\_E-rate > 300 was relatively informative about the gridness score in networks without noise (MIC = 0.624) and a low value of PE-rate >300 was necessary for grid firing (Figure 5F). In contrast, E-ratemax was less informative of grid firing (0.392 <= MIC <= 0.532) and a wide range of values were consistent with grid firing (Figure 5F). Thus, while grid firing is compatible with occasional seizure-like events, when seizure-like events occur on the majority of theta cycles then grid firing is prevented.

**Because seizure-like events tend to initiate early on the depolarizing phase of each theta cycle, we asked if synchronization by theta frequency drive plays a role in their initiation. When theta frequency input was replaced with a constant input with the same mean amplitude, the power of gamma oscillations was still dependent on the levels of noise and changes in gE and gI (Figure 6 – figure supplement 1). However, in contrast to simulations with theta frequency input (Figure 5D,E), noise-free networks without theta exhibited hyper-synchronous firing only when gE was < 0.5 nS (Figure 6A) and generated grid firing fields almost in the complete range of gE and gI (Figure 6D,G). Addition of noise in the absence of theta had mostly detrimental effects on grid firing (Figure 6E,F,H,I and Figure 6 – figure supplement 2). Interestingly, with intermediate levels of noise, the subregion with high gridness scores (> 0.5) retained its crescent-like shape (Figure 6E,H), but was smaller when compared to the networks with theta frequency inputs (size of regions with and without theta: 488/961 vs. 438/961), while the range of gamma frequencies present was much lower than in networks containing theta drive. Together, these data indicate that moderate noise prevents emergence of seizure like states by disrupting synchronization of the attractor network by the shared theta frequency drive. In networks with moderate noise theta drive promotes grid firing and enables a wide range of gamma frequencies to be generated without disrupting grid firing.**

**Our analysis points towards suppression of seizure-like events as the mechanism by which moderate noise promotes grid firing, while interactions between noise and theta appear important for the capacity to multiplex grid firing with a wide range of gamma frequencies. However, we wanted to know if other factors might contribute to these beneficial roles of noise. Grid fields may also fail to form if overall activity levels are too low, in which case neurons with grid fields instead encode head direction** (Bonnevie et al., 2013)**. This observation is unlikely to explain our results as the mean firing rate of E cells in networks that generated grid firing fields (grid score > 0.5, networks with gE or gI set to 0 excluded) was in fact lower than the firing rate of networks without grid fields (1.2; 1.0; 1.0 Hz grid fields vs. 3.0; 2.7; 1.2 Hz no grid fields, in networks with σ = 0; 150; 300 pA respectively). There was also no systematic relationship between grid score and firing frequency (Figure 6 – figure supplement 3). We also wanted to know if other properties of grid fields vary as a function of gE and gI. Parameters used to calibrate velocity integration by the grid network varied very little with changes in gE and gI (Figure 6 – figure supplement 4), whereas drift increased with gI (Figure 6 – figure supplement 5) and place cell input was most effective in opposing attractor drift in noisy networks with high gridness scores (Figure 6 – figure supplement 6). These data are consistent with suppression of seizure like events as the mechanism by which noise promotes grid firing, while interactions between noise and theta frequency inputs profoundly influence the dynamics of attractor networks that generate grid fields.**

**Recurrent inhibition increases the frequency of gamma activity and promotes grid firing**

**Our analysis so far focuses on E-I attractor networks as simple models of grid firing that are compatible with the finding that stellate cells in layer 2 of the MEC are only able to interact indirectly via inhibitory interneurons** (Couey et al., 2013; Dhillon and Jones, 2000; Pastoll et al., 2013)**. However, there is evidence that interneurons active during theta-nested gamma activity make connections to one another as well as to stellate cells** (Pastoll et al., 2013)**. To establish whether this recurrent inhibition substantially modifies our conclusions from simpler E-I networks, we extended the E-I model to also include synapses between interneurons (see Methods). In the resulting E-I-I networks, in the absence of noise, grid firing emerges across a much larger region of parameter space compared to E-I networks (Figure 7A, Figure 7 – figure supplements 1-4). However, as in E-I networks occasional seizure like activity was present across a wide range of gE and gI (Figure 7 – figure supplement 5), and gamma frequency activity was largely absent (Figure 7D, G). Following addition of noise with standard deviation of 150 pA to E-I-I networks, grid firing was maintained, seizure like activity was abolished, and gamma like activity emerged (Figure 7B, E, H and Figure 7 – figure supplement 5). Increasing the noise amplitude to 300 pA reduced grid firing and interfered with the emergence of gamma oscillations (Figure 7C, F, I and Figure 7 – figure supplements 1-5). Importantly, just as in E-I networks, the presence of moderate noise in E-I-I networks enables tuning of gamma activity by varying gE and gI while maintaining the ability of the networks to generate grid firing fields. Gamma activity had a higher frequency in E-I-I compared to E-I networks, with a greater proportion of the parameter space supporting gamma frequencies > 80 Hz. This higher frequency gamma is similar to fast gamma observed experimentally in the MEC** (cf. Chrobak and Buzsaki, 1998; Colgin et al., 2009; Pastoll et al., 2013)**. Thus, by including additional features of local circuits in layer 2 of the MEC, E-I-I models may more closely recapitulate experimental observations. Nevertheless, E-I-I networks maintain the ability, in the presence of moderate noise, for variation in gE and gI to tune gamma oscillations without interfering with grid firing.**

Finally, we asked if addition of synaptic connections between excitatory cells modifies the relationship between gamma, noise, **gE and gI**. While the E-I model is consistent with the connectivity between stellate cells in layer 2 of the MEC, adjacent pyramidal cells may also have grid firing properties. Unlike stellate cells, pyramidal cells interact with one another directly via excitatory connections and indirectly via inhibitory interneurons (Couey et al., 2013). To assess the impact of E-E connections, we first extended the E-I model to allow each E cell to excite other E cells that are nearby in neuron space. The dependence of grid firing, gamma oscillations, and bump formation on noise, **gE and gI** was similar to E-I networks (Figure 7 – figure supplements 6-9). We also attempted to evaluate networks in which E-E connections were structured, but E-I and I-E connections were uniformly distributed. However, in these networks we were unable to identify parameters that support formation of stable activity bumps (Figure 7 – figure supplement 10). This is consistent with instability of simpler network attractors based on E-E connections (Seung et al., 2000).

**Discussion**

We investigated the relationship between rate coded spatial computations and nested gamma oscillations in attractor network models of grid firing. While rate coding and gamma oscillations share the same neural substrate, we find that their sensitivity to variations in excitatory and inhibitory synaptic strengths nevertheless differs. A moderate level of noise promotes generation of both grid fields and nested gamma oscillations, primarily by the disruption of epileptic-like firing of E and I cells in the network. When the strength of E or I connections is varied in the presence of moderate noise a wide range of gamma frequency and power can be obtained without affected grid firing. Thus, noise can be beneficial for computations performed by the nervous system, while the frequency and power of multiplexed gamma oscillations can be tuned independently of rate-coded grid computations, suggesting a mechanism for differential control of multiplexed neural codes.

Our results suggest a novel beneficial role for noise. In general noise in the nervous system is believed to distort the fidelity of transmitted signals (Faisal et al., 2008). Exceptions are stochastic resonance phenomena in which noise promotes detection of small amplitude signals by individual neurons (Benzi et al., 1999; Longtin et al., 1991; Shu et al., 2003), improvements in signal coding through desynchronization of neuronal populations (Hunsberger et al., 2014) and emergence of stochastic weak synchronization in interneuron networks (Tiesinga and Jose, 2000). The beneficial role for noise that we identify here differs in that it emerges through interactions between populations of neurons and in that the grid cell attractor network performs a computation – generation of a spatial code from velocity inputs - rather than propagating input signals. We find that by opposing emergence of hyper-sychronous seizure-like states noise allows the network to generate stable bump attractor states. Noise prevents the seizure-like states by desynchronizing neuronal responses to common theta input. We were able to identify this role for noise because spiking and synaptic dynamics are explicitly represented in the simulated network. These dynamics are absent from other attractor network models of grid firing (Burak and Fiete, 2009; Fuhs and Touretzky, 2006; Guanella et al., 2007)**.** They are also absentfrom other models of theta-nested gamma oscillations that simulate two-dimensional dynamical systems of E and I populations with theta modulated inputs to the network (Onslow et al., 2014). Thus, intrinsic cellular and synaptic dynamics in conjunction with noise sources may be important in accounting for computations and oscillatory activity in neural networks.

The distinct control of rate coded grid computations and gamma oscillations by noise, **gE and gI** was independent of the detailed implementation of the E-I models we considered and was maintained in more complex models incorporating I-I and E-E coupling. Current available experimental data appears to be insufficient to distinguish between these different models. For example, our analysis of interneuron firing indicates that while E-I models predict that interneurons will have spatial firing fields, they have **lower spatial information content, spatial sparsity and grid scores than E cells and therefore** may be difficult to detect in existing experimental datasets and with current analysis tools. Thus, evidence previously interpreted to argue against E-I models for grid firing may in fact not distinguish this from other possible mechanisms. Our results are consistent with local synaptic connections, in addition to those between E cells and I cells, having important functional roles. For example addition of synapses between interneurons to E-I networks causes an overall increase in the frequency of gamma activity and in the stability of grid firing. Nevertheless, we find that in these modified networks moderate noise is still required for variation in **gE and gI** to tune gamma oscillations independently from grid firing.

An intriguing aspect of our results is that they suggest novel approaches to suppressing seizures and to promoting normal cognitive function. Seizures have previously been suggested to result from deficits in inhibition or from alterations in intrinsic excitability of neurons (Lerche et al., 2001; Treiman, 2001). We show that seizures can be induced when these properties are held constant simply by reducing levels of noise within a circuit. A future experimental challenge for dissecting the contribution of intrinsic noise to seizures will be to target biological noise sources. In the brain noise arises from ion channel gating and from background synaptic activity. It is therefore difficult to manipulate noise sources without also affecting intrinsic excitability or excitation-inhibition balance. However, it may be feasible to add noise to circuits through transcranial magnetic stimulation (Ruzzoli et al., 2010). In this case our simulations predict that addition of noise may restore epileptic circuits to normal activity. This mechanism may explain why transcranial magnetic stimulation of the entorhinal cortex in patients with seizures leads to an enhancement of memory performance (Suthana et al., 2012).

While correlations between gamma oscillations and various cognitive and pathological brain states are well established, the proposed computational roles of gamma oscillations have been difficult to reconcile with rate-coded representations with which they co-exist. We were able to address this issue directly by analyzing a circuit in which gamma oscillations and rate-coded computations arise from a shared mechanism. Rather than gamma serving as an index of rate-coded computation, we find instead that there is a substantial parameter space across which rate-coded computation is stable, while the amplitude and frequency of theta-nested gamma oscillations varies. Our analysis leads to several new and testable predictions. First, tuning of recurrent synaptic connections could be used to modify gamma oscillations without affecting rate-coded computation. If multiple networks of the kind we simulate here correspond to grid modules providing input to downstream neurons in the hippocampus (Stensola et al., 2012), then adjusting **gE** or **gI** would alter gamma frequency with minimal effect on the grid firing pattern of each module. If the downstream neurons integrate input at the gamma time scale, then this should lead to re-mapping of their place representation in the absence of any change in either the strength of their synaptic inputs or the information they receive from upstream grid cells. Adjustment of **gE** and **gI** could be achieved dynamically through actions of neuromodulators (Marder, 2012), or on slower developmental time scales (Widloski and Fiete, 2014). Second, subtle differences in gamma could be a sensitive index of network pathology at stages before deficits in rate coded computation are apparent. If cognitive deficits in psychiatric disorders reflect a failure of rate coded computation, then our analysis predicts that a change in noise within a circuit, in addition to synaptic modification, may be necessary for deficits to emerge. From this perspective it is intriguing that seizure phenotypes are often associated with disorders such as autism (Deykin and MacMahon, 1979). Alternatively, cognitive deficits may result from a failure to coordinate gamma frequency synchronization of circuits that converge on downstream targets. In this case we expect cognitive deficits to be phenocopied by manipulations that affect gamma frequency or power without influencing rate-coded computations (Sigurdsson et al., 2010; Spellman and Gordon, 2014)**.**

In conclusion, our systematic exploration of three dimensions of parameter space (**gE**, **gI** and intrinsic noise) illustrates the complexity of relationships between rate-coded computation, gamma frequency oscillations and underlying cellular and molecular mechanisms. Our results highlight the challenges in straightforward interpretation of experiments in which these parameters are correlated to one another, (cf. Wang and Krystal, 2014). While there are parallels to investigations of pace-making activity in invertebrate circuits (Marder and Taylor, 2011), which demonstrate that many parameter combinations can account for higher order behavior, there are also critical differences in that the models we describe account for multiplexing of rate-coded computation and oscillatory activity, while the number of neurons and connections in the simulated circuit is much larger. Future experimentation will be required to test our model predictions for unexpected beneficial roles of noise and for control of gamma oscillations independently from grid firing by modulating the strength of excitatory and inhibitory synaptic connections.

**Methods**

**The model comprised a network of exponential integrate and fire neurons** (Fourcaud-Trocmé et al., 2003) **implemented as a custom-made module of the NEST simulator** (Gewaltig and Diesmann, 2007)**. The network investigated in the majority of simulations (Figures 1-6) is modified from that in Pastoll et al. 2013 and consists of excitatory (E) and inhibitory (I) populations of neurons that were arranged on a twisted torus with dimensions of 34 x 30 neurons. In networks where connection strengths were generated probabilistically instead in an all-to-all way, the synaptic weights from E to I cells and vice versa were constant, while the probability of connection between the pre- and post-synaptic neuron was drawn according to Figure 1B. In addition, some networks also included direct uniform recurrent inhibition between I cells (Figure 7; referred to as E-I-I networks) or direct structured recurrent excitation between E cells (Figure 7 – figure supplements 6 – 10). When recurrent excitation was present, synaptic weights between E cells followed the connectivity profile in which the strongest connection was between cells that were close to each other in network space (Figure 1B) and the weights between E and I cells were generated either according to synaptic profiles from Figure 1B (Figure 7 – figure supplements 6 – 9) or the E-I connectivity was uniform with a probability of connection of 0.1 (Figure 7 – figure supplement 10). In order to oppose drift of the activity bump in networks that simulated exploration of the arena E cells received input from cells with place-like firing fields simulated as Poisson spiking generators with their instantaneous firing rate modeled as a Gaussian function of the animal position. Full details of the connectivity and network parameters are in the Supplementary Methods.**

**In all simulations the networks were parameterized by the standard deviation of noise (σ) injected independently into each E and I cell and by synaptic scaling parameters (gE and gI). Noise was sampled from a Gaussian distribution with standard deviation either set to σ = 0, 150 or 300 pA, or alternatively in the range of 0-300 pA in steps of 10 pA (Figure 2H and 3H). The peaks of the synaptic profile functions (Figure 1B) were determined by the gE and gI parameters that appropriately scaled the maximal conductance values of the excitatory and inhibitory connections respectively.**

**Gridness scores were estimated by simulating exploration in a circular arena with a diameter of 180 cm. For each value of gE and gI the simulations consisted of two phases. In the first phase, animal movement with constant speed and direction (vertically from bottom to top) was simulated in order to calibrate the gain of the velocity input to achieve 60 cm spacing between grid fields in the network. In the second phase, the calibrated velocity input gains were used during a simulation of realistic animal movements with duration of 600 s. Each simulation was repeated 1-4 times. For each trial, gridness score was then estimated from an E or I cell located at position (0, 0) on the twisted torus. In simulations where interneurons received uncorrelated spatial inputs (Figure 2 – figure supplement 5), gridness scores were estimated from 100 randomly selected E and I cells on the twisted torus.**

**For the analysis of bump attractor properties and gamma oscillations a separate set of simulations were run. For each value of gE, gI and noise level, there were 5 trials of 10 s duration during which the velocity and place cell inputs were deactivated. For each trial spiking activity of all cells were recorded. In addition, inhibitory synaptic currents of 25 randomly selected E cells were saved and used for further analysis.**

**The strength and frequency of gamma oscillation were estimated from the inhibitory synaptic currents recorded from E cells. The currents were first band-pass filtered between 20 and 200 Hz. For each trace, autocorrelation function was computed and the first local maximum was detected using a custom-implemented peak detection algorithm. The strength and frequency of gamma oscillation was estimated from the correlation value and lag at the position of the local maximum respectively.**

**Properties of bump attractors were estimated by fitting symmetric Gaussian functions onto successive snapshots of firing rates of each cell in the E population. For each snapshot this procedure yielded the position of the bump center and its width. The probability of bump formation was then estimated as a proportion of population-activity snapshots that were classified as bump attractors, i.e. those fitted Gaussian functions whose width did not exceed the shorter side of the twisted torus. Other properties of bump attractors were estimated by analyzing successive positions of the bump attractor centers. Action potential raster plots of E and I populations (Figure 5A-C, Figure 5 – figure supplement 1 and Figure 7 – figure supplement 10) show neuron indices that are flattened in a row-wise manner with respect to the two-dimensional twisted torus. Data points with white color in Figure 5D,E and Figure 5 – figure supplement 1A have been excluded from analysis since the maximal firing rate of E cells exceeded 500 Hz/2ms window.**

**The calculation of the maximal information coefficient for the relationship between gridness score, gamma and bump scores was estimated by applying the maximal information coefficient measure (MIC) using the minepy package** (Albanese et al., 2013)**. Calculations of spatial information were carried out according to** (Skaggs et al., 1996)**. Spatial sparsity was calculated by following the procedure outlined in** (Buetfering et al., 2014)**. All other data analysis and simulations were performed in Python.**

**Competing interests**

**None**

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**Figure titles and legends**

**Figure 1. Attractor network model with feedback inhibition and theta frequency inputs**

(A) A schematic of populations of excitatory cells (E cells, red) and inhibitory cells (I cells, blue) on a twisted torus of size 34x30 neurons. The synaptic coupling between the two populations was parameterized by the inter-population peak synaptic conductances **gE** (E -> I synapses) and **gI**(I -> E synapses).

(B) Top: Plots illustrate peak synaptic conductances of E (red) and I (blue) synapses as a function of the distance between pre- and post-synaptic neurons. Bottom: Distributions of synaptic weights from all I cells onto an E cell in the model (left) and from all E cells onto an I-cell (right). Parameters **gI** and **gE** determine maximal values of these distributions.

(C) Examples of the membrane potential of an isolated E cell during two consecutive theta cycles in networks without noise (white noise input current standard deviation σ = 0 pA), with an intermediate amount of noise (σ = 150 pA) and with noise levels doubled (σ = 300 pA). Theta signal is illustrated in grey.

**Figure 2. Noise increases the range of synaptic strengths that support grid firing.**

(A-C) Example spatial firing fields (left) and spatial autocorrelation plots (right) of E and I cells for networks without noise (A; σ = 0 pA), with noise level set to σ = 150 pA (B), and noise level set to σ = 300 pA (C) and with the strengths of recurrent synaptic connections indicated by arrows in (D-F). Maximal firing rate is indicated in the top right of each spatial firing plot. The range of spatial autocorrelations is normalized between 0 and 1.

(D-F) Gridness score as a function of **gE** and **gI** for networks with each noise level. Each item in the color plot is an average gridness score of four simulation runs. Arrows indicate the positions of grid field and autocorrelation examples from simulations illustrated in (A-C). Simulations that did not finish in a specified time interval (5 h) are indicated by white color.

(G) Difference between gridness scores of networks with σ = 150 pA and networks with σ = 0 pA plotted as a function of **gE** and **gI**.

(H) Gridness score plotted as a function of the standard deviation of intrinsic noise. Each noise level comprises simulations from a neighborhood of **gE** and **gI** surrounding a center point in the parameter space (center included) indicated by arrows in (D-F).

**Figure 3. Differential sensitivity of gamma oscillations and grid fields to changes in the strength of E and I synapses.**

(A-C) Examples of inhibitory (red) and excitatory (blue) synaptic currents recorded respectively from excitatory and inhibitory neurons from simulations highlighted by arrows in panels (D-F).

(D-F) *Top:* Correlation value at the first local maximum of the autocorrelation of inhibitory synaptic currents (I 🡪 E cells, 25 randomly selected E cells), plotted as a function of **gE** and **gI**, for networks without noise (D), with noise level set to σ = 150 pA (E), and noise level set to σ = 300 pA (F). Each point is an average over five simulation trials. In these simulations velocity and place cell inputs were disabled. The duration of simulations was 10 seconds. *Bottom:* Frequency corresponding to the peaks of the autocorrelation functions for simulations in the top panels. Black lines in (E) indicate the region from Figure 2E where the gridness score = 0.5.

(G) Scatter plots show gridness score as a function of gamma oscillation strength (top) and frequency (bottom) for simulations with noise absent (green), with an intermediate level of noise (red) and highest simulated noise level (blue). Each dot represents data from a single network configuration.

(H) Top: Gamma oscillation strength plotted as a function of standard deviation of the noise current. Grey color indicates simulations with **gE** = 3 nS, **gI** = 1 nS (a). Red color indicates simulations with **gE** = 1 nS, **gI** = 3 nS (b). Bottom: Frequency corresponding to the detected autocorrelation peak.

**Figure 4. Noise promotes formation of continuous attractors.**

(A) Examples of snapshots of network activity of E cells from simulations in which velocity and place cell inputs are inactivated. Each row shows a simulation trial with a value of **gE** and **gI** highlighted by an arrow in panel (B). The corresponding probability of bump formation (P(bumps)) and the maximal firing rate is indicated to the left and right, respectively.

(B) Color plots show probability of bump formation (P(bumps)), for the simulated range of **gE** and **gI** and the three simulated noise levels. Each color point is an average of five 10 s simulation runs. Arrows show positions in the parameter space of examples in (A). Black lines indicate the regions where the gridness score = 0.5 (cf. Figure 2D-F).

(C) Relationship between gridness score computed from the grid field simulation runs (Figure 2D-F) and the probability of bump formation (B).

(D) Relationship between gamma oscillation strength (Figure 3D-F) and the probability of bump formation (B). Each color in (C and D) represents one noise level and each dot in the scatter plots corresponds to simulations of a single pair of values of gE and gI.

**Figure 5. Noise opposes generation of seizure-like states.**

(A-C) Raster plots show activity of all neurons in the excitatory (red) and inhibitory (blue) populations for the duration of two theta cycles (top), along with the average population firing rates for both populations (center and bottom; calculated with a sliding rectangular window with 2 ms duration and 0.5 ms time step), for networks where noise is absent (A; σ = 0), with noise set to σ = 150 pA (B), and with noise set to σ = 300 pA (C). Simulations were performed in the absence of animal movement and place cell input; **gE** = 1 nS and gI = 3 nS.

(D) Maximal average population firing rate of E cells estimated from the whole simulation run (10 s; 500 ms at the beginning of the simulation excluded) for each simulated level of noise. Each point is an average of maxima from 5 simulation runs.

(E) Probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz, i.e. at least 60% of E cells firing synchronously within a time period of 2 ms in the parameter space of **gE** and gI when σ = 0 pA. Black lines indicate regions where gridness score equals 0.5.

(F) Scatter plots show the relationship between gridness score and the maximal firing rate during the simulation (left) and the probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz (right).

**Figure 6. Seizure-like states and grid firing fields in networks without theta frequency inputs.**

(A-C) Maximal average population firing rate of E cells estimated from the whole simulation run (10 s; 500 ms at the beginning of the simulation excluded) for each simulated level of noise indicated by σ, in networks with theta frequency inputs replaced with a constant input with the same mean amplitude. Each point is an average of maxima from 5 simulation trials. Black lines indicate the regions from (G-H) where gridness score = 0.5.

(D-F) Example spatial firing fields (left) and autocorrelation plots (right) for the specific values of **gE** and gI indicated by arrows in (G-I), corresponding to the three simulated noise levels. Maximal firing rate is indicated at the top right of each spatial firing plot. The range of spatial autocorrelations is normalized between 0 and 1.

(G-I) Gridness score as a function of **gE** and **gI**, for each simulated level of noise. Each item in the color plot is an average gridness score of three simulation runs of 600 s duration. Arrows indicate the positions of grid field and autocorrelation examples from simulations illustrated in (D-F). Simulations that did not finish in a specified time interval (5 h) are indicated by white color.

**Figure 7. Gridness scores and gamma activity in networks with recurrent inhibition.**

(A-C) Gridness score as a function of **gE** and **gI** for networks without noise (A; σ = 0 pA), with noise level set to σ = 150 pA (B), and noise level set to σ = 300 pA (C). Simulations that did not finish in a specified time interval (5 h) are indicated by white color.

(D-F) Examples of inhibitory (red) and excitatory (blue) synaptic currents recorded respectively from excitatory and inhibitory neurons from simulations highlighted by arrows in panels (G-I).

(G-I) *Top:* Correlation value at the first local maximum of an autocorrelation of inhibitory synaptic currents (I 🡪 E cells, 25 randomly selected E cells), plotted as a function of **gE** and **gI**, for networks without noise (G), with noise level set to σ = 150 pA (H), and noise level set to σ = 300 pA (I). Each point is an average over five simulation trials. In these simulations velocity and place cell inputs were disabled. The duration of simulations was 10 seconds. *Bottom:* Frequency corresponding to the peaks of the autocorrelation functions for simulations in the top panels. Black lines in (H) indicate the regions from (B) where gridness score = 0.5.

**Figure Supplements**

**Figure 1 - figure supplement 1: Synaptic weights in scaled and probabilistic variants of the network.**

(A) Output (top) and input (bottom) synaptic weights of an E (left) and I (right) neuron in the middle of the twisted torus in a network in which synaptic weights are scaled according to the synaptic profile functions from Figure 1B. (B) Same as (A), but synaptic weights are constant and the probability of connection between a pair of neurons is scaled according to the synaptic profile functions in Figure 1B.

**Figure 2 - figure supplement 1: Examples of spatial firing fields.**

(A-L) Top: Gridness score in the parameter space of the E and I synaptic strength scaling parameters (gE and gI respectively). Bottom: Firing fields of a single cell obtained by simulating animal movement, in the parameter region highlighted by black rectangle in the parameter space plot. Above each firing field is the estimated gridness score (left) and maximal firing rate in the firing field (right). Blank (white) locations in the parameter space are simulations that did not finish in the pre-specified time limit (5 h). Noise level used in each set of simulations is shown by σnoise. Color scale in the firing field plots ranges from 0 Hz (dark blue) to the maximal firing rate for each of the firing fields (dark red).

**Figure 2 - figure supplement 2: Sensitivity of grid firing to changes in feedback inhibition, excitation and noise levels in networks with connection probability between pairs of neurons drawn according to the synaptic profile functions in Figure 1B.**

(A-C) Example spatial firing fields (left) and spatial autocorrelation plots (right) of E and I cells for networks without noise (A; σ = 0 pA), with noise set to σ = 150 pA (B), and noise set to σ = 300 pA (C) and with the strengths of recurrent synaptic connections indicated by arrows in (D-F). Maximal firing rate is indicated in the top right of each spatial firing plot. The range of spatial autocorrelations is normalized between 0 and 1.

(D-F) Gridness score as a function of gE and gI for networks with each noise level. Each item in the color plot is an average gridness score of two simulation runs. Arrows indicate the positions of grid field and autocorrelation examples from simulations illustrated in (A-C). Simulations that did not finish in a specified time interval (5 h) are indicated by white color.

**Figure 2 - figure supplement 3: Spatial information and sparsity of firing fields of E and I cells.**

(A) Spatial information of E (top) and I (bottom) cells as a function of gE and gI in networks from Figure 2.

(B) Same as (A), but the color plots show spatial sparsity of E and I cells. Black lines indicate the region from Figure 2D-F where the gridness score = 0.5.

**Figure 2 - figure supplement 4: Gridness scores of I cells.**

Colour plots show gridness score as a function of gE and gI for networks without noise (A), with noise standard deviation σ = 150 pA (B), and σ = 300 pA (C). Data are from simulations of networks with feedback inhibition only (E-I networks; Figure 2). Black lines indicate the region from Figure 2D-F where the gridness score of E cells = 0.5.

**Figure 2 - figure supplement 5: Spatial firing fields in networks with uncorrelated spatial input applied to each I cell.**

(A) Examples of firing fields of E and I cells. Gridness score and maximal firing rate of the firing field is indicated in the top left and right parts of each firing field, respectively.

(B) Distributions of spatial sparsity (left), spatial information (centre) and gridness score (right) of 100 randomly selected cells from each population of neurons. Each simulation run was repeated 10 times with different random seeds. Network parameters were gE = 3 nS and gI = 1 nS. Each I cell received connections from 3 randomly selected neurons with a place like spatial firing field. Properties of place cells: rmax = 100 Hz, σfield = 80 cm (cf. Supplementary Methods).

**Figure 3 - figure supplement 1: Sensitivity of gamma oscillations to changes in the strength of E and I synapses in networks with connection probability between pairs of neurons drawn according to the synaptic profile functions in Figure 1B.**

(A-C) Examples of inhibitory (red) and excitatory (blue) synaptic currents recorded respectively from excitatory and inhibitory neurons from simulations highlighted by arrows in panels (D-F).

(D-F) Top: Correlation value at the first local maximum of an autocorrelation of inhibitory synaptic currents (I 🡪 E cells, 25 randomly selected E cells), plotted as a function of gE and gI, for networks without noise (D), with noise set to σ = 150 pA (E), and noise set to σ = 300 pA (F). Each point is an average over five simulation trials. In these simulations velocity and place cell inputs were disabled. The duration of simulations was 10 seconds. Bottom: Frequency corresponding to the peaks of the autocorrelation functions for simulations in the top panels. Black lines in (E) indicate the region from Figure 2 - figure supplement 2 where the gridness score = 0.5.

**Figure 3 - figure supplement 2: Scatter plots of gridness score as a function of the amplitude of gamma oscillations.**

(A-C) The plots show relationships between grid field computations (gridness score) and the power of nested gamma oscillations for deterministic networks (A), networks with moderate noise (B) and networks with the highest simulated noise level (C). Noise level is indicated by σ. The strength of the oscillation was obtained by computing autocorrelation functions of inhibitory currents impinging onto 25 randomly selected E cells in the network and detecting their first local maxima. The correlation value at the first local maximum is plotted on the abscissa. Color coding determines the values of gE and gI, as shown in the 2D colorbar.

**Figure 3 - figure supplement 3: Scatter plots of gridness score as a function of the detected oscillation frequency.**

(A-C) The plots show relationships between grid field computations (gridness score) and the frequency of gamma oscillations for deterministic networks (A), networks with moderate noise (B) and networks with the highest simulated noise level (C). Noise level is indicated by σ. The frequency of the oscillation was obtained by computing autocorrelation functions of inhibitory currents impinging onto 25 randomly selected E cells in the network and detecting their first local maxima. The time lag at the first local maximum yielded the frequency of the oscillation, which is plotted on the abscissa. Color coding determines the values of gE and gI, as shown in the 2D colorbar.

**Figure 3 - figure supplement 4: Amplitude and frequency of gamma oscillations in the gE and gI parameter regions where grid fields are robust.**

Amplitude (top) and frequency (bottom) of detected gamma oscillations for simulations in which gridness score is greater than 0.5, in deterministic networks (A), networks with an intermediate level of noise (B) and in networks with the highest simulated level of noise (C). The data in this figure are from simulations in Figure 3.

**Figure 5 - figure supplement 1: Examples of activity in the network.**

(A-C) Top: Mean maximal firing rate per theta cycle (average over 5 trials), outlining the average activity during theta cycles, in the parameter space of gE and gI. Center and bottom: Raster plots (center) and population-average firing rates (bottom) of all cells in selected locations of the E-I parameter space during 16 consecutive θ cycles. Action potentials and firing rates of E and I cells are colored red and blue, respectively. An arrow highlights the position in the parameter space.

**Figure 6 - figure supplement 1: Effect of replacing theta frequency inputs by a constant input with an equal mean amplitude.**

(A-C) Amplitude (top) and frequency (bottom) of detected gamma oscillations (Methods) in deterministic networks (A), networks with an intermediate level of noise (B) and in networks with the highest simulated level of noise (C). Each point is an average of five simulation runs. Data are from the same simulation set. White color indicates simulation runs in which no autocorrelation peaks were detected (cf. Methods).

**Figure 6 - figure supplement 2: Effect of noise on gridness scores in networks without theta frequency inputs.**

The plot shows a difference between gridness scores of networks with σ = 150 pA and networks with σ = 0 pA plotted as a function of gE and gI when theta inputs were replaced with a constant input with an equal mean amplitude.

**Figure 6 - figure supplement 3: Firing rates of E cells.**

(A) Average firing rate of all E cells during simulations of animal movement as a function of gE and gI. Black lines outline the region from Figure 2D-F where gridness score = 0.5.

(B) Relationship between gridness score and firing frequency of E cells.

**Figure 6 - figure supplement 4: Calibration of the gain of the velocity inputs.**

(A-C) Bump attractor speed as a function of the strength of the velocity current for the three simulated levels of noise. Ten simulation runs were performed for each level of noise (blue markers). In each run the speed of the bump was calculated in response to the injected velocity input and the data were used to fit a linear relationship using an estimation procedure outlined in Supplementary Methods (black line).

(D-F) Slope of the estimated velocity gain of the attractor networks as a function of gE and gI for all simulated levels of noise.

(G-I) Same as in (D-F) but the plots show error of fit for the estimated linear relationships. Arrows show locations of the data plotted in (A-C). Black lines in (D-I) indicate the region from Figure 2D-F where gridness score = 0.5.

**Figure 6 - figure supplement 5: Sensitivity of bump attractor spontaneous drift to variations in gE and gI and noise levels.**

(A) Schematic of the bump attractor drift estimation procedure. The first 500 ms of a simulation trial are used to initialize the bump attractor. Onset of theta modulated input current was at 500 ms. The estimated centers of bump attractors measured by the least squares fit of symmetric Gaussians were at 1 s (initial position) and 9 s (final position). The drift was then estimated as the distance on twisted torus between the initial and final position. Simulation time was 10 s.

(B) Color plots show bump attractor drifts averaged over 5 simulation trials, for the simulated ranges of excitatory and inhibitory synaptic strengths and levels of noise. Networks without noise can form stable bump attractors in a subset of their parameter region. Networks with noise suffer from attractor drift in majority of the parameter region. Black lines in (B) indicate the region from Figure 2D-F where gridness score = 0.5.

**Figure 6 - figure supplement 6: Effectivity of the place cell resetting mechanism as a function of gE and gI and noise levels.**

(A) Illustration of the procedure to estimate the difference between the bump position induced by place cells and actual estimated position of the bump state, by using a sliding window with 250 ms duration and 125 ms time step. The resulting distance from the reset position, in one simulation run, was then an average over all sliding windows.

(B) Color plots show the effectivity of place cell mechanism for an average of 5 simulation runs with 10 s duration. Place cells are most effective in networks with an intermediate amount of noise. Black lines in (B) indicate the region from Figure 2D-F where gridness score = 0.5.

**Figure 7 - figure supplement 1: Spatial firing fields in networks that contain recurrent I 🡪 I synapses.**

(A-C) Example spatial firing fields (left) and spatial autocorrelation plots (right) for networks with gE = 3nS and gI = 1 nS (a) and networks with gE = 1 nS and gI = 3 nS (b), corresponding to the three simulated noise levels indicated by σ. Maximal firing rate is indicated to the top right of each spatial firing plot. Range of spatial autocorrelations is normalized between 0 and 1.

**Figure 7 - figure supplement 2: Continuous attractors in networks that contain direct I 🡪 I synapses.**

(A) Examples of E cell population firing rate snapshots from simulations in which velocity and place cell inputs are inactivated. Each row shows a simulation trial with a value of gE and gI highlighted by an arrow in panel (B). The corresponding probability of bump formation (P(bumps)) is indicated to the left. Maximal firing rate for each set of snapshots is indicated to the right.

(B) Color plots show probability of bump formation (P(bumps)), for the simulated range of gE and gI and the three simulated noise levels. Each color point is an average of five 10 s simulation runs. Black lines in (B) indicate the region from Figure 7A-C where gridness score = 0.5.

**Figure 7 - figure supplement 3: Sensitivity of bump attractor spontaneous drift to variations in gE, gI and noise levels in networks that contain direct I** 🡪 **I synapses.**

(A) Schematic of the bump attractor drift estimation procedure. The first 500 ms of a simulation trial are used to initialize the bump attractor. Onset of theta modulated input current was at 500 ms. The estimated centers of bump attractors measured by the least squares fit of symmetric Gaussians were at 1 s (initial position) and 9 s (final position). The drift was then estimated as the distance on twisted torus between the initial and final position. Simulation time was 10 s.

(B) Color plots show bump attractor drifts averaged over 5 simulation trials, for the simulated ranges of excitatory and inhibitory synaptic strengths and levels of noise. Networks without noise can form stable bump attractors in a subset of their parameter region. Networks with noise suffer from attractor drift in the majority of the parameter region. Black lines in (B) indicate the region from Figure 7A-C where gridness score = 0.5.

**Figure 7 - figure supplement 4: Calibration of the gain of the velocity inputs in networks that contain direct I 🡪 I synapses.**

(A-C) Bump attractor speed as a function of the strength of the velocity current for the three simulated levels of noise indicated by σ. Values of gE and gI are indicated by arrows in (D-I). Ten simulation runs were performed for each level of noise (blue markers). In each run the speed of the bump was calculated in response to the injected velocity input and the data were used to fit a linear relationship using an estimation procedure outlined in Supplementary Methods (black line).

(D-F) Slope of the estimated velocity gain of the attractor networks as a function of gE and

gI for all simulated levels of noise.

(G-I) Same as in (D-F) but the plots show error of fit for the estimated linear relationships. Arrows in (D-I) show locations of the data plotted in (A-C). Black lines in (D-I) indicate the region from Figure 7A-C where gridness score = 0.5.

**Figure 7 - figure supplement 5: Seizure-like states in networks that contain direct I 🡪 I synapses.**

(A-C) Raster plots show activity of all neurons in the excitatory (red) and inhibitory (blue) populations for the duration of two theta cycles (top), along with the average population firing rates for both populations (center and bottom; calculated with a sliding rectangular window with 2 ms duration and 0.5 ms time step), for networks where noise is absent (A; σ = 0), with noise set to σ = 150 pA (B), and with noise set to σ = 300 pA (C). Simulations were performed in the absence of animal movement and place cell input; gE = 1 nS and gI = 3 nS.

(D) Maximal average population firing rate of E cells estimated from the whole simulation run (10 s; 500 ms at the beginning of the simulation excluded) for each simulated level of noise. Each point is an average of maxima from 5 simulation runs.

(E) Probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz, i.e. at least 60% of E cells firing synchronously within a time period of 2 ms, in the parameter space of gE and gI when σ = 0 pA. Black lines indicate the regions from Figure 7A-C where gridness score equals 0.5.

(F) Scatter plots show the relationship between gridness score and the maximal firing rate during the simulation (left) and the probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz (right).

**Figure 7 - figure supplement 6: Sensitivity of grid firing to changes in inhibition and excitation in networks that contain direct E 🡪 E synapses.**

(A-C) Example firing fields (left) and spatial autocorrelation plots (right) for the strengths of recurrent synaptic connections indicated by arrows in (D-F) for networks without noise (A; σ = 0 pA), with noise set to σ = 150 pA (B), and noise set to σ = 300 pA (C).

(D-F) Gridness score as a function of gE and gI for networks with each noise level. Each item in the color plot is an average gridness score of two simulation runs. Arrows indicate the positions of grid field and autocorrelation examples from simulations illustrated in (A-C).

**Figure 7 - figure supplement 7: Sensitivity of gamma oscillations to changes in inhibition and excitation in networks that contain direct E 🡪 E synapses.**

(A-C) Examples of inhibitory (red) and excitatory (blue) synaptic currents recorded respectively from excitatory and inhibitory neurons from simulations highlighted by arrows in panels (D-F).

(D-F) Top: Correlation value at the first local maximum of an autocorrelation of inhibitory synaptic currents (I **🡪** E cells, 25 randomly selected E cells), plotted as a function of gE and gI, for networks without noise (D), with noise set to σ = 150 pA (E), and noise set to σ = 300 pA (F). Each point is an average over five simulation trials. In these simulations velocity and place cell inputs were disabled. The duration of simulations was 10 seconds. Bottom: Frequency corresponding to the peaks of the autocorrelation functions for simulations in the top panels. Black lines in (E) indicate the region from Figure 7 – figure supplement 6 where the gridness score = 0.5.

**Figure 7 - figure supplement 8: Continuous attractors in networks that contain direct E 🡪 E synapses.**

(A) Examples of E cell population firing rate snapshots from simulations in which velocity and place cell inputs are inactivated. Each row shows a simulation trial with a value of gE and gI highlighted by an arrow in panel (B). The corresponding probability of bump formation (P(bumps)) is indicated to the left. Maximal firing rate for each row is indicated to the right.

(B) Color plots show probability of bump formation (P(bumps)), for the simulated range of gE and gI and the three simulated noise levels indicated by σ. Each color point is an average of five 10 s simulation runs. Arrows show positions in the parameter space of examples in (A). Black lines indicate the region from Figure 7 – figure supplement 6 where the gridness score = 0.5.

**Figure 7 - figure supplement 9: Seizure-like states in networks that contain direct E 🡪 E synapses.**

(A-C) Raster plots show activity of all neurons in the excitatory (red) and inhibitory (blue) populations for the duration of two theta cycles (top), along with the average population firing rates for both populations (center and bottom; calculated with a sliding rectangular window with 2 ms duration and 0.5 ms time step), for networks where noise is absent (A; σ = 0), with noise set to σ = 150 pA (B), and with noise set to σ = 300 pA (C). Simulations were performed in the absence of animal movement and place cell input; gE = 1 nS and gI = 3 nS.

(D) Maximal average population firing rate of E cells estimated from the whole simulation run (10 s; 500 ms at the beginning of the simulation excluded) for each simulated level of noise. Each point is an average of maxima from 5 simulation runs.

(E) Probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz, i.e. at least 60% of E cells firing synchronously within a time period of 2 ms in the parameter space of gE and gI when σ = 0 pA.

(F) Scatter plots show the relationship between gridness score and the maximal firing rate during the simulation (left) and the probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz (right). Black lines in (D-E) indicate the region from Figure 7 – figure supplement 6 where the gridness score = 0.5.

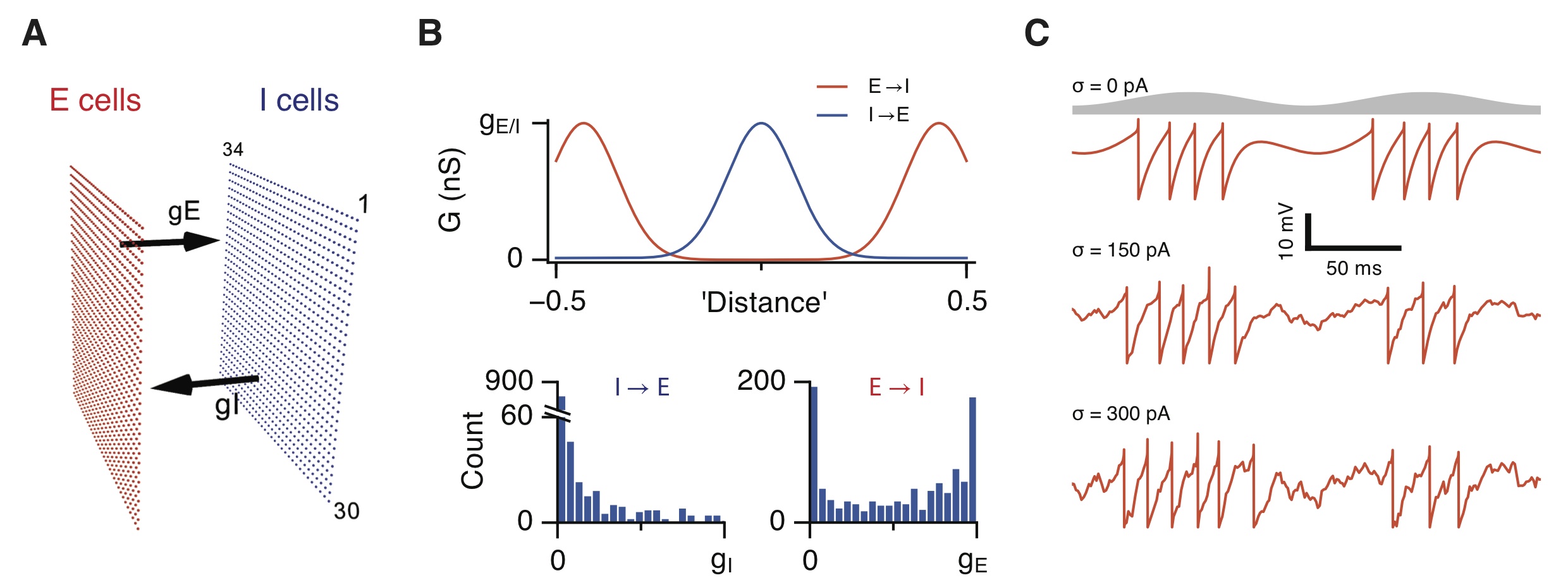
**Figure 7 - figure supplement 10: Probability of bump formation and network activity plots in networks with structured E 🡪 E and unstructured E 🡪 I and I 🡪 E connections.**

Since the presence of bump attractors is necessary for grid computation, we tested whether networks with only structured E-E connections can generate activity bumps. We used the Gaussian fitting procedure (cf. Methods) to estimate the presence of bump attractors in these networks.

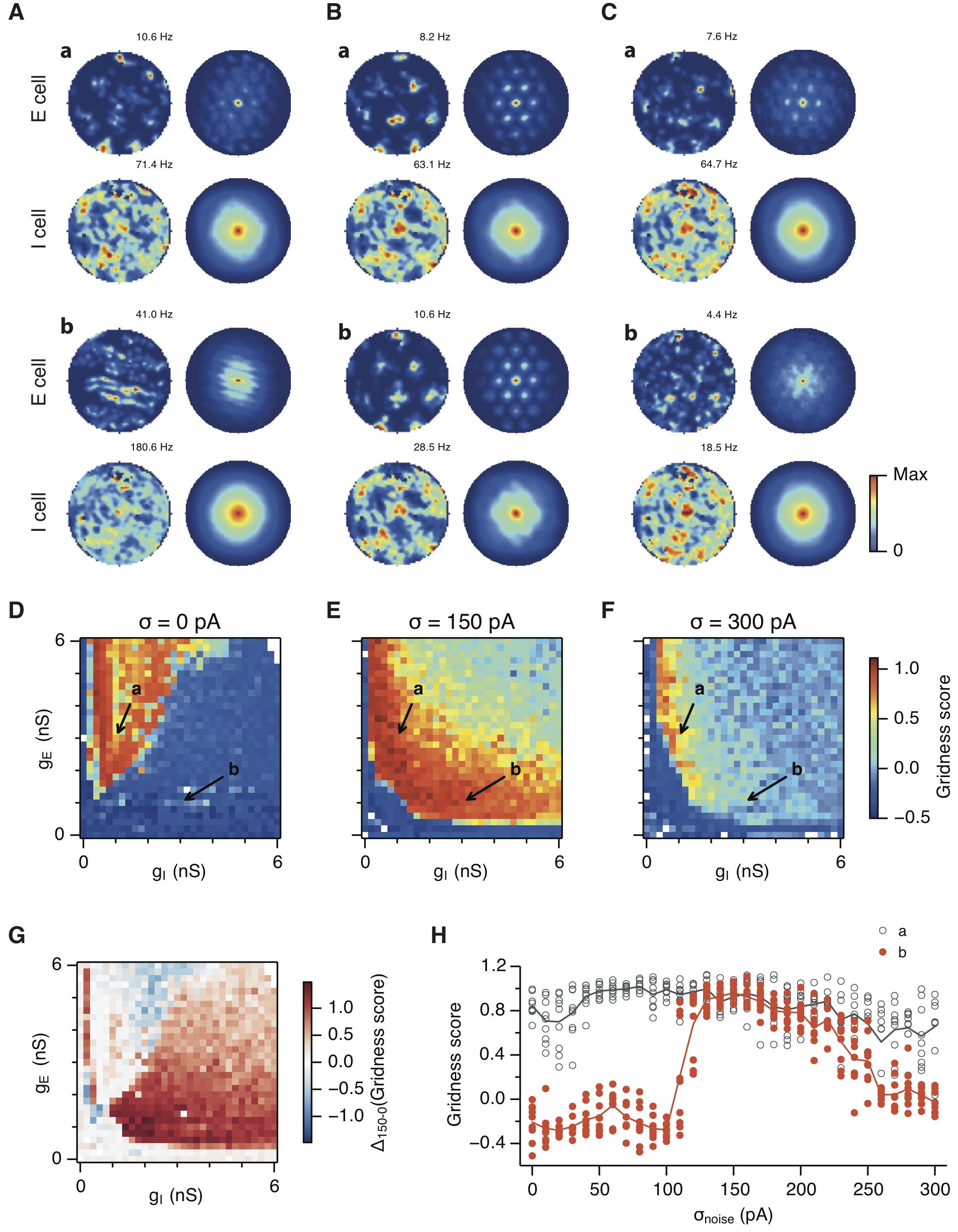
(A) Probability of bump formation as a function of the E-E synaptic scaling factor (gE🡪E) and the width of the synaptic profile (σE🡪E). Arrow highlights the position in the parameter space corresponding to the raster plots (center) and network activity snapshots (bottom) for E and I cells. Firing rate in the network activity color plots are in the range of 0 (dark blue) to the maximum firing rate indicated to the right of the plot (dark red). In these networks gE = 1 nS and gI = 0.1 nS.

(B) Same as (A) but gE = 3 nS and gI = 1 nS.

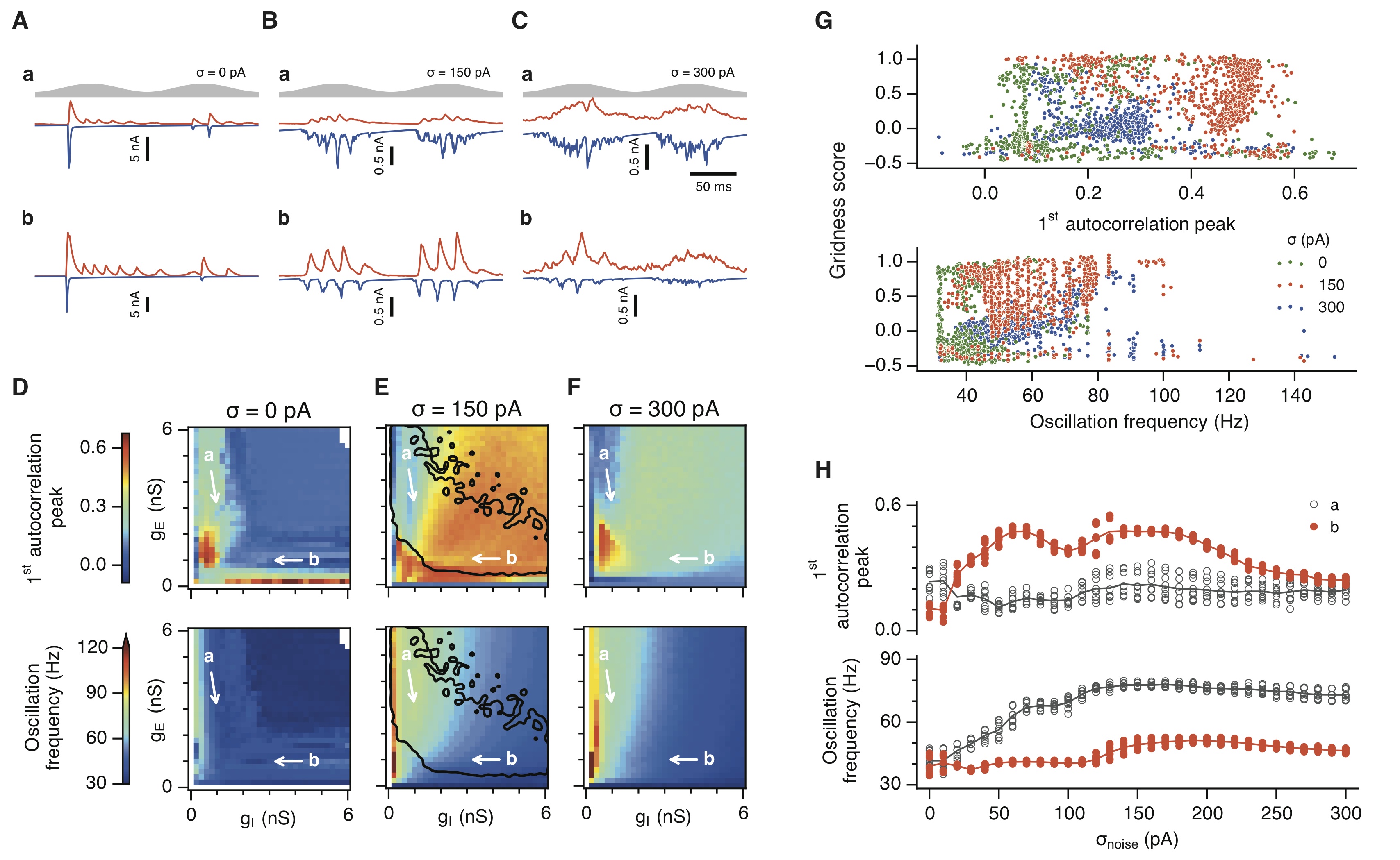
(C) Same as (A) and (B) but in these simulations the synaptic scaling factor of E-E connections and the width of the synaptic profile were fixed (gE🡪E = 3 nS and σE🡪E = 0.0833) and gE and gI varied in the range of 0 – 6 nS. Simulations that produced excessive spiking activity and did not finish in a specified time limit (3h) are indicated by white color. Many networks suffer from runaway excitation and inhibition (A) or generate only background synaptic activity characterized by low firing rates of E and I cells (B-C). The Gaussian fitting procedure used to estimate the probability of bump formation can nevertheless yield a high bump score due to the fact that this procedure can also give a high score to intermittent pockets of activity (A) or pockets of background activity of E cells (B-C). This activity, however, is not stable enough to generate grid firing fields.

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**Figure 1.**

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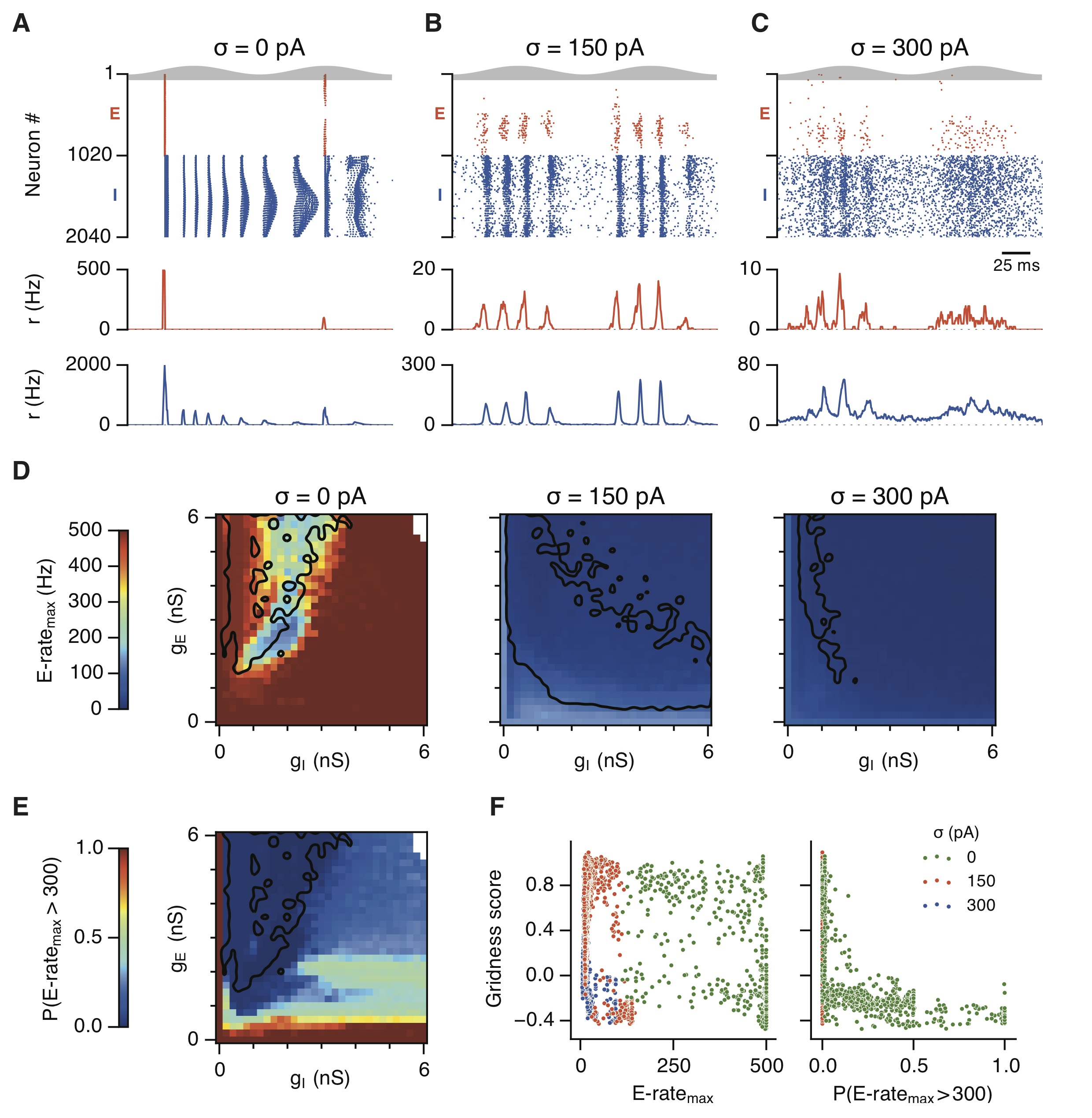
**Figure 2.**

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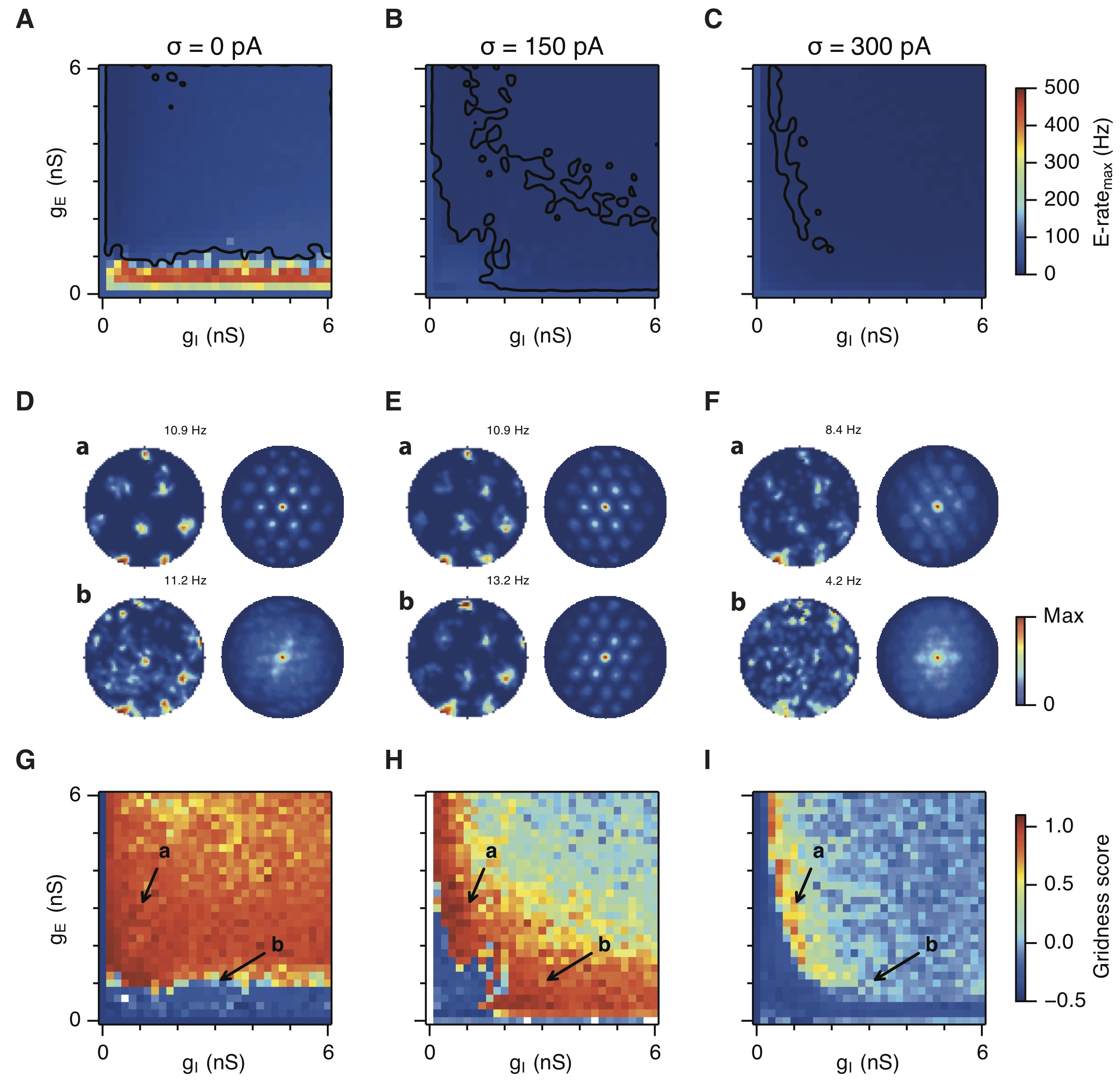
**Figure 3.**

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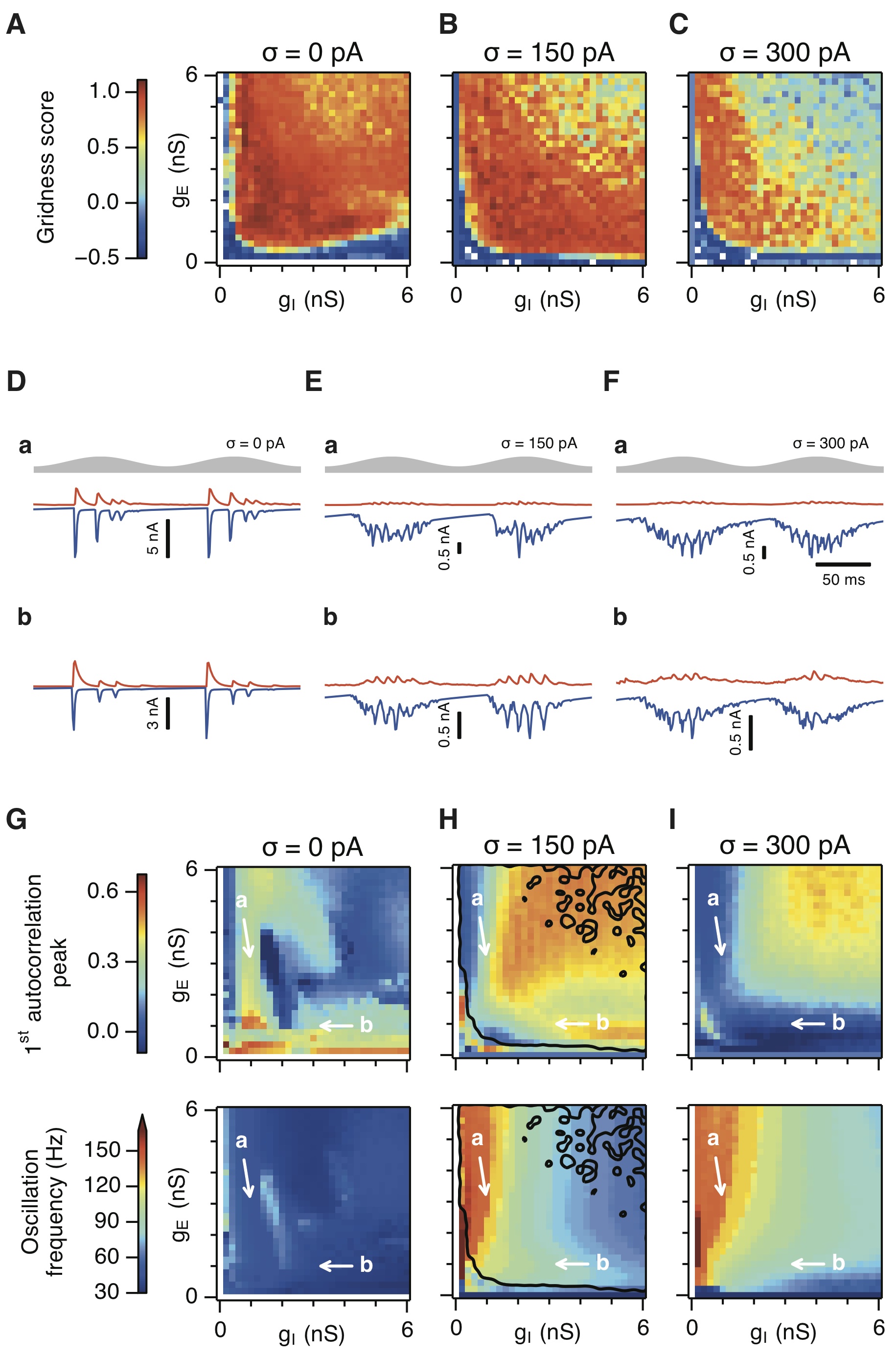
**Figure 4.**

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**Figure 5.**

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**Figure 6.**

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**Figure 7.**