*Classification:* Biological sciences, Neuroscience

**Noise promotes independent control of gamma oscillations and grid firing by regulation of recurrent synaptic connections**

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**Abstract (250 words)**

Neural computations underlying cognitive functions are associated with modulation of gamma frequency oscillations in network activity and require calibration of the strength of excitatory and inhibitory synaptic connections. However, principles relating gamma oscillations, synaptic strength and circuit computations are unclear. We address this issue through systematic variation in the strength of recurrent inhibitory and excitatory connections in attractor network models that account for grid firing and theta-nested gamma oscillations in the medial entorhinal cortex. We show that grid firing and gamma oscillations are differentially sensitive to variation in excitatory and inhibitory synaptic strength, with gamma activity providing little information about grid computations or the probability of a network forming an attractor state. Surprisingly, moderate intrinsic noise massively increases the range of synaptic strengths that support gamma oscillations and grid computation. With moderate noise, variation in excitatory or inhibitory synaptic strength tunes the amplitude and frequency of gamma activity without disrupting grid firing. This beneficial role for noise results primarily from disruption of epileptic-like network states. Thus, gamma activity may have complex relationships to computation, while moderate noise may promote independent control of multiplexed firing rate- and gamma-based computational mechanisms. Our results have implications for tuning of normal circuit function and for disorders in which gamma oscillations and synaptic strength are modified.

**Significance statement (120 words)**

Relating brain activity to computations that mediate cognitive processes and to their underlying synaptic mechanisms is challenging. Gamma frequency network rhythms vary with cognitive states and abilities. While they have been proposed to have specific computational roles, they may instead simply be a byproduct of neural circuit activation. Here we systematically analyze effects of inhibitory and excitatory synaptic strength in a model that accounts for gamma and for rate-coded grid firing fields through a shared synaptic mechanism. We demonstrate that the relationship between gamma and computation is complex and highly sensitive to noise, which suppresses epileptic states. We show how variation in synaptic strength can independently control gamma and grid firing. This is consistent with multiplexed computational roles for gamma.

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**Introduction**

**Cognitive processes require execution of computations by neural circuits and are associated with gamma frequency oscillations in network activity. Gamma activity and cognitive performance often co-vary within tasks and between individuals. For example, cognitive deficits in psychiatric disorders such as autism and schizophrenia are associated with altered gamma frequency network dynamics** (Spellman and Gordon, 2014; Uhlhaas and Singer, 2012)**. Such disorders are also linked to changes in the efficacy of excitatory glutamatergic and inhibitory GABAergic synapses** (Lewis et al., 2012; Rubenstein and Merzenich, 2003)**. A critical and unresolved issue is the mechanistic relationship between gamma oscillations, the strength of excitation and inhibition, and circuit computations. On the one hand, neural codes based on firing rates may be sufficient for circuit computations** (Histed and Maunsell, 2014; Shadlen and Newsome, 1994)**. In this scenario gamma oscillations might index circuit activation, but would not be required for computation. Evidence that rate coded computations and gamma oscillations arise from shared circuit mechanisms could be interpreted to support this view** (Lundqvist et al., 2010; Pastoll et al., 2013)**, which predicts that when synaptic properties of a circuit are altered then gamma activity and the output of the rate-coded computation will co-vary. Alternatively, gamma oscillations, while sharing cellular substrates with rate-coded computations, may nevertheless support independent or multiplexed computational modes. For example, according to the communication through coherence hypothesis, tuning of gamma frequency activity may facilitate selective interactions between distant brain regions** (Fries, 2009)**. In this scenario independent control of rate coded computation and gamma activity would be beneficial, for example by allowing tuning for coherence without disrupting multiplexed rate-coded computations. However, it is unclear how this could be achieved in circuits where gamma and rate-coded computations share common synaptic mechanisms, as this would require variation in synaptic properties to differentially affect gamma activity and the rate coded computation.**

**We address these issues using a model that accounts, through a common synaptic mechanism, for gamma oscillations and spatial computation by neurons in layer II of the medial entorhinal cortex (MEC)** (Pastoll et al., 2013)**. The rate-coded firing of grid cells in the MEC are a well-studied feature of neural circuits for spatial cognition** (Moser and Moser, 2013)**. During exploration of an environment individual grid cells are active at multiple locations that together follow a hexagonal grid-like organization. At the same time MEC circuits generate periods of activity in the high gamma frequency range (60 – 120 Hz) nested within a slower theta (8 – 12 Hz) frequency network oscillation** (Chrobak and Buzsáki, 1998)**. Analysis of spatial correlations in grid firing, of manipulations to grid circuits, and recording of grid cell membrane potential in behaving animals, collectively point towards continuous two-dimensional network attractor states as explanations for grid firing** (Bonnevie et al., 2013; Domnisoru et al., 2013; Schmidt-Hieber and Häusser, 2013; Yoon et al., 2013)**. In layer II of the MEC, which has the highest known density of grid cells, the major population of excitatory neurons projects to the dentate gyrus of the hippocampus** (Sargolini et al., 2006)**. These excitatory (E) neurons interact with one another via intermediate inhibitory (I) neurons** (Couey et al., 2013; Pastoll et al., 2013)**. Models that explicitly incorporate this recurrent E-I-E connectivity can account for grid firing through velocity-dependent update of network attractor states** (Pastoll et al., 2013)**. When these models are implemented with excitable spiking neurons they also account for theta-nested gamma frequency network oscillations** (Pastoll et al., 2013)**. The influence in these, or other classes of attractor network models, of the strength of E-I or I-E connections on gamma oscillations and grid firing, or other attractor computations, has not been systematically investigated.**

**We find that gamma oscillations and grid firing are both sensitive to the strength of excitatory and inhibitory connections, but that their relationship differs. While their underlying synaptic substrates are identical, gamma activity nevertheless provides little information about grid firing or the presence of underlying network attractor states. Thus, gamma activity is not a good predictor of rate-coded computation. Unexpectedly, we find the range of E- and I- synaptic strengths to support gamma and grid firing is massively increased by moderate intrinsic noise through a mechanism involving suppression of seizure like events. In the presence of moderate noise differences in synaptic strength can tune the amplitude and frequency of gamma across a wide range while having relatively little effect on grid firing. Our results suggest constraints for extrapolation of differences in gamma activity to mechanisms for cognition, identify noise as a critical factor for successful circuit computation, and suggest that tuning of excitatory or inhibitory synaptic strength could be used to control gamma-dependent processes multiplexed within circuits carrying out rate coded computations.**

**Results**

**To systematically explore relationships between strengths of excitatory and inhibitory synapses, computations and gamma activity, we have taken advantage of models that account for both grid firing and theta-nested gamma oscillations through E-I-E interactions. In this model a layer of E cells sends synaptic connections to a layer of I cells, which in turn feedback onto the E cell layer (Figure 1A). For attractor dynamics to emerge the strength of E and I connections are set to depend on the relative locations of neurons in network space (Figure 1B). While such connectivity can arise in development through spike timing-dependent synaptic plasticity** (Widloski and Fiete, 2014)**, here we consider networks in which the connection profiles are pre-determined and identical in all simulations** (Pastoll et al., 2013)**. To vary the strength of excitatory or inhibitory connections in the network as a whole we scale the strength of all connections according to a maximum conductance value (gE or gI for excitation and inhibition respectively)(Figure 1B). Each E and I cell is implemented as an exponential integrate and fire neuron and so has membrane potential that approximates the dynamics of a real neuron, as opposed to simpler models in which synaptic input directly updates a spike rate parameter. Addition of noise to a single E or I cell increases variability in its membrane potential trajectory approximating that seen in vivo (Figure 1C). Given that all of the neurons in the model are excitable and that in total the model contains > 1.5 million synaptic connections, systematic analysis of this parameter space requires many thousands of simulations running over several weeks on a computing cluster. We therefore optimized a version of this model to enable faster simulation and automated extraction and analysis of generated data (see Methods), so that the effect on grid firing of 30 x 30 combinations of gE and gI could be evaluated in approximately one week.**

**Intrinsic noise increases the range of synaptic strengths that support grid firing**

**What happens to grid firing patterns when the strengths of excitatory and / or inhibitory synaptic connections in the model are modified? We first evaluated grid firing while simulating exploration within a circular environment with a network from which noise sources were absent (Figure 1D). When we reduce the strength of connections from I cells by 3-fold and increased the strength of connections from E cells by 3-fold we find that grid firing is abolished (Figure 1Db vs 1Da). When we explored the parameter space of gE and gI more systematically we identified a relatively restricted region that supports grid firing (Figure 1G and S1A-D). Rather than the required gI and gE scaling with one another, this region is shifted towards low values of gI and high gE. Thus, the ability of recurrently connected networks to generate grid fields requires specific tuning of synaptic connection strengths.**

**Because neural activity in the brain is noisy** (Faisal et al., 2008; Shadlen and Newsome, 1994)**, we wanted to know if the ability of the circuit to compute location is affected by noise intrinsic to each neuron (Figure 1C). Given that attractor networks are often highly sensitive to noise** (Eliasmith, 2005; Zhang, 1996)**, we expected that intrinsic noise would reduce the parameter space in which computation is successful. In contrast, when we added noise with standard deviation of 150 pA to the intrinsic dynamics of each neuron, we found that both configurations from Figure 1Da,b now supported grid firing patterns (Figure 1Ea,b). When we considered the full space of E and I synaptic strengths in the presence of this moderate noise we now found a much larger region that supports grid firing (Figure 1H and S1E-H). This region has a crescent-like shape, with arms of relatively high gI and low gE, and low gI and high gE. Thus, while tuning of gI and gE continues to be required for grid firing, moderate noise massively increases the range of gE and gI over which grid fields are generated.**

**When intrinsic noise was increased further, to 300 pA, the parameter space that supports grid firing was reduced in line with our initial expectations (Figure 1Fa,b, I and S1I-L). To systematically explore the range of gE and gI over which the network is most sensitive to the beneficial effects of noise we subtracted grid scores for simulations with 150 pA noise from scores with deterministic simulations (Figure 1J). This revealed that the unexpected beneficial effect of noise was primarily in the region of parameter where recurrent inhibition was strong. In this region, increasing noise above a threshold led to high grid scores, while further increases in noise progressively impaired grid firing (Figure 1K).**

**Together these simulations demonstrate that attractor circuit computations that generate grid firing fields require specific tuning of gE and gI. Grid firing is supported in relatively restricted regions of parameter space that depend on neuronal noise. Optimal levels of noise, which produce single cell membrane potential fluctuations of a similar amplitude to experimental observations, promote grid firing by reducing the sensitivity of grid computations to the strength of recurrent synaptic connections, particularly when inhibition is relatively strong and excitation is weak.**

**Differential sensitivity of gamma oscillations and grid firing to the strength of E and I synapses**

**Is the sensitivity of gamma frequency oscillations to synaptic strength and to noise similar to that of grid firing? To evaluate gamma activity we recorded synaptic currents from single E and I cells across multiple theta cycles (Figure 2A-C). For the network configurations illustrated in Figure 1Da,b and in which intrinsic noise is absent, we observed synaptic events entrained to theta cycles (Figure 2Aa,b). However, the timing and amplitude of synaptic events typically differed between theta cycles and no consistent gamma rhythm was apparent. In contrast, in the presence of noise with standard deviation 150 pA we observed nested gamma frequency synaptic activity with timing that was consistent between theta cycles (Figure 2Ba). In this condition the frequency of the gamma oscillations was reduced and their amplitude increased by raising gI and lowering gE (Figure 2Bb). With a further increase in noise to 300 pA, gamma activity remained entrained to theta cycles, but became less ordered (Figure 2Ca,b).**

**To explore gamma activity across a wider range of gI and gE we automated quantification of the strength and frequency of oscillatory input to E cells (see Methods). In the absence of noise gamma frequency activity was largely absent (Figure 2D). Strikingly, following addition of moderate noise the region of parameter space that supports gamma activity was massively expanded (Figure 2E). Within this space, the amplitude of gamma increased with increasing inhibition, whereas the frequency was reduced. As noise is increased further the amplitude and frequency of gamma oscillations are reduced (Figure 2F). Thus, intrinsic noise modifies the amplitude and frequency of nested gamma oscillations.**

**To determine whether there is a systematic relationship between values of gE and gI that generate gamma and grid firing we compared the gridness score and gamma scores for each circuit configuration (Figure 2G, S2, S3). We found this relationship to be complex and highly sensitive to noise. However, we did not find any evidence for strong linear relationships between gamma amplitude or gamma frequency and grid score (R2 < 0.12 for all comparisons), while gamma amplitude and frequency provided only modest amounts of information about grid scores (0.27 < MIC < 0.33 and 0.27 < MIC < 0.37 respectively). The relationship between noise intensity and gamma differed from that for grid computations. Whereas, grids emerged above a sharp noise threshold (Figure 1K), for the same regions in parameter space the frequency and amplitude of oscillations varied smoothly as a function of noise (Figure 2H). Thus, neither the frequency nor the power of gamma appears to be a good predictor of grid firing.**

When we considered only regions of parameter space that generate robust grid fields (grid score > 0.5), we found circuits generating almost the complete observed range of gamma amplitudes (0.02 < autocorrelation peak < 0.59) and frequencies (31 Hz < frequency < 102 Hz)(Figure S4). For example, considering the crescent space region of E-I space that supports grid firing in the presence of intermediate noise (the region within the isocline in Figure 2E), when **gI** is high and **gE** low then the amplitude of gamma is relatively low and the frequency high. Moving towards the region where **gI** is high and **gE** is low, the amplitude of gamma is increased and the frequency is reduced. Thus, variation of synaptic strength across this region of E-I space can be used to tune the properties of gamma activity while maintaining the ability of the network to generate grid fields.

**Together these data indicate that optimal noise promotes emergence of gamma oscillations, while the properties of oscillations may depend on the relative strength of synaptic connections. The relationship between gamma and synaptic strength differs to that for grid computations. Strikingly, while gamma activity provides relatively little information about grid firing, differential sensitivity of gamma and grid firing to gE and gI provides a mechanism for circuits to tune gamma while maintaining the ability to compute rate coded grid firing fields.**

**Noise promotes attractor computation by opposing seizures**

Given the emergence of a large parameter space that supports grid firing following introduction of moderate noise, we were interested to understand how noise influences the dynamics of the circuit. One possibility is that in networks that fail to generate grid firing fields network attractor states form, but their activity bumps are unable to track movement. In this scenario disrupted grid firing would reflect incorrect control of network activity by velocity signals. Alternatively, deficits in grid firing may reflect failure of network attractor states to emerge. To distinguish these possibilities we investigated formation of activity bumps in network space over the first 10 s following initialization of each network (Figure 3).

Our analysis suggests that the deficit in grid firing in deterministic compared to noisy networks reflects a failure of attractor states to emerge. For deterministic simulation of the points in parameter space considered in Figure 1Da, which are able to generate grid patterns, we found that a single stable bump of activity emerged over the first 2.5 s of simulated time (Figure 3Aa). In contrast, for deterministic simulation of the point considered in 1Db, which in deterministic simulations did not generate grid patterns, a single stable bump fails to emerge (Figure 3Ab). Quantification across the wider space of **gE** and **gI** values (see Methods) indicated that when **gI** is low there is a high probability of a bump formation as well as grid firing, whereas when **gI** is high the probability of both is reduced (Figure 3B). In contrast to the deterministic condition, for circuits with intrinsically noisy neurons activity bumps emerged in the first 1.25 s following initialization of the network (Figure 3Ac-e) and the area of parameter space that supported bump formation was much larger than that supporting grid firing (Figure 3B). Plotting gridness scores as a function of bump probability indicated that bump formation was necessary, although not sufficient for grid formation (Figure 3C). Together, these data indicate that noise promotes formation of attractor bumps in network activity and in deterministic simulations the failure of the circuit to generate attractor states largely accounts for disrupted grid firing.

In noisy networks the presence of low grid scores for networks with high bump scores (Figure 3C) is explained by sensitivity of these network configurations to noise. This is illustrated by the region of parameter space from Figure 1Db, where **gI** is relatively high and **gE** relatively low, and which in deterministic simulations fails to generate bumps or grids. With moderate noise, this point generates bumps that show little drift (Figure 3Ac), whereas as noise is increased further the bump begins to drift (Figure 3Ae). In contrast, at the point illustrated in Figure1Da, which forms grids and bumps in the presence or absence of noise, activity bumps are stable in each condition (Figure 3Aa). Thus, intrinsic noise has two opposing effects on bump formation. For much of the parameter space we consider moderate noise promotes emergence of bumps and grid, while across all of parameter space noise noise reduces bump stability leading to deterioration of grids.

To investigate how addition of noise promotes emergence of network attractor states we investigated the dynamics of neurons in the simulated circuits. We focus initially on the point in parameter space identified in Figure 1Db, where grids are found in the presence of moderate noise, and bumps are found when noise is moderate or high. When we examined times of action potentials generated by all neurons in this circuit, we find that in the absence of noise the network generates hyper-synchronous seizure-like states at the start of each theta cycle (Figure 4A and S5A). The number of E cells active on each theta cycle differs, but their activity is typically restricted to the rising phase of theta, and there is no consistent structure in the pattern of activated neurons. The number of simultaneously active I cells is also greatest at the start of each theta cycle. The I-cells continue to fire over the theta cycle, but their synchronization declines. When moderate noise is added to the circuit only a subset of E-cells are active on each theta cycle, forming an activity bump (Figure 4B and S5B). The I-cells are active at gamma frequency and the formation of an activity bump in the E-cell population is reflected by an inverted bump in the I-cell population activity (Figure 4B). With increased noise there is a similar overall pattern of activity, but spike timing becomes more variable, causing the bumps to become unstable and reducing the degree of synchronization at gamma frequencies (Figure 4C and S5C).

To determine whether these changes in network dynamics are seen across wider regions of parameter space we first quantified the presence of seizure like events from the maximum population firing rate in any 2 ms window over 10 s of simulation time (E-ratemax). Strikingly, we found that in the absence of noise epochs with highly synchronized activity were found for almost all combinations of **gE** and **gI**, whereas these seizure-like events were absent in simulations where noise was present (Figure 4D). Interestingly, while grids emerge in deterministic networks in regions of E-I space were E-ratemax is relatively low, there is a substantial region of parameter space in which E-ratemax is > 400 Hz, but grids are nevertheless formed. It is possible that seizure-like states may be rare in this region of parameter space and so do not interfere sufficiently with attractor dynamics to prevent grid firing. To test this we calculate for each combination of **gE** and **gI** the probability per theta cycle of events with population-average rate > 300 Hz (PE-rate > 300). For values of **gE** and **gI** where grid fields are present PE-rate > 300 was relatively low, indicating that seizure-like events are rare (Figure 4E). Consistent with this, when we plotted grid score as a function of PE-rate > 300, we found that P\_E-rate > 300 was relatively informative about the gridness score in networks without noise (MIC = 0.605) and a low value of PE-rate >300 was necessary for grid firing (Figure 4F). In contrast, E-ratemax was less informative of grid firing (0.392 <= MIC <= 0.532) and a wide range of values were consistent with grid firing (Figure 4F). Thus, while occasional seizure-like events do not prevent grid firing, when seizure-like events occur on the majority of theta cycles then grid firing is prevented.

**Our analysis points towards suppression of seizure-like events as the mechanism by which moderate noise promotes grid firing. However, we wanted to know if other factors might contribute to this beneficial role of noise. Grid fields may also fail to form if overall activity levels are too low, in which case neurons with grid fields instead encode head direction** (Bonnevie et al., 2013)**. This observation is unlikely to explain our results as the mean firing rate of E cells in networks that generated grid firing fields (grid score > 0.5, networks with gE or gI set to 0 excluded) was in fact lower than the firing rate of networks without grid fields (1.2; 1.0; 1.0 Hz grid fields vs. 3.0; 2.7; 1.2 Hz no grid fields, in networks with σ = 0; 150; 300 pA respectively). There was also no systematic relationship between grid score and firing frequency (Figure S6). We also wanted to know if other properties of grid fields vary as a function of gE and gI. Parameters used to calibrate velocity integration by the grid network varied very little with changes in gE and gI (Figure S7), whereas drift increased with gI (Figure S8) and place cell input was most effective in opposing attractor drift in noisy networks with high gridness scores (Figure S9). When theta frequency input to the network was replaced with a constant input with the same mean amplitude, the power of gamma oscillations was still dependent on the levels of noise and changes in gE and gI (Figure S10A-C), however the networks formed bumps successfully in almost the full range of gE and gI regardless of the level of noise (Figure S10D-F). These data are consistent with suppression of seizure like events as the mechanism by which noise promotes grid firing and demonstrate that the presence of theta frequency inputs is important in shaping the dynamics of attractor networks that generate grid fields.**

**Discussion**

We investigated the relationship between rate coded spatial computations and nested gamma oscillations in an attractor network model of grid firing. While rate coding and gamma oscillations share the same neural substrate, we find that their sensitivity to variations in excitatory and inhibitory synaptic strengths nevertheless differs. In the absence of noise only a restricted range of synaptic strengths support emergence of grid fields, whereas addition of a moderate level of noise promotes generation of both grid fields and nested gamma oscillations, primarily by the disruption of epileptic-like firing of E and I cells in the network. When the strength of E or I connections is varied in the presence of moderate noise a wide range of gamma frequency and power can be obtained without affected grid firing. Thus, noise can be beneficial for computations performed by the nervous system, while the frequency and power of gamma oscillations can be tuned without affecting rate-coded computations.

**Noise promotes network computations by opposing seizure-like activity**

Our results suggest a novel beneficial role for noise. In general noise in the nervous system is believed to distort the fidelity of transmitted signals (Faisal et al., 2008). An exception is stochastic resonance phenomena in which noise promotes detection of small amplitude signals by individual neurons (Benzi et al., 1999; Longtin et al., 1991; Shu et al., 2003). The beneficial role for noise that we identify here differs in that it emerges through interactions between populations of neurons and in that the grid cell attractor network performs a computation – generation of a spatial code from velocity inputs - rather than propagating input signals. By opposing emergence of hyper-sychronous seizure-like states noise allows the network to generate stable bump attractor states. We were able to identify this role for noise because spiking and synaptic dynamics are explicitly represented in the simulated network. These dynamics are absent from other attractor network models of grid firing (Burak and Fiete, 2009; Fuhs and Touretzky, 2006; Guanella et al., 2007)**.** They are also absentfrom other models of theta-nested gamma oscillations that simulate two-dimensional dynamical systems of E and I populations with theta modulated inputs to the network (Onslow et al., 2014). Thus, intrinsic cellular and synaptic dynamics in conjunction with noise sources may be important in accounting for computations and oscillatory activity in neural networks.

An intriguing aspect of our results is that they suggest novel approaches to suppressing seizures and to promoting normal cognitive function. Seizures have previously been suggested to result from deficits in inhibition or from alterations in intrinsic excitability of neurons (Lerche et al., 2001; Treiman, 2001). We show that seizures can be induced when these properties are held constant simply by reducing levels of noise within a circuit. A future experimental challenge for dissecting the contribution of intrinsic noise to seizures will be to target biological noise sources. In the brain noise arises from ion channel gating and from probabilistic release of neurotransmitter. It is therefore difficult to manipulate noise sources without also affecting intrinsic excitability or excitation-inhibition balance. However, it may be feasible to add noise to circuits through transcranial magnetic stimulation (Ruzzoli et al., 2010). In this case our simulations predict that addition of noise can restore epileptic circuits to normal activity. This mechanism may explain why transcranial magnetic stimulation of the entorhinal cortex in patients with seizures leads to an enhancement of memory performance (Suthana et al., 2012).

**Independent roles for gamma and rate-coded computations**

While correlations between gamma oscillations and various cognitive and pathological brain states are well established, the proposed computational roles of gamma oscillations have been difficult to reconcile with rate-coded representations with which they co-exist. We were able to address this issue directly by analyzing a circuit in which gamma oscillations and rate-coded computations arise from a shared mechanism. Rather than gamma serving as an index of rate-coded computation, we find instead that there is a substantial parameter space across which rate-coded computation is stable, while the amplitude and frequency of theta-nested gamma oscillations varies.

Our analysis leads to several new and testable predictions. First, tuning of recurrent synaptic connects could be used to tune gamma oscillations without affecting rate-coded computation. If multiple networks of the kind we simulate here correspond to grid modules providing input to downstream neurons in the hippocampus (Stensola et al., 2012), then adjusting **gE** or **gI** would alter gamma frequency with minimal effect on the grid firing pattern of each module. If the downstream neurons integrate input at the gamma time scale, then this should lead to re-mapping of their place representation in the absence of any change in either the strength of their synaptic inputs or the information they receive from upstream grid cells. Second, small differences in gamma could be a sensitive index of network pathology at stages before deficits in rate coded computation are apparent. If cognitive deficits in psychiatric disorders reflect a failure of rate coded computation, then our analysis predicts that a change in noise within a circuit, in addition to synaptic modification, may be necessary for deficits to emerge. From this perspective it is intriguing that seizure phenotypes are often associated with disorders such as autism (Deykin and MacMahon, 1979). Alternatively, cognitive deficits may result from a failure to coordinate gamma frequency synchronization of circuits that converge on downstream targets. In this case we expect cognitive deficits to be phenocopied by manipulations that affect gamma frequency or power without influencing rate-coded computations (Sigurdsson et al., 2010; Spellman and Gordon, 2014)**.**

In conclusion, our systematic exploration of three dimensions of parameter space (**gE**, **gI** and intrinsic noise) illustrates the complexity of relationships between rate-coded computation, gamma frequency oscillations and underlying cellular and molecular mechanisms. Our results highlight the challenges in straightforward interpretation of experiments in which these parameters are correlated to one another, cf. (Wang and Krystal, 2014). While there are parallels to investigations of pace-making activity in invertebrate circuits (Marder and Taylor, 2011), which demonstrate that many parameter combinations can account for higher order behavior, there are also critical differences in that the models we describe account for computation and oscillatory activity, while the number of neurons and connections in the simulated circuit is much larger. Future experimentation will be required to test our model predictions for unexpected beneficial roles of noise and for control of gamma oscillations independently from grid firing by modulating the strength of excitatory and inhibitory synaptic connections.

**Methods**

**The model comprised a network of exponential integrate and fire neurons** (Fourcaud-Trocmé et al., 2003) **implemented as a custom-made module of the NEST simulator** (Gewaltig and Diesmann, 2007)**. The network is modified from that in Pastoll et al. 2013 and consists of excitatory (E) and inhibitory (I) populations of neurons that were arranged on a twisted torus with dimensions of 34x30 neurons. Full details of the connectivity and network parameters are in the SI text.**

**In all simulations the networks were parameterized by the standard deviation of noise (σ) and synaptic scaling parameters (gE and gI). Noise was sampled from a Gaussian distribution with standard deviation either set to σ = 0, 150 or 300 pA, or alternatively in the range of 0-300 pA in steps of 10 pA (Figure 1K and 2H). The peaks of the synaptic profile functions (Figure 1B) were determined by the gE and gI parameters that appropriately scaled the maximal conductance values of the excitatory and inhibitory connections respectively.**

**Gridness score was estimated by simulating exploration in a circular arena with a diameter of 180 cm. For each value of gE and gI the simulations consisted of two phases. In the first phase, animal movement with constant speed and direction (horizontally from left to right) was simulated in order to calibrate the gain of the velocity input to achieve 60 cm spacing between grid fields in the network. In the second phase, the calibrated velocity input gains were used during a simulation of realistic animal movements with duration of 600 s. Each simulation was repeated 4 times. For each trial, gridness score was then estimated from an E cell located in position (0, 0) on the twisted torus.**

**For the analysis of bump attractor properties and gamma oscillations a separate set of simulations were run. For each value of gE, gI and noise level, there were 5 trials of 10 s duration during which the velocity and place cell inputs were deactivated. For each trial spiking activity of all cells were recorded. In addition, inhibitory synaptic currents of 25 randomly selected E cells were saved and used for further analysis.**

**The strength and frequency of gamma oscillation were estimated from the inhibitory synaptic currents recorded from E cells. The currents were first band-pass filtered between 20 and 200 Hz. For each trace, autocorrelation function was computed and the first local maximum was detected using a custom-implemented peak detection algorithm. The strength and frequency of gamma oscillation was estimated from the correlation value and lag at the position of the local maximum respectively.**

**Properties of bump attractors were estimated by fitting symmetric Gaussian functions onto successive snapshots of firing rates of each cell in the E population. For each snapshot this procedure yielded the position of the bump center and its width. The probability of bump formation was then estimated as a proportion of population-activity snapshots that were classified as bump attractors, i.e. those fitted Gaussian functions whose width did not exceed the shorter side of the twisted torus. Other properties of bump attractors were estimated by analyzing successive positions of the bump attractor centers.**

**The calculation of the maximal information coefficient for the relationship between gridness score, gamma and bump scores was estimated by applying the maximal information coefficient measure (MIC) using the minepy package** (Albanese et al., 2013)**. All other data analysis and simulations were performed in Python.**

**References**

Albanese, D., Filosi, M., Visintainer, R., Riccadonna, S., Jurman, G., and Furlanello, C. (2013). Minerva and minepy: a C engine for the MINE suite and its R, Python and MATLAB wrappers. Bioinformatics *29*, 407–408.

Benzi, R., Sutera, A., and Vulpiani, A. (1999). The mechanism of stochastic resonance. J. Phys. a: Math. Gen. *14*, L453–L457.

Bonnevie, T., Dunn, B., Fyhn, M., Hafting, T., Derdikman, D., Kubie, J.L., Roudi, Y., Moser, E.I., and Moser, M.-B. (2013). Grid cells require excitatory drive from the hippocampus. Nature Neuroscience *16*, 309–317.

Burak, Y., and Fiete, I.R. (2009). Accurate path integration in continuous attractor network models of grid cells. PLoS Comput Biol *5*, e1000291.

Chrobak, J.J., and Buzsáki, G. (1998). Gamma oscillations in the entorhinal cortex of the freely behaving rat. *18*, 388–398.

Couey, J.J., Witoelar, A., Zhang, S.-J., Zheng, K., Ye, J., Dunn, B., Czajkowski, R., Moser, M.-B., Moser, E.I., Roudi, Y., et al. (2013). Recurrent inhibitory circuitry as a mechanism for grid formation. Nature Neuroscience *16*, 318–324.

Deykin, E.Y., and MacMahon, B. (1979). The incidence of seizures among children with autistic symptoms. Am J Psychiatry *136*, 1310–1312.

Domnisoru, C., Kinkhabwala, A.A., and Tank, D.W. (2013). Membrane potential dynamics of grid cells. Nature *495*, 199–204.

Eliasmith, C. (2005). A unified approach to building and controlling spiking attractor networks. Neural Computation *17*, 1276–1314.

Faisal, A.A., Selen, L.P.J., and Wolpert, D.M. (2008). Noise in the nervous system. Nat Rev Neurosci *9*, 292–303.

Fourcaud-Trocmé, N., Hansel, D., van Vreeswijk, C., and Brunel, N. (2003). How spike generation mechanisms determine the neuronal response to fluctuating inputs. J Neurosci *23*, 11628–11640.

Fries, P. (2009). Neuronal gamma-band synchronization as a fundamental process in cortical computation. Annual Review of Neuroscience *32*, 209–224.

Fuhs, M.C., and Touretzky, D.S. (2006). A spin glass model of path integration in rat medial entorhinal cortex. J Neurosci *26*, 4266–4276.

Gewaltig, M.-O., and Diesmann, M. (2007). NEST (NEural Simulation Tool). Scholarpedia *2*, 1430.

Guanella, A., Kiper, D., and Verschure, P. (2007). A model of grid cells based on a twisted torus topology. International Journal of Neural Systems *17*, 231–240.

Histed, M.H., and Maunsell, J.H.R. (2014). Cortical neural populations can guide behavior by integrating inputs linearly, independent of synchrony. Proceedings of the National Academy of Sciences *111*, E178–E187.

Lerche, H., Jurkat Rott, K., and Lehmann Horn, F. (2001). Ion channels and epilepsy. American Journal of Medical Genetics *106*, 146–159.

Lewis, D.A., Curley, A.A., Glausier, J.R., and Volk, D.W. (2012). Cortical parvalbumin interneurons and cognitive dysfunction in schizophrenia. Trends Neurosci *35*, 57–67.

Longtin, A., Bulsara, A., and Moss, F. (1991). Time-interval sequences in bistable systems and the noise-induced transmission of information by sensory neurons. Physical Review Letters *67*, 656–659.

Lundqvist, M., Compte, A., and Lansner, A. (2010). Bistable, irregular firing and population oscillations in a modular attractor memory network. PLoS Comput Biol *6*, e1000803.

Marder, E., and Taylor, A.L. (2011). Multiple models to capture the variability in biological neurons and networks. Nature Neuroscience *14*, 133–138.

Moser, E.I., and Moser, M.-B. (2013). Grid Cells and Neural Coding in High-End Cortices. Neuron *80*, 765–774.

Onslow, A.C.E., Jones, M.W., and Bogacz, R. (2014). A canonical circuit for generating phase-amplitude coupling. PLoS ONE *9*, e102591.

Pastoll, H., Solanka, L., van Rossum, M.C.W., and Nolan, M.F. (2013). Feedback inhibition enables theta-nested gamma oscillations and grid firing fields. Neuron *77*, 141–154.

Rubenstein, J.L.R., and Merzenich, M.M. (2003). Model of autism: increased ratio of excitation/inhibition in key neural systems. Genes, Brain and Behavior *2*, 255–267.

Ruzzoli, M., Marzi, C.A., and Miniussi, C. (2010). The neural mechanisms of the effects of transcranial magnetic stimulation on perception. J Neurophysiol *103*, 2982–2989.

Sargolini, F., Fyhn, M., Hafting, T., McNaughton, B.L., Witter, M.P., Moser, M.-B., and Moser, E.I. (2006). Conjunctive representation of position, direction, and velocity in entorhinal cortex. Science *312*, 758–762.

Schmidt-Hieber, C., and Häusser, M. (2013). Cellular mechanisms of spatial navigation in the medial entorhinal cortex. Nature Neuroscience *16*, 325–331.

Shadlen, M.N., and Newsome, W.T. (1994). Noise, neural codes and cortical organization. Curr Opin Neurobiol *4*, 569–579.

Shu, Y., Hasenstaub, A., Badoual, M., Bal, T., and McCormick, D.A. (2003). Barrages of synaptic activity control the gain and sensitivity of cortical neurons. J Neurosci *23*, 10388–10401.

Sigurdsson, T., Stark, K.L., Karayiorgou, M., Gogos, J.A., and Gordon, J.A. (2010). Impaired hippocampal-prefrontal synchrony in a genetic mouse model of schizophrenia. Nature *464*, 763–767.

Spellman, T.J., and Gordon, J.A. (2014). Synchrony in schizophrenia: a window into circuit-level pathophysiology. Curr Opin Neurobiol *30C*, 17–23.

Stensola, H., Stensola, T., Solstad, T., Frøland, K., Moser, M.-B., and Moser, E.I. (2012). The entorhinal grid map is discretized. Nature *492*, 72–78.

Suthana, N., Haneef, Z., Stern, J., Mukamel, R., Behnke, E., Knowlton, B., and Fried, I. (2012). Memory enhancement and deep-brain stimulation of the entorhinal area. N. Engl. J. Med. *366*, 502–510.

Treiman, D.M. (2001). GABAergic mechanisms in epilepsy. Epilepsia *42*, 8–12.

Uhlhaas, P.J., and Singer, W. (2012). Neuronal Dynamics and Neuropsychiatric Disorders: Toward a Translational Paradigm for Dysfunctional Large-Scale Networks. Neuron *75*, 963–980.

Wang, X.J., and Krystal, J.H. (2014). Computational Psychiatry. Neuron *84*, 638–654.

Widloski, J., and Fiete, I.R. (2014). A Model of Grid Cell Development through Spatial Exploration and Spike Time-Dependent Plasticity. Neuron *83*, 481–495.

Yoon, K., Buice, M.A., Barry, C., Hayman, R., Burgess, N., and Fiete, I.R. (2013). Specific evidence of low-dimensional continuous attractor dynamics in grid cells. Nature Neuroscience *16*, 1077–1084.

Zhang, K. (1996). Representation of spatial orientation by the intrinsic dynamics of the head-direction cell ensemble: a theory. *16*, 2112–2126.

**Figure Legends**

**Figure 1. Noise increases the range of synaptic strengths that support grid firing.**

(A) A schematic of populations of excitatory cells (E cells, red) and inhibitory cells (I cells, blue) on a twisted torus of size 34x30 neurons. The synaptic coupling between the two populations was parameterized by the inter-population peak synaptic conductances **gE** (E -> I synapses) and **gI**(I -> E synapses).

(B) Top: Plots illustrate peak synaptic conductances of E (red) and I (blue) synapses as a function of the distance between pre- and post-synaptic neurons. Bottom: Distributions of synaptic weights from all I cells onto an E cell in the model (left) and from all E cells onto an I-cell (right). **gE** and **gI** determine maximal values of these distributions.

(C) Examples of the membrane potential of a single E cell during two consecutive theta cycles in networks without noise (white noise input current standard deviation (σ) = 0 pA), with an intermediate amount of noise (σ = 150 pA) and with noise levels doubled (σ = 300 pA). Theta signal is illustrated in grey.

(D-F) Example firing fields (left) and spatial autocorrelation plots (right) for the specific values of strengths of recurrent synaptic connections indicated by arrows in (G-I), corresponding to the three simulated noise levels.

(G-I) Gridness score as a function of **gE** and **gI** for networks without noise (G; σ = 0 pA), with noise level set to σ = 150 pA (H), and noise level set to σ = 300 pA (I). Each item in the color plot is an average gridness score of four simulation runs. Arrows indicate the positions of grid field and autocorrelation examples from simulations illustrated in (D-F). Simulations that did not finish in a specified time interval (5 h) are indicated by white color.

(J) Difference between gridness scores of networks with σ = 150 pA and networks with σ = 0 pA plotted as a function of **gE** and **gI**.

(K) Gridness score plotted as a function of the standard deviation of intrinsic noise. Each noise level comprises simulations from a neighborhood of **gE** and **gI** surrounding a center point in the parameter space (center included) indicated by arrows in (G-I). Each point is an average of 3 simulation runs.

**Figure 2. Differential sensitivity of gamma oscillations and grid fields to changes in the strength of E and I synapses.**

(A-C) Examples of inhibitory (red) and excitatory (blue) synaptic currents recorded respectively from excitatory and inhibitory neurons from simulations highlighted by arrows in panels (D-F).

(D-F) *Top:* Correlation value at the first local maximum of an autocorrelation of inhibitory synaptic currents (I 🡪 E cells, 25 randomly selected E cells), plotted as a function of **gE** and **gI**, for networks without noise (D), with noise level set to σ = 150 pA (E), and noise level set to σ = 300 pA (F). Each point is an average over five simulation trials. In these simulations velocity and place cell inputs were disabled. The duration of simulations was 10 seconds. *Bottom:* Frequency corresponding to the peaks of the autocorrelation functions for simulations in the top panels.

(G) Scatter plots show gridness score as a function of gamma oscillation strength (top) and frequency (bottom) for simulations with noise absent (green), with an intermediate level of noise (red) and highest simulated noise level (blue). Each dot represents data from a single network configuration.

(H) Top: Gamma oscillation strength plotted as a function of standard deviation of the noise current. Grey color indicates simulations with **gE** = 3 nS, **gI** = 1 nS (a). Red color indicates simulations with **gE** = 1 nS, **gI** = 3 nS (b). Bottom: Frequency corresponding to the detected autocorrelation peak.

**Figure 3. Noise promotes formation of continuous attractors.**

(A) Examples of E cell population firing rate snapshots from simulations in which velocity and place cell inputs are inactivated. Each row shows a simulation trial with a value of **gE** and **gI** highlighted by an arrow in panel (B). The corresponding probability of bump formation (P(bumps)) is indicated to the left.

(B) Color plots show probability of bump formation (P(bumps)), for the simulated range of **gE** and **gI** and the three simulated noise levels. Each color point is an average of five 10 s simulation runs. Arrows show positions in the parameter space of examples in (A).

(C) Relationship between gridness score computed from the grid field simulation runs (Figure 1G-I) and the probability of bump formation (B).

(D) Relationship between gamma oscillation strength (Figure 2D-F) and the probability of bump formation (B). Each color in (C and D) represents one noise level and each dot in the scatter plots corresponds to simulations of a single pair of values of gE and gI.

**Figure 4. Noise opposes generation of seizure-like states.**

(A-C) Raster plots show activity of all neurons in the excitatory (red) and inhibitory (blue) populations for the duration of two theta cycles (top), along with the average population firing rates for both populations (center and bottom; calculated with a sliding rectangular window with 2 ms duration and 0.5 ms time step), for networks where noise is absent (A; σ = 0), with noise set to σ = 150 pA (B), and with noise set to σ = 300 pA (C). Simulations were performed in the absence of animal movement and place cell input; **gE** = 1 nS and gI = 3 nS.

(D) Maximal average population firing rate of E cells estimated from the whole simulation run (10 s; 500 ms at the beginning of the simulation excluded) for each simulated level of noise. Each point is an average of maxima from 5 simulation runs.

(E) Probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz, i.e. at least 60% of E cells firing synchronously within a time period of 2 ms in the parameter space of **gE** and gI. Black lines indicate regions where gridness score equals 0.5.

(F) Scatter plots show the relationship between gridness score and the maximal firing rate during the simulation (left) and the probability of the maximal population-average firing rate during each theta cycle exceeding 300 Hz (right).