

## **C**OURSEWORK

## **EDHEC BUSINESS SCHOOL**

MASTER IN MANAGEMENT FINANCIAL ECONOMICS

# Introduction to Machine Learning through Classification

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## 1 Exercise 1: General questions

#### 1.1 Question 1

What are the advantages and disadvantages of a low-dimensional simple model over a very flexible (complex) model?

The advantages of a low-dimensional simple model over a very flexible (complex) model can be summarised as:

- · Easier to understand and thus to implement without errors
- · Less overfitting as the variance of residuals is lower
- It performs better than complex models Out-of-sample
- Finally, according to Occam's razor argument: simpler models should be chosen over complex models as they avoid redundant elements

While, the disadvantages of a low-dimensional simple model over a very flexible (complex) model can be summarised as:

- · Higher bias as it has been fitted loosely
- · captures data less well
- · lower flexibility
- It performs worse than complex models In-sample

#### 1.2 Question 2

A student wants to automatically identify which of her photos were taken indoors, outdoors, day or night. Should you recommend to use four binary classifiers, two binary classifiers or a multi-class classifier? Justify your answer.

To recognize between photos taken indoors, outdoors, day or night we would recommend two binary classifiers. As indoor is mutually exclusive with outdoor and day is mutually exclusive with night the two pairs can be correctly modeled by two binary classifiers:

$$environment = \begin{cases} 1 & if indoor \\ 0 & if outdoor \end{cases}$$
$$time = \begin{cases} 1 & if day \\ 0 & if night \end{cases}$$

Using 4 binary classifiers would be redundant because we have two mutually exclusive pairs.

Using 1 4-class classifiers would incorrectly model the problem as it will not be able to correctly classify for example photos that are taken in a outdoor environment in day time as they will either be classified as outdoor or day and not both.

## 2 Exercise 2: Precision, Recall and Accuracy

#### 2.1 Question 1

What is the main difference between the accuracy and the precision of a model?

The **accuracy** of a model is defined as the percentage of outputs correctly labeled.

Denoting *TP* and *TN* respectively the number of correctly labeled positive and negative outputs.

$$Accuracy = \frac{TP + TN}{n}$$

where n is the number of outputs.

The **precision** of a model (also called positive prediction value) is defined as the proportion of positives among positive predictions.

Denoting *FP* as the number of false positive outputs.

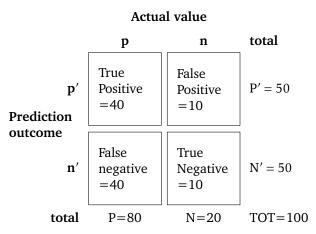
$$Precision = \frac{TP}{TP + FP}$$

Therefore the main difference is that accuracy takes into account the correctly labeled between all outputs, while precision takes into account the correctly labeled between all the similarly predicted.

#### 2.2 Question 2

We are interested in a "random" binary classification algorithm, that is to say that predicts "negative" or "positive" with an occurrence of 0.5 for each class. Suppose that the training set contains 80% of "positive" labels and therefore 20% of "negative" labels. Determine the accuracy, recall, and precision. Interpret.

Taking into consideration the "random" binary classification we construct the following Confusion Matrix table for 100 cases.



Therefore the accuracy, precision and recall are given by

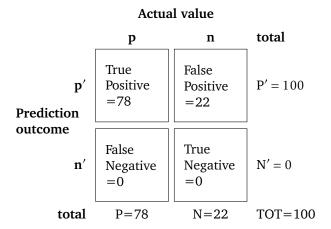
$$Accuracy = \frac{TP + TN}{n} = \frac{40 + 10}{100} = 50\%$$
 
$$Precision = \frac{TP}{TP + FP} = \frac{40}{50} = 80\%$$
 
$$Recall = \frac{TP}{TP + FN} = \frac{40}{40 + 40} = 50\%$$

The interpretation is that the "random" binary classification is a simple benchmark for all other models given its accuracy and recall of 50%. The precision is high just because the dataset is unbalanced towards positives. If we calculate precision for negatives the value would be 20%.

#### 2.3 Question 3

We are interested in a binary classification algorithm by majority rule, that is to say that predicts (here) only "positives". Suppose that the training set contains 78% of "positive" labels and therefore 22% of "negative" labels. Determine the accuracy, recall, and precision. Interpret.

Taking into consideration the majority rule classification we construct the following Confusion Matrix table for 100 cases.



Therefore the accuracy, precision and recall are given by

$$Accuracy = \frac{TP + TN}{n} = \frac{78 + 0}{100} = 78\%$$
 
$$Precision = \frac{TP}{TP + FP} = \frac{78}{100} = 78\%$$
 
$$Recall = \frac{TP}{TP + FN} = \frac{78}{78} = 100\%$$

The interpretation is that the majority rule works very well when the dataset is strongly unbalanced. As we can see, the accuracy and precision are simply given by the prevalence of the positive over the negatives in the dataset. The recall is high for the same reason. The majority rule expresses another benchmark when evaluating a model.

#### 3 Exercise 3: Roc curve and AUC

**Note**: As encourage and approved by the professor in class, we decided to solve the exercises in R. The relevant R file is attached to the report under the name "Exercise\_3\_Roc\_curve\_and\_AUC.R". The input file is an Excel file containing the above table. The input file attached as "coursework\_exercise\_3.xlsx".

#### 3.1 Question 1

Construct and plot the ROC curve with  $\alpha \in [0;1]$  and an increment of 0.10

We construct the Roc curve by calculating the TPR and FPR for every threshold  $\alpha$  between 0 and 1 in steps 0.1. Plotting we start from  $\alpha = 1$  for convention.

TP	TN	FP	FN	TPR	FPR	threshold	Trapeze	AUC
0	12	0	8	0	0	1	0	0
2	11	1	6	0.25	0.083333333	0.9	0.010416667	0.010416667
3	10	2	5	0.375	0.166666667	0.8	0.026041667	0.036458333
4	9	3	4	0.5	0.25	0.7	0.036458333	0.072916667
5	8	4	3	0.625	0.333333333	0.6	0.046875	0.119791667
5	7	5	3	0.625	0.416666667	0.5	0.052083333	0.171875
6	5	7	2	0.75	0.583333333	0.4	0.114583333	0.286458333
6	3	9	2	0.75	0.75	0.3	0.125	0.411458333
8	3	9	0	1	0.75	0.2	0	0.411458333
8	2	10	0	1	0.833333333	0.1	0.083333333	0.494791667
8	0	12	0	1	1	0	0.166666667	0.661458333

Here is the plotted result.

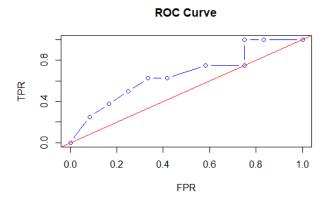


Figure 1: Roc curve for exercise 3

#### 3.2 Question 2

Is the model considered better than a random classification? Explain carefully.

The model is considered better than a random classification as the Roc curve is above the bisecting line x=y which denotes the roc curve of a random classifier.

3.3 Question 3 REFERENCES

#### 3.3 Question 3

What is the AUC?

The Area Under the Curve also called AUC is the numeric value indicating extension of the area that is comprised between the Roc curve, the x axis (denoting antispecificity) and the line x=1. Hastie [2017] Gareth [2021]

From the R calculations the AUC is 0.66145833

## 4 Exercise 4: Application (R code) Pelgrin [2022]

Please see the attached R markdown file

#### References

Robert; Friedman Jerome Hastie, Trevor; Tibshirani. **The Elements of statistical learning**. Springer, 2017. pages 6

Daniela; Hastie Trevor; Tibshirani Robert Gareth, James; Witten. **An introduction to Statistical Learning**. Springer, 2021. pages 6

Florian Pelgrin. Introduction to machine learning through classification. 2022. pages 6

#### **ML Coursework**

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### **Preamble**

Please note that the dataset included (german.data) is the raw subset not yet encoded. We decided to automate the encoding in the first section of the R markdown that follows.

```
library(ggplot2)
library(tidyverse)
library(rpart)
library(rpart.plot)
library(plotROC)
library(ROCR)
library(pROC)
library(caret)
library(ggpubr)
library(InformationValue)
library(tidyverse)
library(leaps)
library(glmnet)
library(mlbench)
#Library(doMC)
library(caret)
library(class)
library(reshape2)
library(dplyr)
```

## **Question 1**

We start by downloading the German credit data

```
##
## A91 A92 A93 A94
## 0.050 0.310 0.548 0.092
##We compute margins so to see the distribution of each category
## and to choose how to divide them
```

We prooceed by encoding all the explanatory variables wheter quantitative or qualitative

```
#1 Credit balance
Balance <- c()
for (i in 1:1000){
  if (data$V1[i] == "A12") {
    Balance[i]= 1
  } else if ( data$V1[i]=="A13") {
    Balance[i]= 1} else {
    Balance[i]= 0}
}
#That way, I have created a vector in which users with no account or zero
#balance are assigned to 0, users with some balance are assigned 1. The
#Distinction make sense, as the 2 groups have similar magnitude.
#2 Duration in months : it is nuymerical
Duration months <- data$V2
#3 Credit history
History <- c()
for (i in 1:1000){
  if (data$V3[i] == "A30") {
    History[i]= 1
  } else if ( data$V3[i]=="A31") {
    History[i]= 1} else if ( data$V3[i]=="A32") {
      History[i]= 1} else {
      History[i]= 0}
#Here I have assigned 1 to users with good credit history, 0 to others
#4 Purpose
#For this group I will select 3 kinds of purspose : buying a car, buying
#something related to house and others
Purpose1 <- c()</pre>
for (i in 1:1000){
  if (data$V4[i] == "A40") {
    Purpose1[i]= 1
  } else if ( data$V4[i]=="A41") {
    Purpose1[i]= 1} else {
        Purpose1[i]= 0}
}
```

```
Purpose2 <- c()
for (i in 1:1000){
  if (data$V4[i] == "A42") {
    Purpose2[i]= 1
  } else if (data$V4[i]=="A43") {
    Purpose2[i]= 1} else if ( data$V4[i]=="A44") {
      Purpose2[i]= 1} else if (data$V5[i]== "A45"){
        Purpose2[i] = 1
      } else {
        Purpose2[i]= 0}
}
#So, Purpose1 will tell me if the person has used the money to buy a car,
#Purpose2 will tell me if she used it for her house, the control group
#(all zeros) is composed by people using it for other purposes
#5 Credit ammount (numerical)
Credit ammount <- data$V5
#6 Savings account
#Here I will create 4 groups with each value being the inferior boundary of
the set
Savings1 <- c()
for (i in 1:1000){
  if (data$V6[i] == "A61") {
    Savings1[i]= 0
  } else if ( data$V6[i]=="A62") {
    Savings1[i]= 100} else if (data$V6[i] == "A63"){
      Savings1[i] = 500else if (data$V6[i] == "A64"){
        Savings1[i]= 1000} else {
      Savings1[i]= 0}
}
#7 Employment Length
#Here I will create 3 groups : employed for less than 1 year (including
#unemployed), employed for 1 to 4 years, employed for more than 4 years
Employment_length1<- c()</pre>
for (i in 1:1000){
  if (data$V7[i] == "A71") {
    Employment length1[i]= 1
  } else if ( data$V7[i]=="A74") {
    Employment length1[i]= 1} else {
        Employment_length1[i]= 0}
}
Employment length2<- c()</pre>
for (i in 1:1000){
if (data$V7[i] == "A75") {
```

```
Employment length2[i]= 1
  } else {
      Employment_length2[i]= 0}
}
#So, Employment length1 displays the users with 1 to 4 years of work,
#Employment length2 the users with more than 4 years and the control group
#are the ones with less than 1 year + unemployed
#8 Installment rate in percentage of disposable income (numerical)
Installment rate <- data$V8</pre>
#9 sex and marital status
#Here I divide by sex. However,
#there seems to be some kind of mistake in the explanation of data,
#as A95 value (single female) seems to be missing.
#I will proceed by considering A91 as male divorced/seprated,
#A92 as female divorced/separated/married, A93 as male single
#and A94 as male married/widowed.
Male <-c()</pre>
for (i in 1:1000){
  if (data$V9[i] != "A92") {
    Male[i] = 1
  } else {
    Male[i] = 0
}
#10 Guarantor
Guarantor<- c()</pre>
for (i in 1:1000){
  if (data$V10[i] != "A101") {
    Guarantor[i]= 1
  } else {
    Guarantor[i]= 0}
}
#Here, the vector displays 1 if the user has a quarantor, 0 if not
#11 Present redisence since (numerical)
Residence_since <- data$V11</pre>
#12
House <- c()
for (i in 1:1000){
  if (data$V12[i] == "A121") {
    House[i] = 1
  } else {
      House[i]= \emptyset}
```

```
Insurance <- c()</pre>
for (i in 1:1000){
  if (data$V12[i] == "A122") {
    Insurance[i]= 1
  } else {
    Insurance[i]= 0}
}
Car <-c()
for (i in 1:1000){
  if (data$V12[i] == "A123") {
    Car[i]= 1
  } else {
    Car[i]= 0}
}
#The vector house displays 1 if the users owns a house; if not, the
#vector Insurance displays 1 if she owns an insurance. If not, the vector
#car displays 1 if she owns a car
#13 Age (numerical)
Age<-data$V13
#14 Other installment plans
Other_plans<- c()
for (i in 1:1000){
  if (data$V14[i] != "A143") {
    Other plans[i]= 1
  } else {
    Other_plans[i]= 0}
#Here the vector displays 1 if the user has a concurrent creditor, 0 if not
#15 Housing
FreeHousing <-c()</pre>
for (i in 1:1000){
  if (data$V15[i] == "A153") {
    FreeHousing[i]= 1
  } else {
    FreeHousing[i]= 0}
}
OwnHouse <- c()
for (i in 1:1000){
  if (data$V15[i] == "A152") {
    OwnHouse[i] = 1
 } else {
```

```
OwnHouse[i]= 0}
}
# Here the vector Free housing displays the users with a free house, the
# vetor OwnHouse users who own their house and the ones renting have
# zeros in both
#16 Number of existing credits at this bank (numerical)
Number_credits <- data$V16</pre>
#17 Job
Skilled <- c()
for (i in 1:1000){
  if (data$V17[i] == "A173") {
    Skilled[i]= 1
  } else {
    Skilled[i]= 0}
}
Highly_Qualified <- c()</pre>
for (i in 1:1000){
  if (data$V17[i] == "A174") {
    Highly_Qualified[i]= 1
  } else {
    Highly_Qualified[i]= 0}
}
#Skilled displays 1 if the users is a skilled worker, Highly Qualified
#displays 1 if she is highly qualified; if both display zeros, the user
#is unemployed/unskilled
#18 Number of people being liable to provide maintenance for (numerical)
People to mantain <- data$V18
#19 Telephone
Telephone <- c()
for (i in 1:1000){
  if (data$V19[i] == "A192") {
    Telephone[i]= 1
  } else {
    Telephone[i]= 0}
}
#20 foreign worker
Foreign_worker <- c()</pre>
for (i in 1:1000){
  if (data$V20[i] == "A201") {
    Foreign worker[i]= 1
 } else {
```

```
Foreign_worker[i]= 0}

#21 Output
Output <- data$V21-1
```

Finally we create the dataframe

After having encode our dataset and having described each of its components, we want to have a closer look at its summary statistics:

```
summary(German)
##
       Balance
                    Duration months
                                        History
                                                         Purpose1
                                             :0.000
##
                            : 4.0
   Min.
           :0.000
                    Min.
                                     Min.
                                                      Min.
                                                             :0.000
                                     1st Qu.:0.000
    1st Qu.:0.000
                    1st Qu.:12.0
                                                      1st Qu.:0.000
##
##
    Median :0.000
                    Median :18.0
                                     Median :1.000
                                                      Median:0.000
##
   Mean
           :0.332
                    Mean
                            :20.9
                                     Mean
                                             :0.619
                                                      Mean
                                                             :0.337
    3rd Qu.:1.000
                    3rd Qu.:24.0
                                     3rd Qu.:1.000
                                                      3rd Qu.:1.000
##
                    Max.
##
    Max.
           :1.000
                            :72.0
                                     Max.
                                             :1.000
                                                      Max.
                                                             :1.000
##
       Purpose2
                    Credit ammount
                                        Savings1
                                                       Employment_length1
##
           :0.000
                           : 250
                                                       Min.
    Min.
                    Min.
                                     Min.
                                                 0.0
                                                              :0.000
##
    1st Qu.:0.000
                    1st Qu.: 1366
                                     1st Qu.:
                                                 0.0
                                                       1st Qu.:0.000
    Median :0.000
                    Median : 2320
##
                                     Median :
                                                 0.0
                                                       Median :0.000
##
    Mean
                            : 3271
           :0.473
                    Mean
                                     Mean
                                               89.8
                                                       Mean
                                                              :0.236
##
    3rd Qu.:1.000
                     3rd Qu.: 3972
                                     3rd Qu.:
                                                 0.0
                                                       3rd Qu.:0.000
##
   Max.
           :1.000
                    Max.
                            :18424
                                     Max.
                                             :1000.0
                                                       Max.
                                                              :1.000
##
    Employment length2 Installment rate
                                              Male
                                                           Guarantor
##
    Min.
           :0.000
                       Min.
                               :1.000
                                         Min.
                                                 :0.00
                                                         Min.
                                                                :0.000
##
    1st Qu.:0.000
                        1st Qu.:2.000
                                         1st Qu.:0.00
                                                         1st Qu.:0.000
##
    Median :0.000
                       Median :3.000
                                         Median :1.00
                                                         Median :0.000
##
    Mean
           :0.253
                        Mean
                               :2.973
                                         Mean
                                                 :0.69
                                                         Mean
                                                                :0.093
##
    3rd Qu.:1.000
                        3rd Qu.:4.000
                                         3rd Qu.:1.00
                                                         3rd Qu.:0.000
##
   Max.
           :1.000
                       Max.
                               :4.000
                                         Max.
                                                 :1.00
                                                         Max.
                                                                :1.000
##
    Residence since
                         House
                                       Insurance
                                                           Car
                            :0.000
                                                             :0.000
##
    Min.
           :1.000
                    Min.
                                     Min.
                                             :0.000
                                                      Min.
##
    1st Qu.:2.000
                    1st Qu.:0.000
                                     1st Qu.:0.000
                                                      1st Qu.:0.000
                                                      Median:0.000
##
    Median :3.000
                    Median:0.000
                                     Median :0.000
##
    Mean
           :2.845
                    Mean
                            :0.282
                                     Mean
                                             :0.232
                                                      Mean
                                                             :0.332
##
    3rd Ou.:4.000
                     3rd Ou.:1.000
                                     3rd Ou.:0.000
                                                      3rd Ou.:1.000
##
    Max.
           :4.000
                    Max.
                            :1.000
                                     Max.
                                             :1.000
                                                      Max.
                                                             :1.000
##
                     Other_plans
                                      FreeHousing
                                                         OwnHouse
         Age
##
    Min. :19.00
                    Min.
                          :0.000
                                             :0.000
                                                      Min. :0.000
                                     Min.
```

```
1st Ou.:27.00
                    1st Ou.:0.000
                                     1st Ou.:0.000
                                                      1st Ou.:0.000
##
    Median :33.00
                    Median :0.000
                                     Median :0.000
                                                      Median :1.000
##
    Mean
           :35.55
                    Mean
                            :0.186
                                     Mean
                                             :0.108
                                                      Mean
                                                             :0.713
##
    3rd Qu.:42.00
                    3rd Qu.:0.000
                                     3rd Qu.:0.000
                                                      3rd Qu.:1.000
##
    Max.
           :75.00
                    Max.
                            :1.000
                                     Max.
                                             :1.000
                                                      Max.
                                                             :1.000
    Number_credits
                        Skilled
                                    Highly_Qualified People_to_mantain
##
    Min.
           :1.000
                    Min.
                            :0.00
                                    Min.
                                           :0.000
                                                      Min.
                                                             :1.000
                    1st Qu.:0.00
##
    1st Qu.:1.000
                                    1st Qu.:0.000
                                                      1st Qu.:1.000
##
    Median :1.000
                    Median :1.00
                                    Median :0.000
                                                      Median :1.000
##
    Mean
           :1.407
                    Mean
                            :0.63
                                    Mean
                                           :0.148
                                                      Mean
                                                             :1.155
##
    3rd Qu.:2.000
                    3rd Qu.:1.00
                                    3rd Qu.:0.000
                                                      3rd Qu.:1.000
                    Max.
                            :1.00
                                                             :2.000
##
   Max.
           :4.000
                                    Max.
                                           :1.000
                                                      Max.
##
      Telephone
                    Foreign worker
                                         Output
##
   Min.
           :0.000
                    Min.
                            :0.000
                                     Min.
                                             :0.0
##
    1st Qu.:0.000
                    1st Qu.:1.000
                                     1st Qu.:0.0
    Median :0.000
                    Median :1.000
                                     Median :0.0
##
    Mean
           :0.404
                    Mean
                            :0.963
                                     Mean
                                             :0.3
##
    3rd Qu.:1.000
                    3rd Qu.:1.000
                                     3rd Qu.:1.0
## Max.
         :1.000
                    Max.
                            :1.000
                                     Max.
                                             :1.0
```

For the majority of our variables (namely, the qualitative ones) the only use of descriptive statistics is to see by how much the condition is more/less respected than not. In other words, how many are the ones relatively to the zeros. For example, if mean of Balance is 0.332, it means that we have 32.2% of ones. To better visualize this issue, we could use a table showing the percentages of the dummy variables

And by choosing the item we are interested in, we can see how many its proportions. In particular, we have that History, Male, OwnHouse, Skilled, ForeignWorker are the only items with more ones than zeros. As far as quantitative variables are concerned:

```
summary(cbind(Duration_months, Credit_ammount, Installment_rate, Residence_si
nce,
        Number_credits,People_to_mantain, Age))
##
   Duration months Credit ammount Installment rate Residence since
##
   Min.
           : 4.0
                                                    Min.
                   Min.
                           :
                             250
                                   Min.
                                           :1.000
                                                            :1.000
## 1st Qu.:12.0
                   1st Qu.: 1366
                                   1st Qu.:2.000
                                                    1st Qu.:2.000
```

```
Median :18.0
                    Median: 2320
                                     Median :3.000
                                                       Median :3.000
##
    Mean
           :20.9
                    Mean
                            : 3271
                                             :2.973
                                                       Mean
                                                              :2.845
                                     Mean
    3rd Qu.:24.0
                     3rd Qu.: 3972
                                     3rd Qu.:4.000
                                                       3rd Qu.:4.000
##
                    Max.
##
    Max.
           :72.0
                            :18424
                                     Max.
                                             :4.000
                                                       Max.
                                                              :4.000
    Number_credits
                     People_to_mantain
##
                                            Age
##
    Min.
           :1.000
                    Min.
                            :1.000
                                       Min.
                                               :19.00
##
    1st Qu.:1.000
                    1st Qu.:1.000
                                       1st Qu.:27.00
    Median :1.000
                    Median :1.000
                                       Median :33.00
##
##
    Mean
           :1.407
                                       Mean
                                               :35.55
                    Mean
                            :1.155
##
    3rd Qu.:2.000
                     3rd Qu.:1.000
                                       3rd Qu.:42.00
    Max. :4.000
                    Max. :2.000
                                       Max. :75.00
```

We have that on average the duration is 20.9 months, and that duration is between 4 and 72 months. The user with the lowest credit amount has 250DM, the one with the highest has 18424 DM, with an average of 3271. Given that the 3rd quarter is not far from the mean (3972), we can say that the distance between that value and the max is very high.

On average, users have owned a residence for 2.845 years and they have 1.407 existing credits at this bank. They have on average 1.155 people to maintain (and in no case more than 2). The average age of the users is 35.55 years, however it seems that the distribution displays similarities with respect to the amount of credits, as the maximum age is much larger than the mean and the 3rd quarter. We expect to have a skewed distribution.

## **QUESTION 2**

Now we want to investigate how much correlated are our variables to our outcome. We will do it only for our training sample, which we define as follows:

```
set.seed(5257)
random_vector <- sample(c(1:1000), replace = FALSE, prob = NULL)
German_rd <- c()
for (i in random_vector) {
    German_rd = rbind(German_rd, German[i,])
}
Training_Validation <- German_rd[1:750,]
Just_training<-German_rd[1:500,]
Just_validation<-German_rd[501:750,]
Testing <- German_rd[751:1000,]

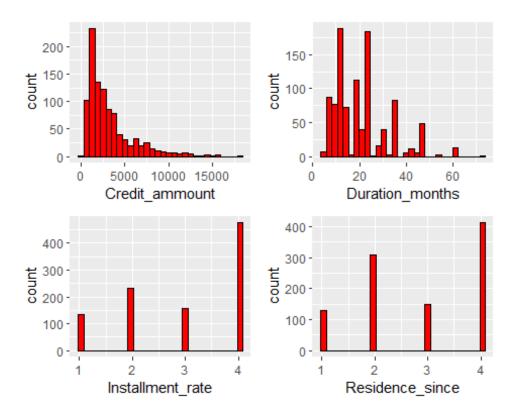
German_data <- as.data.frame(German_rd)
Training_sample <- as.data.frame(Training_Validation)
Testing_sample <- as.data.frame(Testing)
dTRAIN<-as.data.frame(Just_training)
dcv<-as.data.frame(Just_validation)</pre>
```

We have randomly created the two groups, the training and the testing Now, just to get an idea, let's plot Outcome and the variables.

Here we have histograms for the quantitative variables; the more interesting to comment are age and Credit\_ammount, that seems skewned to the left. This proves our suspects of having high values in one of the extremes. Then, we provided barplots for the qualitative parameters. This plots simply show us graphically, for each parameters, the relative frequency of each attribute.

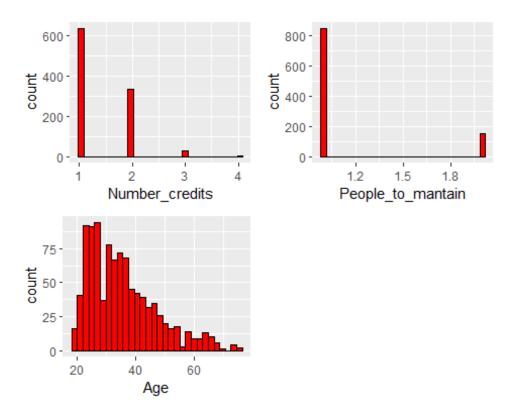
```
ggarrange(
ggplot(German_data, aes(x=Credit_ammount)) + geom_histogram(color="black", fi
ll="red"),
ggplot(German_data, aes(x=Duration_months)) + geom_histogram(color="black", f
ill="red"),
ggplot(German_data, aes(x=Installment_rate)) + geom_histogram(color="black",
fill="red"),
ggplot(German_data, aes(x=Residence_since)) + geom_histogram(color="black", f
ill="red"))

## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

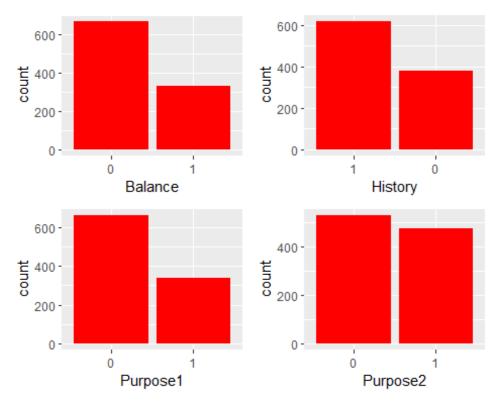


```
ggarrange(
  ggplot(German_data, aes(x=Number_credits)) + geom_histogram(color="black",
fill="red"),
  ggplot(German_data, aes(x=People_to_mantain)) + geom_histogram(color="black
", fill="red"),
  ggplot(German_data, aes(x=Age)) + geom_histogram(color="black", fill="red")
)

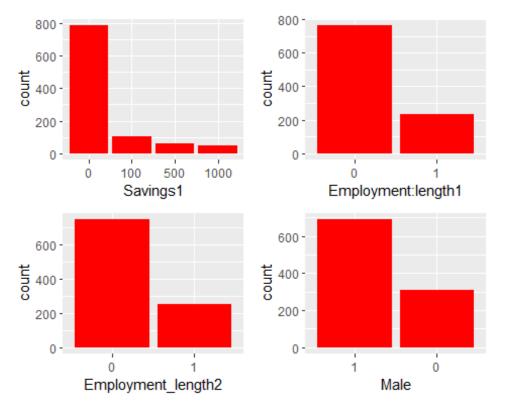
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



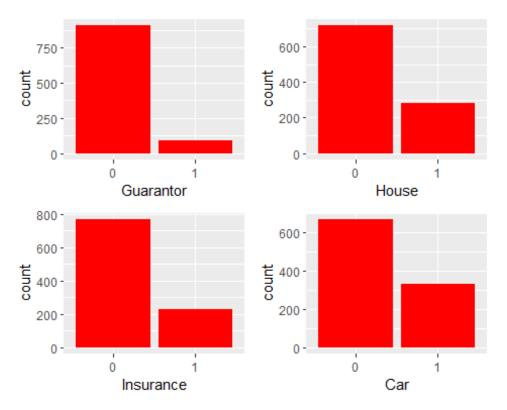
```
ggarrange(
ggplot(German_data, aes(x=reorder(Balance, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='Balance'),
ggplot(German_data, aes(x=reorder(History, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='History'),
ggplot(German_data, aes(x=reorder(Purpose1, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='Purpose1'),
ggplot(German_data, aes(x=reorder(Purpose2, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='Purpose2'))
```



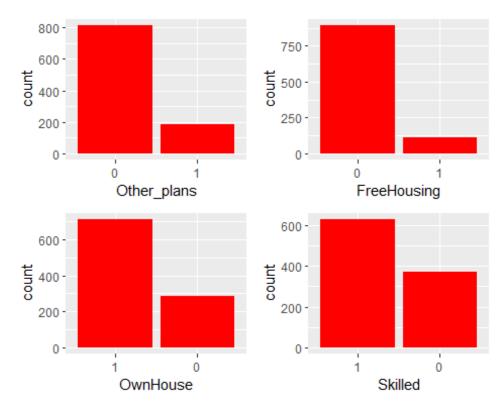
```
ggarrange(
ggplot(German_data, aes(x=reorder(Savings1, Output, function(x)-length(x))))
+
    geom_bar(fill='red') + labs(x='Savings1'),
ggplot(German_data, aes(x=reorder(Employment_length1, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='Employment:length1'),
ggplot(German_data, aes(x=reorder(Employment_length2, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='Employment_length2'),
ggplot(German_data, aes(x=reorder(Male, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='Male'))
```



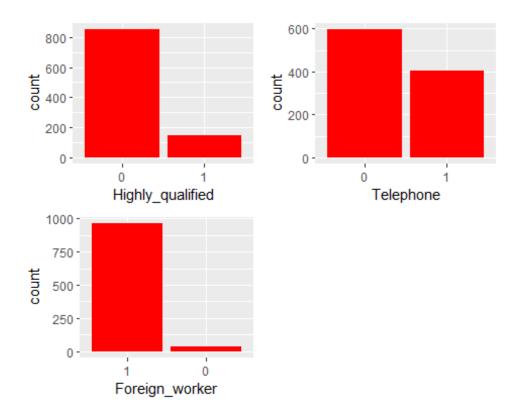
```
ggarrange(
ggplot(German_data, aes(x=reorder(Guarantor, Output, function(x)-length(x))))
+
    geom_bar(fill='red') + labs(x='Guarantor'),
ggplot(German_data, aes(x=reorder(House, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='House'),
ggplot(German_data, aes(x=reorder(Insurance, Output, function(x)-length(x))))
+
    geom_bar(fill='red') + labs(x='Insurance'),
ggplot(German_data, aes(x=reorder(Car, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='Car'))
```



```
ggarrange(
ggplot(German_data, aes(x=reorder(Other_plans, Output, function(x)-length(x))
)) +
    geom_bar(fill='red') + labs(x='Other_plans'),
ggplot(German_data, aes(x=reorder(FreeHousing, Output, function(x)-length(x))
)) +
    geom_bar(fill='red') + labs(x='FreeHousing'),
ggplot(German_data, aes(x=reorder(OwnHouse, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='OwnHouse'),
ggplot(German_data, aes(x=reorder(Skilled, Output, function(x)-length(x)))) +
    geom_bar(fill='red') + labs(x='Skilled'))
```



```
ggarrange(
ggplot(German_data, aes(x=reorder(Highly_Qualified, Output, function(x)-lengt
h(x)))) +
  geom_bar(fill='red') + labs(x='Highly_qualified'),
ggplot(German_data, aes(x=reorder(Telephone, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='Telephone'),
ggplot(German_data, aes(x=reorder(Foreign_worker, Output, function(x)-length(x)))) +
  geom_bar(fill='red') + labs(x='Foreign_worker'))
```



## **Question 3**

First we randomly split the dataset into two parts: the training and the testing

```
Y <- German_data[1:1000,27]
donnees <- German_data
indapp <- 1:750
dapp <- Training_sample
dtest <-Testing_sample
loss = rbind(c(0,1), c(5,0))
dapp.X<-model.matrix(Output~.,data=dapp)
dtest.X<-model.matrix(Output~.,data=dtest)</pre>
```

We have many explanatory variables so we have to perform variable selection for some models.

### **Linear Probability Model**

Let's first have a look at a linear regression on all the data

The problem is to explain the Output (column 27) by the other variables. We first consider the linear model. For linear models we will have to first fit the betas on the training sample (dTRAIN) and then use the cross-validation sample (dcv) to select the hyperparameter which in this case is the number of explanatory variables

```
#recall that dcv is our cross validation set and
linear.model <- lm(Output~.,data=dTRAIN)</pre>
summary(linear.model)
##
## Call:
## lm(formula = Output ~ ., data = dTRAIN)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -0.6941 -0.3046 -0.1574 0.4181 0.9716
##
## Coefficients:
##
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      -4.804e-02 2.026e-01 -0.237
                                                    0.81270
## Balance
                      5.177e-02 4.192e-02
                                             1.235
                                                    0.21744
## Duration_months
                      5.333e-03 2.332e-03
                                             2.287
                                                    0.02265 *
## History
                      1.343e-01 4.848e-02
                                             2.771
                                                    0.00581 **
## Purpose1
                      9.958e-02 5.543e-02
                                             1.796
                                                    0.07308 .
## Purpose2
                      1.569e-02 5.396e-02
                                             0.291
                                                    0.77140
## Credit ammount
                      7.064e-06 1.138e-05
                                             0.621
                                                    0.53518
## Savings1
                      -1.428e-04 8.528e-05 -1.675
                                                    0.09469
## Employment length1 -1.254e-01 5.016e-02
                                            -2.499
                                                    0.01279 *
## Employment length2 -1.223e-01 5.468e-02 -2.236 0.02578 *
```

```
## Installment rate 3.073e-02 1.973e-02
                                           1.557
                                                  0.12002
## Male
                     -1.393e-02 4.522e-02 -0.308
                                                  0.75813
## Guarantor
                     -1.683e-02 6.442e-02 -0.261
                                                  0.79403
## Residence since
                                          0.795
                     1.515e-02 1.906e-02
                                                  0.42711
## House
                     -2.088e-01 9.535e-02 -2.190
                                                  0.02901 *
## Insurance
                     -1.196e-01 9.417e-02
                                          -1.270
                                                  0.20456
## Car
                     -1.600e-01 9.284e-02
                                          -1.723
                                                  0.08554 .
## Age
                     -3.103e-03
                                1.894e-03
                                          -1.639
                                                  0.10193
## Other_plans
                     6.774e-02 5.226e-02
                                          1.296
                                                  0.19551
## FreeHousing
                     -1.362e-01
                                          -1.220
                                                  0.22316
                                1.116e-01
                     -1.372e-01 5.704e-02 -2.405
## OwnHouse
                                                  0.01657 *
## Number credits
                                           1.811
                     7.212e-02 3.982e-02
                                                  0.07074 .
## Skilled
                    -3.406e-03 5.064e-02 -0.067
                                                  0.94641
## Highly_Qualified
                    2.460e-02 7.734e-02
                                          0.318
                                                  0.75058
## People_to_mantain 2.405e-02 5.893e-02
                                           0.408
                                                  0.68343
## Telephone
                     -4.657e-02 4.464e-02 -1.043
                                                  0.29734
## Foreign_worker
                     2.608e-01 1.176e-01
                                           2.217
                                                  0.02708 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4248 on 473 degrees of freedom
## Multiple R-squared: 0.1531, Adjusted R-squared: 0.1066
## F-statistic: 3.289 on 26 and 473 DF, p-value: 1.719e-07
```

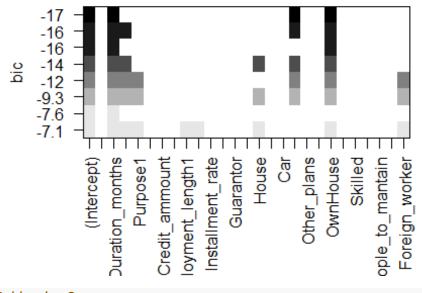
Some variables seem not to be useful so we would have to proceed with some selection tecniques

We can try with subset selection:

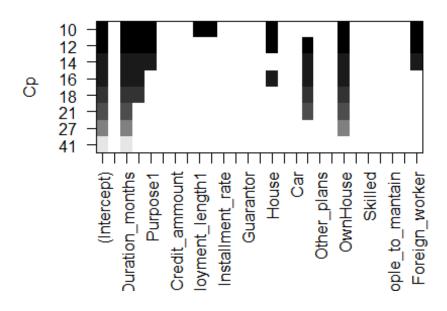
```
# either best subset
mod.sel <- regsubsets(Output~.,data=dTRAIN)
#or backward stepwise selection
m.back1 <- regsubsets(Output~.,data=dTRAIN,method="backward")
m.for1 <- regsubsets(Output~.,data=dTRAIN, method="forward")</pre>
```

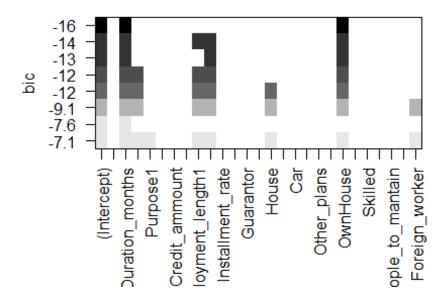
We can select the best models according to BIC and Cp

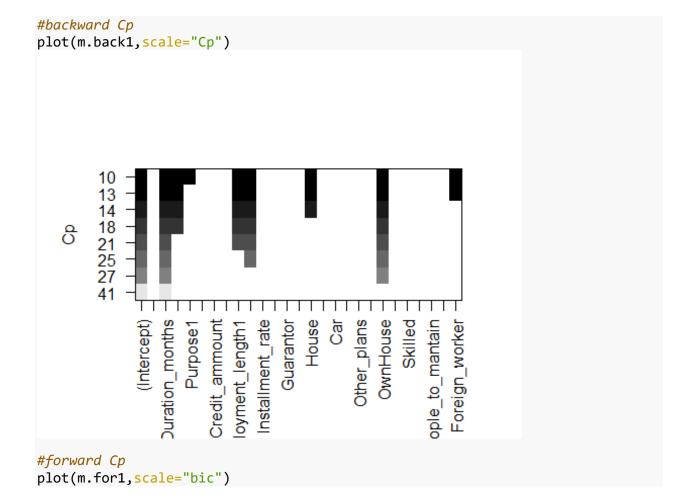
```
#BIC
plot(mod.sel,scale="bic")
```

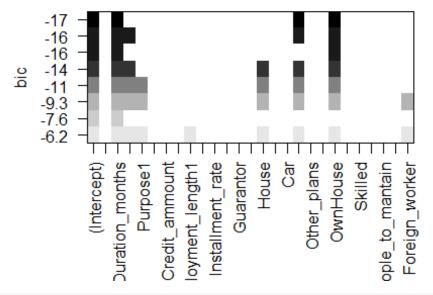


#Mallow's Cp
plot(mod.sel,scale="Cp")

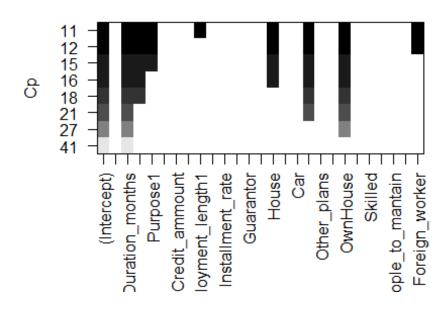








#forward Cp
plot(m.for1,scale="Cp")



```
a <- summary(mod.sel)</pre>
number <- order(a$bic)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.BIC <- lm(form,data=dTRAIN)</pre>
a <- summary(mod.sel)</pre>
number <- order(a$cp)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.CP <- lm(form, data=dTRAIN)</pre>
a <- summary(m.back1)</pre>
number <- order(a$bic)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form.back <- formula(paste("Output~",var.sel1,sep=""))</pre>
mod.BIC.back <- lm(form.back,data=dTRAIN)</pre>
a <- summary(m.back1)</pre>
number <- order(a$cp)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.CP.back <- lm(form, data=dTRAIN)</pre>
a <- summary(m.for1)</pre>
number <- order(a$bic)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.BIC.for <- lm(form, data=dTRAIN)</pre>
a <- summary(m.for1)</pre>
number <- order(a$cp)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.CP.for <- lm(form,data=dTRAIN)</pre>
```

We consider the quadratic risk for the models:

$$E\left[\left(Y-\widehat{m}(X)\right)^{2}\right].$$

This risk is estimated with the test set according to

$$\frac{1}{n_{test}} \sum_{i \in test} (Y_i - \widehat{m}(X_i))^2.$$

Compute the estimated risks for the three linear models:

```
prev <- data.frame(Y=dtest$Output,lin=predict(linear.model,newdata=dcv),BIC=p</pre>
redict(mod.BIC,newdata=dcv),CP=predict(mod.CP,newdata=dcv),BIC.back=predict(m
od.BIC.back, newdata=dcv), CP.back=predict(mod.CP.back, newdata=dcv), BIC.for=pre
dict(mod.BIC.for, newdata=dcv), CP.for=predict(mod.CP.for, newdata=dcv))
prev %>% summarize(Err lin=mean((Y-lin)^2),Err BIC=mean((Y-BIC)^2),Err CP=mea
n((Y-CP)^2), Err BIC back=mean((Y-BIC.back)^2), Err CP back=mean((Y-CP.back)^2)
,Err_BIC_for=mean((Y-BIC.for)^2),Err_CP_for=mean((Y-CP.for)^2))
##
       Err lin
                 Err BIC
                            Err CP Err BIC back Err CP back Err BIC for Err C
P for
## 1 0.2586208 0.2319694 0.2479865
                                       0.2313648
                                                   0.2479865
                                                               0.2319694 0.24
69547
```

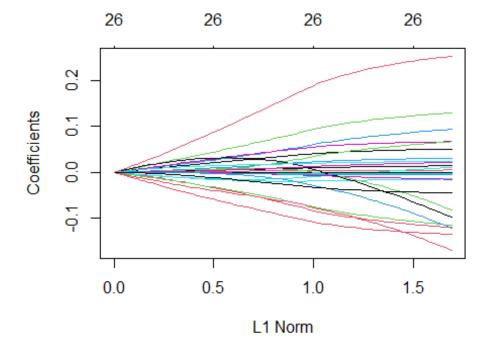
The first variable selection procedure is obtained through a backward selection approach. The statistical information criteria is BIC.

Let us run also a RIDGE and LASSO regressions

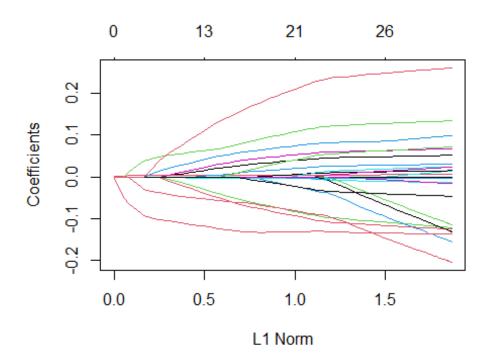
```
dTRAIN.X <- model.matrix(Output~.,data=dTRAIN)
dcv.X <- model.matrix(Output~.,data=dcv)</pre>
```

We draw the coefficient paths for ridge and lasso.

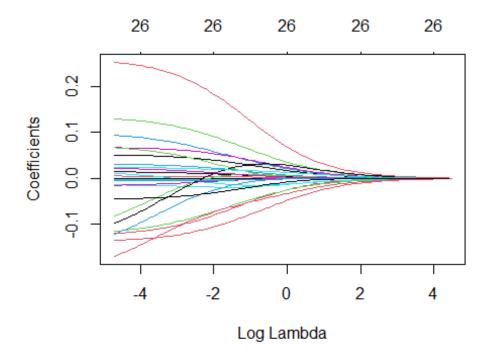
```
mod.R <- glmnet(dTRAIN.X,dTRAIN$Output,alpha=0)
mod.L <- glmnet(dTRAIN.X,dTRAIN$Output,alpha=1)
plot(mod.R)</pre>
```



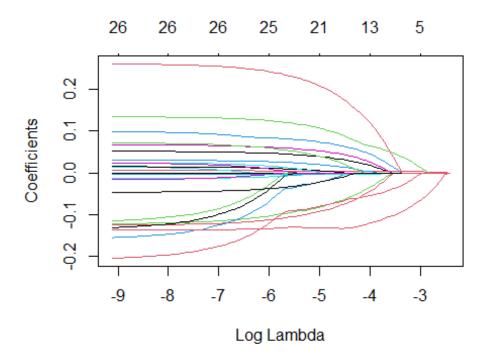
plot(mod.L)



plot(mod.R,xvar="lambda")



plot(mod.L,xvar="lambda")



 $shrinkage\ parameter\ for\ lasso\ regression\ with\ \textbf{cv.glmnet}.$ 

We select the

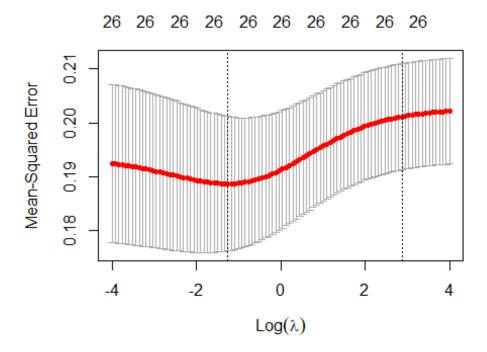
```
lassoCV <- cv.glmnet(dTRAIN.X,dTRAIN$Output,alpha=1)
lassoCV$lambda.min

## [1] 0.006569549

lasso.sel <- glmnet(dTRAIN.X,dTRAIN$Output,alpha=1,lambda=lassoCV$lambda.min)

Now fit the selected ridge model.

ridgeCV <- cv.glmnet(dTRAIN.X,dTRAIN$Output,alpha=0,lambda=exp(seq(-4,4,lengt h=100)))
plot(ridgeCV)</pre>
```



ridge.sel <- glmnet(dTRAIN.X,dTRAIN\$Output,alpha=0,lambda=ridgeCV\$lambda.min)</pre>

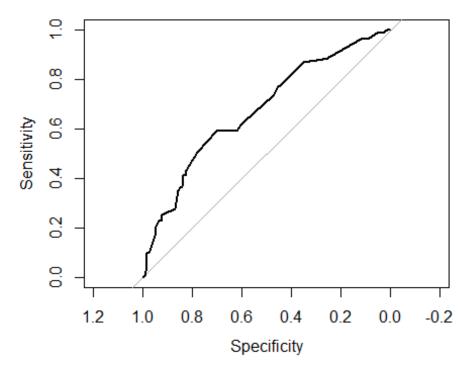
Estimate the quadratic error for the selected ridge and lasso models.

```
prev1 <- prev %>% mutate(ridge=as.vector(predict(ridge.sel,newx=dcv.X)),lasso
=as.vector(predict(lasso.sel,newx=dcv.X)))
prev1 %>% summarize(Err lin=mean((Y-lin)^2), Err BIC=mean((Y-BIC)^2), Err CP=me
an((Y-CP)^2), <a href="mailto:Err BIC">Err BIC</a> back=mean((Y-BIC.back)^2), <a href="mailto:Err CP">Err CP</a> back=mean((Y-CP.back)^2)
), Err_BIC_for=mean((Y-BIC.for)^2), Err_CP_for=mean((Y-CP.for)^2), Err_ridge=mea
n((Y-ridge)^2), Err_lasso=mean((Y-lasso)^2))
##
                   Err BIC
                               Err_CP Err_BIC_back Err_CP_back Err_BIC_for Err_C
       Err lin
P for
## 1 0.2586208 0.2319694 0.2479865
                                          0.2313648
                                                       0.2479865
                                                                     0.2319694 0.24
69547
```

```
## Err_ridge Err_lasso
## 1 0.2365286 0.245584
```

Conclusion: we select the best explanatory variables subset which is the one given by the model called Err\_BIC\_back. Therefore can rerun a regression on the training+cross-validation samples and do our final predictions with the test set

```
#rerun
a <- summary(m.back1)</pre>
number <- order(a$bic)[1]</pre>
var.sel <- a$which[number,][-1]</pre>
var.sel1 <- names(var.sel)[var.sel] %>% paste(collapse="+")
form <- formula(paste("Output~", var.sel1, sep=""))</pre>
mod.BIC.back <- lm(form,data=dapp)</pre>
#final prediction
prevlm<- predict(mod.BIC.back,newdata=dtest)</pre>
#MSE
MSE_lm<- mean(round(prevlm)!=dtest$Output)</pre>
MSE_lm
## [1] 0.316
#Roc and AUC
plot(roc(dtest$Output,prevlm))
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases</pre>
```



```
AUC_lm<-auc(roc(dtest$Output,prevlm))
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
AUC_lm
## Area under the curve: 0.6759
#confusionMatrix(data=prevlog,reference =dtest$Output)
#Misclassification error
optimal_lm <- optimalCutoff(dtest$Output, prevlm)[1]
conf_lm<-confusionMatrix(dtest$Output, prevlm)
misclass_lm <- (conf_lm[1,2]*loss[1,2]+conf_lm[2,1]*loss[2,1])/nrow(dapp)/mea
n(dapp$Output==1)
misclass_lm
## [1] 0.437788</pre>
```

#### **Logistic model**

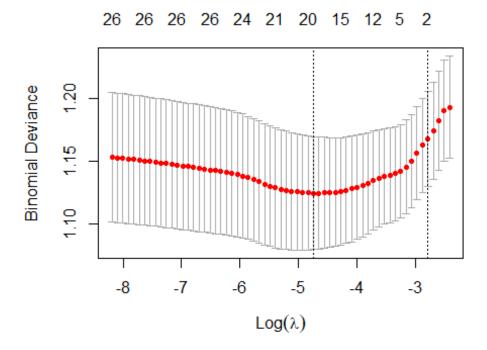
```
full.logit <- glm(Output~.,data=dTRAIN,family="binomial")</pre>
full.logit
##
## Call: glm(formula = Output ~ ., family = "binomial", data = dTRAIN)
##
## Coefficients:
                                                Duration_months
##
          (Intercept)
                                   Balance
                                                                             His
tory
                                 3.262e-01
                                                                           7.737
##
           -3.788e+00
                                                      2.844e-02
e-01
                                  Purpose2
                                                 Credit_ammount
##
             Purpose1
                                                                            Savi
ngs1
##
            6.292e-01
                                 1.201e-01
                                                      3.912e-05
                                                                          -9.856
e-04
## Employment length1
                        Employment length2
                                               Installment rate
Male
##
           -7.310e-01
                                -7.178e-01
                                                      2.080e-01
                                                                          -8.431
e-02
##
            Guarantor
                           Residence since
                                                          House
                                                                           Insur
ance
##
           -6.238e-02
                                 6.325e-02
                                                     -1.262e+00
                                                                          -6.414
e-01
                                                    Other_plans
##
                  Car
                                                                         FreeHou
                                       Age
sing
##
           -8.884e-01
                                -2.184e-02
                                                      4.608e-01
                                                                          -7.402
e-01
                            Number_credits
                                                                   Highly Quali
##
             OwnHouse
                                                        Skilled
fied
##
           -7.581e-01
                                 4.384e-01
                                                     -7.269e-03
                                                                           1.895
e-01
## People_to_mantain
                                 Telephone
                                                 Foreign_worker
##
            1.540e-01
                                -3.038e-01
                                                      2.314e+00
##
## Degrees of Freedom: 499 Total (i.e. Null);
                                                473 Residual
## Null Deviance:
                         593
## Residual Deviance: 508.7
                                 AIC: 562.7
```

We implement a variable selection procedure with a backward selection approach using BIC criterion. You just have to use the step function with the direction="backward" and k=log(nrow(train)) options. We call it mod.back

```
mod.back <- step(full.logit, direction="backward", k=log(nrow(dTRAIN)), trace=0)</pre>
```

we Fit a logistic lasso model on the training data (select the shrinkage parameter with **cv.glmnet**).

```
set.seed(1234)
cv.lasso <- cv.glmnet(dTRAIN.X,dTRAIN[,27],family="binomial",alpha=1)
plot(cv.lasso)</pre>
```

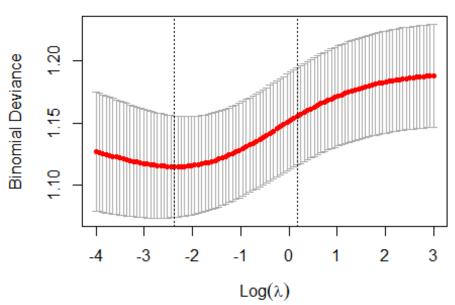


```
lambda.lasso <- cv.lasso$lambda.min
mod.lasso <- glmnet(dTRAIN.X,dTRAIN[,27],family="binomial",lambda=lambda.lass
o,alpha=1)</pre>
```

The fit a logistic ridge model on the training data (select the shrinkage parameter with **cv.glmnet**).

```
set.seed(1234)
cv.ridge <- cv.glmnet(dTRAIN.X,dTRAIN[,27],family="binomial",alpha=0,lambda=e
xp(seq(-4,3,length=100)))
plot(cv.ridge)</pre>
```





```
lambda.ridge<-cv.ridge$lambda.min
mod.ridge <- glmnet(dTRAIN.X,dTRAIN[,27],family="binomial",lambda=lambda.ridg
e,alpha=0)</pre>
```

Make a comparison of the methods with the error probability (estimated on the test dataset).

```
prev.full <- predict(full.logit,newdata=dcv,type="response") %>% round() %>%
as.factor()
prev.back <- predict(mod.back,newdata=dcv,type="response") %>% round() %>% as
.factor()

prev.lasso <- predict(mod.lasso,newx=dcv.X,type="class")
prev.ridge <- predict(mod.ridge,newx=dcv.X,type="class")
prev <- data.frame(full=prev.full,back=prev.back,lasso=as.vector(prev.lasso),
ridge=as.vector(prev.ridge))
prev %>% summarise_at(vars(1:4),~(mean((.!=Y)^2)))

## full back lasso ridge
## 1 0.344 0.316 0.324 0.31
```

Conclusion best model is ridge

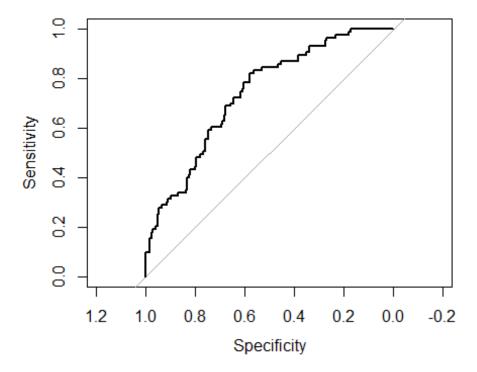
Therefore can rerun a regression on the training+cross-validation samples and do our final predictions with the test set

```
#rerun
mod.ridge <- glmnet(dapp.X,dapp[,27],family="binomial",lambda=lambda.ridge,al</pre>
```

```
pha=0)
#final prediction
prevlog<- predict(mod.ridge,newx=dtest.X,type="response")
#prevlog

#MSE
MSE_log<- mean(round(prevlog)!=dtest$Output)
MSE_log
## [1] 0.296

#Roc and AUC
plot(roc(dtest$Output,prevlog))
## Setting levels: control = 0, case = 1
## Warning in roc.default(dtest$Output, prevlog): Deprecated use a matrix as ## predictor. Unexpected results may be produced, please pass a numeric vecto r.
## Setting direction: controls < cases</pre>
```



```
AUC_log<-auc(roc(dtest$Output,prevlog))
## Setting levels: control = 0, case = 1
```

```
## Warning in roc.default(dtest$Output, prevlog): Deprecated use a matrix as
## predictor. Unexpected results may be produced, please pass a numeric vecto
r.

## Setting direction: controls < cases

AUC_log

## Area under the curve: 0.737

#confusionMatrix(data=prevlog,reference =dtest$Output)

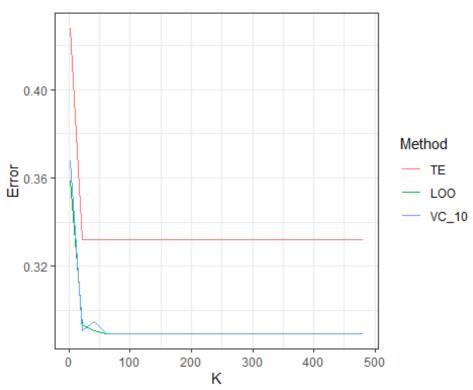
#Misclassification error
optimal_log <- optimalCutoff(dtest$Output, prevlog)[1]
conf_log<-confusionMatrix(dtest$Output, prevlog)
misclass_log <- (conf_log[1,2]*loss[1,2]+conf_log[2,1]*loss[2,1])/nrow(dapp)/
mean(dapp$Output==1)
misclass_log

## [1] 0.4884793</pre>
```

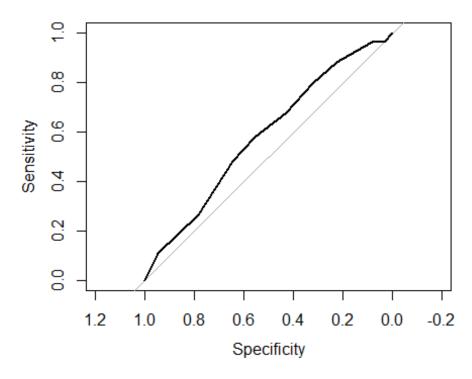
#### KNN Model

```
#cross-validation
library(class)
regle_ppv <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=81)</pre>
#function 1
K_{cand} \leftarrow seq(1,500,by=20)
err1 <- rep(0,length(K_cand))</pre>
for (i in 1:length(K cand)){
  err1[i] <- mean(knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=K_cand[i])!=dte
st$Output)
K_cand[which.min(err1)]
## [1] 21
#Function 2 : Leave-one-out cross-validation
err2 <- rep(0,length(K_cand))</pre>
for (i in 1:length(K_cand)){
  prev_cv <- knn.cv(dapp[,-27],cl=dapp$Output,k=K_cand[i])</pre>
  err2[i] <- mean(prev_cv!=dapp$Output)</pre>
K_cand[which.min(err2)]
## [1] 61
```

```
#Function 3 : M-fold cross-validation method
err3 <- rep(0,length(K_cand))</pre>
M < -10
prev <- rep(0,nrow(dapp))</pre>
n_CV <- nrow(dapp)/M</pre>
for (i in 1:length(K_cand)){
  for (j in 1:M){
    ind_testj <- ((j-1)*n_CV+1):(j*n_CV)</pre>
    prev[ind_testj] <- knn(dapp[-ind_testj,-27],dapp[ind_testj,-27],cl=dapp$0</pre>
utput[-ind_testj],k=K_cand[i])
  err3[i] <- mean((prev-1)!=dapp$Output)</pre>
K_cand[which.min(err3)]
## [1] 61
# Visual inspection
a <- data.frame(K_cand,err1,err2,err3)</pre>
names(a) <- c("K","TE","L00","VC_10")
library(reshape2)
aa <- melt(a,id="K")</pre>
names(aa) <- c("K","Method","Error")</pre>
ggplot(aa)+aes(x=K,y=Error,color=Method)+geom_line()+theme_bw()
```



```
pred_21 <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=21)</pre>
pred_61 <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=61)</pre>
pred_81 <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=81)</pre>
MSE_f1<-mean(pred_21!=dtest$Output)</pre>
MSE_f2<-mean(pred_61!=dtest$Output)</pre>
MSE_f3<-mean(pred_81!=dtest$Output)</pre>
MSE_f1
## [1] 0.332
MSE_f2
## [1] 0.332
MSE_f3
## [1] 0.332
pred_final <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=21)</pre>
#MSE
MSE_KNN<-mean(pred_final!=dtest$Output)</pre>
MSE_KNN
## [1] 0.332
#Roc and AUC
prev1 <- knn(dapp[,-27],dtest[,-27],cl=dapp$Output,k=21,prob=TRUE)</pre>
D <- data.frame(pred=attributes(prev1)$prob,obs=dtest$Output)</pre>
plot(roc(D$obs, D$pred))
## Setting levels: control = 0, case = 1
## Setting direction: controls > cases
```

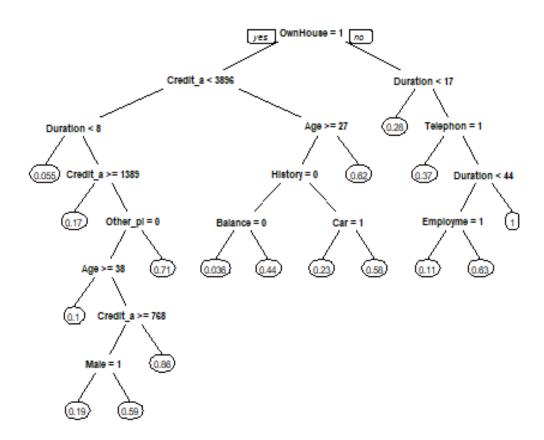


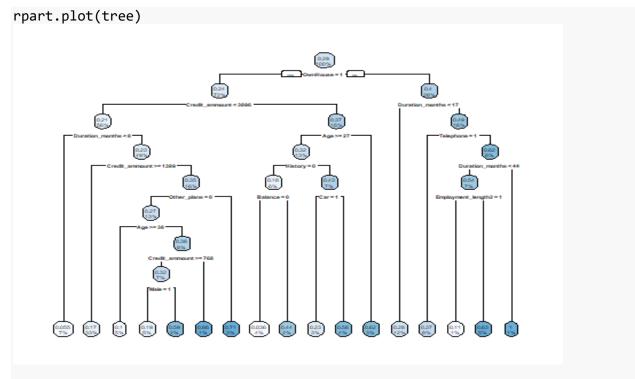
```
AUC_KNN<-auc(roc(D$obs, D$pred))
## Setting levels: control = 0, case = 1
## Setting direction: controls > cases
AUC_KNN
## Area under the curve: 0.5843
#Mispecification error
conf_KNN <- table(dtest$Output,pred_final)</pre>
conf_KNN
##
      pred_final
##
         0
             1
##
     0 160
             7
             7
##
       76
misclass\_KNN<-(conf\_KNN[1,2]*loss[1,2]+conf\_KNN[2,1]*loss[2,1])/nrow(dapp)/me
an(dapp$Output==1)
misclass_KNN
## [1] 1.78341
```

# **Decision trees**

We start by inspecting the regression tree to have a "feeling" of the model.

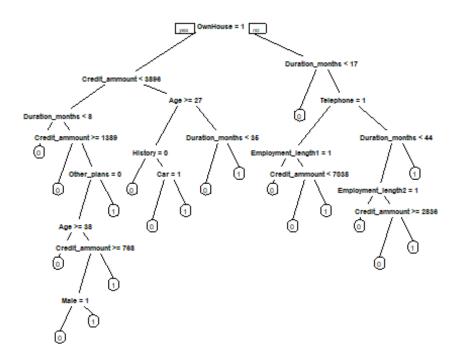
```
#regression tree
tree <- rpart(dapp$Output~.,data=dapp[,-27])
prp(tree)</pre>
```





### #decision tree

datafact<-as.factor(dapp\$Output)
tree2<-rpart(datafact~.,data=dapp[,-27])
prp(tree2)</pre>



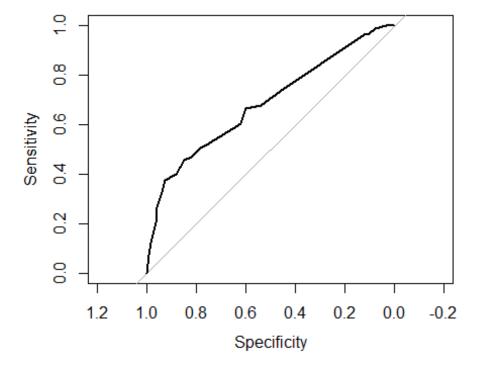
```
predtree<-predict(tree2, newdata=dtest)</pre>
```

Nice interactive visualization that however has to be commented out for the markdown to knit properly

```
#library(visNetwork)
#library('sparkline')
#visTree(tree2)
```

Finally we calculate our error and model selection values.

```
#MSE
MSE_tree<-mean(predtree!=dtest$Output)
MSE_tree
## [1] 0.986
#Roc and AUC
plot(roc(dtest$Output,predtree[,2]))
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases</pre>
```



```
AUC_tree<-auc(roc(dtest$Output,predtree[,2]))

## Setting levels: control = 0, case = 1

## Setting direction: controls < cases
```

```
AUC tree
## Area under the curve: 0.6863
#table<-table(predtree[,2],dtest$Output)</pre>
#Misclassification error
predtree<-predict(tree2, newdata=dtest,type='class')</pre>
conf tree <- table(dtest$Output,predtree)</pre>
conf tree
##
      predtree
##
         0
            1
##
     0 142 25
##
     1 45 38
misclass_tree<-(conf_tree[1,2]*loss[1,2]+conf_tree[2,1]*loss[2,1])/nrow(dapp)
/mean(dapp$Output==1)
misclass tree
## [1] 1.152074
```

## **Question 4**

Finally, we summarise our findings in the following table

```
mytable <- data.frame(MSE=c(MSE lm, MSE log, MSE KNN, MSE tree),
    AUC=c(AUC_lm,AUC_log,AUC_KNN,AUC_tree),
    Misclassification error=c(misclass lm, misclass log, misclass KNN, misclass
tree), row.names = c("linear probability", "logistic", "KNN", "decision tree")
print(mytable)
##
                        MSE
                                  AUC Misclassification error
                                                    0.4377880
## linear probability 0.316 0.6758892
## logistic
                      0.296 0.7369598
                                                    0.4884793
## KNN
                      0.332 0.5843013
                                                    1.7834101
## decision tree
                      0.986 0.6863141
                                                    1.1520737
View(mytable)
```

By looking at the table, we can see how the Logistic model seems more performing according to both MSE (as it displays the lowest value for the errors) and AUC (as it displays the largest area under the curve).

If we look at misclassification error, on the other hand, the linear probability model seems the most performing, as it displays the lowest value. Our recommendation would be to choose one of the two; in particular, the logistic seems the best one, as it outperformes the others according to 2 criteria out of 3.