NI & AC

A NS Agent for Pacman Maze



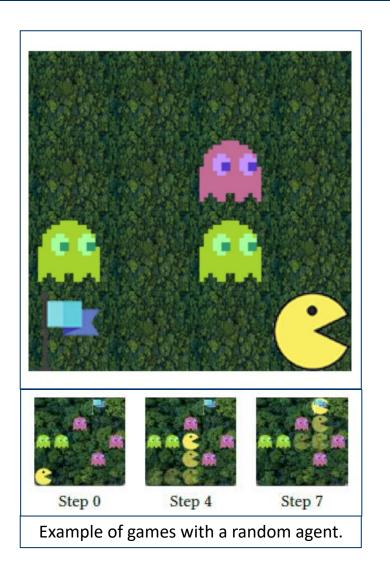
UNIVERSITÀ DEGLI STUDI D

Pacman Maze

Pacman Maze:

- Grid: M x N cells.
- 4 possible moves: $\uparrow \downarrow \leftarrow \rightarrow$.
- *K* enemies, all initial positions are randomly chosen.
- **Goal**: the agent must reach the flag within *T* moves without stepping on a cell occupied by an enemy.

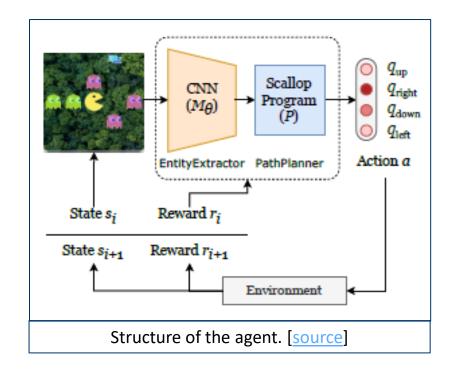






DQNS Agent

- Neural-symbolic agent:
 - Neural component:
 - CNN-like to extract entities (PyTorch).
 - From image to distribution over [agent, empty, enemy, target] for each cell.
 - Logical component:
 - Predict next move (Scallopy).
 - Probabilistic path search on a graph.
- Agent trained using (Deep) Q-learning:
 - ε-greedy policy network = neural comp. + logical comp.
 - Soft update of the target network.



$$\theta' \leftarrow \tau \cdot \theta + (1 - \tau) \cdot \theta$$

Soft update of the target network's parameters.



Loss & Backpropagation

- Loss based on three factors:
 - Expected vs predicted state-action value → Humber loss.
 - Constraints violation → Smooth L1 loss:
 - Number (probability) of cells identified as targets (should be 1).
 - Number (probability) of cells identified as enemies (should be K).
- Single backpropagation step:
 - Neural component: inherently differentiable.
 - Logical component: logical equations are written using differentiable provenance, i.e. logical operators are mapped to differentiable ones.

$$l_n = \begin{cases} 0.5(x_n - y_n)^2, & \text{if } |x_n - y_n| < \delta \\ \delta(|x_n - y_x| - 0.5\delta), & \text{otherwise} \end{cases}$$

Huber loss. [source]

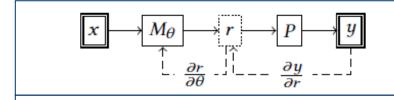


$$l_n = \begin{cases} 0.5(x_n - y_n)^2/\beta, & \text{if } |x_n - y_n| < \beta \\ |x_n - y_x| - 0.5\beta, & \text{otherwise} \end{cases}$$

Smooth L1 loss. [source]



loss(X,Y) = Humber(X,Y) + SmoothL1(X,Y)



Backpropagation in a NS model. [source]



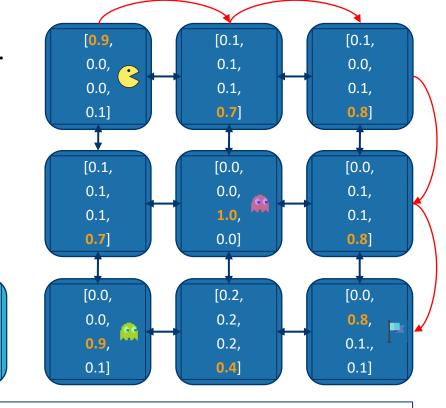
Logical Component

Logical component:

- 1. Read the prediction of the neural component for each cell.
- 2. Assign each node a probability equal to the complement of the enemy presence probability.
- 3. Path probability = conjunction of traversed nodes' probabilities.
- 4. Compute the next move by conjoining the probabilities of:
 - 1. The current position;
 - 2. The goal position;
 - 3. And the path to follow.

```
next_position(xp, yp, a) = agent(x, y)
    and edge(x, y, xp, yp, a)
next_action(a) = next_position(x, y, a) and
    path(x, y, gx, gy) and
    target(gx, gy)

Formula used to compute the next action.
```



Probabilistic path search on a graph.

[Agent (%),

Target (%),

Enemy (%),

Empty (%)]

Q-Learning

- In Q-Learning:
 - Policy network's output is an approximation of the state-action value function Q.
 - At each step, this estimate is used, together with the reward obtained, to improve the quality of the next predictions.
- But here the logical component returns a distribution over the action space. It only works thanks to the chosen rewards.

```
class AvoidingArena(gym.Env):
    def __init__(
        self,
        grid_dim: Tuple[int, int] =(5, 5),
        cell_size: float = 0.5,
        dpi: int = 80,
        num_enemies: int = 5,
        easy: bool = False,
        default_reward: float = 0.00,
        on_success_reward: float = 1.0,
        on_failure_reward: float = 0.0,
        remain_unchanged_reward: float = 0.0,
    ):
    """
```

$$Q^{\pi}(s,a) = r(s,a) + \gamma \sum_{s' \in S} V^{\pi}(s') \mathbb{P}(s'|s,a)$$

Q function: π is the policy, s the state, a the action, r the reward and V is the state value function.

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha_t(r_t + \gamma \max_{a_{t+1}} Q(s_{t+1}, a_{t+1}) - Q(s_t, a_t))$$

Q-Learning update rule.



Extending the Rewards

Custom Provenance

Reward as Tuple Element

```
# ---- Custom provenance ----
    class MyProvenance(scallopy.provenance.ScallopProvenance):
        def init (self, min :float, max :float):
            super(MyProvenance, self). init ()
            self.min = min
            self.max = max
            return
        def name(self):
            return "custom-provenance"
10
11
12
        def zero(self):
13
            return self.min
14
15
        def one(self):
16
            return self.max
17
18
        def add(self, t1, t2):
            raise Exception("Not implemented")
19
20
21
        def mult(self, t1, t2):
            return torch.clip(t1 + t2, min=self.min, max=self.max)
22
23
24
        def negate(self, t):
25
            return torch.clip(-t, min=self.min, max=self.max)
26
27
        def saturated(self, t1, t2):
28
            return bool(t1 > t2)
```

```
# connectivity: path(node i, node j, num moves, reward)
# {L} is the maximum number of moves allowed
# {R} is a lower bound for the reward
path(x, y, x, y, 1, r) = node(x, y, r)
path(x, y, xp, yp, 1, r) =
     edge(x, y, xp, yp, ) and
     node(xp, yp, r)
path(x, y, xpp, ypp, \{L\}, \{R\}) =
     node(x, y, ) and
     node(xpp, ypp, ) and
     abs(x - xpp) + abs(y - ypp) > 1 # lower bound
path(x, y, xpp, ypp, l + 1, rp + rn) =
     path(x, y, xp, yp, 1, rp) and
     edge(xp, yp, xpp, ypp, _) and
     node(xpp, ypp, rn) and
     path(x, y, xpp, ypp, , r) and
     r < rp + rn and
     1 + 1 <= \{L\}
```



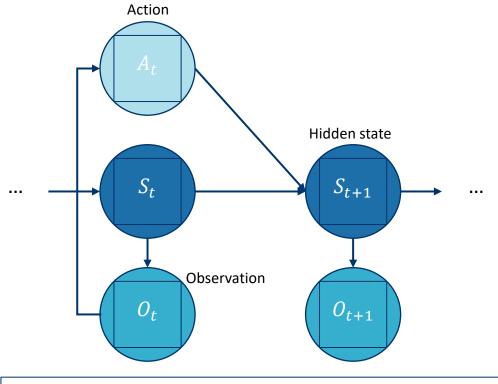
Limitations of Scallop

- Main Scallop limitations:
 - **A.** Lack of documentation for advanced operations.
 - **B.** Lack of support for filtering tuples at generation time.
 - **C. Limited** provenance **customizability**.
 - **D.** GPU unused by logic component → High training time even for small neural component.
 [Git Issue]
- In practice, proposed solutions for handling different rewards are ineffective:
 - Reward as tuple element → Huge memory footprint even for small grids (due to point B).
 - Custom provenance → Incorrect rewards due to inability to implement the saturation criterion correctly (due to point C).



Neural Component

- How can the logical component be improved, considering the limitations of Scallop?
- Original neural component → CNN:
 - 2x 2D-Convolutional layers;
 - 2x Dense layers;
 - ReLu as activation function;
 - Softmax as last activation function.

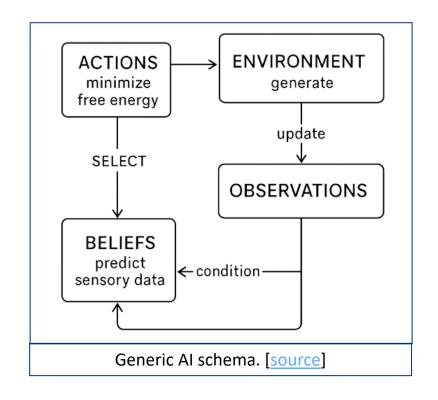


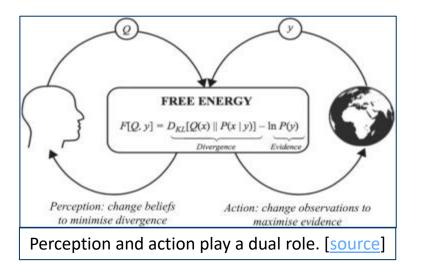
PGM of the game: in dark blue the hidden states.



Active Inference

- A different approach to the problem:
 - **Minimize uncertainty** instead of maximizing the reward.





• Challenges:

- A detailed generative model is needed.
- Simulating and managing uncertainty.
- Scalability.

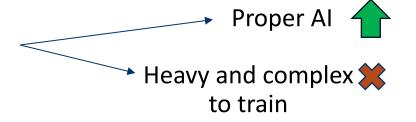


Possible Implementations

- Deep Active Inference with Variation Policy Gradient (DAI_{VPG}):
 - Gradient descent to minimize Expected Free Energy (EFE).

- Deep Active Inference Free Action Model (DAI_{FA}):
 - Minimizes the Variational Free Energy.

- Deep Active Inference with Monte Carlo Tree (DAI_{MC}):
 - Monte Carlo Tree Search to explore action sequences.



_____ No scalability 💥

Unclear preferences 💥

→ Not full Al 💢

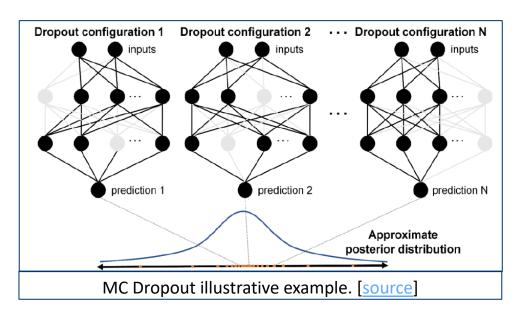
Inaccurate 🗶



Our Approach: MC Dropout

Monte Carlo (MC) Dropout:

- Dropout layers kept active also during evaluation.
- So multiple passes with different dropout masks for each input → multiple predictions.
- This allows uncertainty estimation in predictions, and it approximates variational inference (Gal et al.).



Pros:

- Training time unaffected.
- Parallel evaluation → time unchanged.

Cons:

- Poorly approximates complex posterior distributions.
- Sensitive to hyperparameters (e.g., dropout rate).



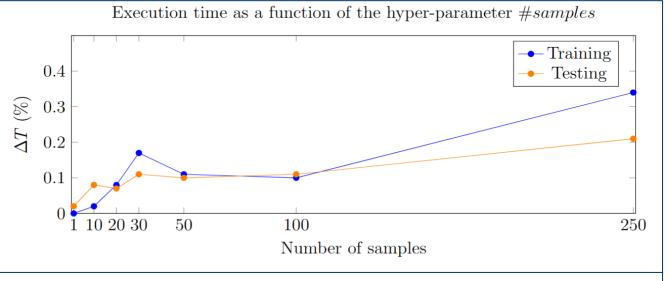
Experimental Results

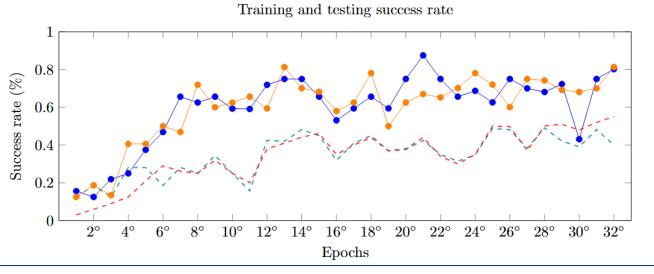
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Execution Time (sec)			
#Samples	T _{train}	T _{test}	
1	2,43	0,54	
10	2,49	0,55	
20	2,69	0,55	
30	2,88	0,56	
50	3,21	0,56	
100	3,53	0,67	
250	4,74	0,81	

Legend		
	DQNS Agent	Original Agent
Train		
Test		



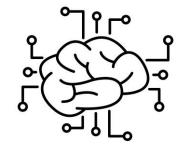


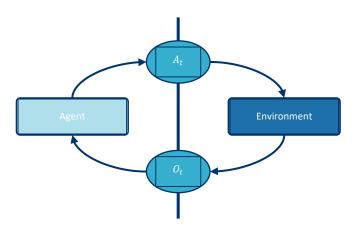


Conclusions

• Scallop:

- A framework for neuro-symbolic programming .
- With its strengths and potential limitations.





- MC Dropout:
 - A trade-off between efficiency and Bayesian inference.
 - Good accuracy and less prone to overfitting.

- Further developments:
 - More training & testing → more reliable conclusions.
 - More complex neural and/or logical components.







Grazie

