



Intro to Graphs

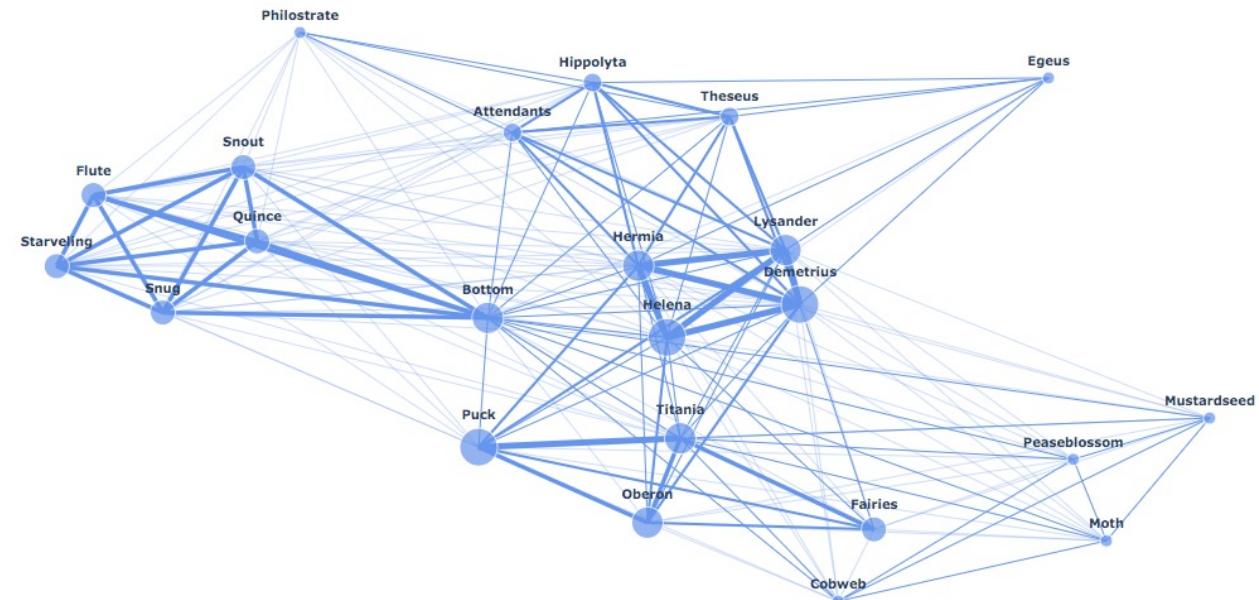
NetworkX

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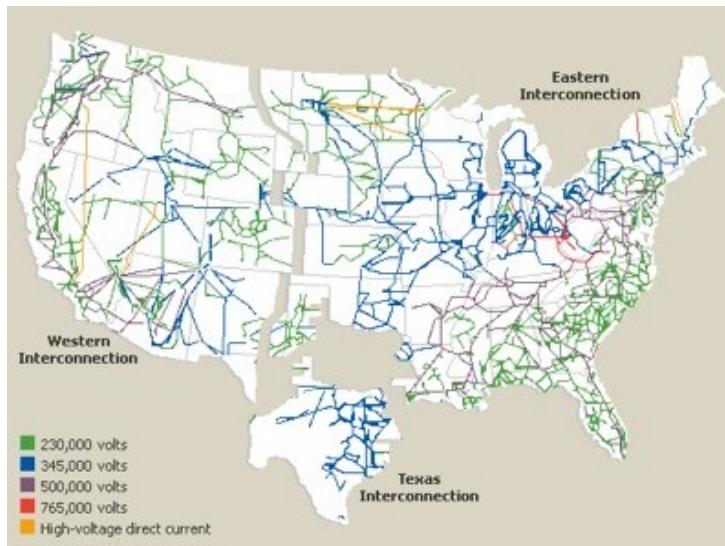
INTRODUCTION TO NETWORKX

Introduction to NetworkX - network analysis

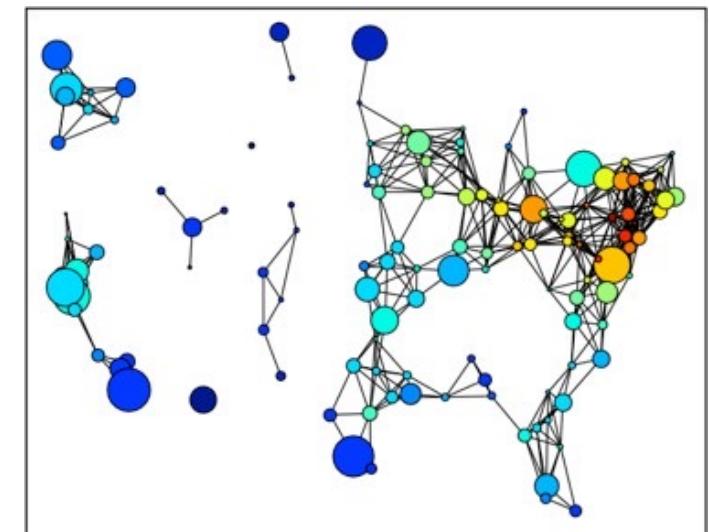
- Vast amounts of network data are being generated and collected
- Sociology: web pages, mobile phones, social networks
- Technology: Internet routers, vehicular flows, power grids

NetworkX è una libreria Python che permette di lavorare con i grafi!

How can we analyse these networks?



Python + NetworkX!

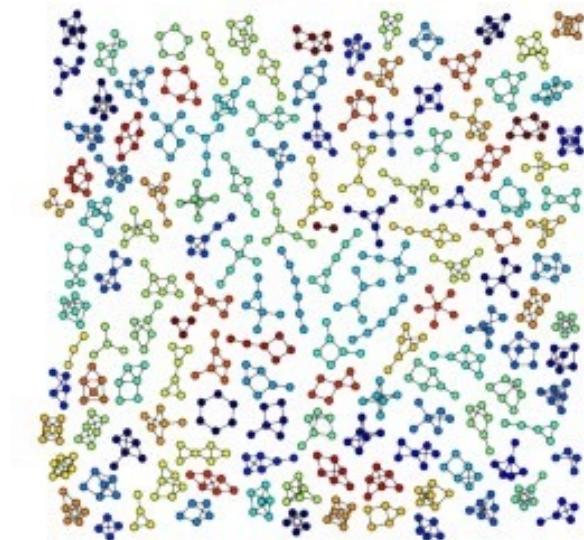
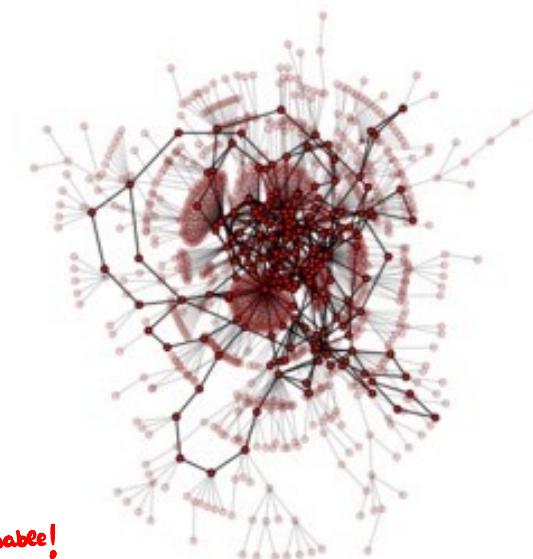


Introduction to NetworkX

“Python package for the creation, manipulation and study of the structure, dynamics and functions of complex networks.”

- Data structures for representing many types of data in the form of graphs
- Nodes can be any (hashable) Python object, edges can contain arbitrary data
- Flexibility ideal for representing networks found in many different fields
- Easy to install on multiple platforms
- Online up-to-date documentation
- First public release in April 2005

→ nodi sono rappresentati da oggetti che devono essere hashable!



Introduction to NetworkX - design requirements

- Tool to study the structure and dynamics of social, biological, and infrastructure networks
- Ease-of-use and rapid development
- Open-source tool base that can easily grow in a multidisciplinary environment with non-expert users and developers
- An easy interface to existing code bases written in C, C++, and FORTRAN
- To painlessly slurp in relatively large nonstandard data sets

Introduction to NetworkX - object model

NetworkX defines no custom node objects or edge objects

- node-centric view of network
- nodes can be any hashable object, while edges are tuples with optional edge data (stored in dictionary)
- any Python object is allowed as edge data and it is assigned and stored in a Python dictionary (default empty)

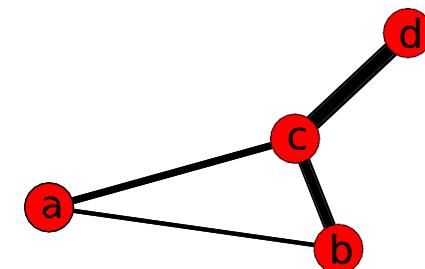
- I nodi sono qualsiasi oggetto **hashable**;
- Gli archi sono **tuple** con eventuali informazioni aggiuntive salvate in dizionari.

Introduction to NetworkX - quick example

- Search for the shortest path in a weighted and unweighted network:

N.B.: I nodi sono **unici!** Non posso aggiungere due volte lo stesso nodo a un grafo.

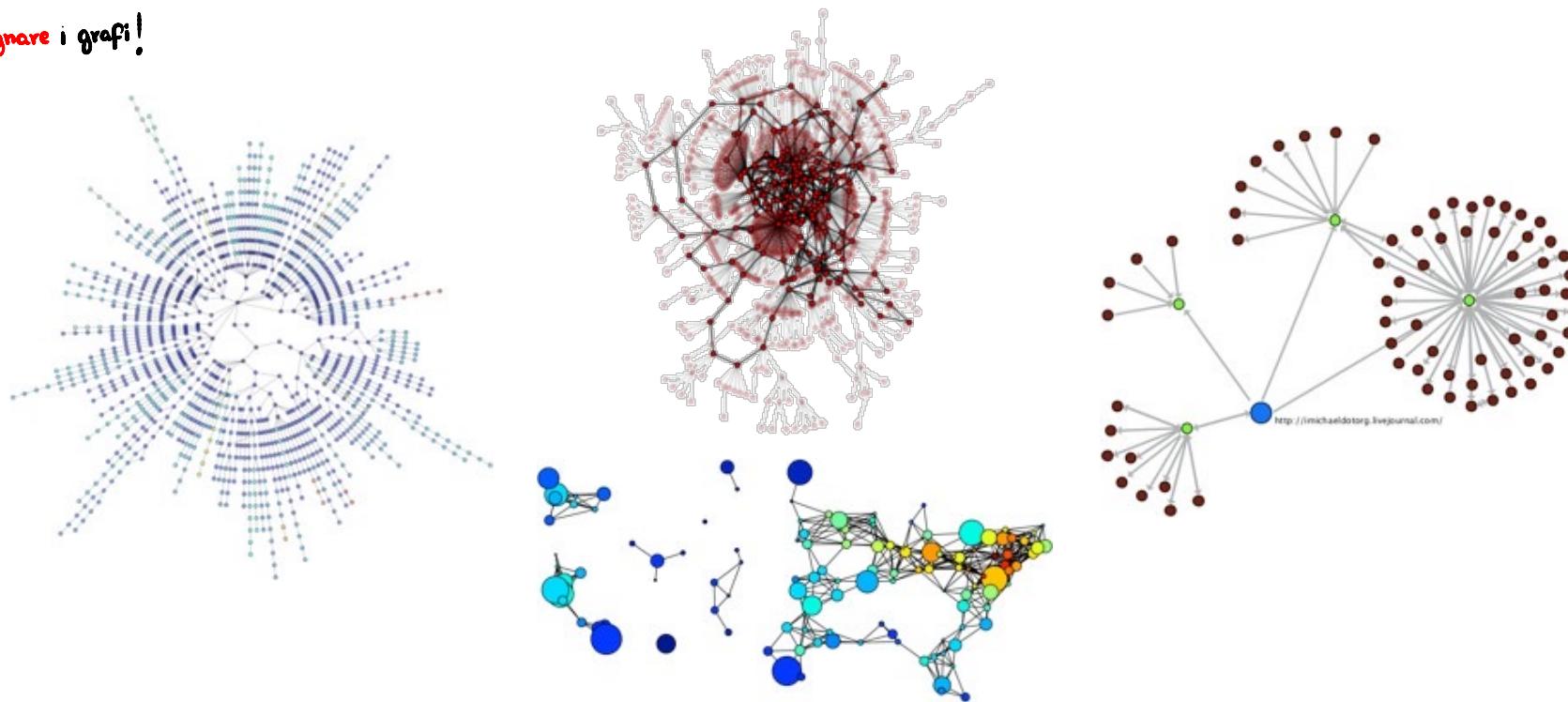
```
● ● ●  
Importo la libreria  
1 import networkx as nx  
2 g = nx.Graph() ~ Creo un grafo  
3 g.add_edge("a", "b", weight=1)  
4 g.add_edge("b", "c", weight=100) { Creo degli archi; automaticamente vengono aggiunti i nodi se non presenti!  
5 g.add_edge("a", "c", weight=1)  
6 g.add_edge("c", "d", weight=1) .shortest_path() restituisce il percorso + breve  
7 print(nx.shortest_path(g, "b", "d")) .dijkstra_path(): con l'algoritmo di Dijkstra!  
8 print(nx.dijkstra_path(g, "b", "d", weight='weight'))
```



Introduction to NetworkX - drawing and plotting

- It is possible to draw small graphs within NetworkX and to export network data and draw with other programs (i.e., GraphViz, matplotlib)

• Con NetworkX si possono anche **dipingere** i grafi!



Introduction to NetworkX - official website

- <https://networkx.org/>

Documentazione di NetworkX!

The screenshot shows the NetworkX official website with a dark theme. At the top, there is a navigation bar with links for Install, Tutorial, Reference (which is underlined in blue), Gallery, Developer, Releases, and Guides. To the right of the navigation bar are search, refresh, and other browser controls, along with a dropdown menu showing "3.2.1 (stable)". The main content area has a header "Reference" with a breadcrumb trail "Home > Reference". Below this, a box displays the release information: "Release: 3.2.1" and "Date: Oct 28, 2023". The left sidebar, titled "Section Navigation", lists various sections: Introduction, Graph types, Algorithms, Functions, Graph generators, Linear algebra, Converting to and from other data formats, Relabeling nodes, Reading and writing graphs, Drawing, Randomness, Exceptions, Utilities, and Glossary. The right main content area is titled "Reference" and contains a list of topics: Introduction (NetworkX Basics, Graphs, Graph Creation, Graph Reporting, Algorithms, Drawing, Data Structure), Graph types (Which graph class should I use?, Basic graph types, Graph Views, Core Views, Filters), Algorithms (Approximations and Heuristics, Assortativity).



GETTING STARTED WITH PYTHON AND NETWORKX

Getting started – import NetworkX

- NetworkX supports many different graph types, like:
 - `nx.Graph()` – undirected
 - `nx.DiGraph()` – directed
 - `nx.MultiGraph()` – supports multiple edges between nodes
 - `nx.MultiDiGraph()` – directed multigraph
- Also provide implementation of notable graphs (like heawood)

Con `networkx`, a seconda del metodo utilizzato,
posso creare grafi di tipo #.

```
1 import networkx as nx
2 import math
3 import flet as ft
4
5 g = nx.heawood_graph()
6 print(g.nodes, g.edges)
7
8 g.add_node(math.cos) # cosine functionx
9 g.add_node(ft.Text("Pippo"))
10 g.add_edge("math.cos", 3)
11 print(g.nodes, g.edges)
```

- `Graph()`: grafo non diretto
- `DiGraph()`: grafo diretto
- `Multigraph()`: multgrafo non diretto
- `MultDiGraph()`: multagrafo diretto

N.B.: I nodi sono UNICI! Non posso aggiungere due volte lo stesso nodo a un grafo.

Getting started – build a graph

- Nodes could be (almost) anything
 - Numbers, strings
 - Objects
 - Functions
 - Flet containers
 - Edges connect nodes (even heterogeneous)
 - Nodes and edges could have attributes
- Sia i nodi che gli archi possono avere attributi!
- I nodi possono essere oggetti di qualsiasi tipo!
- Gli archi possono anche connettere oggetti di tipo #.



```
import networkx as nx
import math
import flet as ft

g = nx.Graph()
g.add_edge(1, 2) # default edge data=1
g.add_edge(2, 3, weight=0.9) # specify edge data

g.add_edge('y', 'x', function=math.cos)
g.add_node(math.cos) # any hashable can be a node

elist = [(1, 2), (2, 3), (1, 4), (4, 2)]
g.add_edges_from(elist)
elist = [('a', 'b', 5.0), ('b', 'c', 3.0), ('a', 'c', 1.0), ('c', 'd', 7.3)]
g.add_weighted_edges_from(elist)
g.add_node(ft.Text("Pippo"))

print(g.nodes())
print(g.edges())
print(g.get_edge_data('a','b'))
```

Se voglio aggiungere archi pesati, dovrò creare delle tuple formate da tre elementi in cui i primi due identificano l'arco, e il terzo identifica il peso associato all'arco!

Getting started – Data Structure

- A graph is essentially a “dictionary of dictionaries of dictionaries”
- The keys are the nodes
- Indeed, `g[n]` yields a dictionary where keys are all the nodes connected with `n` (adjacency) and values are the edges params (like `weight`)

↓ `g[n]`: mi restituisce tutti i nodi che sono connessi al nodo `n`!

• I grafî in realtà sono dizionari in cui i nodi sono le chiavi e i valori sono tutti i nodi raggiungibili da quel nodo sotto forma di dizionario, in cui le chiavi sono i nodi e i valori sono tutti i nodi raggiungibili da quel nodo sotto forma di dizionario, e così via...



```
import networkx as nx

g = nx.Graph()
g.add_edge(1, 2) # default edge data=1
g.add_edge(2, 3, weight=0.9) # specify edge data

elist = [(1, 2, 1), (2, 3, 1), (1, 4, 1), (4, 2, 1),
          ('a', 'b', 5.0), ('b', 'c', 3.0), ('a', 'c', 1.0), ('c', 'd', 7.3)]
g.add_weighted_edges_from(elist)

print(g[2])
```

```
{1: {'weight': 1}, 3: {'weight': 1}, 4: {'weight': 1}}
```

```
Process finished with exit code 0
```

Getting started – Data Structure

- `g[u][v]` yields the edge attributes
 - `n in g` tests if node `n` is in `g` True/False se il nodo n è presente nel grafo.
 - `for n in g:` iterates through the graph Itero sui nodi del grafo
 - `for nbr in g[n]:` iterates through the neighbors of `n` Itero sui nodi collegati al nodo n.
 - Data struct for direct graphs is only slightly more complex (two dics, one for successors and one for predecessors)
 - You can also use `g.nodes()` and `g.edges()` to get corresponding data
 - Edges can have arbitrary attributes
- `g.nodes():` restituisce i nodi del grafo
`g.edges():` restituisce gli archi del grafo.



```
import networkx as nx

g = nx.Graph()
g.add_edge(1, 2) # default edge data=1
g.add_edge(2, 3, weight=0.9) # specify edge data

elist = [(1, 2, 1), (2, 3, 1), (1, 4, 1), (4, 2, 1),
          ('a', 'b', 5.0), ('b', 'c', 3.0), ('a', 'c', 1.0), ('c', 'd', 7.3)]
g.add_weighted_edges_from(elist)
g.add_edge(2,5,arbitraryAttr = "foo")

print(g[2])
print("-----")
print(g['a']['b'])
print("-----")
print('e' in g)
print("-----")
for n in g:
    print(n)
print("-----")
for nbr in g[2]:
    print(nbr)
print("-----")
print(g[2][5]['arbitraryAttr'])
```

Getting started – Directed and Multi

- Graphs can be directed, therefore differentiating neighbors in predecessors and successors
- Two nodes can have more than one edge

`.predecessors(n)`: restituisce una lista con tutti i nodi predecessori di `n`.
`.successors(n)`: restituisce una lista con tutti i nodi successori di `n`.



```
import networkx as nx

dg = nx.DiGraph()
dg.add_weighted_edges_from([(1,4,0.5), (3,1,0.75)])

print([s for s in dg.successors(1)])
print([p for p in dg.predecessors(1)])

mg = nx.MultiGraph()

mg.add_weighted_edges_from([(1,2,.5), (1,2,.75),
                           (2,3,.5)])

print(mg[1][2])
```

Getting started - graph operators

Classic graph operations

- `subgraph(G, nbunch)` - induce subgraph of G on nodes in nbunch
- `union(G1, G2)` - graph union
- `disjoint_union(G1, G2)` - graph union assuming all nodes are different
- `compose(G1, G2)` - combine graphs identifying nodes common to both
- `complement(G)` - graph complement
- `create_empty_copy(G)` - return an empty copy of the same graph class
- `convert_to_undirected(G)` - return an undirected representation of G
- `convert_to_directed(G)` - return a directed representation of G

↳ Questi due metodi servono rispettivamente a ricevere una versione non orientata di un grafo orientato passato in input, o viceversa!

• ACCEDERE AGLI ATTRIBUTI DEGLI ARCHI:

```
myGraph.edges(data=True)  
# In questo modo, con data=True, .edges mi restituisce non solo una lista di tuple formate da due elementi in cui vengono  
# indicati i nodi tra cui è presente un arco, ma all'interno delle tuple ci sono tanti altri argomenti quanti sono gli attributi  
# di quell'arco sotto forma di dizionari. Quindi se scrivo .add_edge(1,2,weight=10), quando mi prendo gli edges del grafo con data=True,  
# oltre ad avere (1,2), avrò (1,2,{'weight':10}).  
# Un'altra opzione che posso avere dato i nodi di un arco per ottenere gli attributi associati all'arco, è utilizzare  
# il metodo .get_edge_data(), a cui passo come parametri i due nodi e mi restituisce un dizionario con tutti gli attributi  
# e i valori associati a quegli attributi dell'arco.
```



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