WST ETC

January 24, 2023

```
[1]: #from mpdaf.obj import Sepctrum, Cube, Image
   import matplotlib
   from mpdaf.obj import mag2flux, flux2mag
   from matplotlib import pyplot as plt
   import numpy as np
   from astropy.table import Table
   matplotlib.rcParams.update({'font.size': 20})
[2]: from pyetc.wst import WST
   from pyetc.etc import show noise, get seeing fwhm
```

1 Initialise ETC module

We start by creating the wst object with wst = WST(). To get more or less message, it is possible to use wst = WST(log='DEBUG') or wst = WST(log='WARNING') to have less.

```
[3]: wst = WST(log='DEBUG')
```

Currently only the IFS (2 channels blue and red) and MOS-LR (2 channels blue and red) are defined.

- The IFS channels are based on 4K CCD with a f/1 camera, leading to 0.25 arcsec spaxel. The LSF of 2.5 pixels, throughputs are inspired by MUSE and BlueMUSE. Note that the throughputs curves are for the telescope + instrument (excluding atmosphere).
- The MOS-LR channels are based on 6k detectors. Throughputs are inspired by 4MOST. Fiber have a 1 arcsec sky aperture. Sampling is 0.25 arcsec.
- In addition, paranal sky absorption and emssion are pre-computed for different conditions:
 - Moon: darksky (new moon), greysky (FLI = 0.5) and brightsky (full moon)
 - Airmass: 1, 1.2, 1.5, 2.0
 - Sky are computed with the ESO skycalc tool, using the proper spectral binning and LSF convolution for each channel

the detail of the configuration is shown with wst.info()

```
[4]: wst.info()

[INFO] WST ETC version: 0.1

[INFO] Diameter: 11.25 m Area: 100.0 m2

[INFO] IFS type IFS Channel blue

[INFO] Inspired from BlueMUSE throughput 5/01/2022
```

```
[INFO]
         Spaxel size: 0.25 arcsec Image Quality tel+ins fwhm: 0.10 arcsec beta:
2.50
[INFO]
         Wavelength range [3700. 6100.] A step 0.64 A LSF 2.5 pix Npix 3751
[INFO]
         Instrument transmission peak 0.38 at 5315 - min 0.28 at 3700
         Detector RON 3.0 e- Dark 3.0 e-/h
[INFO]
[INFO]
         Sky moon brightsky airmass 1.0 table ifs blue brightsky 1.0.fits
[INFO]
         Sky moon brightsky airmass 1.2 table ifs blue brightsky 1.2.fits
[INFO]
         Sky moon brightsky airmass 1.5 table ifs_blue_brightsky_1.5.fits
         Sky moon brightsky airmass 2.0 table ifs blue brightsky 2.0.fits
[INFO]
[INFO]
         Sky moon darksky airmass 1.0 table ifs_blue_darksky_1.0.fits
         Sky moon darksky airmass 1.2 table ifs_blue_darksky_1.2.fits
[INFO]
         Sky moon darksky airmass 1.5 table ifs_blue_darksky_1.5.fits
[INFO]
[INFO]
         Sky moon darksky airmass 2.0 table ifs_blue_darksky_2.0.fits
         Sky moon greysky airmass 1.0 table ifs_blue_greysky_1.0.fits
[INFO]
[INFO]
         Sky moon greysky airmass 1.2 table ifs_blue_greysky_1.2.fits
[INFO]
         Sky moon greysky airmass 1.5 table ifs_blue_greysky_1.5.fits
[INFO]
         Sky moon greysky airmass 2.0 table ifs_blue_greysky_2.0.fits
[INFO]
         Instrument transmission table ifs_blue_noatm.fits
[INFO] IFS type IFS Channel red
[INFO]
         Inspired from MUSE throughput 5/01/2022
[INFO]
         Spaxel size: 0.25 arcsec Image Quality tel+ins fwhm: 0.10 arcsec beta:
2.50
         Wavelength range [6058. 9299.9] A step 0.85 A LSF 2.5 pix Npix 3815
[INFO]
[INFO]
         Instrument transmission peak 0.39 at 6830 - min 0.14 at 9300
[INFO]
        Detector RON 3.0 e- Dark 3.0 e-/h
[INFO]
         Sky moon brightsky airmass 1.0 table ifs_red_brightsky_1.0.fits
[INFO]
         Sky moon brightsky airmass 1.2 table ifs_red_brightsky_1.2.fits
[INFO]
         Sky moon brightsky airmass 1.5 table ifs_red_brightsky_1.5.fits
[INFO]
         Sky moon brightsky airmass 2.0 table ifs_red_brightsky_2.0.fits
[INFO]
         Sky moon darksky airmass 1.0 table ifs_red_darksky_1.0.fits
[INFO]
         Sky moon darksky airmass 1.2 table ifs_red_darksky_1.2.fits
[INFO]
         Sky moon darksky airmass 1.5 table ifs_red_darksky_1.5.fits
[INFO]
         Sky moon darksky airmass 2.0 table ifs_red_darksky_2.0.fits
[INFO]
         Sky moon greysky airmass 1.0 table ifs_red_greysky_1.0.fits
         Sky moon greysky airmass 1.2 table ifs red greysky 1.2.fits
[INFO]
[INFO]
         Sky moon greysky airmass 1.5 table ifs red greysky 1.5.fits
         Sky moon greysky airmass 2.0 table ifs red greysky 2.0.fits
[INFO]
[INFO]
         Instrument transmission table ifs red noatm.fits
[INFO] MOSLR type MOS Channel blue
         Inspired from 4MOST LR throughput 5/01/2022
[INFO]
[INFO]
         Spaxel size: 0.25 arcsec Image Quality tel+ins fwhm: 0.30 arcsec beta:
2.50
[INFO]
         Fiber aperture: 1.0 arcsec
         Wavelength range [3700. 6120.] A step 0.40 A LSF 2.5 pix Npix 6051
[INFO]
[INFO]
         Instrument transmission peak 0.12 at 5402 - min 0.01 at 3700
[INFO]
         Detector RON 3.0 e- Dark 3.0 e-/h
[INFO]
         Sky moon brightsky airmass 1.0 table moslr_blue_brightsky_1.0.fits
[INFO]
         Sky moon brightsky airmass 1.2 table moslr_blue_brightsky_1.2.fits
```

```
[INFO]
         Sky moon brightsky airmass 1.5 table moslr_blue_brightsky_1.5.fits
[INFO]
         Sky moon brightsky airmass 2.0 table moslr_blue_brightsky_2.0.fits
[INFO]
         Sky moon darksky airmass 1.0 table moslr_blue_darksky_1.0.fits
[INFO]
         Sky moon darksky airmass 1.2 table moslr_blue_darksky_1.2.fits
         Sky moon darksky airmass 1.5 table moslr blue darksky 1.5.fits
[INFO]
[INFO]
         Sky moon darksky airmass 2.0 table moslr blue darksky 2.0.fits
[INFO]
         Sky moon greysky airmass 1.0 table moslr blue greysky 1.0.fits
[INFO]
         Sky moon greysky airmass 1.2 table moslr_blue_greysky_1.2.fits
[INFO]
         Sky moon greysky airmass 1.5 table moslr blue greysky 1.5.fits
[INFO]
         Sky moon greysky airmass 2.0 table moslr_blue_greysky_2.0.fits
         Instrument transmission table moslr_blue_noatm.fits
[INFO]
[INFO] MOSLR type MOS Channel red
         Inspired from 4MOST LR throughput 5/01/2022
[INFO]
         Spaxel size: 0.25 arcsec Image Quality tel+ins fwhm: 0.30 arcsec beta:
[INFO]
2.50
[INFO]
         Fiber aperture: 1.0 arcsec
[INFO]
         Wavelength range [6073. 9299.5] A step 0.54 A LSF 2.5 pix Npix 5976
         Instrument transmission peak 0.13 at 7112 - min 0.05 at 9300
[INFO]
[INFO]
         Detector RON 3.0 e- Dark 3.0 e-/h
[INFO]
         Sky moon brightsky airmass 1.0 table moslr red brightsky 1.0.fits
         Sky moon brightsky airmass 1.2 table moslr red brightsky 1.2.fits
[INFO]
         Sky moon brightsky airmass 1.5 table moslr red brightsky 1.5.fits
[INFO]
[INFO]
         Sky moon brightsky airmass 2.0 table moslr_red_brightsky_2.0.fits
[INFO]
         Sky moon darksky airmass 1.0 table moslr_red_darksky_1.0.fits
[INFO]
         Sky moon darksky airmass 1.2 table moslr_red_darksky_1.2.fits
[INFO]
         Sky moon darksky airmass 1.5 table moslr_red_darksky_1.5.fits
[INFO]
         Sky moon darksky airmass 2.0 table moslr_red_darksky_2.0.fits
         Sky moon greysky airmass 1.0 table moslr_red_greysky_1.0.fits
[INFO]
[INFO]
         Sky moon greysky airmass 1.2 table moslr_red_greysky_1.2.fits
[INFO]
         Sky moon greysky airmass 1.5 table moslr_red_greysky_1.5.fits
[INFO]
         Sky moon greysky airmass 2.0 table moslr_red_greysky_2.0.fits
[INFO]
         Instrument transmission table moslr_red_noatm.fits
```

2 Instruments and channels

The wst object has one telescope and two instruments: wst.tel, wst.ifs and wst.moslr. Each instrument has 2 channels: blue and red. For example, to access the red channel of the ifs we have to use wst.ifs['red']. Each channel is a dictionary with all instrument properties.

For example to list all elements of the MOS-LR blue channel, we will use wst.moslr['blue'].keys().

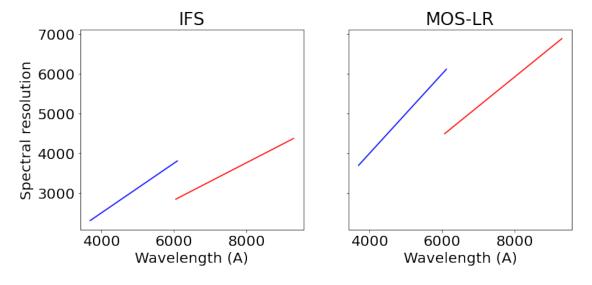
The dictionary keys are the following:

- desc: description of the channel
- name: channel name (eg ifs or moslr)
- chan: channel name (blue or red)
- type: instrument type (IFS or MOS)
- iq_fwhm: the FWHM of the image quality of telescope + instrument, excluding atmosphere
- iq beta: the beta parameter of the MOFFAT image quality
- aperture: the fiber diameter aperture in arcsec (only for MOS)
- spaxel size: the spaxel size in arcsec
- dlbda: the wavelength increment in A
- lbda1: starting wavelength in A
- lbda2: ending wavelength in A
- lsfpix: the LSF size in spectels (spectral pixels)
- ron: read-out noise in e- by pixel
- dcurrent: dark current in e-/hour by pixel
- wave: wavelength WaveCoord MPDAF object (see MPDAF spectrum documentation)
- instrans: total telescope + instrument transmission, excluding atmosphere (Spectrum MPDAF object)
- skys: the list of the name of all moon configuration e.g. wst.ifs['blue']['skys'] = ['brightsky', 'darksky', 'greysky']
- sky: a list of dictionnaries related to each sky configuration

One can view them the first one with wst.ifs['blue']['sky'][0]

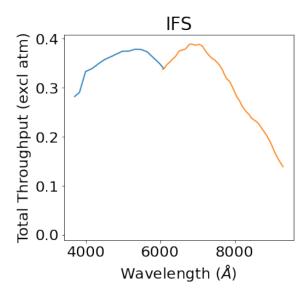
3 Spectral resolution

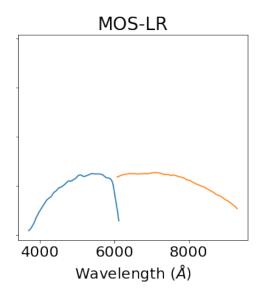
We now note ins a specific instrument channel, eg ins = wst.ifs['red'] The function ins.get_spectral_resolution() return an array with the spectral resolution. The ins['wave'].coord() return the corresponding wavelength array.



4 Throughput

The ins['instrans'] is a MPDAF spectrum with the total instrument plus telescope throughput.



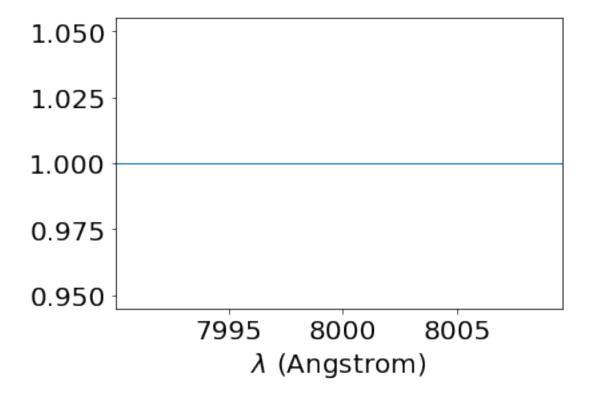


5 Surface Brightness

We now derive S/N estimate for surface brightness sources. In this case the source is just defined by a spectrum. The function spec = wst.get_spec(ins, dspec) is used to build the source spectrum. The dspec dictionnary has the spectrum parameters, there are currently three categories of sources: flatcont, line and template.

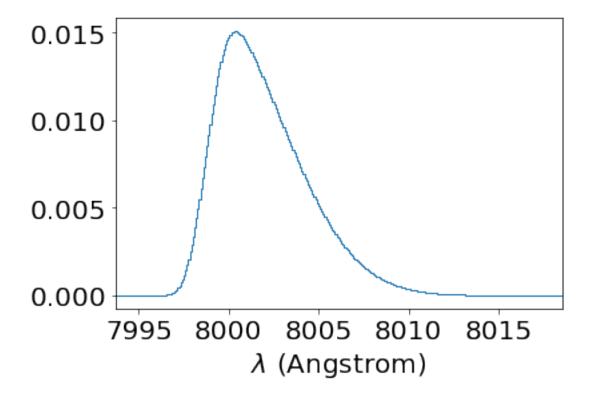
The flatcont type describe a flat continuum source: dict(type='flatcont', wave=[lbda1,lbda2]) where wave is the wavelength range, in A. The result of the get_spec function is a MPDAF spectrum. The spectrum is normalized at 1. See here for the MPDAF Spectrum documentation.

```
[9]: ifs = wst.ifs['red']
  wave = 8000
  dspec = dict(type='flatcont', wave=[wave-10,wave+10])
  spec = wst.get_spec(ifs, dspec)
  spec.plot()
```



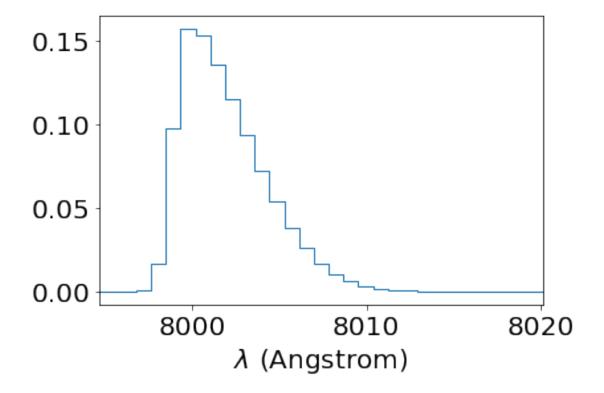
The line type, describe an emission line. The emission line is modelled by a skewed gaussin function with the following parameters: dict(type='line', lbda=wave, sigma=4.0, skew=7.0) where wave is the wavelength of the peak, sigma is the gaussian sigma and skew is the skew parameter. A Gaussian has skew=0.

```
[10]: wave = 8000
dspec = dict(type='line', lbda=wave, sigma=4.0, skew=7.0)
spec = wst.get_spec(ifs, dspec)
spec.plot()
```



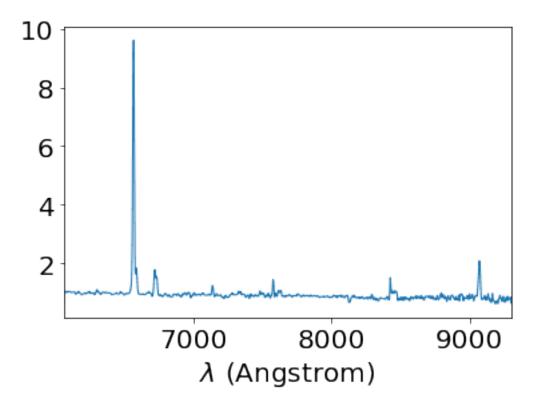
By default, the returned emission line spectrum is oversampled by a factor 10 with respect to the instrument spectral sampling and convolved with the LSF. The rebinning and trunctation of the spectral is performed later. It is possible to change this parameters, but it is recommneded to keep the default LSF convolution and oversampling.

```
[11]: spec = wst.get_spec(ifs, dspec, oversamp=1, lsfconv=False)
spec.plot()
```



The **template** type describe one of the source of the **spextra** python library. Check the documentation here for the complete list. The parameters are the following: - name, the name of the template - wave_center, the central wavelength in A used to normalize the spectrum - wave_wdth, the window in A used for the normalisation

Note that window does not need to be within the channel wavelngth interval. The template spectrum is LSF convolved and resampled to the channel sampling.



The next step is to define the observation parameters. They are written in a dictionnary which is add to the wst object by the wst.set_obs(obs) command.

The content of wst.obs is function of the source type. For surface brightness source it is composed of:

- moon: the moon phase, it must be part of the pre-loaded configurations (currently darksky, greysky or brightsky).
- airmass: the observation airmass. Note that it must be part of the pre-loaded sky configuration, otherwise the program will raise an exception.
- ndit: the number of exposures
- dit: the integration time of one exposure in sec
- ima_type: sb, for surface brightness
- ima_area: the size of the area to be considered for S/N computation. It is needed only for IFS, for the MOS it is defined by the fiber aperture.
- spec_type: must be one of cont,line,template

in addition if spec_type is set to **line**, additional parameters are needed: - spec_range_type: can be **fixed** or **adaptative**, used to define the spectral range to consider for the S/N computation. - spec_range_hsize_spectels: if spec_range_type is fixed, it define the number of spectels to consider, the total size is 2 * spec_range_hsize_spectels + 1 - spec_range_kfwhm: if spec_range_type is adaptative, it compute the size of the window relative to the FWHM of the line.

The last parameter needed is the **flux** of the source in $erg.s^{-1}.cm^{-2}.arcsec^{-2}$ unit.

5.1 Continuum source

The estimate of S/N is then computed with the wst.snr_from_source() command.

Note that the ima parameter is set to None because we are in the surface brightness mode.

```
[14]: flux = 5.e-19
res = wst.snr_from_source(ifs, flux, ima=None, spec=spec)
```

[DEBUG] Source type sb & cont Flux 5.00e-19 S/N 2.7 FracFlux 1.000 Nspaxels 16 Nspectels 1

The output of snr_from_source is the dictionary res. It contains the following elements:

- input: a dictionnary with some input data used in S/N computation
- cube: a dictionary that contains S/N measurements by voxels
- spec: a dictionnary that contains S/N summed over the spatial direction
- aper: a dictionnary with values summed over an aperture (only for line spectral type)

We detail the content of each dictionnary in the next paragraphs.

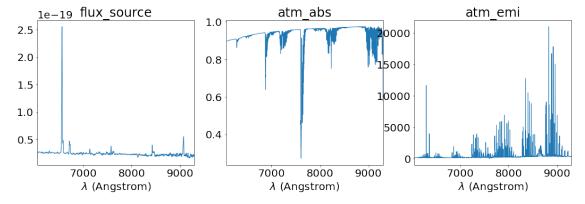
The **input** dictionary contains the following items:

- flux source: the source flux in erg/s/cm2/voxel
- atm_abs: the atmospheric absorption
- atm emi: the atmospheric emission in e-/s
- and all used **obs** parameters

```
[15]: res['input']
```

```
'ima_area': 1.0}

[16]: r = res['input']
    fig,ax = plt.subplots(1,3,figsize=(18,5))
    r['flux_source'].plot(ax=ax[0], title='flux_source')
    r['atm_abs'].plot(ax=ax[1], title='atm_abs')
    r['atm_emi'].plot(ax=ax[2], title='atm_emi')
```



The **cube** dictionary contains all quantities by voxels. Depending of the type of the source it can be datacubes, images or spectra. In the case of surface brightness source, it is restricted to spectra, because all spaxels are identical.

- snr: the snr spectrum by voxel which can be displayed with snr.plot().
- noise: the noise dictionnary contains all sources of noise by voxel.
 - ron: the detector readout noise in e- (constant with wavelength)
 - dark: the detector dark current in e- (cosntant with wavelength)
 - sky: the sky noise spectrum in e-

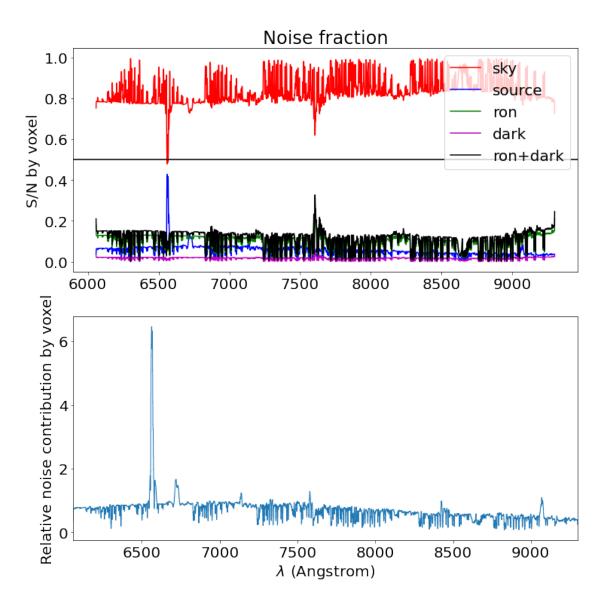
'ima_type': 'sb',

- source: the source noise spectrum in e-
- tot: the total noise spectrum in e-
- nph source: the number of source photo-electrons received by voxel
- nph sky: the number of source photo-electrons received by voxel

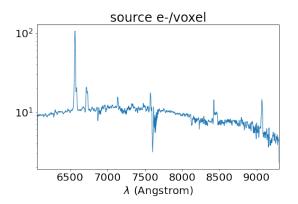
The show_noise(res['cube']['noise'], ax) can be used to display the relative noise contrbution.

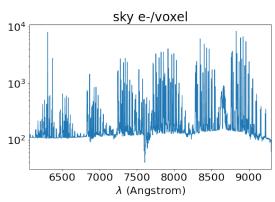
One can see in this example, that we are in photon noise regime, with 80% of the noise contribution due to the sky brightness.

```
[17]: fig,ax = plt.subplots(2,1,figsize=(12,12))
    res['cube']['snr'].plot(ax=ax[1])
    ax[0].set_ylabel('S/N by voxel')
    show_noise(res['cube']['noise'], ax[0], legend=True)
    ax[1].set_ylabel('Relative noise contribution by voxel');
```



```
[18]: fig,ax = plt.subplots(1,2,figsize=(18,5))
res['cube']['nph_source'].plot(ax=ax[0], stretch='log', title='source e-/voxel')
res['cube']['nph_sky'].plot(ax=ax[1], stretch='log', title='sky e-/voxel')
```



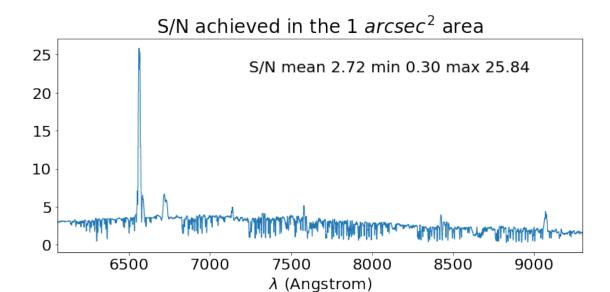


The **spec** dictionary contains all spatially integrated quantities, in MPDAF spectrum format. Specifically it is composed of:

- frac flux: the total fraction of flux recovered (it is 1 in our case)
- frac ima: thre fraction of flux recoovered in the spatial axis
- frac_spec: thre fraction of flux recoovered in the spectral axis
- nb_spaxels: the number of spaxels that have been summed
- nph_source: the number of source photo-electrons received by spectel
- nph sky: the number of source photo-electrons received by spectel
- snr: the snr spectrum by spectel
- snr_mean: the average value of the S/N by spectels
- snr min: the minimum value of the S/N by spectels
- snr_max: the maximum value of the S/N by spectels
- noise: the noise dictionnary contains all sources of noise by spectel.
 - ron: the detector readout noise in e- (constant with wavelength)
 - dark: the detector dark current in e- (cosntant with wavelength)
 - sky: the sky noise spectrum in e-
 - source: the source noise spectrum in e-
 - tot: the total noise spectrum in e-

```
[19]: fig,ax = plt.subplots(1,1,figsize=(12,5))
sp = res['spec']
sp['snr'].plot(ax=ax, title=r'S/N achieved in the 1 $arcsec^2$ area')
ax.text(0.9, 0.9, f"S/N mean {sp['snr_mean']:.2f} min {sp['snr_min']:.2f} max_\[ \to \{sp['snr_max']:.2f}\],
transform=ax.transAxes, ha='right', va='top')
```

[19]: Text(0.9, 0.9, 'S/N mean 2.72 min 0.30 max 25.84')



5.2 Emission line source

Computation for an emission line extended source is similar. This gives:

```
[20]: wave = 8000
      dspec = dict(type='line', lbda=wave, sigma=4.0, skew=7.0)
      spec = wst.get_spec(ifs, dspec)
      obs = dict(
          moon='darksky',
          airmass = 1.2,
          ndit = 2,
          dit = 1800,
          spec_type = 'line',
          spec_range_type = 'fixed',
          spec_range_hsize_spectels = 7,
          ima_type = 'sb',
          ima_area = 1.0,
      wst.set_obs(obs)
      flux = 1.e-18
      res = wst.snr_from_source(ifs, flux, ima=None, spec=spec)
```

[DEBUG] Source type sb & line Flux 1.00e-18 S/N 0.8 FracFlux 0.943 Nspaxels 16 Nspectels 15

The **res** dictionary now contains an additional item: **aper**. This new directory contains measurements once integrated both spatially and spectrally. Specifically it contains:

- frac flux: the total fraction of captured flux
- frac_ima: the fraction of flux captured within the spatial aperture

- frac_spec: the fraction of flux captured along the spectral direction
- nb spaxels: the number of summed spaxels
- $\bullet\,$ nb_spectels: the number of summed spectels
- nb_voxels: the total number of summed voxels
- nph_source: the number of source photo-electrons
- nph_sky: the number of sky photo-electrons
- snr: the snr spectrum
- ron: the detector readout noise in e-
- dark: the detector dark current in e-
- sky_noise: the sky noise in e-
- source_noise: the source noise in e-
- tot noise: the total noise in e-
- frac_detnoise: the ratio of the detector (ron+dark) variance to the total variance

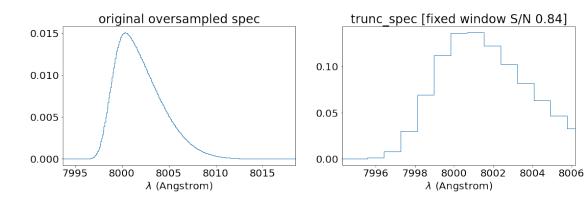
The wst.print_aper(res, title) can be used to display the result

```
[21]: wst.print_aper(res, 'aperture values')
```

[21]: <Table length=17>

item	aperture values	
bytes20	bytes20	
snr	0.844	
size	1	
area	1	
<pre>frac_flux</pre>	0.9427	
frac_ima	1	
<pre>frac_spec</pre>	0.9427	
nb_spaxels	16	
nb_spectels	15	
nb_voxels	240	
nph_source	378.2	
nph_sky	1.954e+05	
ron	65.73	
dark	26.83	
sky_noise	442	
source_noise	19.45	
tot_noise	448.1	
<pre>frac_detnoise</pre>	0.0251	

The **cube** dictionary contains an additional element: **trunc_spec** which the spectrum after truncation by a window specified by the **spec_range_hsize_spectels** obs keyword. It is displayed here:



Rather than using a window of fixed size, we can use an adaptative size which is function of the fwhm of the line.

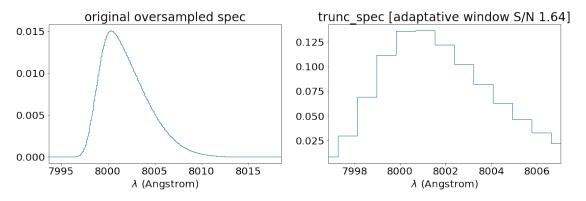
```
cobs = dict(
    moon='darksky',
    airmass = 1.2,
    ndit = 2,
    dit = 1800,
    spec_type = 'line',
    spec_range_type = 'adaptative',
    spec_range_kfwhm = 2,
    ima_type = 'sb',
    ima_area = 1.0,
)

wst.set_obs(obs)
res = wst.snr_from_source(ifs, flux, ima=None, spec=spec)
```

[DEBUG] Source type sb & line Flux 1.00e-18 S/N 1.6 FracFlux 0.963 Nspaxels 16 Nspectels 13

```
[24]: fig,ax = plt.subplots(1,2,figsize=(18,5))
spec.plot(ax=ax[0], title='original oversampled spec')
res['cube']['trunc_spec'].plot(ax=ax[1], title=f"trunc_spec [adaptative window_

S/N {res['aper']['snr']:.2f}]")
```



We see that the adptative window better follow the asymetric line shape and provide a S/N improved by a factor 2.

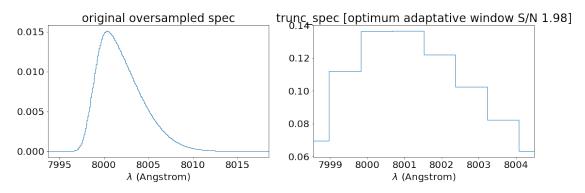
We can go one step further by using the wst.optimum_spectral_range() function to find the spec_range_fkwhm parameter whihe maximize the S/N. The optimum parameter is saved in the obs parameters, so we just need to rerun snr from source after.

```
[25]: kfwhm = wst.optimum_spectral_range(ifs, flux, None, spec)
res = wst.snr_from_source(ifs, flux, ima=None, spec=spec)
```

[DEBUG] Optimizing kwhm in [0.25439668200258014, 3.5717294153162253]

[DEBUG] Optimum spectral range nit=12 kfwhm=1.13 S/N=2.0 Size=6.0 Flux=1.00e-18 Frac=0.82

[DEBUG] Source type sb & line Flux 1.00e-18 S/N 2.0 FracFlux 0.824 Nspaxels 16 Nspectels 8



5.3 Retrieve flux for a given S/N

It is often useful to evaluate the flux limit, i.e. the flux which is needed to obtain a S/N of 3. For this, we can use the wst.flux_from_source function.

```
[27]: snr = 3
res = wst.flux_from_source(ifs, snr, None, spec)
```

[DEBUG] Source type sb & line Flux 1.52e-18 S/N 3.0 FracFlux 0.824 Nspaxels 16 Nspectels 8

[DEBUG] SN 3.00 Flux 1.52e-18 Iter 5 Fcall 6 converged True

In the case of an emission line source, the estimated flux value is saved in res['aper']['flux'].

```
[28]: wst.print_aper(res, 'res')
```

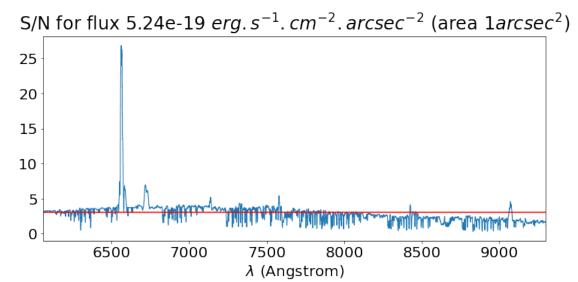
[28]: <Table length=18>

item	res	
bytes20	bytes20	
snr	3	
size	1	
area	1	
<pre>frac_flux</pre>	0.8237	
frac_ima	1	
frac_spec	0.8237	
nb_spaxels	16	
nb_spectels	8	
nb_voxels	128	
nph_source	500.9	
nph_sky	2.469e+04	
ron	48	
dark	19.6	
sky_noise	157.1	
source_noise	22.38	
tot_noise	167	
${\tt frac_detnoise}$	0.09641	
flux	1.517e-18	

But in the case of a **cont** or **template** source, we have to specify a window range to compute an average target S/N. This is done with the **waves** parameter of the wst.flux_from_source function. Here is an example:

[DEBUG] Source type sb & cont Flux 5.24e-19 S/N 2.8 FracFlux 1.000 Nspaxels 16 Nspectels 1

[DEBUG] SN 3.00 Flux 5.24e-19 Iter 5 Fcall 6 converged True



6 Point Source

All objects with a size much smaller than the PSF are considered as point source. Their shape is given by the predicted atmospheric + telescope + instrument PSF. The atmospheric seeing limited model is taken from the ESO VLT ETC, adapted to the larger size of the WST. The telescope plus instrument image quality is currently estimated to be 0.1 arcsec FWHM for the IFS and 0.3 arcsec FWHM for the MOS.

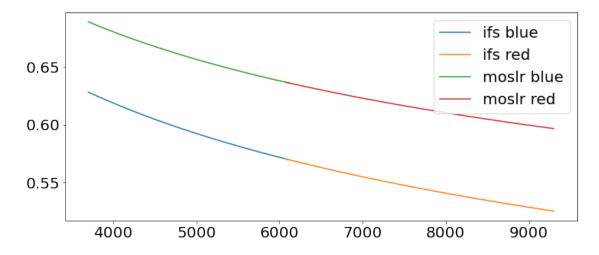
6.1 Image Quality

Here is the total PSF at zenith for a seeing of 0.7 arcsec @ 500 nm.

```
[31]: fig,ax = plt.subplots(1,1,figsize=(12,5))
seeing = 0.7
airmass = 1
for ins in [wst.ifs, wst.moslr]:
    for chan in ins['channels']:
        inst = ins[chan]
        wave = inst['wave'].coord()
        fwhm = get_seeing_fwhm(seeing, airmass, wave, wst.tel['diameter'], usinst['iq_fwhm'])
```

```
ax.plot(wave, fwhm, label=f"{inst['name']} {chan}")
ax.legend()
```

[31]: <matplotlib.legend.Legend at 0x7fef56aee4f0>



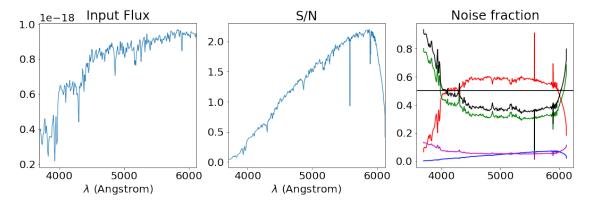
6.2 Continuum source

To compute the S/N for a point source, we need to define the spectrum and the **seeing** and airmass of the observation. The **ima_type** is set to **ps**. Here is an example for a sun-like star with V AB mag of 23.

```
[32]: mos = wst.moslr['blue']
      wave, dw = 5500,500
      dspec = dict(type='template', name='ref/sun',
                   wave_center=wave, wave_width=dw)
      spec = wst.get_spec(mos, dspec)
      mag = 23
      flux = mag2flux(mag, wave)
      obs = dict(
          moon = 'brightsky',
          seeing = 0.7,
          airmass = 1.0,
          ndit = 2,
          dit = 1800,
          spec_type = 'cont',
          ima_type = 'ps',
      wst.set_obs(obs)
      res = wst.snr_from_source(mos, flux, None, spec)
```

```
[DEBUG] Computing frac and nspaxels for 20 wavelengths (lbin 20)
[DEBUG] Performing interpolation
[DEBUG] At 3700.0 A FWHM: 0.69 Flux fraction: 0.62 Aperture: 1.0 Nspaxels: 19
[DEBUG] At 6120.0 A FWHM: 0.64 Flux fraction: 0.64 Aperture: 1.0 Nspaxels: 17
[DEBUG] Source type ps & cont Flux 2.27e-18 S/N 1.3 FracFlux 0.636 Nspaxels 18
Nspectels 1
```

```
[33]: fig,ax = plt.subplots(1,3,figsize=(18,5))
res['input']['flux_source'].plot(ax=ax[0], title='Input Flux')
res['spec']['snr'].plot(ax=ax[1], title='S/N')
show_noise(res['spec']['noise'], ax=ax[2])
```



One can see that we are readout noise limited below 4000 A.

To perform the same computation with the IFS we need to define further parameters for the aperture. While it is fixed by the fiber aperture in the MOS design, for the IFS we have the choice between **circular_adaptative** or **square_fixed**. As indicated by its name **square_fixed** use a square aperture with a fixed size in spaxels defined by 2 x **ima_aperture_hsize_spaxels** + 1 spaxels.

The **circular_adaptative** method, is relative to the FWHM size of the image and use the **ima_kfwhm** parameter. As for the spectrum, it can be optimized using the optimum_circular_aperture method.

We show an example using the same source with the IFS blue channel. Note that for the optimisation we have to define the lrange parameter in the routine

```
obs = dict(
          moon = 'brightsky',
          seeing = 0.7,
          airmass = 1.0,
          ndit = 2,
          dit = 1800,
          spec_type = 'cont',
          ima_type = 'ps',
          ima_aperture_type = 'circular_adaptative',
      )
      wst.set_obs(obs)
      kfwhm = wst.optimum_circular_aperture(ifs, flux, None, spec, lrange=[4500,5500])
      res = wst.snr from source(ifs, flux, None, spec)
     [DEBUG] Optimum circular aperture nit=4 kfwhm=8.35 S/N=1.5 Aper=1.4
     Flux=2.27e-18 Frac=0.96
     [DEBUG] Computing optimum values for kfwhm
     [DEBUG] Optimum circular aperture nit=6 kfwhm=7.47 S/N=1.2 Aper=1.4
     Flux=2.27e-18 Frac=0.82
     [DEBUG] Optimum circular aperture nit=9 kfwhm=8.81 S/N=1.4 Aper=1.5
     Flux=2.27e-18 Frac=0.96
     [DEBUG] Optimum values of kfwhm at wavelengths edges: [7.472135899375999,
     8.809235395639938]
     [DEBUG] Computing frac and nspaxels for 20 wavelengths (lbin 20)
     [DEBUG] Performing interpolation
     [DEBUG] At 3700.0 A FWHM: 0.63 Flux fraction: 0.82 Aperture: 1.4 Nspaxels: 21
     [DEBUG] At 6100.0 A FWHM: 0.57 Flux fraction: 0.96 Aperture: 1.5 Nspaxels: 21
     [DEBUG] Source type ps & cont Flux 2.27e-18 S/N 5.4 FracFlux 0.949 Nspaxels 21
     Nspectels 1
[35]: fig,ax = plt.subplots(1,3,figsize=(18,5))
      res['input']['flux_source'].plot(ax=ax[0], title='Input Flux')
      res['spec']['snr'].plot(ax=ax[1], title='S/N')
      show_noise(res['spec']['noise'], ax=ax[2])
                                                S/N
                                                                     Noise fraction
          1.50
                                      8
                                                             0.8
          1.25
                                      6
                                                             0.6
          1.00
                                      4
                                                             0.4
          0.75
                                                             0.2
                                     2
          0.50
                                                             0.0
              4000
                       5000
                                6000
                                        4000
                                                 5000
                                                         6000
                                                                  4000
                                                                          5000
                                                                                  6000
```

 λ (Angstrom)

 λ (Angstrom)

6.3 Emission line source

We can repeat this computation with an emission line source. The process is similar to the surface brightness computation.

```
[36]: mos = wst.moslr['blue']
      ifs = wst.ifs['blue']
      wave = 4900
      dspec = dict(type='line', lbda=wave, sigma=4.0, skew=7.0)
      flux= 5.e-18
      obs = dict(
          moon = 'darksky',
          seeing = 0.7,
          airmass = 1.0,
          ndit = 2,
          dit = 1800.
          spec_type = 'line',
          spec_range_type = 'adaptative',
          spec_range_kfwhm = 2,
          ima_type = 'ps',
          ima_aperture_type = 'circular_adaptative',
          ima kfwhm = 2
      )
      wst.set_obs(obs)
      spec = wst.get_spec(ifs, dspec)
      kfwhm_ima = wst.optimum_circular_aperture(ifs, flux, None, spec)
      kfwhm_spec = wst.optimum_spectral_range(ifs, flux, None, spec)
      res1 = wst.snr_from_source(ifs, flux, None, spec)
      spec = wst.get_spec(mos, dspec)
      res2 = wst.snr_from_source(mos, flux, None, spec)
     [DEBUG] Optimum circular aperture nit=4 kfwhm=8.39 S/N=7.3 Aper=1.4
     Flux=5.00e-18 Frac=0.96
     [DEBUG] Optimizing kwhm in [0.2155925230162143, 3.919472055443478]
     [DEBUG] Optimum spectral range nit=8 kfwhm=1.06 S/N=7.9 Size=5.1 Flux=5.00e-18
     Frac=0.77
     [DEBUG] Computing PSF at 4901.3 fwhm 0.59 beta 2.5
     [DEBUG] Adaptive circular aperture diameter 1.43 frac_flux 0.96
     [DEBUG] Source type resolved & line Flux 5.00e-18 S/N 7.9 FracFlux 0.737
     Nspaxels 21 Nspectels 9
     [DEBUG] Computing PSF at 4901.4 fwhm 0.66 beta 2.5
     [DEBUG] Source type resolved & line Flux 5.00e-18 S/N 2.2 FracFlux 0.499
     Nspaxels 19 Nspectels 14
```

The function wst.print_aper() can be used to display the tabulated differences between the MOS and the IFS

```
[37]: wst.print_aper([res1,res2],['ifs','mos'])
```

```
[37]: <Table length=17>
           item
                      ifs
                              mos
        bytes20
                   bytes20 bytes20
                      7.891
                              2.236
               snr
                      1.427
                                  1
              size
                         1.6 0.7854
              area
         frac_flux 0.7366 0.4992
          frac_ima
                     0.9556 0.6405
         frac_spec
                     0.7708
                             0.7793
        nb_spaxels
                         21
                                 19
       nb_spectels
                          9
                                 14
         nb_voxels
                        189
                                266
        nph_source
                       1041
                              213.2
           nph_sky 1.24e+04
                               3297
                      58.33
                               69.2
               ron
              dark
                      23.81
                              28.25
         sky_noise 111.3
                              57.42
      source_noise
                      32.27
                               14.6
         tot noise
                      131.9
                              95.37
      frac_detnoise
                      0.228 0.6141
```

6.4 Retrieve flux for a given S/N

It is also possible to retreive the flux to achieve a given S/N. Here is an example.

```
[38]: mos = wst.moslr['red']
      ifs = wst.ifs['red']
      moon = 'darksky'
      wave = 8000
      dspec = dict(type='line', lbda=wave, sigma=4.0, skew=7.0)
      flux= 5.e-18
      obs = dict(
          moon = 'darksky',
          seeing = 0.7,
          airmass = 1.0,
          ndit = 2,
          dit = 1800,
          spec_type = 'line',
          spec_range_type = 'adaptative',
          spec_range_kfwhm = 1.2,
          ima_type = 'ps',
          ima_aperture_type = 'circular_adaptative',
          ima kfwhm = 5
      wst.set_obs(obs)
      snr = 3
```

```
spec = wst.get_spec(ifs, dspec)
res1 = wst.flux_from_source(ifs, snr, None, spec)
spec = wst.get_spec(mos, dspec)
res2 = wst.flux_from_source(mos, snr, None, spec)

[DEBUG] Computing PSF at 8001.5 fwhm 0.54 beta 2.5
[DEBUG] Adaptive circular aperture diameter 0.83 frac_flux 0.67
[DEBUG] Source type resolved & line Flux 1.59e-18 S/N 3.0 FracFlux 0.551
Nspaxels 9 Nspectels 8
[DEBUG] SN 3.00 Flux 1.59e-18 Iter 5 Fcall 6 converged True
[DEBUG] Computing PSF at 8001.6 fwhm 0.61 beta 2.5
[DEBUG] Source type resolved & line Flux 3.50e-18 S/N 3.0 FracFlux 0.632
Nspaxels 17 Nspectels 12
[DEBUG] SN 3.00 Flux 3.50e-18 Iter 5 Fcall 6 converged True
[39]: wst.print_aper([res1,res2],['ifs','mos'])
```

[39]: <Table length=18>

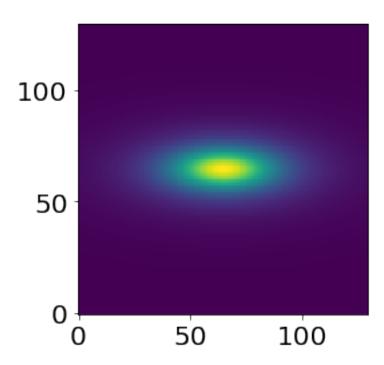
item	ifs	mos
bytes20	bytes20	bytes20
snr	3	3
size	0.827	1
area	0.5371	0.7854
<pre>frac_flux</pre>	0.5511	0.6325
frac_ima	0.6691	0.7605
<pre>frac_spec</pre>	0.8237	0.8316
nb_spaxels	9	17
nb_spectels	8	12
nb_voxels	72	204
nph_source	353.7	341.7
nph_sky	1.203e+04	8349
ron	36	60.6
dark	14.7	24.74
sky_noise	109.7	91.37
source_noise	18.81	18.49
tot_noise	117.9	113.9
<pre>frac_detnoise</pre>	0.1088	0.3302
flux	1.587e-18	3.496e-18

7 Resolved source

Resolved sources are defined by an image and a spectrum. The image is computed with the wst.get_image(ins, dima) function, with ins the instrument channel and dima a dictionary describing the image model. Currentkly there is only one image model, the moffat model. It is describe by a fwhm, a beta shape parameter, and optionnally an ellipticity ell.

```
[40]: ifs = wst.ifs['red']
  dima = dict(type='moffat', fwhm=1.0, beta=2.0, ell=0.6)
  ima = wst.get_ima(ifs, dima)
  ima.plot()
```

[40]: <matplotlib.image.AxesImage at 0x7fef5660e2e0>



7.1 Continuum source

In MOS instrument, the spatial aperture is fixed by the fiber diameter in arcsec.

For IFS there are two sort of apertures:

- square_fixed, the size of the aperture in spaxels is given by 2 * ima_aperture_hsize_spaxels + 1
- circular_adaptative, the aperture diameter is computed relativelt to the FWHM of the image and is given by ima_kfwhm

Note that currently no PSF convolution is done on the image

The final aperture used for the S/N computation can be found in the res['cube']['trunc_ima'] image. An example is given below:

```
[41]: ifs = wst.ifs['red']
  wave = 7000
  dspec = dict(type='flatcont', wave=[wave-10,wave+10])
  spec = wst.get_spec(ifs, dspec)
```

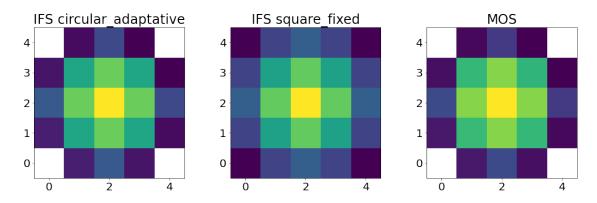
```
dima = dict(type='moffat', fwhm=1.0, beta=2.5)
ima = wst.get_ima(ifs, dima)
mag = 23
flux = mag2flux(mag, wave)
obs = dict(
   moon = 'greysky',
    airmass = 1.0,
   ndit = 2,
    dit = 1800,
    spec_type = 'cont',
    ima_type = 'resolved',
    ima_aperture_type = 'circular_adaptative',
    ima_kfwhm = 5,
)
wst.set_obs(obs)
res1 = wst.snr_from_source(ifs, flux, ima, spec)
obs = dict(
   moon = 'greysky',
    airmass = 1.0,
   ndit = 2,
    dit = 1800,
    spec_type = 'cont',
    ima_type = 'resolved',
    ima_aperture_type = 'square_fixed',
    ima_aperture_hsize_spaxels = 2,
wst.set_obs(obs)
res2 = wst.snr_from_source(ifs, flux, ima, spec)
mos = wst.moslr['red']
spec = wst.get_spec(mos, dspec)
ima = wst.get_ima(mos, dima)
obs = dict(
   moon = 'greysky',
    airmass = 1.0,
   ndit = 2,
    dit = 1800,
    spec_type = 'cont',
    ima_type = 'resolved',
wst.set_obs(obs)
res3 = wst.snr_from_source(mos, flux, ima, spec)
```

[DEBUG] Adaptive circular aperture diameter 1.18 frac_flux 0.46 [DEBUG] Source type resolved & cont Flux 1.40e-18 S/N 3.0 FracFlux 0.461 Nspaxels 21 Nspectels 1 [DEBUG] Source type resolved & cont Flux 1.40e-18 S/N 3.3 FracFlux 0.565

Nspaxels 25 Nspectels 1 [DEBUG] Source type resolved & cont Flux 1.40e-18 S/N 1.0 FracFlux 0.371 Nspaxels 21 Nspectels 1

```
[42]: fig,ax = plt.subplots(1,3,figsize=(18,5))
res1['cube']['trunc_ima'].plot(ax=ax[0], title='IFS circular_adaptative')
res2['cube']['trunc_ima'].plot(ax=ax[1], title='IFS square_fixed')
res3['cube']['trunc_ima'].plot(ax=ax[2], title='MOS')
```

[42]: <matplotlib.image.AxesImage at 0x7fef57473a90>



As for the spectrum adaptative spectral range, it is possible for the IFS to find the optimum **ima_kfwm** parameter to maximize the S/N. The function wst.optimum_circular_aperture() perform this task. We illustrate this in the following.

```
[43]: | ifs = wst.ifs['red']
      wave = 7000
      dspec = dict(type='flatcont', wave=[wave-10,wave+10])
      spec = wst.get_spec(ifs, dspec)
      dima = dict(type='moffat', fwhm=1.0, beta=2.5)
      ima = wst.get_ima(ifs, dima)
      mag = 23
      flux = mag2flux(mag, wave)
      obs = dict(
          moon = 'greysky',
          airmass = 1.0,
          ndit = 2,
          dit = 1800,
          spec_type = 'cont',
          ima_type = 'resolved',
          ima_aperture_type = 'circular_adaptative',
          ima_kfwhm = 5,
      wst.set_obs(obs)
```

```
kfwhm = wst.optimum_circular_aperture(ifs, flux, ima, spec, __
       →lrange=[wave-5,wave+5])
      res4 = wst.snr_from_source(ifs, flux, ima, spec)
     [DEBUG] Optimum circular aperture nit=7 kfwhm=7.05 S/N=3.2 Aper=1.7
     Flux=1.40e-18 Frac=0.66
     [DEBUG] Adaptive circular aperture diameter 1.66 frac_flux 0.66
     [DEBUG] Source type resolved & cont Flux 1.40e-18 S/N 3.2 FracFlux 0.659
     Nspaxels 37 Nspectels 1
[44]: for res, name in zip([res3,res2,res1,res4],['MOS','IFS square fix','IFS circular_
       →adaptative','IFS optimum circular adaptative']):
          print(f"{name} S/N mean {res['spec']['snr mean']:.2f} min__
       Gres['spec']['snr_min']:.2f} max {res['spec']['snr_max']:.2f}")
     MOS S/N mean 0.98 min 0.82 max 1.02
     IFS square fix S/N mean 3.34 min 2.90 max 3.48
     IFS circular adaptative S/N mean 2.98 min 2.58 max 3.10
     IFS optimum circular adaptative S/N mean 3.22 min 2.79 max 3.35
```

7.2 Emission line source

The emission line source follow the same scheme.

```
[45]: ifs = wst.ifs['blue']
      wave = 4900
      obs = dict(
          moon='darksky',
          airmass = 1.2,
          ndit = 2,
          dit = 1800,
          spec_type = 'line',
          spec_range_type = 'adaptative',
          spec_range_kfwhm = 2,
          ima_type = 'resolved',
          ima_aperture_type = 'circular_adaptative',
          ima_kfwhm = 5,
      wst.set obs(obs)
      flux = 1.e-18
      dspec = dict(type='line', lbda=wave, sigma=4.0, skew=7.0)
      spec = wst.get_spec(ifs, dspec)
      dima = dict(type='moffat', fwhm=1.0, beta=2.5)
      ima = wst.get_ima(ifs, dima)
      flux = 5.e-18
      kfwhm = wst.optimum_circular_aperture(ifs, flux, ima, spec)
      kfwhm = wst.optimum_spectral_range(ifs, flux, ima, spec)
      res1 = wst.snr_from_source(ifs, flux, ima, spec)
```

```
mos = wst.moslr['blue']
spec = wst.get_spec(mos, dspec)
ima = wst.get_ima(mos, dima)
kfwhm = wst.optimum_spectral_range(mos, flux, ima, spec)
res2 = wst.snr_from_source(mos, flux, ima, spec)
```

[DEBUG] Optimum circular aperture nit=7 kfwhm=7.05 S/N=3.6 Aper=1.7 Flux=5.00e-18 Frac=0.66

[DEBUG] Optimizing kwhm in [0.21559252230162143, 3.919472055443478]

[DEBUG] Optimum spectral range nit=10 kfwhm=0.98 S/N=3.9 Size=5.1 Flux=5.00e-18 Frac=0.77 $\,$

[DEBUG] Adaptive circular aperture diameter 1.66 frac_flux 0.66

MOG

[DEBUG] Source type resolved & line Flux 5.00e-18 S/N 3.9 FracFlux 0.508 Nspaxels 37 Nspectels 9

[DEBUG] Optimizing kwhm in [0.14836601005213773, 4.246235207692182]

[DEBUG] Optimum spectral range nit=9 kfwhm=1.24 S/N=1.2 Size=6.4 Flux=5.00e-18 Frac=0.86

[DEBUG] Source type resolved & line Flux 5.00e-18 S/N 1.2 FracFlux 0.319 Nspaxels 21 Nspectels 17

[46]: wst.print_aper([res1,res2],['IFS','MOS'])

TEC

[46]: <Table length=17>

item	IFS	MOS
bytes20	bytes20	bytes20
snr	3.919	1.183
size	1.665	1
area	2.177	0.7854
<pre>frac_flux</pre>	0.5081	0.3188
frac_ima	0.6592	0.371
frac_spec	0.7708	0.8594
nb_spaxels	37	21
nb_spectels	9	17
nb_voxels	333	357
nph_source	696.4	132.1
nph_sky	2.389e+04	4841
ron	77.42	80.16
dark	31.61	32.73
sky_noise	154.6	69.58
source_noise	26.39	11.49
tot_noise	177.7	111.7
<pre>frac_detnoise</pre>	0.2214	0.6012

[]: