### SINTASSI DI L (BNF)

C ::= nil | Id = E | C;C | if (E) {C} /else {C}/ | while (E) {C} | D;C | return E |

do {C} while (E) | for (D; E; C) {C} | switch (E) {cList}

**E** ::= v | **Id** | **uop E** | **E bop E** | (**E**) | **id**(**ae**)

D ::= nil | let Id /:T/ = E | var Id /:T/ = E | D;D | func Id(form) -> T {C; return E} | form = ae |

rec **D**  $\mid \rho$ 

cList ::= case Val: C; break cList | case Val: C; break | default: C; break

**Val** ::=  $\mathbb{N} \cup \mathbb{Z} \cup \mathbb{R} \cup \{\text{true, false}\} \cup \{s \mid s \in \mathsf{ASCII}^*\}$ 

T ::= Int | Double | Bool | String

form := nil | let ld:T, form | var ld:T, form

ae ::= nil | E, ae | Loc, ae

uop ::= + | - | !

**bop** ::= + | - | \* | \ | % | == | != | > | >= | < | <= | && | || | ·

Id ::= insieme degli identificatori validi

Loc ::= insieme delle locazioni

METAVARIABILI			
С	C, C', C0, C1,	Т	T, T', T1, T2,
E	E, E', E0, E1,	Val	v, v', v0, v1,
D	D, D', D0, D1,	Int	n, n', n0, n1,
form	form, form', form0, form1,	Double	d, d', d0, d1,
ae	ae, ae', ae0, ae1,	Bool	b, b', b0, b1,
ld	ld, ld', ld1, ld2,	String	s, s', s0, s1,

#### SEMANTICA STATICA

Ambiente statico:  $\Delta$  : Id  $\cup$  Val  $\rightarrow$  T  $\cup$  TLoc

$$\Delta[\Delta'](x) = \begin{cases} \Delta'(x) & \text{if } \Delta'(x) \text{ defined} \\ \Delta(x) & \text{otherwise} \end{cases}$$

**ESPRESSIONI** formato:  $\Delta \vdash_F E : T$ 

Assiomi:

 $(A1) \varnothing \vdash_E n : Int (A2) \varnothing \vdash_E d : Double (A3) \varnothing \vdash_E b : Bool (A4) \varnothing \vdash_E s : String$ Regole di Inferenza:

$$(R1) \ \frac{\Delta(\mathrm{Id}) = \mathrm{T} \vee \Delta(\mathrm{Id}) = \mathrm{TLoc}}{\Delta \vdash_E \mathrm{Id}: \mathrm{T}} \qquad (R2) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T1}, \mathrm{uop}: \mathrm{T1} \to \mathrm{T}}{\Delta \vdash_E \mathrm{uop} \ \mathrm{E}: \mathrm{T}} \qquad (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T2}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \mathrm{T3}} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T3}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta \vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta} = (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta}}{\Delta \vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta\vdash_E \mathrm{E}: \Delta}$$

$$(R1) \ \frac{\Delta(\mathrm{Id}) = \mathrm{T} \vee \Delta(\mathrm{Id}) = \mathrm{TLoc}}{\Delta \vdash_E \mathrm{Id}: \mathrm{T}} \qquad (R2) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T1}, \mathrm{uop}: \mathrm{T1} \to \mathrm{T}}{\Delta \vdash_E \mathrm{uop} \; \mathrm{E}: \mathrm{T}} \qquad (R3) \ \frac{\Delta \vdash_E \mathrm{E}: \mathrm{T}}{\Delta \vdash_E \mathrm{(E)}: \mathrm{T}} \qquad (R4) \ \frac{\Delta \vdash_E \mathrm{E1}: \mathrm{T1}, \mathrm{E2}: \mathrm{T2}, \mathrm{bop}: \mathrm{T1} \mathrm{x} \mathrm{T2} \to \mathrm{T}}{\Delta \vdash_E \mathrm{E1} \; \mathrm{bop} \; \mathrm{E2}: \mathrm{T}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{ae}: \mathrm{ae}: \mathrm{ae}: \mathrm{A}(\mathrm{Id}) = \mathrm{ae}\: \mathrm{t} \to \mathrm{T}}{\Delta \vdash_E \mathrm{Id}(\mathrm{ae}): \mathrm{T}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{ae}: \mathrm{ae}: \mathrm{top}: \mathrm{T1} \times \mathrm{T2} \to \mathrm{T}}{\Delta \vdash_E \mathrm{Id}(\mathrm{ae}): \mathrm{T}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{ae}: \mathrm{top}: \mathrm{T1} \times \mathrm{T2} \to \mathrm{T2}}{\Delta \vdash_E \mathrm{T1} \times \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{top}: \mathrm{T2} \to \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{top}: \mathrm{T2} \to \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{top}: \mathrm{T2} \to \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{top}: \mathrm{T2} \to \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_{ae} \mathrm{top}: \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac{\Delta \vdash_E \mathrm{T2}}{\Delta \vdash_E \mathrm{T2}} \qquad (R5) \ \frac$$

**COMANDI** formato:  $\Delta \vdash_C C$ 

Assiomi:  $(A2) \varnothing \vdash_C nil$ 

Regole di Inferenza:

$$(R6) \ \frac{\Delta(\operatorname{Id}) = \operatorname{TLoc}, \ \Delta \vdash_E \operatorname{E:T}}{\Delta \vdash_C \operatorname{Id} = \operatorname{E}} \qquad (R7) \ \frac{\Delta \vdash_C \operatorname{C1}, \ \Delta \vdash_C \operatorname{C2}}{\Delta \vdash_C \operatorname{C1;C2}} \qquad (R8) \ \frac{\Delta \vdash_E \operatorname{E:Bool}, \ \Delta \vdash_C C}{\Delta \vdash_C \operatorname{while} (\operatorname{E}) \operatorname{do}\{\operatorname{C}\}} \\ (R9) \ \frac{\Delta \vdash_E \operatorname{E:Bool}, \ \Delta \vdash_C \operatorname{C1}, \ \Delta \vdash_C \operatorname{C2}}{\Delta \vdash_C \operatorname{if} (\operatorname{E})\{\operatorname{C1}\} \operatorname{else}\{\operatorname{C2}\}} \qquad (R10) \ \frac{\vdash_D \operatorname{D:}\Delta', \ \Delta \vdash_D D, \ \Delta[\Delta'] \vdash_C \operatorname{C}}{\Delta \vdash_C \operatorname{D;C}}$$

$$(R9) \frac{\Delta \vdash_{E} \mathsf{E:Bool}, \Delta \vdash_{C} \mathsf{C1}, \Delta \vdash_{C} \mathsf{C2}}{\Delta \vdash_{C} \mathsf{if} (\mathsf{E}) \{\mathsf{C1}\} \mathsf{else} \{\mathsf{C2}\}} \qquad (R10) \frac{\vdash_{D} \mathsf{D:}\Delta', \Delta \vdash_{D} D, \Delta[\Delta'] \vdash_{C} \mathsf{C}}{\Delta \vdash_{C} \mathsf{D;} \mathsf{C}}$$

$$(R11) \frac{\Delta \vdash_{E} \mathsf{E:T}}{\Delta \vdash_{C} \mathsf{return} \, \mathsf{E}}$$

**DICHIARAZIONI** formato:  $\vdash_D D$  :  $\Delta$  (costruzione) e  $\Delta \vdash_D D$  (validazione) Assiomi costruzione:

$$(A3) \vdash_D \text{nil}: \emptyset (A4) \vdash_D \text{const Id}: T=E : [Id:T] (A5) \vdash_D \text{var Id}: T=E : [Id:TLoc]$$

$$(A6) \; \vdash_D \mathsf{func} \; \mathsf{Id}(\mathsf{form}) \to \mathsf{T}\{\mathsf{var} \; \mathsf{res} : \mathsf{T} = \mathsf{E}; \mathsf{C}; \mathsf{return} \; \mathsf{E}\} \; : \; [(\mathsf{Id}, \mathscr{T}(\mathsf{form}) \to \mathsf{T})] \; \mathsf{dove}$$

$$\mathcal{T} = \begin{cases} \mathcal{T}(\mathsf{nil}) = \mathsf{nil} \\ \mathcal{T}(\mathsf{const} \ \mathsf{Id} : \mathsf{T}, \mathsf{form}) = \mathsf{T}, \mathsf{form} \\ \mathcal{T}(\mathsf{var} \ \mathsf{Id} : \mathsf{T}, \mathsf{form}) = \mathsf{T}, \mathsf{form} \end{cases}$$

Regole di Inferenza costruzione:

$$(R12) \frac{\vdash_D D1:\Delta 1, \vdash_D D2:\Delta 2}{\vdash_D D1;D2:\Delta 1[\Delta 2]}$$

$$(R13) \frac{\vdash_D \mathsf{D}:\Delta}{\vdash_D \mathsf{rec}\; \mathsf{D}:\Delta}$$

Assiomi validazione:  $(A7) \Delta \vdash_D$ nil

Regole di Inferenza validazione:

$$(R14) \; \frac{\Delta \vdash_E \mathsf{E:T}}{\Delta \vdash_D \mathsf{const} \; \mathsf{Id:T} = \mathsf{E}}$$

$$(R15) \frac{\Delta \vdash_E E:T}{\Delta \vdash_D \text{var Id:T} = E}$$

$$(R16) \; \frac{\vdash_D \mathsf{D1} : \Delta 1, \Delta \vdash_D \mathsf{D1}, \Delta[\Delta 1] \vdash_D \mathsf{D2}}{\Delta \vdash_D \mathsf{D1} ; \mathsf{D2}}$$

$$(R17) \; \frac{\vdash_D \mathsf{D} : \Delta', \Delta[\Delta'_{|I_0}] \vdash_D \mathsf{D}}{\Delta \vdash_D \mathsf{rec}\; \mathsf{D}}, I_0 = FI(\mathsf{D}) \cap BI(\mathsf{D})$$

$$(R18) \frac{\text{form:} \Delta 0, \Delta[\Delta 0] \vdash_{C} \text{var res:} T=E; C; \text{ return res}}{\Delta \vdash_{D} \text{func Id(form)} \rightarrow T\{\text{var res:} T=E; C; \text{ return res}\}}$$

**FORMALI** formato: form :  $\Delta$  Assiomi costruzione: (A8) nil: $\emptyset$ 

Regole di Inferenza:

$$(R19) \frac{\text{form:} \Delta, \text{Id} \notin \Delta}{\text{const Id:T : } \Delta[(\text{Id,T})]}$$

$$(R20) \frac{\text{form:} \Delta, \text{Id} \notin \Delta}{\text{var Id:T : } \Delta[(\text{Id,TLoc})]}$$

**ATTUALI** formato:  $\vdash_D D:\Delta$  (costruzione) e  $\Delta \vdash_D D$  (validazione)

Assiomi costruzione: (A9)  $\Delta \vdash_{ae}$  nil

Regole di Inferenza:

$$(R21) \frac{\Delta \vdash_E \text{E:T}, \Delta \vdash_{ae} \text{ae:aet}}{\Delta \vdash_{ae} \text{E, ae: T, aet}}$$

### **SEMANTICA DINAMICA (ERRATA CORRIGE)**

La regola FD1 diventa:

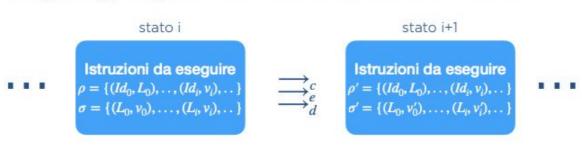
$$\langle \text{func Id(form)} -> \mathsf{T} \ \{\mathsf{C}\}, \rho, \sigma \rangle \to_D \langle [Id, \lambda \text{form .} \{\rho'; C\}], \sigma \rangle, \quad \rho' = \begin{cases} \rho_{|FI(C)} - \text{form} & \text{scoping statico} \\ \varnothing & \text{scoping dinamico} \end{cases}$$
 Regola mancante:

$$\langle \mathsf{return} \; \mathsf{E}, \rho, \sigma \rangle \to_C \langle \mathsf{E}, \rho, \sigma \rangle$$

## Semantica Dinamica

esecuzione **C**: 
$$\langle C, \rho, \sigma \rangle \longrightarrow_c \langle C', \rho', \sigma' \rangle$$
,  $\operatorname{Exec}(C, \rho, \sigma) = \sigma' \iff \langle C, \rho, \sigma \rangle \longrightarrow_c^* \sigma'$  valutazione **E**:  $\langle E, \rho, \sigma \rangle \longrightarrow_e \langle E', \rho, \sigma \rangle$ ,  $\operatorname{Eval}(E, \rho, \sigma) = v \in \operatorname{Val} \iff \langle E, \rho, \sigma \rangle \longrightarrow_e^* v$  elaborazione **D**:  $\langle D, \rho, \sigma \rangle \longrightarrow_d \langle D', \rho', \sigma' \rangle$ ,  $\operatorname{Elab}(D, \rho, \sigma) = \langle \rho', \sigma' \rangle \iff \langle D, \rho, \sigma \rangle \longrightarrow_d^* \langle \rho', \sigma' \rangle$  ambiente (dinamico)  $\rho$ : Id  $\longrightarrow$  Loc U Val memoria  $\sigma$ : Loc  $\longrightarrow$  Val

 $\longrightarrow_c$  ,  $\longrightarrow_e$  ,  $\longrightarrow_d$  sono le funzioni di interpretazione semantica di C, E e D



stato finale

nil
$$\rho = \{ (Id_0, L_0), ..., (Id_i, v_i), ... \} \\
\sigma = \{ (L_0, v_0), ..., (L_i, v_i), ... \}$$

Sistema di transioni

Semantica Dinamica Espressioni

$$(Id1) \ \frac{\rho(Id) = v \ \lor \ (\rho(Id) = L \in Loc \land \sigma(L) = v)}{\langle Id, \rho, \sigma \rangle \longrightarrow_e v}$$

$$(uop1) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e \langle E', \rho, \sigma \rangle}{\langle uop \, E, \rho, \sigma \rangle \longrightarrow_e \langle uop \, E', \rho, \sigma \rangle} \qquad (uop2) \, \langle uop \, v, \rho, \sigma \rangle \longrightarrow_e v' = \mathsf{uop} \, v$$

$$(bop1) \frac{\langle E_1, \rho, \sigma \rangle \longrightarrow_e \langle E_1', \rho, \sigma \rangle}{\langle E_1 \, bop \, E_2, \rho, \sigma \rangle \longrightarrow_e \langle E_1' \, bop \, E_2, \rho, \sigma \rangle} \quad (bop2) \frac{\langle E_2, \rho, \sigma \rangle \longrightarrow_e \langle E_2', \rho, \sigma \rangle}{\langle v_1 \, bop \, E_2, \rho, \sigma \rangle \longrightarrow_e \langle v_1 \, bop \, E_2', \rho, \sigma \rangle}$$

(bop3) 
$$\langle v_1bop\ v_2, \rho, \sigma \rangle \longrightarrow_e v = v_1 \text{ bop } v_2$$
 bop è sintassi bop è semantica

Semantica Dinamica Comandi

$$(id2) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* \nu}{\langle Id = E, \rho, \sigma \rangle \longrightarrow_c \langle Id = \nu, \rho, \sigma \rangle} \qquad (id3) \langle Id = \nu, \rho, \sigma \rangle \longrightarrow_c \sigma[\rho(Id) = \nu]$$

$$(seq1) \frac{\langle C_1, \rho, \sigma \rangle \longrightarrow_c \langle C_1', \rho, \sigma' \rangle}{\langle C_1; C_2, \rho, \sigma \rangle \longrightarrow_c \langle C_1'; C_2, \rho, \sigma' \rangle} \qquad (seq2) \frac{\langle C_1, \rho, \sigma \rangle \longrightarrow_c \sigma'}{\langle C_1; C_2, \rho, \sigma \rangle \longrightarrow_c \langle C_2, \rho, \sigma' \rangle}$$

$$(if1) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* true}{\langle \mathbf{if}(E) \{ C_1 \} \, \mathbf{else} \, \{ C_2 \}, \rho, \sigma \rangle \longrightarrow_e \langle C_1, \rho, \sigma \rangle} \qquad (if2) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* false}{\langle \mathbf{if}(E) \{ C_1 \} \, \mathbf{else} \, \{ C_2 \}, \rho, \sigma \rangle \longrightarrow_e \langle C_2, \rho, \sigma \rangle}$$

$$(rep1) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* true}{\langle \mathsf{while}\,(E) \{C\} \, \rho, \sigma \rangle \longrightarrow_c \langle C; \mathsf{while}\,(E) \{C\}, \rho, \sigma \rangle} \qquad (rep2) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* false}{\langle \mathsf{while}\,(E) \{C\}, \rho, \sigma \rangle \longrightarrow_c \sigma}$$

$$(b1) \frac{\langle D, \rho, \sigma \rangle \longrightarrow_d^* \langle \rho', \sigma' \rangle}{\langle D; C, \rho, \sigma \rangle \longrightarrow_c \langle C, \rho[\rho'], \sigma[\sigma'] \rangle}$$

Semantica Dinamica Dichiarazioni

$$(let1) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_e^* v}{\langle let \ Id : T = E, \rho, \sigma \rangle \longrightarrow_d \langle [(Id, v)], \sigma \rangle}$$

$$(var1) \frac{\langle E, \rho, \sigma \rangle \longrightarrow_{e}^{*} v}{\langle var \ Id : T = E, \rho, \sigma \rangle \longrightarrow_{d} \langle [(Id, new \ L)], [(L, v)] \rangle}$$

$$(dd1) \ \frac{\langle D_1, \rho, \sigma \rangle \longrightarrow_d \langle D_1', \rho', \sigma' \rangle}{\langle D_1; D_2, \rho, \sigma \rangle \longrightarrow_d \langle D_1'; D_2, \rho', \sigma' \rangle} \qquad (dd2) \ \frac{\langle D_2, \rho[\rho_1], \sigma \rangle \longrightarrow_d \langle D_2', \rho[\rho_1]', \sigma' \rangle}{\langle \rho_1; D_2, \rho[\rho_1], \sigma \rangle \longrightarrow_d \langle \rho_1; D_2', \rho[\rho_1]', \sigma' \rangle}$$

$$(dd3) \langle \rho_1; \rho_2, \rho, \sigma \rangle \longrightarrow_d \langle \rho_1[\rho_2], \sigma \rangle$$



le regole (dd2) e (dd3) contengono configurazioni non ammissibili rispetto alla definizione di sistema di transizione

 $(dd2) \langle \rho_1; D_2, \rho, \sigma \rangle, \langle \rho_1; D_2', \rho, \sigma' \rangle (dd3) \langle \rho_1; \rho_2, \rho, \sigma \rangle$ 

la parte codice delle configurazioni di stato deve essere generabile dalla grammatiche che definisce D, e questo non vale per le configurazioni sopra

# aggiungo gli ambienti alla sintassi

**D** ::= nil | let  $Id[:T] = E | var Id[:T] = E | D;D | \rho$  **T** ::= Int | Double | Bool | String

solo il compilatore può generare gli ambienti della sintassi, non l'utente

Il sistema di transizione delle dichiarazioni è

 $(\{\langle D, \rho, \sigma \rangle \cup \langle \rho', sigma' \rangle\}, \longrightarrow_d, \{\langle \rho', sigma' \rangle\}, \langle dichiarazione da elaborare, ambiente iniziale, memoria iniziale \rangle)$ 

Semantica Dinamica Funzioni

$$(FD1) \frac{\langle \operatorname{func} \operatorname{Id}(\operatorname{form}) \to T\{C; \operatorname{return} E\}, \rho, \sigma \rangle}{\langle (\operatorname{Id}, \lambda \operatorname{form} . \{\rho'; C; \operatorname{return} E\}), \sigma \rangle} \qquad \begin{cases} \rho' = \rho_{|FV(C) - BV(form)} & \operatorname{scoping statico} \\ \rho' = \operatorname{nil} & \operatorname{scoping dinamico} \end{cases}$$
 
$$(FD2) \frac{\rho(\operatorname{Id}) = \lambda \operatorname{form} . C}{\langle \operatorname{Id}(\operatorname{ae}), \rho, \sigma \rangle \to_{e} \langle \{\operatorname{form} = \operatorname{ae}; C\}, \rho, \sigma \rangle} \qquad (FD3) \frac{\langle E, \rho, \sigma \rangle \to_{e} \langle E', \rho, \sigma \rangle}{\langle E, \operatorname{ae}, \rho, \sigma \rangle \to_{ae} \langle \operatorname{E'}, \rho, \sigma \rangle} \qquad (FD4) \frac{\langle \operatorname{ae}, \rho, \sigma \rangle \to_{ae} \langle \operatorname{ae'}, \rho, \sigma \rangle}{\langle \operatorname{k}, \operatorname{ae}, \rho, \sigma \rangle \to_{ae} \langle \operatorname{k}, \operatorname{ae'}, \rho, \sigma \rangle} \qquad (FD5) \frac{\langle \operatorname{ae}, \rho, \sigma \rangle \to_{ae} \langle \operatorname{ae'}, \rho, \sigma \rangle}{\langle \operatorname{form} = \operatorname{ae}, \rho, \sigma \rangle \to_{d} \langle \operatorname{form} = \operatorname{ae'}, \rho, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} = \operatorname{ak}, \rho, \sigma \rangle \to_{d} \langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash \operatorname{form} : \rho_{0}}{\langle \operatorname{form} : \rho_{0}, \sigma \rangle} \qquad (FD6) \frac{\operatorname{ak} \vdash$$

$$\begin{split} (RD1) & \frac{\langle D, \rho - I_0, \sigma \rangle \rightarrow_d \langle D', \rho', \sigma' \rangle}{\langle rec \ D, \rho, \sigma \rangle \rightarrow_d \langle rec \ D', \rho', \sigma' \rangle}, I_0 = FI(D) \cap BI(D) \\ (RD2) & \langle rec \ \rho_0, \rho, \sigma \rangle \rightarrow \langle \{ (f, \lambda form \ . \ (rec \ \rho_0) - form; C) \mid \rho_0(f) = \lambda form \ . \ C \}, \sigma \rangle \end{split}$$



### Scoping e Identificatori Liberi

```
FI_d: D \rightarrow \{\text{occorrenze } Id \text{ liberi}\}
FI_e: E \rightarrow \{\text{occorrenze } Id \text{ liberi}\}
                                                            FI_c: C \rightarrow \{\text{occorrenze } Id \text{ liberi}\}
FI_{o}(\vee) = \emptyset
                                                            FI_c(nil) = \emptyset
                                                                                                                              FI_d(nil) = \emptyset
FI_{\varrho}(\mathrm{Id}) = \{\mathrm{Id}\}
                                                            FI_c(\text{Id} = \text{E}) = \{\text{Id}\} \cup FI_e(\text{E})
                                                                                                                              FI_d(let ld:T = E) = FI_e(E)
FI_{\rho}(\text{uop E}) = FI_{\rho}(E)
                                                            FI_c(C1;C2) = FI_c(C1) \cup FI_c(C2)
                                                                                                                              FI_d(var ld:T = E) = FI_e(E)
                                                            FI_c(if (E) {C1} else {C2}) =
FI_o(E1 \text{ bop } E2) = FI_o(E1) \cup FI_o(E2)
                                                                                                                              FI_d(D1;D2) = FI_d(D1) \cup (FI_d(D2)-BI_d(D1))
                                                                         FI_c(E) \cup FI_c(C1) \cup FI_c(C2)
                                                            FI_c(\text{while (E) {C}}) = FI_c(\text{E}) \cup FI_c(\text{C})
                                                            FI_c(D;C) = FI_d(D) \cup (FI_c(C) - BI_d(D))
   BI_c = \overline{FI}_c
    BI_e = \overline{FI}_e
    BI_d = \overline{FI}_d
FI_c(return E) = FI_e(E)
FI_e(\text{Id(ae)}) = \{\text{Id}\} \cup FI_{ae}(ae)
FI_d(func ld(form))->T{C} =
         FI_c(\mathbb{C}) - BI_{form}(\text{form})
FI_{form}(form) = \emptyset
FI_{ae}(\mathsf{E,ae}) = FI_{e}(E) \cup FI_{ae}(ae)
```

# Anatomia Funzioni

