

8) Hp.  $0 - (-6) \frac{-6}{2} x - (-6t)$

$\xi(t) = 0,1 \sin(6t)$  estremo corde

$T = 4N$

$\mu = 0,01 \text{ kg/m}$

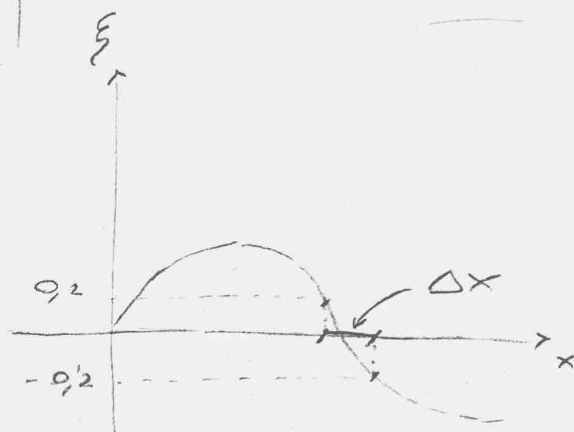
Th.

a)  $v = ?$

b)  $\Delta x_{\min}$  @  $\Delta y = 0,02$

c) eq. ne di un punto a 40 m.

a)  $\omega = 6 \frac{\text{rad}}{\text{s}} \rightarrow \left| f = \frac{\omega}{2\pi} = 0,95 \text{ Hz} \right|$   
 $\left| v = \sqrt{\frac{T}{\mu}} = 20 \text{ m/s} \right|$



b)  $0,02 = 0,1 \sin(kx - \omega t)$

$\hookrightarrow \sin(kx - \omega t) = 0,2 = \frac{1}{5}$

$\arcsin\left(\frac{1}{5}\right) \approx 0,20 \text{ rad}$

$\Rightarrow$  2 angoli più vicini:  $\pi + 0,2$  e  $\pi - 0,2$

$$\left. \begin{aligned} 0,2 &= \sin(kx_1 - \omega t) \Rightarrow kx_1 - \omega t = \pi - 0,2 \\ -0,2 &= \sin(kx_2 - \omega t) \Rightarrow kx_2 - \omega t = \pi + 0,2 \end{aligned} \right\} x_2 - x_1 = \frac{0,2 + 0,2}{k}$$

$\left| \Delta x = \frac{v(0,4)}{\omega} \approx 1,39 \text{ m} \right|$

c)  $\xi_{(x=40\text{m})} = 0,1 \text{ m} \sin\left(40 \cdot \frac{6}{20} - 6t\right) = 0,1 \text{ m} \sin\left(12 - 6 \frac{\text{rad}}{\text{s}} \cdot t\right)$

7) Hp.

$$\xi_0 = 0,01 \text{ m}$$

$$f = 80 \text{ Hz}$$

$$P = 10 \text{ W} = \bar{P}$$

$$k = 25,1 \text{ rad/m}$$

Th.

i)  $\lambda$  e  $v = ?$

ii)  $T = ?$   $\mu = ?$

iii)  $\xi'_0$  t.c.  $f' = 20 \text{ Hz}$  e  $\bar{P}' = 5 \text{ W}$

i)  $k = \frac{2\pi}{\lambda} \rightarrow \lambda = \frac{2\pi}{k} = 0,25 \text{ m}$

$v = \lambda f = 20 \text{ m/s}$

ii)  $v = \sqrt{\frac{T}{\mu}} \rightarrow T = v^2 \mu^{(*)} = 15,83 \text{ N}$

$$\bar{P} = \frac{1}{2} \mu \omega^2 \xi_0^2 v \rightarrow \mu = \frac{2\bar{P}}{\omega^2 \xi_0^2 v} = \frac{2\bar{P}}{(2\pi f)^2 \xi_0^2 v}$$

(\*)  $\mu = 3,95 \cdot 10^{-2} \text{ kg/m}$

iii)  $\bar{P}' = \frac{1}{2} \mu \omega'^2 \xi_0'^2 v = \frac{1}{2} \mu (2\pi f')^2 \xi_0'^2 v$

$$\xi_0'^2 = \frac{2\bar{P}'}{\mu (2\pi f')^2 v} \rightarrow \xi_0' = \sqrt{\frac{2\bar{P}'}{\mu (2\pi f')^2 v}} = 0,028 \text{ m}$$

6)

Hp.

$$t = 10^\circ \text{C}$$

$$p = 50 \text{ atm}$$

$$v = 1420 \text{ m/s}$$

$$f = 1000 \text{ Hz}$$

$$\xi_0 = 1 \cdot 10^{-9} \text{ m}$$

$$\rho_0 = 1000 \text{ kg/m}^3$$

Th.

$$\text{i) } \Delta p_{\text{max}} = ?$$

$$\text{ii) } W_{\tau} = ?$$

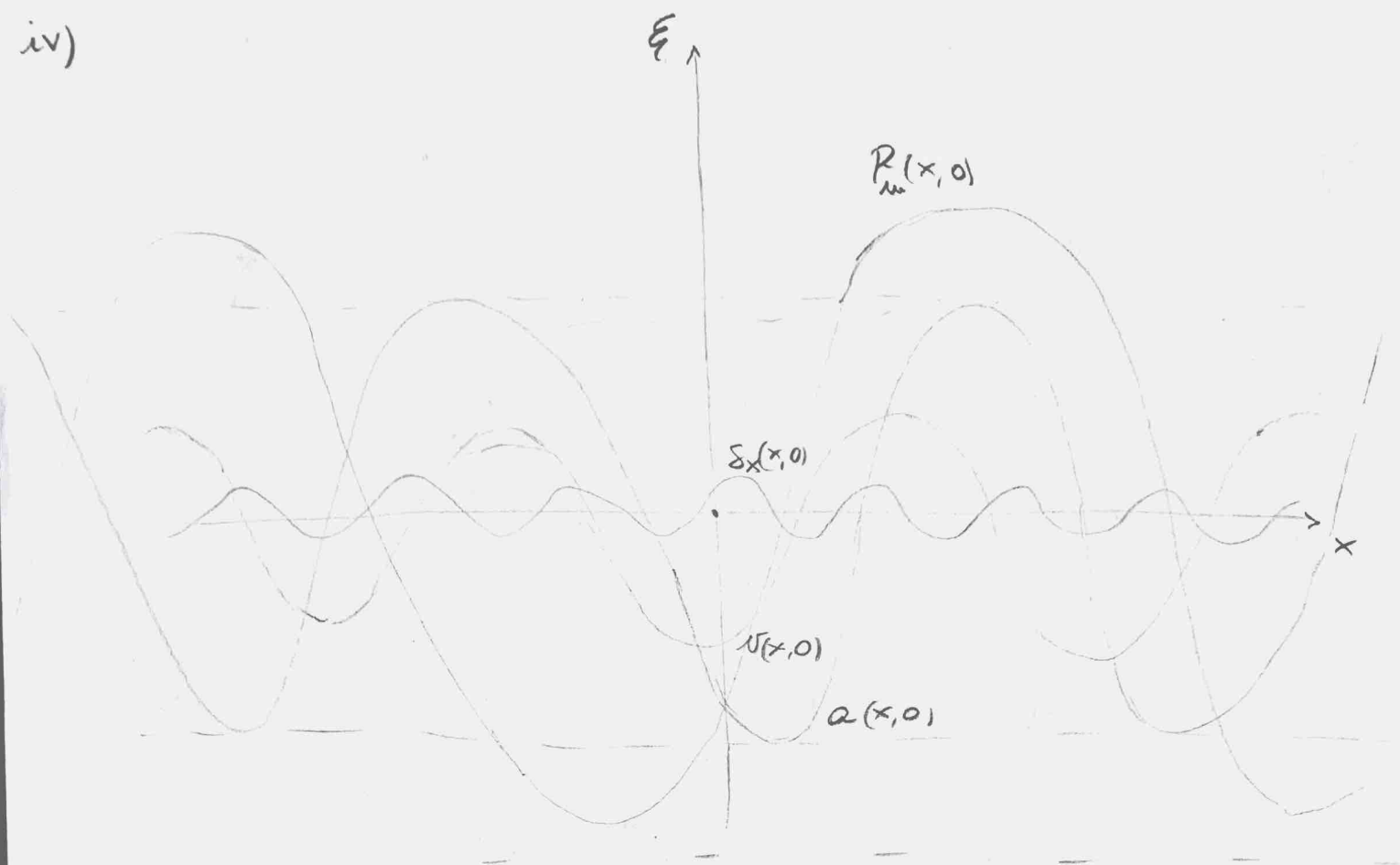
$$\text{iii) } I = ?$$

$$\text{i) } \Delta p_{\text{max}} = 2\pi \rho_0 f v \xi_0 = \boxed{8,9 \text{ Pa}}$$

$$\text{ii) } W_{\tau} = \frac{1}{2} \rho_0 (2\pi f)^2 \xi_0^2 = \boxed{1,98 \cdot 10^{-8} \frac{\text{J}}{\text{m}^3}}$$

$$\text{iii) } I = W_{\tau} v = \boxed{2,81 \cdot 10^{-5} \frac{\text{W}}{\text{m}^2}}$$

iv)



5)

Hp.

$$\mu = 300 \text{ g/m}$$

$$P_{\text{max}} = 600 \text{ W}$$

$$T = 120 \text{ N}$$

$$\xi_0 = 0,2 \text{ m}$$

Th.

a)  $f_{\text{max}} = ?$

$$a) P = T \xi_0^2 \omega k \cos^2(kx - \omega t) \Rightarrow P_{\text{max}} = T \xi_0^2 \omega k = T \xi_0^2 \frac{\omega^2}{v}$$

$$v = \sqrt{\frac{T}{\mu}} = 20 \text{ m/s}$$

$$\sqrt{\frac{P_{\text{max}} v}{T \xi_0^2}} = \omega$$

$$\omega = 81,65 \text{ rad/s}$$

$$f = \frac{\omega}{2\pi} = 12,99 \text{ Hz}$$

4) Hp.

$$\rho = 7,8 \cdot 10^3 \frac{\text{Kg}}{\text{dm}^3}$$

$$S = 1 \text{ dm}^2 = 0,01 \text{ m}^2$$

$$f = 200 \text{ Hz}$$

$$E = 2 \cdot 10^{11} \text{ Pa}$$

$$\bar{P} = 100 \text{ W}$$

$$s_x(x, t) = A \cos(kx - \omega t - \frac{\pi}{3})$$

Th.

$$i) \omega, k, v, T, \lambda, A = ?$$

$$ii) \frac{\partial s_x}{\partial t} = ? \quad \frac{\partial^2 s_x}{\partial t^2} = ?$$

$$iii) P \text{ in } x = \frac{\lambda}{4} \text{ et } t = \frac{T}{2} = ?$$

$$i) \omega = 2\pi f = 1256,63 \frac{\text{rad}}{\text{s}}$$

$$v = \sqrt{\frac{E}{\rho}} = 5063,70 \text{ m/s}$$

$$T = \frac{2\pi}{\omega} = 5 \cdot 10^{-3} \text{ s}$$

$$\lambda = vT = 25,32 \text{ m}$$

$$k = \frac{2\pi}{\lambda} = 0,25 \frac{\text{rad}}{\text{m}}$$

$$\bar{P} = \frac{1}{2} \rho \omega^2 A^2 v S \Rightarrow A = \sqrt{\frac{2\bar{P}}{\rho \omega^2 v S}} = 1,79 \cdot 10^{-5} \text{ m}$$

$$ii) \frac{\partial s_x}{\partial t} = A \omega \sin(kx - \omega t - \frac{\pi}{3}) = v_{s_x}(x, t)$$

$$\frac{\partial^2 s_x}{\partial t^2} = -A \omega^2 \cos(kx - \omega t - \frac{\pi}{3}) = a_{s_x}(x, t)$$

$$iii) P = F \cdot v = -ES \frac{\partial s}{\partial x} \cdot \frac{\partial s}{\partial t} = \underbrace{ESA^2 k \omega \sin^2(kx - \omega t - \frac{\pi}{3})}$$

$$\frac{\partial s}{\partial x} = -A k \sin(kx - \omega t - \frac{\pi}{3})$$

$$P(x = \frac{\lambda}{4}, t = \frac{T}{2}) = 135,99 \text{ W}$$