

Computer Vision
and Geometry Lab

Computer Vision

Local Features

Where are we now

Exercises						
Lab #	Topic	Date	Date	TA	SA	Submission date
	Overview	22-Sep	23-Sep	Mihai		
1	Feature Extraction & Optical Flow	29-Sep	30-Sep	Shaohui	SA1	14-Oct
	Exam Prep Session	6-Oct	7-Oct	Shaohui		
2	Deep Learning for CV	13-Oct	14-Oct	Songyou	SA2	28-Oct
	Exam Prep Session	20-Oct	21-Oct	Songyou		
3	Recognition	27-Oct	28-Oct	Siwei	SA1	11-Nov
	Exam Prep Session	3-Nov	4-Nov	Siwei		
4	Image Segmentation	10-Nov	11-Nov	Shaofei	SA2	25-Nov
	Exam Prep Session	17-Nov	18-Nov	Shaofei		
5	Object Detection & Tracking	24-Nov	25-Nov	Korrawe	SA1	9-Dec
	Exam Prep Session	1-Dec	2-Dec	Korrawe		
6	SfM & Model Fitting	8-Dec	9-Dec	Fangjinhua	SA2	23-Dec
	Exam Prep Session	15-Dec	16-Dec	Fangjinhua		

Assignment

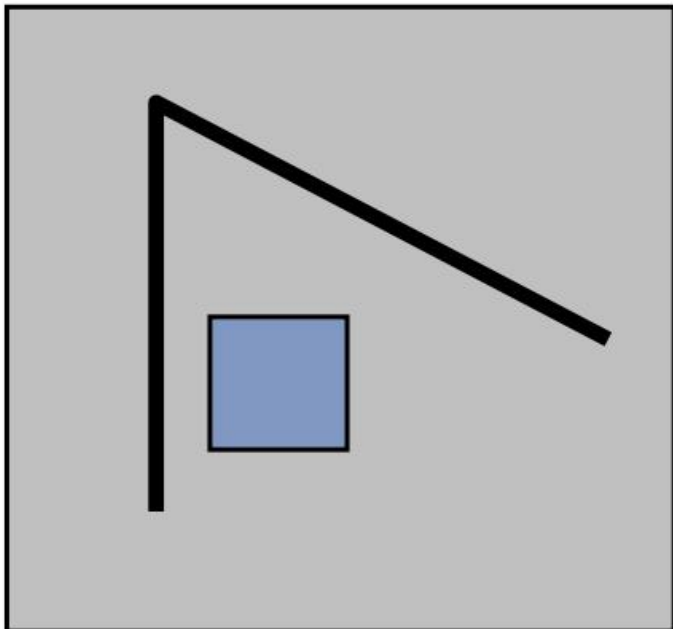
- Task 1: Harris corner detection
- Task 2: Description & matching

Harris corner detection

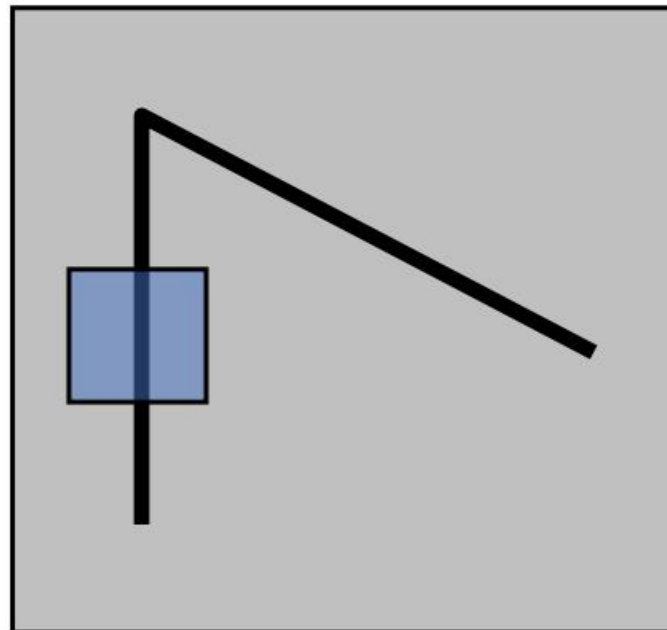
- Compute intensity gradients in x and y direction
- Blur Images to get rid of noise
- Compute Harris response
- Thresholding and non-maximum suppression

Harris corner detection

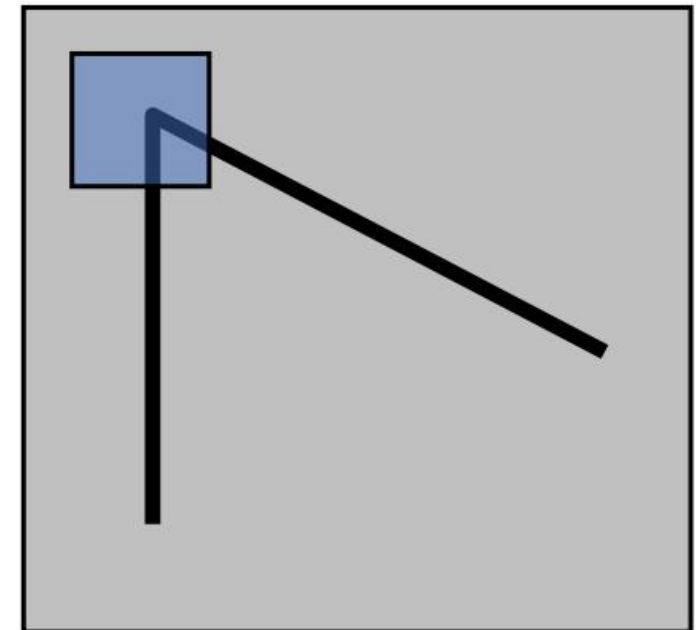
- Corners: area of large intensity changes



flat area: no change
in all directions



edge area: no change
along edge direction

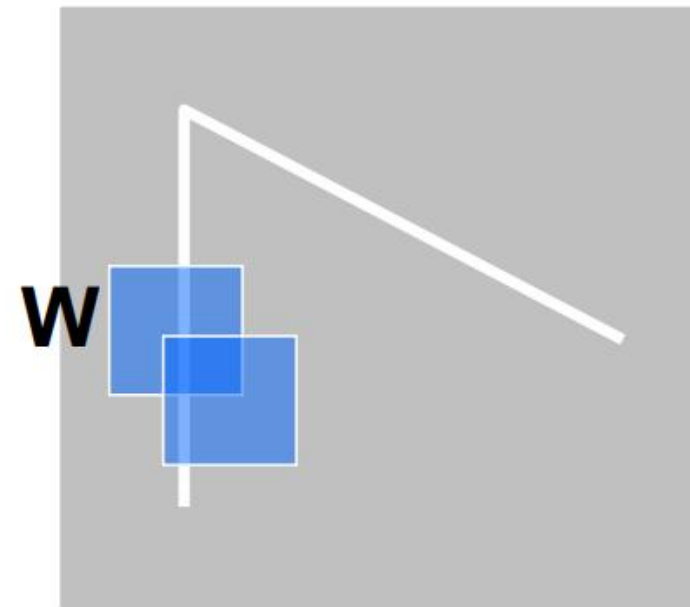


corner area: large
change in all directions

Harris corner detection

Now Consider shifting the patch or
'window' **W** by (u,v)

Consider shifting the patch or
'window' W by (u,v)



- how do the pixels in W change?
- compare each pixel before and after by summing up the squared differences (SSD)
- this defines an SSD “error” or $E(u,v)$:

$$E(u, v) = \sum_{(x,y) \in W} [I(x + u, y + v) - I(x, y)]^2$$

Harris corner detection

$$E(\Delta x, \Delta y) = \sum_{(x,y) \in W} [I(x + \Delta x, y + \Delta y) - I(x, y)]^2 \quad (1)$$



$$\begin{aligned} I(x + \Delta x, y + \Delta y) &= I(x, y) + I_x(x, y)\Delta x + I_y(x, y)\Delta y + O(\Delta x^2, \Delta y^2) \\ &\approx I(x, y) + I_x(x, y)\Delta x + I_y(x, y)\Delta y \end{aligned}$$

$$\begin{aligned} E(\Delta x, \Delta y) &\approx \sum_{(x,y) \in W} [I_x(x, y)\Delta x + I_y(x, y)\Delta y]^2 \\ &= [\Delta x \quad \Delta y] M \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix} \end{aligned}$$

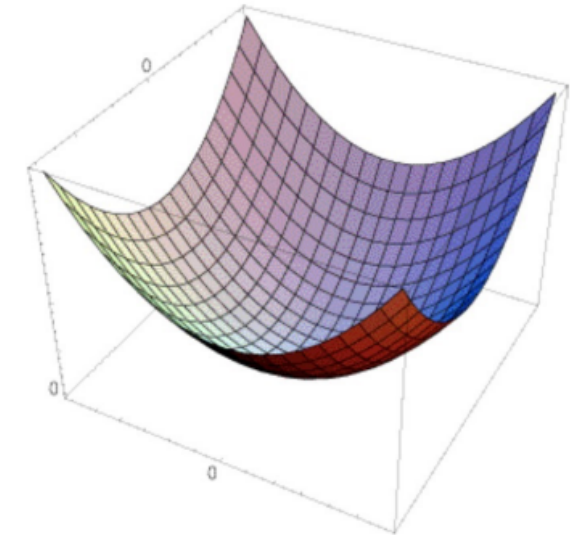
$$\text{Where } M = \sum_{(x,y) \in W} \begin{bmatrix} I_x^2(x, y) & I_x(x, y)I_y(x, y) \\ I_x(x, y)I_y(x, y) & I_y^2(x, y) \end{bmatrix}$$

Harris corner detection

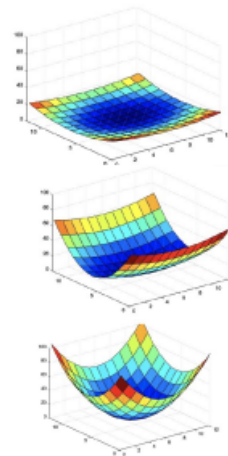
- Direction of largest changes in the intensity: eigen vector of λ_{max}
- Direction of smallest changes in the intensity: eigen vector of λ_{min}

$$E(\Delta x, \Delta y) \approx [\Delta x \ \Delta y] M \begin{bmatrix} \Delta x \\ \Delta y \end{bmatrix}$$

$$M = \sum \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$



- λ_1, λ_2 both small: flat areas
- $\lambda_1 \gg \lambda_2$ or $\lambda_1 \ll \lambda_2$: edge
- λ_1, λ_2 both large: corner



Harris corner detection

- Step 1: compute image gradients

$$I_x = \frac{I(x+1, y) - I(x-1, y)}{2}$$

$$I_y = \frac{I(x, y+1) - I(x, y-1)}{2}$$

$$M = \sum \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

You may use `scipy.signal.convolve2d`

Harris corner detection

- Step 2: blur the image

$$M = \sum_{(x,y) \in W} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Window function w : gaussian with standard deviation σ

You may use `cv2.GaussianBlur`

Harris corner detection

■ Step 3: compute Harris response

λ_1, λ_2 both large: corner

$$M = \sum_{(x,y) \in W} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

$$R = \det(M) - k \operatorname{trace}^2(M) \quad k=0.04 \sim 0.06$$

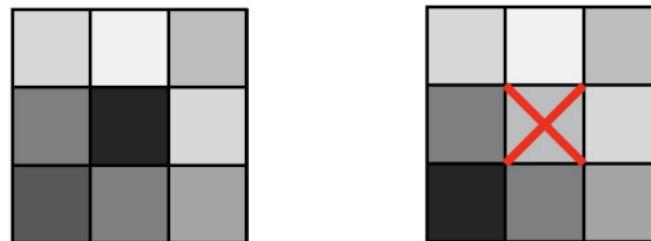
- $\det(H)$ = product of eigenvalues
- $\operatorname{trace}(H)$ = sum eigenvalues
- related to eigenvalues but cheaper to compute

Harris corner detection

■ Step 4: non-maximum suppression

For every pixel above the threshold, check the surrounding pixels inside a window for the maximum response intensity.

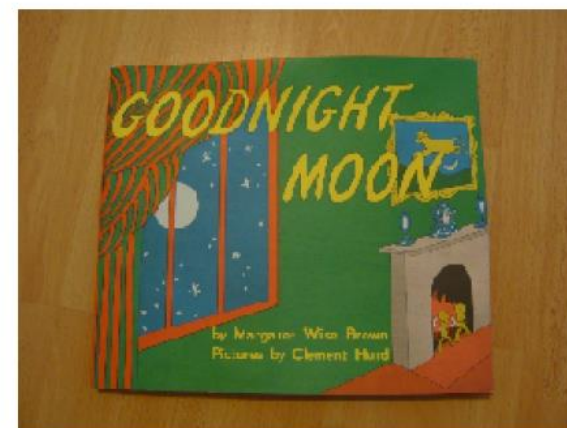
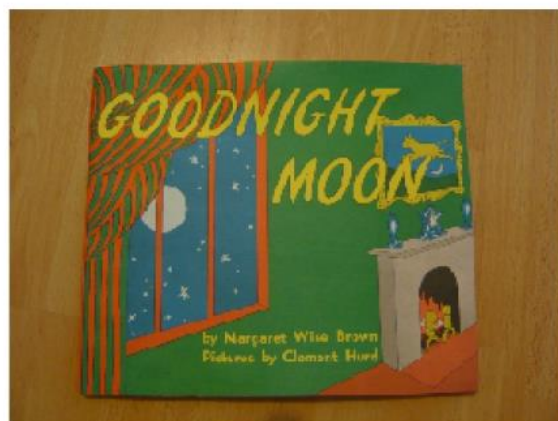
If the center pixel response is smaller than a pixel inside the window, remove the center pixel from the corner candidates.



You may use `scipy.ndimage.maximum_filter`

Description & Matching

- Input: a pair of images
- Convert to gray image -> Harris corner detection
- Extract local patch descriptors
 - Filter out keypoints around the edges
 - Extract 9x9 patches around the detected keypoints as descriptor (this function is provided)



Description & Matching

■ Feature distances:
$$SSD(p, q) = \sum_i (p_i - q_i)^2$$

Make sure to avoid Python for-loop with vectorized computation.

Description & Matching

- One-way nearest neighbors matching
 - each feature from the img1 is matched to its closest feature from img2
- Mutual nearest neighbors matching
 - for each one-way match, check if it's also valid if switch img1 and img2
- Ratio test matching
 - in one-way match, if the ratio between the 1st and the 2nd nearest neighbor is lower than a threshold

Hand-in

- Source code (please do not change the interface)
- Write up a short report explaining the main steps of your implementation.
- Include images showing the results and write down your comments.

By 12:00 pm on Saturday 15th October, 2022 on Moodle.