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I pledge my honor that I have abided by the Stevens Honor System

### Code

```
function main = main(image,sigma,threshold)
%Default Values
arguments
    image string = "plane.pgm";
    sigma string = "2";
    threshold string = "70";
end
sigma = str2double(sigma);
threshold = str2double(threshold);

%Read Image
image = imread(image);

%Gets the magnitude matrix using the gaussian image and applying
both
%sobels on it (gaussian done inside magnitude function)
sobel_matrix = magnitude(double(image),sigma,threshold);

%Finds Orientation Matrix
orientation_matrix = orientation(double(image),sigma);

%Uses Magnitude Matrix and Orientation Matrix to find the Non-
Maximum
%suppresion of the image
non_max = non_maxsuppression(sobel_matrix,orientation_matrix);

imshow(non_max);
end

%Pads Matrix
function padded_array = pad(image,sigma)
    %original rows, original columns
    [or,oc] = size(image);
    new_sigma = 5*sigma;
    m = zeros(or+(2*new_sigma), oc+(2*new_sigma), "double");
    m(new_sigma+1:or+new_sigma,new_sigma+1:oc+new_sigma)=image;

    %Top Left Corner
    for r = 1:new_sigma+1
        for c = 1:new_sigma+1
```

```

        m(r,c) = m(new_sigma+1,new_sigma+1);
    end
end
%Left side
for r = new_sigma+1:or+new_sigma-1
    for c = 1:new_sigma+1
        m(r,c) = m(r,new_sigma+1);
    end
end
%Bottom Left Corner
for r = or+new_sigma:or+(2*new_sigma)
    for c = 1:new_sigma+1
        m(r,c) = m(or+new_sigma,new_sigma+1);
    end
end
%Top
for r = 1:new_sigma
    for c = new_sigma+1:oc+new_sigma
        m(r,c) = m(new_sigma+1,c);
    end
end
%Top Right Corner
for r = 1:new_sigma+1
    for c = oc+new_sigma+1:oc+(2*new_sigma)
        m(r,c) = m(new_sigma+1,oc+new_sigma);
    end
end
%Right Side
for r = new_sigma+1:or+new_sigma-1
    for c = oc+new_sigma+1:oc+(2*new_sigma)
        m(r,c) = m(r,oc+new_sigma);
    end
end
%Bottom Right Corner
for r = or+new_sigma:or+(2*new_sigma)
    for c = oc+new_sigma+1:oc+(2*new_sigma)
        m(r,c) = m(or+new_sigma,oc+new_sigma);
    end
end
%Bottom
for r = or+new_sigma:or+(2*new_sigma)
    for c = new_sigma+1:oc+new_sigma
        m(r,c) = m(or+new_sigma,c);
    end
end
padded_array=m;

```

```

end

%Applies any filter to an image
%Takes in a filter, image, and the extended image
function apply_filter = app(filter,image,ext_image)
    [row,col] = size(image);
    [re,ce] = size(ext_image);
    [~,len] = size(filter);
    newx = re - row;
    newy = ce - col;
    image2 = zeros(row, col);
    for r = 1:row
        for c = 1:col
            newr = r + ((newx)/2);
            newc = c + ((newy)/2);
            piece = ext_image((newr)-((len-1)/2):(newr)+((len-1)/2), (newc)-((len-1)/2):(newc)+((len-1)/2));
            %mult_matrix = mult_matrices(filter,piece);
            mult_matrix = filter .* piece;
            image2(r,c) = sum(mult_matrix(:));
        end
    end
    apply_filter = image2;
end

```

```

%Gets the Gaussian Filter
function get_gaussian = gauss(sigma)
    size = 10*sigma;
    filter = zeros(size-1,size-1);
    for r = 1:size-1
        for c = 1:size-1
            x = abs(r - size/2);
            y = abs(c - size/2);
            filter(r,c) = (1/(2*pi*sigma))*exp(-(x^2 + y^2)/(2*sigma^2));
        end
    end
    sumof = sum(filter(:));
    get_gaussian = filter;
end

```

```

%Applies the Gaussian filter
function appgauss = appgauss(image,sigma)
    %Do the Gauss
    gaussian = gauss(sigma);

```

```

        padded_matrix = pad(image,sigma);
        appgauss = app(gaussian,image,padded_matrix);
end

%Applies the Vertical Sobel Filter
function sob1 = sobel1(image,gaussimage)
    single_pad = pad(gaussimage,1);
    sobelfilt1 = [-1 0 1; -2 0 2; -1 0 1];
    sob1 = app(sobelfilt1,gaussimage,single_pad);
    sob1 = double(sob1);

end

%Applies the Horizontal Sobel Filter
function sob2 = sobel2(image,gaussimage)
    single_pad = pad(gaussimage,1);
    sobelfilt2 = [1 2 1; 0 0 0; -1 -2 -1];
    sob2 = app(sobelfilt2,gaussimage,single_pad);
    sob2 = double(sob2);

end

function magnitude = magnitude(image,sigma,threshold)
    %Apply gauss on image, apply both sobel on gauss image,
    calc gradient
    %magnitude for each using formula, under certain threshhold
    get rid of
    %pixels
    [row,col] = size(image);

    %Do the Gauss
    gaussimage = appgauss(image,sigma);

    %App both Sobs
    sob1 = sobel1(image,gaussimage);
    sob2 = sobel2(image,gaussimage);
    image2 = gaussimage;

    %Gradient Matrix
    for r = 1:row
        for c= 1:col
            image2(r,c) = sqrt(((sob1(r,c))^2) +
((sob2(r,c))^2));
            %Under threshold remove
            if(image2(r,c)<threshold)
                image2(r,c) = 0;
            end
        end
    end
end

```

```

    end

    magnitude = image2;

end

%Gets the orientation matrix for non-max suppression
function orientation = orientation(image,sigma)
    [row,col] = size(image);
    gaussimage = appgauss(image,sigma);
    sob1 = sobel1(image,gaussimage);
    sob2 = sobel2(image,gaussimage);
    image2 = gaussimage;
    for r = 1:row
        for c= 1:col
            image2(r,c) =
atan(double(sob2(r,c))/double(sob1(r,c)));
        end
    end
    orientation = image2;
end

%Gets the image with non-maximum suppression
function non_max = non_maxsuppression(magnitude,orientation)
    [row,col] = size(orientation);
    m = zeros(row,col, "double");
    magnitude2 = pad(magnitude,1);

    for r = 1:row
        for c= 1:col
            newr=r+3;
            newc=c+3;
            %Horizontal
            if((orientation(r,c) >= (-pi/2)) &&
(orientation(r,c) <= (-3*pi/8)))
                if(magnitude2(newr,newc) > magnitude2(newr-
1,newc) && magnitude2(newr,newc) > magnitude2(newr+1,newc))
                    m(r,c) = 255;
                else
                    m(r,c) = 0;
                end
            end
            %Vertical
            if( (orientation(r,c) > (-3*pi/8)) &&
(orientation(r,c) <= (-pi/8)))

```

```

        if(magnitude2(newr,newc) >
magnitude2(newr,newc-1) && magnitude2(newr,newc) >
magnitude2(newr,newc+1))
            m(r,c) = 255;
        else
            m(r,c) = 0;
        end
    end
    %Left Diagonal
    if( (orientation(r,c) > (-pi/8)) &&
(orientation(r,c) <= (pi/8)) )
        if(magnitude2(newr,newc) > magnitude2(newr-
1,newc-1) && magnitude2(newr,newc) > magnitude2(newr+1,newc+1))
            m(r,c) = 255;
        else
            m(r,c) = 0;
        end
    end
    %Right Diagonal
    if( (orientation(r,c) > (pi/8)) &&
(orientation(r,c) <= (3*pi/8)))
        if(magnitude2(newr,newc) >
magnitude2(newr+1,newc-1) && magnitude2(newr,newc) >
magnitude2(newr-1,newc+1))
            m(r,c) = 255;
        else
            m(r,c) = 0;
        end
    end
    %Also Horizontal
    if( (orientation(r,c) > (3*pi/8)) &&
(orientation(r,c) <= (pi/2)))
        if(magnitude2(newr,newc) > magnitude2(newr-
1,newc) && magnitude2(newr,newc) > magnitude2(newr+1,newc))
            m(r,c) = 255;
        else
            m(r,c) = 0;
        end
    end

end
end
non_max = m;

end

```

## Resulting Images

### Part1 Gaussian Filters



Image: kangaroo

Sigma : 2



Image: kangaroo

Sigma : 3



Image: plane

Sigma : 2



Image: plane

Sigma : 3



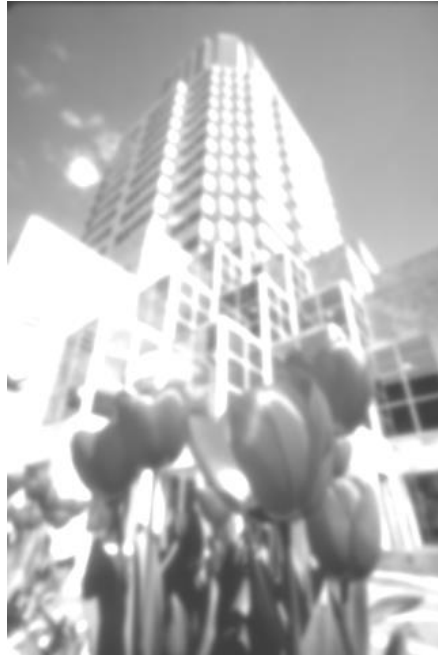


Image: red

Sigma : 2



Image: red

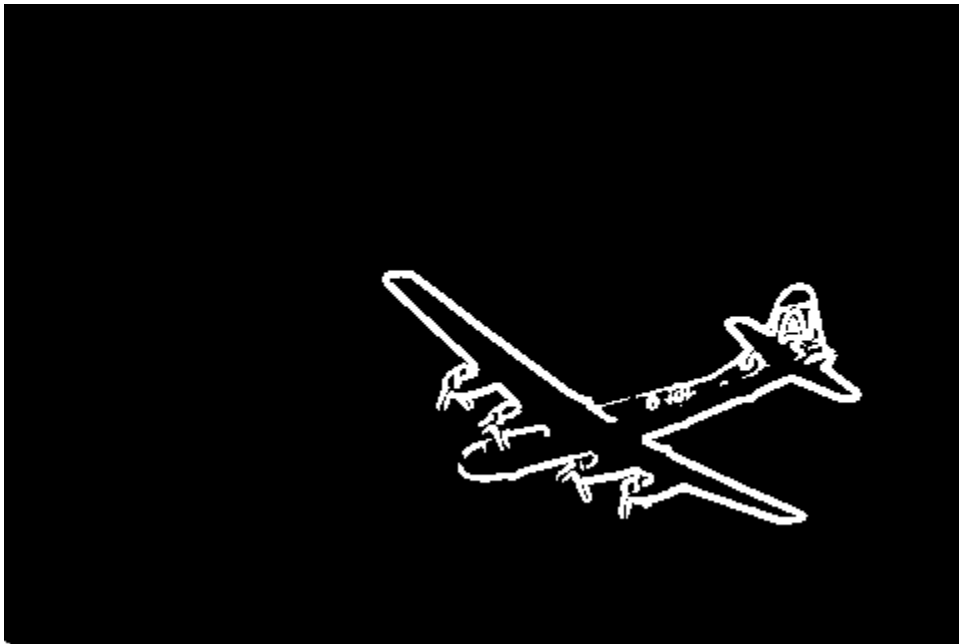
Sigma : 3

## Part 2 Sobel Magnitude



$\text{Sigma} = 2$

Threshold = 70



$\text{Sigma} = 1$

Threshold = 70



Sigma = 1

Threshold = 70

### Part 3 : Non-maximum Suppression



Sigma = 2

Threshold = 70



Sigma = 1

Threshold = 70



$\text{Sigma} = 1$

$\text{Threshold} = 70$

I split up the code into 3 major steps as outlined by the homework. First I applied the gaussian filter to the image, then found the magnitude matrix of the image, and then found the non-maximum suppressed image. I further split up my work into smaller steps.

#### Step 1 (Finding the Gaussian):

In order to do this I first padded the matrix as described in the assignment (“replicate boundary pixels when the filter window falls out of bounds”). Then I created the gaussian matrix based on the sigma inputted. **Note: my gaussian matrix is of size  $10 \times \text{sigma}$ , with a half length of  $5 \times \text{sigma}$ , since this way the gaussian matrix sums to 1.**

Then I created a function that applied all filters given the image, the filter, and the padded image. This was later used to apply the sobel filters, but in this case it was used to create a function, `appgauss`, that would apply the gaussian filter generated by the sigma inputted onto an image.

#### Step 2 (Finding the Magnitude Matrix):

In order to find the Magnitude matrix I used my apply filter function (`app`) to apply both the vertical and horizontal sobel filters onto the image which has had the gaussian applied to it. Then I calculate the magnitude using the formula `sqrt(((sobel(r,c))^2) + ((sobel2(r,c))^2))`.

#### Step 3 (Finding the non-maximum suppression image):

This step used all of the previous functions in order to be accomplished. I also generate an orientation matrix. With both the magnitude and orientation matrices I created an algorithm that identifies which direction the pixel is and then check the neighbors based on that. If it is greater than both of its neighbors I set the pixel to 255 (white) and otherwise 0 (black).